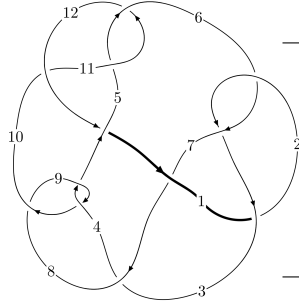
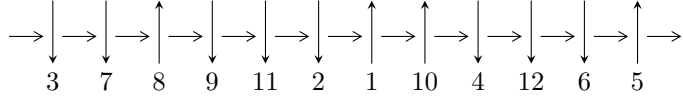


12a<sub>0516</sub> (K12a<sub>0516</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$4,9 \xrightarrow{c_4} 5 \xrightarrow{c_9} 10,12 \xrightarrow{c_{10}} 11 \xrightarrow{c_5} 6 \xrightarrow{c_{12}} 1 \xrightarrow{c_8} 8 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_2} 2 \twoheadrightarrow c_1, c_6, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -3u^{26} + 19u^{25} + \dots + 4b + 2, 11u^{26} - 57u^{25} + \dots + 8a - 62, u^{27} - 5u^{26} + \dots - 12u + 4 \rangle$$

$$I_2^u = \langle 153018u^{43}a + 172574u^{43} + \dots + 267932a + 346978, -5u^{43}a - 8u^{42}a + \dots - 7a - 8, u^{44} + 2u^{43} + \dots + 2u + 1 \rangle$$

$$I_3^u = \langle -au + b + a, a^2 - a + 1, u^2 + 1 \rangle$$

$$I_4^u = \langle au + b + a - u, a^2 - a + 1, u^2 + 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 123 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -3u^{26} + 19u^{25} + \dots + 4b + 2, 11u^{26} - 57u^{25} + \dots + 8a - 62, u^{27} - 5u^{26} + \dots - 12u + 4 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1.37500u^{26} + 7.12500u^{25} + \dots - 19.8750u + 7.75000 \\ \frac{3}{4}u^{26} - \frac{19}{4}u^{25} + \dots + \frac{33}{4}u - \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{3}{8}u^{26} + \frac{13}{8}u^{25} + \dots - \frac{35}{8}u + \frac{5}{4} \\ \frac{1}{4}u^{26} - \frac{5}{4}u^{25} + \dots + \frac{11}{4}u - \frac{1}{2} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{8}u^{26} + \frac{1}{8}u^{25} + \dots - \frac{67}{8}u + \frac{27}{4} \\ -\frac{1}{4}u^{26} + \frac{1}{4}u^{25} + \dots + \frac{35}{4}u - \frac{11}{2} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1.62500u^{26} + 8.37500u^{25} + \dots - 20.1250u + 8.25000 \\ \frac{7}{4}u^{26} - \frac{29}{4}u^{25} + \dots + \frac{37}{4}u - \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^6 - u^4 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{8}u^{26} + \frac{3}{8}u^{25} + \dots - \frac{1}{8}u - \frac{1}{4} \\ -\frac{1}{4}u^{26} + \frac{5}{4}u^{25} + \dots - \frac{9}{4}u + \frac{3}{2} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{8}u^{26} - \frac{23}{8}u^{25} + \dots + \frac{129}{8}u - \frac{25}{4} \\ \frac{3}{4}u^{26} - \frac{1}{4}u^{25} + \dots - \frac{1}{4}u - \frac{5}{2} \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -3u^{25} + 11u^{24} - 41u^{23} + 94u^{22} - 201u^{21} + 350u^{20} - 555u^{19} + 811u^{18} - 1060u^{17} + 1348u^{16} - 1524u^{15} + 1683u^{14} - 1695u^{13} + 1624u^{12} - 1489u^{11} + 1249u^{10} - 1017u^9 + 745u^8 - 495u^7 + 304u^6 - 145u^5 + 54u^4 - 7u^3 - 21u^2 + 20u - 6$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$u^{27} + 14u^{26} + \dots + 4u + 1$
