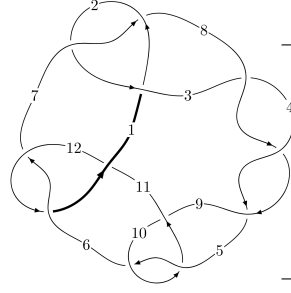
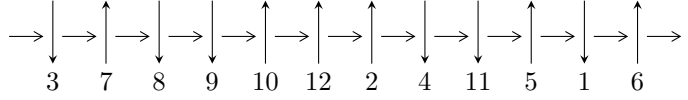


12a<sub>0503</sub> (K12a<sub>0503</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,8 \xrightarrow{c_7} 7 \xrightarrow{c_2} 3 \xrightarrow{c_3} 4 \xrightarrow{c_8} 9 \xrightarrow{c_4} 5 \xrightarrow{c_1} 1,12 \xrightarrow{c_6} 6 \xrightarrow{c_{11}} 11 \xrightarrow{c_{10}} 10 \twoheadrightarrow c_5, c_9, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -u^5 - 2u^3 + b + 1, u^5 + u^3 + a - 1, u^7 + 2u^5 + 2u^3 - u^2 - u - 1 \rangle$$

$$I_2^u = \langle -u^{15} - 5u^{13} - u^{12} - 12u^{11} - 4u^{10} - 15u^9 - 8u^8 - 10u^7 - 8u^6 - 2u^5 - 5u^4 + u^3 - 2u^2 + b - 1, \\ u^{15} + 2u^{14} + 5u^{13} + 9u^{12} + 12u^{11} + 19u^{10} + 15u^9 + 19u^8 + 10u^7 + 8u^6 + 2u^5 - 2u^4 - u^2 + a + 2u, \\ u^{16} + u^{15} + 5u^{14} + 5u^{13} + 12u^{12} + 12u^{11} + 15u^{10} + 15u^9 + 10u^8 + 10u^7 + 2u^6 + 2u^5 + u^2 + 1 \rangle$$

$$I_3^u = \langle -u^{15} + 2u^{14} - 7u^{13} + 9u^{12} - 18u^{11} + 16u^{10} - 21u^9 + 12u^8 - 8u^7 + 2u^6 + 4u^5 - u^4 + 2u^3 + 2u^2 + b - 3u + \\ - u^{15} - 3u^{13} - 2u^{12} - 2u^{11} - 6u^{10} + 3u^9 - 6u^8 + 4u^7 + 4u^4 - 2u^3 + 2u^2 + 2a + u - 1, \\ u^{16} - 2u^{15} + 7u^{14} - 10u^{13} + 18u^{12} - 20u^{11} + 21u^{10} - 18u^9 + 8u^8 - 4u^7 - 4u^6 + 4u^5 - 2u^4 + 3u^2 - 3u + 2 \rangle$$

$$I_4^u = \langle u^{15} + 3u^{13} + 4u^{11} - u^9 - 4u^7 - 4u^5 + u^3 + b - 1, -u^{15} - 3u^{13} - 4u^{11} + u^9 + 4u^7 + 4u^5 - 2u^3 + a + 1, \\ u^{16} + u^{15} + 5u^{14} + 5u^{13} + 12u^{12} + 12u^{11} + 15u^{10} + 15u^9 + 10u^8 + 10u^7 + 2u^6 + 2u^5 + u^2 + 1 \rangle$$

$$I_5^u = \langle b + u - 1, a - u + 2, u^2 - u + 1 \rangle$$

$$I_6^u = \langle u^5 - u^2a + 2u^3 - u^2 + b - a + u - 1, -2u^5a - u^5 - 4u^3a + u^4 + 2u^2a - 2u^3 + a^2 - au + 4u^2 + 2a - 2u + 2, \\ u^6 + 2u^4 - u^3 + u^2 - u - 1 \rangle$$

$$I_7^u = \langle b - u - 1, a + 2u + 1, u^2 + 1 \rangle$$

\* 7 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 71 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -u^5 - 2u^3 + b + 1, u^5 + u^3 + a - 1, u^7 + 2u^5 + 2u^3 - u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^6 - u^4 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^5 + u^4 - u^3 + u^2 - u \\ u^5 - u^4 + u^3 - 2u^2 - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^5 - u^3 + 1 \\ u^5 + 2u^3 - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^6 - u^4 + u + 1 \\ u^6 + 2u^4 + u^2 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3 + 1 \\ u^3 + u^2 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^6 + u^5 - u^4 - u^2 + 1 \\ u^6 - u^5 + u^4 - u^3 + u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-6u^6 - 6u^4 - 6u^2 + 6u + 6$

