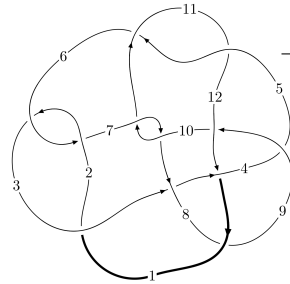
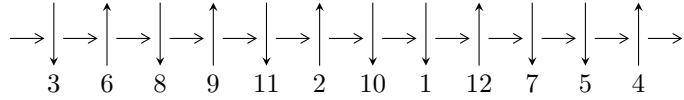


12a<sub>0286</sub> (K12a<sub>0286</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$4,9 \xrightarrow{c_4} 5,12 \xrightarrow{c_9} 10 \xrightarrow{c_{12}} 1 \xrightarrow{c_8} 8 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 11 \xrightarrow{c_5} 6 \xrightarrow{c_2} 2 \twoheadrightarrow c_1, c_6, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -1.08457 \times 10^{28} u^{31} - 9.68465 \times 10^{27} u^{30} + \dots + 3.30621 \times 10^{28} b + 6.26853 \times 10^{28}, \\ 1.00919 \times 10^{29} u^{31} - 4.41562 \times 10^{28} u^{30} + \dots + 3.30621 \times 10^{28} a + 4.42115 \times 10^{28}, u^{32} - 2u^{30} + \dots + 2u + 1 \rangle$$

$$I_2^u = \langle -u^3 + u^2 + 4b - 5u + 2, a, u^4 - u^3 + 5u^2 - 2u + 4 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 36 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -1.08 \times 10^{28} u^{31} - 9.68 \times 10^{27} u^{30} + \dots + 3.31 \times 10^{28} b + 6.27 \times 10^{28}, 1.01 \times 10^{29} u^{31} - 4.42 \times 10^{28} u^{30} + \dots + 3.31 \times 10^{28} a + 4.42 \times 10^{28}, u^{32} - 2u^{30} + \dots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -3.05243u^{31} + 1.33556u^{30} + \dots - 5.33264u - 1.33723 \\ 0.328041u^{31} + 0.292923u^{30} + \dots + 0.733300u - 1.89599 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 6.38763u^{31} - 3.08529u^{30} + \dots + 7.92825u + 8.64307 \\ -0.227028u^{31} + 0.570345u^{30} + \dots - 1.64514u + 1.43963 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -2.72438u^{31} + 1.62848u^{30} + \dots - 4.59934u - 3.23322 \\ 0.328041u^{31} + 0.292923u^{30} + \dots + 0.733300u - 1.89599 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 5.67422u^{31} - 2.13572u^{30} + \dots + 1.41383u + 9.56776 \\ -0.486384u^{31} + 0.379216u^{30} + \dots - 2.86928u - 0.514941 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -3.24515u^{31} + 1.67422u^{30} + \dots - 3.02690u - 4.97838 \\ 0.304612u^{31} - 0.193228u^{30} + \dots + 3.65994u - 0.679133 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 7.00844u^{31} - 0.808937u^{30} + \dots - 7.09680u + 17.1331 \\ -2.34735u^{31} - 0.0978616u^{30} + \dots - 1.67702u - 2.05955 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -3.95240u^{31} + 1.64688u^{30} + \dots - 4.21803u - 4.56877 \\ 0.349246u^{31} + 0.484634u^{30} + \dots + 0.455964u - 1.58467 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -2.33177u^{31} + 0.938856u^{30} + \dots + 3.06552u - 9.72970 \\ 2.18533u^{31} - 0.590773u^{30} + \dots + 3.26730u + 2.12120 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -8.37149u^{31} + 5.01296u^{30} + \dots - 12.6435u - 10.7929 \\ -1.24677u^{31} - 0.611740u^{30} + \dots + 8.72740u - 2.92118 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4.80290u^{31} - 0.110659u^{30} + \dots - 8.67744u + 4.28329$

(iv)  $u$ -Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{32} - 16u^{31} + \dots - 10u + 1$