$c_2, c_5, c_6$ $c_{11}$	$u^{27} - 7u^{25} + \dots - 2u^2 + 1$
$c_3$	$u^{27} + 5u^{26} + \dots - 320u^2 + 64$
$c_4, c_9$	$u^{27} - 5u^{26} + \dots - 12u + 4$
$c_7, c_{12}$	$u^{27} + 5u^{25} + \dots - 2u + 3$
$c_8$	$u^{27} - 15u^{26} + \dots + 56u + 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$y^{27} + 2y^{26} + \dots + 8y - 1$
$c_2, c_5, c_6$ $c_{11}$	$y^{27} - 14y^{26} + \dots + 4y - 1$
$c_3$	$y^{27} - 13y^{26} + \dots + 40960y - 4096$
$c_4, c_9$	$y^{27} + 15y^{26} + \dots + 56y - 16$
$c_7, c_{12}$	$y^{27} + 10y^{26} + \dots - 20y - 9$
$c_8$	$y^{27} - 5y^{26} + \dots + 8480y - 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.730663 + 0.630842I$		
$a = -1.15948 + 1.36199I$	$-6.78998 - 5.25258I$	$-11.87823 + 4.55008I$
$b = 1.380630 + 0.132263I$		
$u = -0.730663 - 0.630842I$		
$a = -1.15948 - 1.36199I$	$-6.78998 + 5.25258I$	$-11.87823 - 4.55008I$
$b = 1.380630 - 0.132263I$		
$u = -0.496338 + 0.799160I$		
$a = 0.491347 - 1.120530I$	$-0.34967 + 2.03126I$	$-2.38031 - 3.61940I$
$b = -0.828650 + 0.873109I$		
$u = -0.496338 - 0.799160I$		
$a = 0.491347 + 1.120530I$	$-0.34967 - 2.03126I$	$-2.38031 + 3.61940I$
$b = -0.828650 - 0.873109I$		
$u = 0.893419 + 0.201765I$		
$a = 0.47034 + 1.60999I$	$-1.56275 + 12.48900I$	$-7.13823 - 8.79182I$
$b = -1.108620 - 0.003316I$		
$u = 0.893419 - 0.201765I$		
$a = 0.47034 - 1.60999I$	$-1.56275 - 12.48900I$	$-7.13823 + 8.79182I$
$b = -1.108620 + 0.003316I$		
$u = -0.178235 + 1.084250I$		
$a = -0.213163 - 0.502908I$	$1.94164 + 2.20192I$	$-0.56198 - 2.41318I$
$b = 0.659574 + 0.702653I$		
$u = -0.178235 - 1.084250I$		
$a = -0.213163 + 0.502908I$	$1.94164 - 2.20192I$	$-0.56198 + 2.41318I$
$b = 0.659574 - 0.702653I$		
$u = -0.664783 + 0.914963I$		
$a = -0.39003 + 1.65011I$	$-5.96942 + 10.50660I$	$-9.69062 - 10.08606I$
$b = 1.72361 - 1.44912I$		
$u = -0.664783 - 0.914963I$		
$a = -0.39003 - 1.65011I$	$-5.96942 - 10.50660I$	$-9.69062 + 10.08606I$
$b = 1.72361 + 1.44912I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.728836 + 0.456068I$		
$a = -0.664583 + 0.952860I$	$-5.99030 - 2.50292I$	$-13.30644 + 3.87606I$
$b = -0.840437 - 0.847346I$		
$u = 0.728836 - 0.456068I$		
$a = -0.664583 - 0.952860I$	$-5.99030 + 2.50292I$	$-13.30644 - 3.87606I$
$b = -0.840437 + 0.847346I$		
$u = 0.799916 + 0.147492I$		
$a = -0.553123 - 0.901764I$	$2.62362 + 2.33182I$	$-0.926585 - 0.602280I$
$b = 0.879493 + 0.088034I$		
$u = 0.799916 - 0.147492I$		
$a = -0.553123 + 0.901764I$	$2.62362 - 2.33182I$	$-0.926585 + 0.602280I$
$b = 0.879493 - 0.088034I$		
$u = 0.563387 + 1.046610I$		
$a = 1.253280 + 0.526603I$	$-4.25210 - 2.40888I$	$-10.75070 + 1.81073I$