(iv) u-Polynomials at the component

| Crossings                                | u-Polynomials at each crossing            |
|--|---|
| $c_1, c_9, c_{11}$                       | $u^7 + 4u^6 + 8u^5 + 6u^4 - 5u^2 - u - 1$ |
| $c_2, c_5, c_6$<br>$c_7, c_{10}, c_{12}$ | $u^7 + 2u^5 + 2u^3 + u^2 - u + 1$         |
| $c_3, c_4, c_8$                          | $u^7 - 5u^5 - 2u^4 + 7u^3 + 4u^2 + 4$     |

(v) Riley Polynomials at the component

| Crossings                                | Riley Polynomials at each crossing               |
|--|--|
| $c_1, c_9, c_{11}$                       | $y^7 + 16y^5 + 2y^4 + 52y^3 - 13y^2 - 9y - 1$    |
| $c_2, c_5, c_6$<br>$c_7, c_{10}, c_{12}$ | $y^7 + 4y^6 + 8y^5 + 6y^4 - 5y^2 - y - 1$        |
| $c_3, c_4, c_8$                          | $y^7 - 10y^6 + 39y^5 - 74y^4 + 65y^3 - 32y - 16$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = 0.863824$<br>$a = -0.125557$<br>$b = 0.770135$                                      | -4.43886                              | 0.872100               |
| $u = -0.506221 + 1.104710I$<br>$a = 1.49617 + 1.94571I$<br>$b = 0.22746 - 2.44461I$      | $-5.20269 - 11.20360I$                | $-5.65627 + 10.71805I$ |
| $u = -0.506221 - 1.104710I$<br>$a = 1.49617 - 1.94571I$<br>$b = 0.22746 + 2.44461I$      | $-5.20269 + 11.20360I$                | $-5.65627 - 10.71805I$ |
| $u = -0.426442 + 0.491723I$<br>$a = 0.719469 - 0.043211I$<br>$b = -0.487688 + 0.192580I$ | $0.805836 - 1.099860I$                | $4.64625 + 4.74954I$   |
| $u = -0.426442 - 0.491723I$<br>$a = 0.719469 + 0.043211I$<br>$b = -0.487688 - 0.192580I$ | $0.805836 + 1.099860I$                | $4.64625 - 4.74954I$   |
| $u = 0.500751 + 1.264820I$<br>$a = -1.15286 + 2.51108I$<br>$b = -1.12484 - 3.58304I$     | $-15.5903 + 14.7635I$                 | $-8.42603 - 8.80481I$  |
| $u = 0.500751 - 1.264820I$<br>$a = -1.15286 - 2.51108I$<br>$b = -1.12484 + 3.58304I$     | $-15.5903 - 14.7635I$                 | $-8.42603 + 8.80481I$  |

**II.**

$$I_2^u = \langle -u^{15} - 5u^{13} + \dots + b - 1, u^{15} + 2u^{14} + \dots + a + 2u, u^{16} + u^{15} + \dots + u^2 + 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^6 - u^4 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^9 + 2u^7 + u^5 - 2u^3 - u \\ -u^9 - 3u^7 - 3u^5 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{15} - 2u^{14} + \dots + u^2 - 2u \\ u^{15} + 5u^{13} + \dots + 2u^2 + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{15} + 3u^{13} + 3u^{11} - 3u^9 - 6u^7 - 2u^5 + 3u^3 + u - 1 \\ u^{11} + 3u^9 + 4u^7 + u^5 - u^3 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{15} - 2u^{14} + \dots + u^4 - u \\ u^8 + 2u^6 + 2u^4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{15} - 2u^{14} + \dots - u^2 - u \\ -u^{10} - 2u^8 - u^6 + 2u^4 + u^2 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =**  $-4u^{14} - 4u^{13} - 16u^{12} - 20u^{11} - 32u^{10} - 44u^9 - 28u^8 - 44u^7 - 12u^6 - 12u^5 + 4u^4 + 12u^3 - 4u^2 + 4u - 6$

(iv) u-Polynomials at the component

| Crossings                   | u-Polynomials at each crossing       |
|-----------------------------|--------------------------------------|
| $c_1, c_9$                  | $u^{16} + 9u^{15} + \dots + 2u + 1$  |
| $c_2, c_5, c_7$<br>$c_{10}$ | $u^{16} - u^{15} + \dots + u^2 + 1$  |
| $c_3, c_4, c_8$             | $u^{16} - 2u^{15} + \dots - u + 2$   |
| $c_6, c_{12}$               | $u^{16} + 2u^{15} + \dots + 3u + 2$  |
| $c_{11}$                    | $u^{16} + 10u^{15} + \dots + 3u + 4$ |