$c_2$	$u^{32} - 4u^{31} + \dots - 6u + 1$
$c_3$	$u^{32} + 8u^{30} + \dots + 6u + 1$
$c_4$	$u^{32} - 2u^{30} + \dots + 2u + 1$
$c_5$	$u^{32} - 4u^{31} + \dots + 8u + 1$
$c_6$	$u^{32} + 4u^{31} + \dots + 6u + 1$
$c_7$	$u^{32} - 10u^{31} + \dots - 2u + 1$
$c_8$	$u^{32} + 6u^{31} + \dots + 4u + 1$
$c_9$	$u^{32} + 10u^{31} + \dots + 538u + 73$
$c_{10}$	$u^{32} + 10u^{31} + \dots + 2u + 1$
$c_{11}$	$u^{32} + 4u^{31} + \dots - 8u + 1$
$c_{12}$	$u^{32} + 4u^{31} + \dots - 2u + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{32} + 4y^{31} + \dots + 10y + 1$
$c_2, c_6$	$y^{32} + 16y^{31} + \dots + 10y + 1$
$c_3$	$y^{32} + 16y^{31} + \dots - 12y + 1$
$c_4$	$y^{32} - 4y^{31} + \dots - 16y + 1$
$c_5, c_{11}$	$y^{32} + 20y^{31} + \dots + 16y + 1$
$c_7, c_{10}$	$y^{32} + 18y^{31} + \dots + 22y + 1$
$c_8$	$y^{32} - 12y^{31} + \dots + 14y + 1$
$c_9$	$y^{32} - 14y^{31} + \dots + 77162y + 5329$
$c_{12}$	$y^{32} - 4y^{31} + \dots + 20y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.011430 + 0.076540I$ $a = -0.299553 - 1.057440I$ $b = 0.066450 + 1.277390I$	$1.95636 + 4.51992I$	$-2.62248 - 7.58475I$
$u = -1.011430 - 0.076540I$ $a = -0.299553 + 1.057440I$ $b = 0.066450 - 1.277390I$	$1.95636 - 4.51992I$	$-2.62248 + 7.58475I$
$u = -0.195501 + 0.960625I$ $a = -0.54851 - 1.43505I$ $b = -0.037707 - 0.482351I$	$-1.46529 - 0.97885I$	$-11.84592 - 4.46110I$
$u = -0.195501 - 0.960625I$ $a = -0.54851 + 1.43505I$ $b = -0.037707 + 0.482351I$	$-1.46529 + 0.97885I$	$-11.84592 + 4.46110I$
$u = 0.963349 + 0.082588I$ $a = 0.874463 + 0.489100I$ $b = -1.056860 - 0.880917I$	$0.52518 - 1.70904I$	$1.303152 + 0.227505I$
$u = 0.963349 - 0.082588I$ $a = 0.874463 - 0.489100I$ $b = -1.056860 + 0.880917I$	$0.52518 + 1.70904I$	$1.303152 - 0.227505I$
$u = 0.897933 + 0.134537I$ $a = -0.079600 - 1.057370I$ $b = -0.417549 + 0.423958I$	$-1.93841 - 3.89093I$	$-2.89352 + 9.56275I$
$u = 0.897933 - 0.134537I$ $a = -0.079600 + 1.057370I$ $b = -0.417549 - 0.423958I$	$-1.93841 + 3.89093I$	$-2.89352 - 9.56275I$
$u = -0.790801 + 0.178174I$ $a = -1.07264 + 1.31010I$ $b = 0.144360 - 0.486258I$	$-1.66071 - 1.88565I$	$0.611617 + 0.405112I$
$u = -0.790801 - 0.178174I$ $a = -1.07264 - 1.31010I$ $b = 0.144360 + 0.486258I$	$-1.66071 + 1.88565I$	$0.611617 - 0.405112I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.725473 + 0.306578I$ $a = 2.59490 + 0.04955I$ $b = -1.370940 - 0.282852I$	$-0.233393 + 0.291097I$	$-5.20473 + 2.81677I$
$u = 0.725473 - 0.306578I$ $a = 2.59490 - 0.04955I$ $b = -1.370940 + 0.282852I$	$-0.233393 - 0.291097I$	$-5.20473 - 2.81677I$
$u = -0.358787 + 1.159020I$ $a = 0.506557 + 0.930883I$ $b = -0.576105 + 0.212433I$	$7.03446 - 10.43960I$	$3.24799 + 7.92017I$
$u = -0.358787 - 1.159020I$ $a = 0.506557 - 0.930883I$ $b = -0.576105 - 0.212433I$	$7.03446 + 10.43960I$	$3.24799 - 7.92017I$
$u = -1.236250 + 0.423599I$ $a = -1.23017 + 0.89428I$ $b = 1.08185 - 1.47183I$	$4.04750 - 6.51115I$	$7.4827 + 17.7604I$
$u = -1.236250 - 0.423599I$ $a = -1.23017 - 0.89428I$ $b = 1.08185 + 1.47183I$	$4.04750 + 6.51115I$	$7.4827 - 17.7604I$