$b = -1.42614 + 0.54904I$		
$u = 0.563387 - 1.046610I$		
$a = 1.253280 - 0.526603I$	$-4.25210 + 2.40888I$	$-10.75070 - 1.81073I$
$b = -1.42614 - 0.54904I$		
$u = 0.021698 + 1.237970I$		
$a = 0.353870 + 0.098440I$	$-0.30811 - 4.23523I$	$-8.52197 + 5.94232I$
$b = -0.986014 + 0.581923I$		
$u = 0.021698 - 1.237970I$		
$a = 0.353870 - 0.098440I$	$-0.30811 + 4.23523I$	$-8.52197 - 5.94232I$
$b = -0.986014 - 0.581923I$		
$u = 0.371922 + 1.216990I$		
$a = -0.047378 - 0.727973I$	$6.71645 - 1.62939I$	$3.63674 + 2.67627I$
$b = -0.420071 + 0.350884I$		
$u = 0.371922 - 1.216990I$		
$a = -0.047378 + 0.727973I$	$6.71645 + 1.62939I$	$3.63674 - 2.67627I$
$b = -0.420071 - 0.350884I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.517374 + 1.188310I$ $a = -0.98424 - 1.30505I$ $b = 1.59567 + 1.17935I$	$5.67800 - 7.17879I$	$1.95902 + 3.78339I$
$u = 0.517374 - 1.188310I$ $a = -0.98424 + 1.30505I$ $b = 1.59567 - 1.17935I$	$5.67800 + 7.17879I$	$1.95902 - 3.78339I$
$u = 0.322363 + 1.283180I$ $a = -0.258472 + 0.363453I$ $b = 1.027060 + 0.465180I$	$3.19039 + 8.39996I$	$-2.59631 - 7.43442I$
$u = 0.322363 - 1.283180I$ $a = -0.258472 - 0.363453I$ $b = 1.027060 - 0.465180I$	$3.19039 - 8.39996I$	$-2.59631 + 7.43442I$
$u = 0.559888 + 1.210030I$ $a = 1.36303 + 1.45255I$ $b = -2.57082 - 1.28259I$	$1.4727 - 17.7774I$	$-3.91820 + 11.76326I$
$u = 0.559888 - 1.210030I$ $a = 1.36303 - 1.45255I$ $b = -2.57082 + 1.28259I$	$1.4727 + 17.7774I$	$-3.91820 - 11.76326I$
$u = -0.417568$ $a = 1.17723$ $b = -0.170545$	$-1.02561$	$-9.85230$

$$\text{II. } I_2^u = \langle 1.53 \times 10^5 au^{43} + 1.73 \times 10^5 u^{43} + \dots + 2.68 \times 10^5 a + 3.47 \times 10^5, -5u^{43}a - 8u^{42}a + \dots - 7a - 8, u^{44} + 2u^{43} + \dots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ -0.671774au^{43} - 0.757628u^{43} + \dots - 1.17627a - 1.52329 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0879130au^{43} - 1.35545u^{43} + \dots + 1.75763a - 1.80612 \\ -0.0707343au^{43} - 1.51109u^{43} + \dots - 0.630357a - 1.70508 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1.17627au^{43} + 1.52329u^{43} + \dots + 1.06336a + 1.87686 \\ -au \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.671774au^{43} - 0.757628u^{43} + \dots - 0.176265a - 1.52329 \\ -0.887094au^{43} + 0.646425u^{43} + \dots - 1.55887a - 1.11120 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^6 - u^4 + 1 \\ u^6 + 2u^4 + u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.757628au^{43} - 1.80612u^{43} + \dots + 1.52329a - 3.62675 \\ -1.40405au^{43} + 0.130050u^{43} + \dots - 0.412087a - 1.35545 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.337208au^{43} - 1.77370u^{43} + \dots + 0.402077a - 0.183860 \\ -0.671774au^{43} + 1.74237u^{43} + \dots - 1.17627a - 1.02329 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-8u^{42} - 14u^{41} + \dots - 10u - 8$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$u^{88} + 39u^{87} + \dots + 18u + 1$