(v) Riley Polynomials at the component

| Crossings                   | Riley Polynomials at each crossing    |
|-----------------------------|---------------------------------------|
| $c_1, c_9$                  | $y^{16} - 3y^{15} + \dots - 2y + 1$   |
| $c_2, c_5, c_7$<br>$c_{10}$ | $y^{16} + 9y^{15} + \dots + 2y + 1$   |
| $c_3, c_4, c_8$             | $y^{16} - 18y^{15} + \dots + 19y + 4$ |
| $c_6, c_{12}$               | $y^{16} + 10y^{15} + \dots + 3y + 4$  |
| $c_{11}$                    | $y^{16} - 10y^{15} + \dots - y + 16$  |



(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.892953 + 0.035958I$<br>$a = -0.652536 + 1.200890I$<br>$b = 0.02318 + 2.24381I$   | $-8.19036 + 4.73480I$                 | $-2.47201 - 3.02289I$ |
| $u = -0.892953 - 0.035958I$<br>$a = -0.652536 - 1.200890I$<br>$b = 0.02318 - 2.24381I$   | $-8.19036 - 4.73480I$                 | $-2.47201 + 3.02289I$ |
| $u = -0.458901 + 0.734878I$<br>$a = -0.104273 - 0.435411I$<br>$b = 0.247757 + 0.757374I$ | $0.85997 - 1.95072I$                  | $3.06114 + 4.17042I$  |
| $u = -0.458901 - 0.734878I$<br>$a = -0.104273 + 0.435411I$<br>$b = 0.247757 - 0.757374I$ | $0.85997 + 1.95072I$                  | $3.06114 - 4.17042I$  |
| $u = -0.379593 + 1.079580I$<br>$a = -0.56037 - 2.03187I$<br>$b = -1.36347 + 1.32712I$    | $-7.04324 - 3.37292I$                 | $-8.93248 + 5.20888I$ |
| $u = -0.379593 - 1.079580I$<br>$a = -0.56037 + 2.03187I$<br>$b = -1.36347 - 1.32712I$    | $-7.04324 + 3.37292I$                 | $-8.93248 - 5.20888I$ |
| $u = 0.469252 + 1.053160I$<br>$a = -0.371270 - 0.561834I$<br>$b = 0.161095 + 0.362888I$  | $-2.68724 + 6.60937I$                 | $-2.51664 - 7.40663I$ |
| $u = 0.469252 - 1.053160I$<br>$a = -0.371270 + 0.561834I$<br>$b = 0.161095 - 0.362888I$  | $-2.68724 - 6.60937I$                 | $-2.51664 + 7.40663I$ |
| $u = 0.190701 + 0.810384I$<br>$a = 0.33485 - 2.32194I$<br>$b = 0.569648 + 0.391218I$     | $-3.86698 + 1.08438I$                 | $-3.75949 - 5.90127I$ |
| $u = 0.190701 - 0.810384I$<br>$a = 0.33485 + 2.32194I$<br>$b = 0.569648 - 0.391218I$     | $-3.86698 - 1.08438I$                 | $-3.75949 + 5.90127I$ |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.487539 + 1.254270I$ |                                       |                       |
| $a = 0.652357 - 0.643137I$  | $-11.8837 - 9.6751I$                  | $-5.50822 + 5.97678I$ |
| $b = -0.736189 + 0.110556I$ |                                       |                       |
| $u = -0.487539 - 1.254270I$ |                                       |                       |
| $a = 0.652357 + 0.643137I$  | $-11.8837 + 9.6751I$                  | $-5.50822 - 5.97678I$ |
| $b = -0.736189 - 0.110556I$ |                                       |                       |
| $u = 0.469746 + 1.263010I$  |                                       |                       |
| $a = 0.70256 - 1.98263I$    | $-16.0195 + 4.8597I$                  | $-9.14726 - 3.11789I$ |
| $b = 1.83074 + 2.27175I$    |                                       |                       |
| $u = 0.469746 - 1.263010I$  |                                       |                       |
| $a = 0.70256 + 1.98263I$    | $-16.0195 - 4.8597I$                  | $-9.14726 + 3.11789I$ |
| $b = 1.83074 - 2.27175I$    |                                       |                       |
| $u = 0.589289 + 0.270476I$  |                                       |                       |
| $a = 0.998682 + 0.324734I$  | $-0.51702 - 2.45923I$                 | $1.27496 + 3.25382I$  |
| $b = -0.232766 + 1.375450I$ |                                       |                       |
| $u = 0.589289 - 0.270476I$  |                                       |                       |
| $a = 0.998682 - 0.324734I$  | $-0.51702 + 2.45923I$                 | $1.27496 - 3.25382I$  |
| $b = -0.232766 - 1.375450I$ |                                       |                       |