$u = 0.754987 + 1.099260I$ $a = -0.851878 + 0.547278I$ $b = 0.676413 + 0.328413I$	$8.54048 + 4.66147I$	$5.60896 - 3.18468I$
$u = 0.754987 - 1.099260I$ $a = -0.851878 - 0.547278I$ $b = 0.676413 - 0.328413I$	$8.54048 - 4.66147I$	$5.60896 + 3.18468I$
$u = -0.541157 + 0.373122I$ $a = -0.611032 - 0.446290I$ $b = 1.48390 - 0.85410I$	$2.56066 - 1.39415I$	$8.59786 - 1.04596I$
$u = -0.541157 - 0.373122I$ $a = -0.611032 + 0.446290I$ $b = 1.48390 + 0.85410I$	$2.56066 + 1.39415I$	$8.59786 + 1.04596I$



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.078990 + 0.816307I$ $a = 1.071980 - 0.021161I$ $b = -1.00062 - 1.06785I$	$0.04554 + 9.55039I$	$0.17757 - 7.82747I$
$u = 1.078990 - 0.816307I$ $a = 1.071980 + 0.021161I$ $b = -1.00062 + 1.06785I$	$0.04554 - 9.55039I$	$0.17757 + 7.82747I$
$u = 0.349670 + 0.386213I$ $a = -0.448966 - 0.257825I$ $b = 1.82694 + 1.31311I$	$3.77595 + 1.55640I$	$-10.9090 - 16.7964I$
$u = 0.349670 - 0.386213I$ $a = -0.448966 + 0.257825I$ $b = 1.82694 - 1.31311I$	$3.77595 - 1.55640I$	$-10.9090 + 16.7964I$
$u = 1.21893 + 0.86163I$ $a = -0.997262 - 0.051859I$ $b = 0.766581 + 0.643238I$	$7.91161 + 4.63893I$	$7.21423 - 8.93330I$
$u = 1.21893 - 0.86163I$ $a = -0.997262 + 0.051859I$ $b = 0.766581 - 0.643238I$	$7.91161 - 4.63893I$	$7.21423 + 8.93330I$
$u = -1.27730 + 0.81643I$ $a = -0.841795 + 0.203609I$ $b = 0.93799 - 1.07457I$	$2.06970 - 6.21261I$	$-3.30852 + 0.I$
$u = -1.27730 - 0.81643I$ $a = -0.841795 - 0.203609I$ $b = 0.93799 + 1.07457I$	$2.06970 + 6.21261I$	$-3.30852 + 0.I$
$u = -0.435914 + 0.191346I$ $a = 3.01618 - 0.43588I$ $b = -0.516431 - 0.791322I$	$1.57422 - 2.11475I$	$0.389556 + 1.338497I$
$u = -0.435914 - 0.191346I$ $a = 3.01618 + 0.43588I$ $b = -0.516431 + 0.791322I$	$1.57422 + 2.11475I$	$0.389556 - 1.338497I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.14221 + 1.69421I$		
$a = -0.082679 - 0.594170I$	$1.44470 + 2.66235I$	$7.15055 - 3.68105I$
$b = -0.008276 - 0.433413I$		
$u = -0.14221 - 1.69421I$		
$a = -0.082679 + 0.594170I$	$1.44470 - 2.66235I$	$7.15055 + 3.68105I$
$b = -0.008276 + 0.433413I$		

$$\text{II. } I_2^u = \langle -u^3 + u^2 + 4b - 5u + 2, a, u^4 - u^3 + 5u^2 - 2u + 4 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ \frac{1}{4}u^3 - \frac{1}{4}u^2 + \frac{5}{4}u - \frac{1}{2} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{4}u^3 - \frac{1}{4}u^2 + \frac{5}{4}u - \frac{1}{2} \\ \frac{1}{4}u^3 - \frac{1}{4}u^2 + \frac{5}{4}u - \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{4}u^3 + \frac{1}{4}u^2 - \frac{5}{4}u + \frac{1}{2} \\ -\frac{1}{4}u^3 + \frac{1}{4}u^2 - \frac{5}{4}u + \frac{1}{2} \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{1}{8}u^3 + \frac{1}{8}u^2 + \frac{3}{8}u + 1 \\ \frac{1}{8}u^3 - \frac{1}{8}u^2 + \frac{3}{8}u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{4}u^3 + \frac{1}{4}u^2 - \frac{5}{4}u + \frac{1}{2} \\ -\frac{1}{4}u^3 + \frac{1}{4}u^2 - \frac{5}{4}u + \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{4}u^3 - \frac{1}{4}u^2 + \frac{5}{4}u - \frac{1}{2} \\ \frac{1}{4}u^3 - \frac{1}{4}u^2 + \frac{9}{4}u - \frac{1}{2} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{8}u^3 - \frac{1}{8}u^2 - \frac{3}{8}u \\ -\frac{1}{8}u^3 - \frac{9}{8}u^2 - \frac{3}{8}u - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{4}u^2 + \frac{1}{4}u + \frac{3}{4} \\ -\frac{3}{4}u^2 + \frac{5}{4}u - \frac{5}{4} \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -\frac{103}{32}u^3 + \frac{223}{32}u^2 - \frac{279}{32}u + \frac{21}{16}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$(u^2 - u + 1)^2$
$c_2$	$(u^2 + u + 1)^2$
$c_3$	$4(4u^4 - 6u^3 + 11u^2 - 6u + 1)$
$c_4$	$u^4 - u^3 + 5u^2 - 2u + 4$
$c_5$	$4(4u^4 + 2u^3 + 5u^2 + u + 1)$
$c_7, c_8$	$(u - 1)^4$
$c_9$	$u^4$
$c_{10}$	$(u + 1)^4$
$c_{11}, c_{12}$	$4(4u^4 - 2u^3 + 5u^2 - u + 1)$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$	$(y^2 + y + 1)^2$
$c_3$	$16(16y^4 + 52y^3 + 57y^2 - 14y + 1)$
$c_4$	$y^4 + 9y^3 + 29y^2 + 36y + 16$
$c_5, c_{11}, c_{12}$	$16(16y^4 + 36y^3 + 29y^2 + 9y + 1)$
$c_7, c_8, c_{10}$	$(y - 1)^4$
$c_9$	$y^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.175835 + 1.026610I$		
$a = 0$	$-1.64493 + 2.02988I$	$-5.57770 - 3.25874I$
$b = -0.162083 + 0.946318I$		
$u = 0.175835 - 1.026610I$		
$a = 0$	$-1.64493 - 2.02988I$	$-5.57770 + 3.25874I$
$b = -0.162083 - 0.946318I$		
$u = 0.32417 + 1.89264I$		
$a = 0$	$-1.64493 - 2.02988I$	$-14.6411 + 11.9508I$
$b = -0.087917 + 0.513305I$		
$u = 0.32417 - 1.89264I$		
$a = 0$	$-1.64493 + 2.02988I$	$-14.6411 - 11.9508I$
$b = -0.087917 - 0.513305I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^2)(u^{32} - 16u^{31} + \dots - 10u + 1)$
$c_2$	$((u^2 + u + 1)^2)(u^{32} - 4u^{31} + \dots - 6u + 1)$
$c_3$	$4(4u^4 - 6u^3 + \dots - 6u + 1)(u^{32} + 8u^{30} + \dots + 6u + 1)$
$c_4$	$(u^4 - u^3 + 5u^2 - 2u + 4)(u^{32} - 2u^{30} + \dots + 2u + 1)$
$c_5$	$4(4u^4 + 2u^3 + \dots + u + 1)(u^{32} - 4u^{31} + \dots + 8u + 1)$
$c_6$	$((u^2 - u + 1)^2)(u^{32} + 4u^{31} + \dots + 6u + 1)$
$c_7$	$((u - 1)^4)(u^{32} - 10u^{31} + \dots - 2u + 1)$
$c_8$	$((u - 1)^4)(u^{32} + 6u^{31} + \dots + 4u + 1)$
$c_9$	$u^4(u^{32} + 10u^{31} + \dots + 538u + 73)$
$c_{10}$	$((u + 1)^4)(u^{32} + 10u^{31} + \dots + 2u + 1)$
$c_{11}$	$4(4u^4 - 2u^3 + \dots - u + 1)(u^{32} + 4u^{31} + \dots - 8u + 1)$
$c_{12}$	$4(4u^4 - 2u^3 + \dots - u + 1)(u^{32} + 4u^{31} + \dots - 2u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^2)(y^{32} + 4y^{31} + \dots + 10y + 1)$
$c_2, c_6$	$((y^2 + y + 1)^2)(y^{32} + 16y^{31} + \dots + 10y + 1)$
$c_3$	$16(16y^4 + 52y^3 + \dots - 14y + 1)(y^{32} + 16y^{31} + \dots - 12y + 1)$
$c_4$	$(y^4 + 9y^3 + 29y^2 + 36y + 16)(y^{32} - 4y^{31} + \dots - 16y + 1)$
$c_5, c_{11}$	$16(16y^4 + 36y^3 + \dots + 9y + 1)(y^{32} + 20y^{31} + \dots + 16y + 1)$
$c_7, c_{10}$	$((y - 1)^4)(y^{32} + 18y^{31} + \dots + 22y + 1)$
$c_8$	$((y - 1)^4)(y^{32} - 12y^{31} + \dots + 14y + 1)$
$c_9$	$y^4(y^{32} - 14y^{31} + \dots + 77162y + 5329)$
$c_{12}$	$16(16y^4 + 36y^3 + \dots + 9y + 1)(y^{32} - 4y^{31} + \dots + 20y + 1)$