$c_2, c_5, c_6$ $c_{11}$	$u^{88} - u^{87} + \dots - 6u + 1$
$c_3$	$(u^{44} - 2u^{43} + \dots - 16u + 4)^2$
$c_4, c_9$	$(u^{44} + 2u^{43} + \dots + 2u + 1)^2$
$c_7, c_{12}$	$u^{88} - 3u^{87} + \dots - 138u + 33$
$c_8$	$(u^{44} - 24u^{43} + \dots - 4u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$y^{88} + 21y^{87} + \dots + 238y + 1$
$c_2, c_5, c_6$ $c_{11}$	$y^{88} - 39y^{87} + \dots - 18y + 1$
$c_3$	$(y^{44} - 26y^{43} + \dots - 232y + 16)^2$
$c_4, c_9$	$(y^{44} + 24y^{43} + \dots + 4y + 1)^2$
$c_7, c_{12}$	$y^{88} - 3y^{87} + \dots + 50850y + 1089$
$c_8$	$(y^{44} - 4y^{43} + \dots - 24y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.312877 + 0.963899I$ $a = -0.027282 + 0.403408I$ $b = 0.952689 + 0.414115I$	$0.80202 + 2.36066I$	$-5.22306 - 1.04915I$
$u = 0.312877 + 0.963899I$ $a = 2.00737 - 0.22584I$ $b = -1.84409 + 1.07166I$	$0.80202 + 2.36066I$	$-5.22306 - 1.04915I$
$u = 0.312877 - 0.963899I$ $a = -0.027282 - 0.403408I$ $b = 0.952689 - 0.414115I$	$0.80202 - 2.36066I$	$-5.22306 + 1.04915I$
$u = 0.312877 - 0.963899I$ $a = 2.00737 + 0.22584I$ $b = -1.84409 - 1.07166I$	$0.80202 - 2.36066I$	$-5.22306 + 1.04915I$
$u = -0.137606 + 0.955862I$ $a = -0.094806 - 1.142040I$ $b = 0.023143 + 1.183290I$	$1.78035 + 2.09885I$	$0.44851 - 4.43063I$
$u = -0.137606 + 0.955862I$ $a = 0.106234 - 0.261688I$ $b = 0.767571 + 0.488152I$	$1.78035 + 2.09885I$	$0.44851 - 4.43063I$
$u = -0.137606 - 0.955862I$ $a = -0.094806 + 1.142040I$ $b = 0.023143 - 1.183290I$	$1.78035 - 2.09885I$	$0.44851 + 4.43063I$
$u = -0.137606 - 0.955862I$ $a = 0.106234 + 0.261688I$ $b = 0.767571 - 0.488152I$	$1.78035 - 2.09885I$	$0.44851 + 4.43063I$
$u = -0.684571 + 0.780204I$ $a = 0.01313 + 1.55377I$ $b = 1.38055 - 1.35627I$	$-6.79265 + 2.59501I$	$-11.85224 - 3.15453I$
$u = -0.684571 + 0.780204I$ $a = -1.29051 + 1.09598I$ $b = 1.44905 + 0.25653I$	$-6.79265 + 2.59501I$	$-11.85224 - 3.15453I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.684571 - 0.780204I$ $a = 0.01313 - 1.55377I$ $b = 1.38055 + 1.35627I$	$-6.79265 - 2.59501I$	$-11.85224 + 3.15453I$
$u = -0.684571 - 0.780204I$ $a = -1.29051 - 1.09598I$ $b = 1.44905 - 0.25653I$	$-6.79265 - 2.59501I$	$-11.85224 + 3.15453I$
$u = 0.603047 + 0.858448I$ $a = -0.604320 - 1.107190I$ $b = 1.027440 + 0.829602I$	$-3.07660 - 6.10396I$	$-6.28400 + 6.94365I$
$u = 0.603047 + 0.858448I$ $a = 0.20059 + 1.86245I$ $b = -1.55420 - 1.62720I$	$-3.07660 - 6.10396I$	$-6.28400 + 6.94365I$