**III.**

$$I_3^u = \langle -u^{15} + 2u^{14} + \dots + b + 3, -u^{15} - 3u^{13} + \dots + 2a - 1, u^{16} - 2u^{15} + \dots - 3u + 2 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^6 - u^4 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^9 + 2u^7 + u^5 - 2u^3 - u \\ -u^9 - 3u^7 - 3u^5 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}u^{15} + \frac{3}{2}u^{13} + \dots - \frac{1}{2}u + \frac{1}{2} \\ u^{15} - 2u^{14} + \dots + 3u - 3 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{2}u^{15} + 2u^{14} + \dots - \frac{3}{2}u + \frac{3}{2} \\ u^{15} - 2u^{14} + \dots + 2u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{2}u^{15} - 2u^{14} + \dots + \frac{5}{2}u - \frac{3}{2} \\ -u^{15} + 2u^{14} + \dots - 2u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{1}{2}u^{15} - \frac{3}{2}u^{13} + \dots + \frac{1}{2}u + \frac{1}{2} \\ -u^{15} + 2u^{14} + \dots - 2u + 3 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =  $4u^{13} + 16u^{11} + 24u^9 + 4u^7 - 20u^5 - 12u^3 + 4u - 6$**

(iv) u-Polynomials at the component

| Crossings                      | u-Polynomials at each crossing       |
|--------------------------------|--------------------------------------|
| $c_1$                          | $u^{16} + 10u^{15} + \dots + 3u + 4$ |
| $c_2, c_7$                     | $u^{16} + 2u^{15} + \dots + 3u + 2$  |
| $c_3, c_4, c_8$                | $u^{16} - 2u^{15} + \dots - u + 2$   |
| $c_5, c_6, c_{10}$<br>$c_{12}$ | $u^{16} - u^{15} + \dots + u^2 + 1$  |
| $c_9, c_{11}$                  | $u^{16} + 9u^{15} + \dots + 2u + 1$  |

(v) Riley Polynomials at the component

| Crossings                      | Riley Polynomials at each crossing    |
|--------------------------------|---------------------------------------|
| $c_1$                          | $y^{16} - 10y^{15} + \dots - y + 16$  |
| $c_2, c_7$                     | $y^{16} + 10y^{15} + \dots + 3y + 4$  |
| $c_3, c_4, c_8$                | $y^{16} - 18y^{15} + \dots + 19y + 4$ |
| $c_5, c_6, c_{10}$<br>$c_{12}$ | $y^{16} + 9y^{15} + \dots + 2y + 1$   |
| $c_9, c_{11}$                  | $y^{16} - 3y^{15} + \dots - 2y + 1$   |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.402991 + 0.968083I$ |                                       |                       |
| $a = 0.222795 - 0.609931I$  | $-0.51702 - 2.45923I$                 | $1.27496 + 3.25382I$  |
| $b = -0.059233 + 0.569202I$ |                                       |                       |
| $u = -0.402991 - 0.968083I$ |                                       |                       |
| $a = 0.222795 + 0.609931I$  | $-0.51702 + 2.45923I$                 | $1.27496 - 3.25382I$  |
| $b = -0.059233 - 0.569202I$ |                                       |                       |
| $u = 0.921586 + 0.049492I$  |                                       |                       |
| $a = 0.594426 + 1.196160I$  | $-11.8837 - 9.6751I$                  | $-5.50822 + 5.97678I$ |
| $b = -0.09325 + 2.32148I$   |                                       |                       |
| $u = 0.921586 - 0.049492I$  |                                       |                       |
| $a = 0.594426 - 1.196160I$  | $-11.8837 + 9.6751I$                  | $-5.50822 - 5.97678I$ |
| $b = -0.09325 - 2.32148I$   |                                       |                       |
| $u = 0.059705 + 1.152710I$  |                                       |                       |
| $a = 0.23551 - 1.67559I$    | $-3.86698 - 1.08438I$                 | $-3.75949 + 5.90127I$ |
| $b = 0.10924 + 1.44246I$    |                                       |                       |
| $u = 0.059705 - 1.152710I$  |                                       |                       |
| $a = 0.23551 + 1.67559I$    | $-3.86698 + 1.08438I$                 | $-3.75949 - 5.90127I$ |
| $b = 0.10924 - 1.44246I$    |                                       |                       |
| $u = -0.270509 + 1.207500I$ |                                       |                       |
| $a = -0.55626 - 1.86816I$   | $-7.04324 + 3.37292I$                 | $-8.93248 - 5.20888I$ |
| $b = -0.82968 + 1.87098I$   |                                       |                       |
| $u = -0.270509 - 1.207500I$ |                                       |                       |
| $a = -0.55626 + 1.86816I$   | $-7.04324 - 3.37292I$                 | $-8.93248 + 5.20888I$ |
| $b = -0.82968 - 1.87098I$   |                                       |                       |
| $u = -0.724264 + 0.230405I$ |                                       |                       |
| $a = -0.784571 + 0.654294I$ | $-2.68724 + 6.60937I$                 | $-2.51664 - 7.40663I$ |
| $b = 0.31772 + 1.62349I$    |                                       |                       |
| $u = -0.724264 - 0.230405I$ |                                       |                       |
| $a = -0.784571 - 0.654294I$ | $-2.68724 - 6.60937I$                 | $-2.51664 + 7.40663I$ |
| $b = 0.31772 - 1.62349I$    |                                       |                       |

| Solutions to $I_3^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.507077 + 0.543596I$  | $0.85997 - 1.95072I$                  | $3.06114 + 4.17042I$  |
| $a = 0.458679 - 0.248786I$  |                                       |                       |
| $b = -0.339347 + 0.997289I$ |                                       |                       |
| $u = 0.507077 - 0.543596I$  | $0.85997 + 1.95072I$                  | $3.06114 - 4.17042I$  |
| $a = 0.458679 + 0.248786I$  |                                       |                       |
| $b = -0.339347 - 0.997289I$ |                                       |                       |
| $u = 0.465530 + 1.245910I$  | $-8.19036 + 4.73480I$                 | $-2.47201 - 3.02289I$ |
| $a = -0.629795 - 0.668340I$ |                                       |                       |
| $b = 0.723472 + 0.198002I$  |                                       |                       |
| $u = 0.465530 - 1.245910I$  | $-8.19036 - 4.73480I$                 | $-2.47201 + 3.02289I$ |
| $a = -0.629795 + 0.668340I$ |                                       |                       |
| $b = 0.723472 - 0.198002I$  |                                       |                       |
| $u = 0.443866 + 1.287090I$  | $-16.0195 - 4.8597I$                  | $-9.14726 + 3.11789I$ |
| $a = 0.70921 - 1.95738I$    |                                       |                       |
| $b = 1.67108 + 2.40426I$    |                                       |                       |
| $u = 0.443866 - 1.287090I$  | $-16.0195 + 4.8597I$                  | $-9.14726 - 3.11789I$ |
| $a = 0.70921 + 1.95738I$    |                                       |                       |
| $b = 1.67108 - 2.40426I$    |                                       |                       |

$$\text{IV. } I_4^u = \langle u^{15} + 3u^{13} + 4u^{11} - u^9 - 4u^7 - 4u^5 + u^3 + b - 1, -u^{15} - 3u^{13} + \dots + a + 1, u^{16} + u^{15} + \dots + u^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^6 - u^4 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^9 + 2u^7 + u^5 - 2u^3 - u \\ -u^9 - 3u^7 - 3u^5 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{15} + 3u^{13} + 4u^{11} - u^9 - 4u^7 - 4u^5 + 2u^3 - 1 \\ -u^{15} - 3u^{13} - 4u^{11} + u^9 + 4u^7 + 4u^5 - u^3 + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^{15} - 2u^{14} + \dots - u^2 - u \\ u^{15} + 2u^{14} + \dots + u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{15} + 3u^{13} + 4u^{11} - u^9 - 4u^7 - 3u^5 + 2u^3 - 1 \\ -u^{15} - 3u^{13} - 4u^{11} + u^9 + 5u^7 + 5u^5 + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^{15} + 3u^{13} + 4u^{11} - u^{10} - u^9 - 3u^8 - 4u^7 - 4u^6 - 4u^5 - u^4 + u^3 + u^2 - u \\ 2u^{13} + 8u^{11} + \dots - u + 2 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -4u^{14} - 4u^{13} - 16u^{12} - 20u^{11} - 32u^{10} - 44u^9 - 28u^8 - 44u^7 - 12u^6 - 12u^5 + 4u^4 + 12u^3 - 4u^2 + 4u - 6$$



(iv) u-Polynomials at the component

| Crossings                   | u-Polynomials at each crossing       |
|-----------------------------|--------------------------------------|
| $c_1, c_{11}$               | $u^{16} + 9u^{15} + \dots + 2u + 1$  |
| $c_2, c_6, c_7$<br>$c_{12}$ | $u^{16} - u^{15} + \dots + u^2 + 1$  |
| $c_3, c_4, c_8$             | $u^{16} - 2u^{15} + \dots - u + 2$   |
| $c_5, c_{10}$               | $u^{16} + 2u^{15} + \dots + 3u + 2$  |
| $c_9$                       | $u^{16} + 10u^{15} + \dots + 3u + 4$ |