$u = 0.603047 - 0.858448I$ $a = -0.604320 + 1.107190I$ $b = 1.027440 - 0.829602I$	$-3.07660 + 6.10396I$	$-6.28400 - 6.94365I$
$u = 0.603047 - 0.858448I$ $a = 0.20059 - 1.86245I$ $b = -1.55420 + 1.62720I$	$-3.07660 + 6.10396I$	$-6.28400 - 6.94365I$
$u = 0.618739 + 0.681900I$ $a = -0.539910 - 0.998880I$ $b = 0.882079 + 0.626536I$	$-3.58269 + 1.33395I$	$-7.91617 - 0.65820I$
$u = 0.618739 + 0.681900I$ $a = 1.41810 + 1.31949I$ $b = -1.50309 + 0.14230I$	$-3.58269 + 1.33395I$	$-7.91617 - 0.65820I$
$u = 0.618739 - 0.681900I$ $a = -0.539910 + 0.998880I$ $b = 0.882079 - 0.626536I$	$-3.58269 - 1.33395I$	$-7.91617 + 0.65820I$
$u = 0.618739 - 0.681900I$ $a = 1.41810 - 1.31949I$ $b = -1.50309 - 0.14230I$	$-3.58269 - 1.33395I$	$-7.91617 + 0.65820I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.845401 + 0.185803I$ $a = 0.552294 - 0.890537I$ $b = -0.913023 + 0.113662I$	$0.59532 - 7.36573I$	$-4.12046 + 4.87801I$
$u = -0.845401 + 0.185803I$ $a = -0.45725 + 1.68541I$ $b = 1.113550 - 0.030175I$	$0.59532 - 7.36573I$	$-4.12046 + 4.87801I$
$u = -0.845401 - 0.185803I$ $a = 0.552294 + 0.890537I$ $b = -0.913023 - 0.113662I$	$0.59532 + 7.36573I$	$-4.12046 - 4.87801I$
$u = -0.845401 - 0.185803I$ $a = -0.45725 - 1.68541I$ $b = 1.113550 + 0.030175I$	$0.59532 + 7.36573I$	$-4.12046 - 4.87801I$
$u = -0.377246 + 1.071500I$ $a = -1.321220 + 0.020635I$ $b = 1.41639 + 0.83546I$	$1.70903 + 2.55111I$	$-3.11914 - 3.94978I$
$u = -0.377246 + 1.071500I$ $a = 0.108848 - 0.668784I$ $b = 0.549372 + 0.372801I$	$1.70903 + 2.55111I$	$-3.11914 - 3.94978I$
$u = -0.377246 - 1.071500I$ $a = -1.321220 - 0.020635I$ $b = 1.41639 - 0.83546I$	$1.70903 - 2.55111I$	$-3.11914 + 3.94978I$
$u = -0.377246 - 1.071500I$ $a = 0.108848 + 0.668784I$ $b = 0.549372 - 0.372801I$	$1.70903 - 2.55111I$	$-3.11914 + 3.94978I$
$u = 0.805706 + 0.294033I$ $a = -0.681975 + 0.547340I$ $b = -0.808577 - 0.504319I$	$-4.21399 + 4.93430I$	$-10.72232 - 3.42025I$
$u = 0.805706 + 0.294033I$ $a = 0.64947 + 1.70247I$ $b = -1.179970 - 0.018130I$	$-4.21399 + 4.93430I$	$-10.72232 - 3.42025I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.805706 - 0.294033I$ $a = -0.681975 - 0.547340I$ $b = -0.808577 + 0.504319I$	$-4.21399 - 4.93430I$	$-10.72232 + 3.42025I$
$u = 0.805706 - 0.294033I$ $a = 0.64947 - 1.70247I$ $b = -1.179970 + 0.018130I$	$-4.21399 - 4.93430I$	$-10.72232 + 3.42025I$
$u = 0.336351 + 0.713930I$ $a = -0.549874 - 0.605883I$ $b = -0.764991 + 0.324297I$	$0.07018 - 5.32036I$	$-6.18214 + 9.40095I$
$u = 0.336351 + 0.713930I$ $a = -1.00871 + 2.88605I$ $b = -0.42659 - 2.41866I$	$0.07018 - 5.32036I$	$-6.18214 + 9.40095I$
$u = 0.336351 - 0.713930I$ $a = -0.549874 + 0.605883I$ $b = -0.764991 - 0.324297I$	$0.07018 + 5.32036I$	$-6.18214 - 9.40095I$