(v) Riley Polynomials at the component

| Crossings                   | Riley Polynomials at each crossing    |
|-----------------------------|---------------------------------------|
| $c_1, c_{11}$               | $y^{16} - 3y^{15} + \dots - 2y + 1$   |
| $c_2, c_6, c_7$<br>$c_{12}$ | $y^{16} + 9y^{15} + \dots + 2y + 1$   |
| $c_3, c_4, c_8$             | $y^{16} - 18y^{15} + \dots + 19y + 4$ |
| $c_5, c_{10}$               | $y^{16} + 10y^{15} + \dots + 3y + 4$  |
| $c_9$                       | $y^{16} - 10y^{15} + \dots - y + 16$  |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_4^u$         | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|------------------------------|---------------------------------------|-----------------------|
| $u = -0.892953 + 0.035958I$  |                                       |                       |
| $a = 0.1015470 + 0.0314751I$ | $-8.19036 + 4.73480I$                 | $-2.47201 - 3.02289I$ |
| $b = -0.810093 + 0.054493I$  |                                       |                       |
| $u = -0.892953 - 0.035958I$  |                                       |                       |
| $a = 0.1015470 - 0.0314751I$ | $-8.19036 - 4.73480I$                 | $-2.47201 + 3.02289I$ |
| $b = -0.810093 - 0.054493I$  |                                       |                       |
| $u = -0.458901 + 0.734878I$  |                                       |                       |
| $a = 1.317400 + 0.329697I$   | $0.85997 - 1.95072I$                  | $3.06114 + 4.17042I$  |
| $b = -0.670552 - 0.262290I$  |                                       |                       |
| $u = -0.458901 - 0.734878I$  |                                       |                       |
| $a = 1.317400 - 0.329697I$   | $0.85997 + 1.95072I$                  | $3.06114 - 4.17042I$  |
| $b = -0.670552 + 0.262290I$  |                                       |                       |
| $u = -0.379593 + 1.079580I$  |                                       |                       |
| $a = 2.22885 + 2.07396I$     | $-7.04324 - 3.37292I$                 | $-8.93248 + 5.20888I$ |
| $b = -0.95631 - 2.86552I$    |                                       |                       |
| $u = -0.379593 - 1.079580I$  |                                       |                       |
| $a = 2.22885 - 2.07396I$     | $-7.04324 + 3.37292I$                 | $-8.93248 - 5.20888I$ |
| $b = -0.95631 + 2.86552I$    |                                       |                       |
| $u = 0.469252 + 1.053160I$   |                                       |                       |
| $a = -1.74058 + 1.75441I$    | $-2.68724 + 6.60937I$                 | $-2.51664 - 7.40663I$ |
| $b = 0.28250 - 2.22682I$     |                                       |                       |
| $u = 0.469252 - 1.053160I$   |                                       |                       |
| $a = -1.74058 - 1.75441I$    | $-2.68724 - 6.60937I$                 | $-2.51664 + 7.40663I$ |
| $b = 0.28250 + 2.22682I$     |                                       |                       |
| $u = 0.190701 + 0.810384I$   |                                       |                       |
| $a = -2.50371 - 1.26517I$    | $-3.86698 + 1.08438I$                 | $-3.75949 - 5.90127I$ |
| $b = 2.13493 + 0.82139I$     |                                       |                       |
| $u = 0.190701 - 0.810384I$   |                                       |                       |
| $a = -2.50371 + 1.26517I$    | $-3.86698 - 1.08438I$                 | $-3.75949 + 5.90127I$ |
| $b = 2.13493 - 0.82139I$     |                                       |                       |

| Solutions to $I_4^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.487539 + 1.254270I$ |                                       |                       |
| $a = 1.21664 + 2.51902I$    | $-11.8837 - 9.6751I$                  | $-5.50822 + 5.97678I$ |
| $b = 0.96843 - 3.59781I$    |                                       |                       |
| $u = -0.487539 - 1.254270I$ |                                       |                       |
| $a = 1.21664 - 2.51902I$    | $-11.8837 + 9.6751I$                  | $-5.50822 - 5.97678I$ |
| $b = 0.96843 + 3.59781I$    |                                       |                       |
| $u = 0.469746 + 1.263010I$  |                                       |                       |
| $a = -1.23893 + 2.59409I$   | $-16.0195 + 4.8597I$                  | $-9.14726 - 3.11789I$ |
| $b = -0.90542 - 3.77274I$   |                                       |                       |
| $u = 0.469746 - 1.263010I$  |                                       |                       |
| $a = -1.23893 - 2.59409I$   | $-16.0195 - 4.8597I$                  | $-9.14726 + 3.11789I$ |
| $b = -0.90542 + 3.77274I$   |                                       |                       |
| $u = 0.589289 + 0.270476I$  |                                       |                       |
| $a = -0.381211 + 0.088717I$ | $-0.51702 - 2.45923I$                 | $1.27496 + 3.25382I$  |
| $b = 0.456516 + 0.173272I$  |                                       |                       |
| $u = 0.589289 - 0.270476I$  |                                       |                       |
| $a = -0.381211 - 0.088717I$ | $-0.51702 + 2.45923I$                 | $1.27496 - 3.25382I$  |
| $b = 0.456516 - 0.173272I$  |                                       |                       |

$$\mathbf{V. } I_5^u = \langle b + u - 1, a - u + 2, u^2 - u + 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2 \\ u - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u - 2 \\ -u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ -u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2u - 1 \\ -2u \end{pmatrix}$$

**(ii) Obstruction class =  $-1$**

**(iii) Cusp Shapes =  $-12u + 6$**

(iv) u-Polynomials at the component

| Crossings  | u-Polynomials at each crossing |
|--|--------------------------------|
| $c_1, c_2, c_5$<br>$c_6, c_7, c_9$<br>$c_{10}, c_{11}, c_{12}$ | $u^2 + u + 1$                  |
| $c_3, c_4, c_8$  | $u^2 - u + 1$                  |

(v) Riley Polynomials at the component

| Crossings                | Riley Polynomials at each crossing |
|--------------------------|------------------------------------|
| $c_1, c_2, c_3$          | $y^2 + y + 1$                      |
| $c_4, c_5, c_6$          |                                    |
| $c_7, c_8, c_9$          |                                    |
| $c_{10}, c_{11}, c_{12}$ |                                    |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_5^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape       |
|---|---------------------------------------|------------------|
| $u = 0.500000 + 0.866025I$<br>$a = -1.50000 + 0.86603I$<br>$b = 0.500000 - 0.866025I$ | $6.08965I$                            | $0. - 10.39230I$ |
| $u = 0.500000 - 0.866025I$<br>$a = -1.50000 - 0.86603I$<br>$b = 0.500000 + 0.866025I$ | $- 6.08965I$                          | $0. + 10.39230I$ |



$$\text{VI. } I_6^u = \langle u^5 - u^2a + 2u^3 - u^2 + b - a + u - 1, -2u^5a - u^5 + \dots + 2a + 2, u^6 + 2u^4 - u^3 + u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^4 - u^3 + u^2 - u \\ u^3 + u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^4 - u^2 + 1 \\ -u^3 - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ -u^5 + u^2a - 2u^3 + u^2 + a - u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^5a + u^5 + 2u^3a - u^4 - u^2a + 2u^3 - 4u^2 - a + 2u - 1 \\ -u^3a - u^4 - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^4a - u^5 + a \\ u^4a - u^3a - u^4 + u^2a - 2u^3 - au - 2u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^5 + u^2a + 2u^3 - u^2 - u - 1 \\ u^4a - u^5 + u^2a - 4u^3 + u^2 + a - 2u + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

| Crossings                                | u-Polynomials at each crossing                |
|--|---|
| $c_1, c_9, c_{11}$                       | $(u^6 + 4u^5 + 6u^4 + u^3 - 5u^2 - 3u + 1)^2$ |
| $c_2, c_5, c_6$<br>$c_7, c_{10}, c_{12}$ | $(u^6 + 2u^4 + u^3 + u^2 + u - 1)^2$          |
| $c_3, c_4, c_8$                          | $(u^2 + u - 1)^6$                             |

(v) Riley Polynomials at the component

| Crossings                                | Riley Polynomials at each crossing                 |
|--|--|
| $c_1, c_9, c_{11}$                       | $(y^6 - 4y^5 + 18y^4 - 35y^3 + 43y^2 - 19y + 1)^2$ |
| $c_2, c_5, c_6$<br>$c_7, c_{10}, c_{12}$ | $(y^6 + 4y^5 + 6y^4 + y^3 - 5y^2 - 3y + 1)^2$      |
| $c_3, c_4, c_8$                          | $(y^2 - 3y + 1)^6$                                 |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_6^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.896795$              |                                       |            |
| $a = 0.66668 + 1.26617I$    | -12.1725                              | -6.00000   |
| $b = 0.08778 + 2.28447I$    |                                       |            |
| $u = 0.896795$              |                                       |            |
| $a = 0.66668 - 1.26617I$    | -12.1725                              | -6.00000   |
| $b = 0.08778 - 2.28447I$    |                                       |            |
| $u = 0.248003 + 1.088360I$  |                                       |            |
| $a = -0.296970 - 0.873464I$ | -4.27683                              | -6.00000   |
| $b = 0.309017 + 0.820596I$  |                                       |            |
| $u = 0.248003 + 1.088360I$  |                                       |            |
| $a = 0.44704 - 1.96182I$    | -4.27683                              | -6.00000   |
| $b = 0.80502 + 1.35611I$    |                                       |            |
| $u = 0.248003 - 1.088360I$  |                                       |            |
| $a = -0.296970 + 0.873464I$ | -4.27683                              | -6.00000   |
| $b = 0.309017 - 0.820596I$  |                                       |            |
| $u = 0.248003 - 1.088360I$  |                                       |            |
| $a = 0.44704 + 1.96182I$    | -4.27683                              | -6.00000   |
| $b = 0.80502 - 1.35611I$    |                                       |            |
| $u = -0.448397 + 1.266170I$ |                                       |            |
| $a = 0.648271 - 0.701773I$  | -12.1725                              | -6.00000   |
| $b = -0.809017 + 0.247864I$ |                                       |            |
| $u = -0.448397 + 1.266170I$ |                                       |            |
| $a = -0.69692 - 1.96794I$   | -12.1725                              | -6.00000   |
| $b = -1.70581 + 2.28447I$   |                                       |            |
| $u = -0.448397 - 1.266170I$ |                                       |            |
| $a = 0.648271 + 0.701773I$  | -12.1725                              | -6.00000   |
| $b = -0.809017 - 0.247864I$ |                                       |            |
| $u = -0.448397 - 1.266170I$ |                                       |            |
| $a = -0.69692 + 1.96794I$   | -12.1725                              | -6.00000   |
| $b = -1.70581 - 2.28447I$   |                                       |            |

| Solutions to $I_6^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.496006$             |                                       |            |
| $a = -1.76810 + 1.08835I$   | -4.27683                              | -6.00000   |
| $b = -0.186989 + 1.356110I$ |                                       |            |
| $u = -0.496006$             |                                       |            |
| $a = -1.76810 - 1.08835I$   | -4.27683                              | -6.00000   |
| $b = -0.186989 - 1.356110I$ |                                       |            |

$$\text{VII. } I_7^u = \langle b - u - 1, a + 2u + 1, u^2 + 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2u - 1 \\ u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u - 1 \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u - 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = -12**

(iv) u-Polynomials at the component

| Crossings                                | u-Polynomials at each crossing |
|--|--------------------------------|
| $c_1, c_9, c_{11}$                       | $(u - 1)^2$                    |
| $c_2, c_5, c_6$<br>$c_7, c_{10}, c_{12}$ | $u^2 + 1$                      |
| $c_3, c_4, c_8$                          | $u^2$                          |

(v) Riley Polynomials at the component

| Crossings                                | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_9, c_{11}$                       | $(y - 1)^2$                        |
| $c_2, c_5, c_6$<br>$c_7, c_{10}, c_{12}$ | $(y + 1)^2$                        |
| $c_3, c_4, c_8$                          | $y^2$                              |



(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_7^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 1.000000I$<br>$a = -1.00000 - 2.00000I$<br>$b = 1.00000 + 1.00000I$  | -4.93480                              | -12.0000   |
| $u = -1.000000I$<br>$a = -1.00000 + 2.00000I$<br>$b = 1.00000 - 1.00000I$ | -4.93480                              | -12.0000   |

### VIII. u-Polynomials

| Crossings                                | u-Polynomials at each crossing  |
|--|---|
| $c_1, c_9, c_{11}$                       | $(u-1)^2(u^2+u+1)(u^6+4u^5+6u^4+u^3-5u^2-3u+1)^2$ $\cdot (u^7+4u^6+8u^5+6u^4-5u^2-u-1)(u^{16}+9u^{15}+\dots+2u+1)^2$ $\cdot (u^{16}+10u^{15}+\dots+3u+4)$ |
| $c_2, c_5, c_6$<br>$c_7, c_{10}, c_{12}$ | $(u^2+1)(u^2+u+1)(u^6+2u^4+u^3+u^2+u-1)^2$ $\cdot (u^7+2u^5+2u^3+u^2-u+1)(u^{16}-u^{15}+\dots+u^2+1)^2$ $\cdot (u^{16}+2u^{15}+\dots+3u+2)$               |
| $c_3, c_4, c_8$                          | $u^2(u^2-u+1)(u^2+u-1)^6(u^7-5u^5-2u^4+7u^3+4u^2+4)$ $\cdot (u^{16}-2u^{15}+\dots-u+2)^3$   |

### IX. Riley Polynomials

| Crossings                                | Riley Polynomials at each crossing  |
|--|---|
| $c_1, c_9, c_{11}$                       | $(y-1)^2(y^2+y+1)(y^6-4y^5+18y^4-35y^3+43y^2-19y+1)^2$ $\cdot (y^7+16y^5+\dots-9y-1)(y^{16}-10y^{15}+\dots-y+16)$ $\cdot (y^{16}-3y^{15}+\dots-2y+1)^2$   |
| $c_2, c_5, c_6$<br>$c_7, c_{10}, c_{12}$ | $(y+1)^2(y^2+y+1)(y^6+4y^5+6y^4+y^3-5y^2-3y+1)^2$ $\cdot (y^7+4y^6+8y^5+6y^4-5y^2-y-1)(y^{16}+9y^{15}+\dots+2y+1)^2$ $\cdot (y^{16}+10y^{15}+\dots+3y+4)$ |
| $c_3, c_4, c_8$                          | $y^2(y^2-3y+1)^6(y^2+y+1)$ $\cdot (y^7-10y^6+39y^5-74y^4+65y^3-32y-16)$ $\cdot (y^{16}-18y^{15}+\dots+19y+4)^3$   |