$u = 0.336351 - 0.713930I$ $a = -1.00871 - 2.88605I$ $b = -0.42659 + 2.41866I$	$0.07018 + 5.32036I$	$-6.18214 - 9.40095I$
$u = 0.451669 + 1.130720I$ $a = -0.184575 + 0.446454I$ $b = 1.012320 + 0.416675I$	$3.33637 - 3.89932I$	$-2.16553 + 3.93444I$
$u = 0.451669 + 1.130720I$ $a = 1.55267 + 1.97505I$ $b = -2.74463 - 1.74556I$	$3.33637 - 3.89932I$	$-2.16553 + 3.93444I$
$u = 0.451669 - 1.130720I$ $a = -0.184575 - 0.446454I$ $b = 1.012320 - 0.416675I$	$3.33637 + 3.89932I$	$-2.16553 - 3.93444I$
$u = 0.451669 - 1.130720I$ $a = 1.55267 - 1.97505I$ $b = -2.74463 + 1.74556I$	$3.33637 + 3.89932I$	$-2.16553 - 3.93444I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.187726 + 1.204930I$ $a = 0.586324 - 0.078067I$ $b = -1.015170 + 0.721089I$	$0.63647 + 1.88253I$	$-5.88964 - 2.78829I$
$u = 0.187726 + 1.204930I$ $a = -0.222273 + 0.265114I$ $b = 0.990291 + 0.491707I$	$0.63647 + 1.88253I$	$-5.88964 - 2.78829I$
$u = 0.187726 - 1.204930I$ $a = 0.586324 + 0.078067I$ $b = -1.015170 - 0.721089I$	$0.63647 - 1.88253I$	$-5.88964 + 2.78829I$
$u = 0.187726 - 1.204930I$ $a = -0.222273 - 0.265114I$ $b = 0.990291 - 0.491707I$	$0.63647 - 1.88253I$	$-5.88964 + 2.78829I$
$u = -0.409396 + 1.159590I$ $a = 0.192660 + 0.417968I$ $b = -1.011500 + 0.429689I$	$5.11542 - 1.06835I$	0
$u = -0.409396 + 1.159590I$ $a = 0.97698 - 1.55522I$ $b = -1.56050 + 1.51219I$	$5.11542 - 1.06835I$	0
$u = -0.409396 - 1.159590I$ $a = 0.192660 - 0.417968I$ $b = -1.011500 - 0.429689I$	$5.11542 + 1.06835I$	0
$u = -0.409396 - 1.159590I$ $a = 0.97698 + 1.55522I$ $b = -1.56050 - 1.51219I$	$5.11542 + 1.06835I$	0
$u = -0.523577 + 1.128340I$ $a = -1.139810 + 0.393041I$ $b = 1.35919 + 0.61090I$	$0.51289 + 4.91293I$	$-4.00000 - 3.32925I$
$u = -0.523577 + 1.128340I$ $a = 0.88118 - 1.31204I$ $b = -1.45124 + 1.17483I$	$0.51289 + 4.91293I$	$-4.00000 - 3.32925I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.523577 - 1.128340I$ $a = -1.139810 - 0.393041I$ $b = 1.35919 - 0.61090I$	$0.51289 - 4.91293I$	$-4.00000 + 3.32925I$
$u = -0.523577 - 1.128340I$ $a = 0.88118 + 1.31204I$ $b = -1.45124 - 1.17483I$	$0.51289 - 4.91293I$	$-4.00000 + 3.32925I$
$u = -0.699549 + 0.280530I$ $a = 0.567058 - 0.884436I$ $b = -0.805456 + 0.201612I$	$-1.95648 - 0.23544I$	$-7.71045 - 0.71060I$
$u = -0.699549 + 0.280530I$ $a = 0.915779 + 0.590948I$ $b = 0.609805 - 0.560083I$	$-1.95648 - 0.23544I$	$-7.71045 - 0.71060I$
$u = -0.699549 - 0.280530I$ $a = 0.567058 + 0.884436I$ $b = -0.805456 - 0.201612I$	$-1.95648 + 0.23544I$	$-7.71045 + 0.71060I$
$u = -0.699549 - 0.280530I$ $a = 0.915779 - 0.590948I$ $b = 0.609805 + 0.560083I$	$-1.95648 + 0.23544I$	$-7.71045 + 0.71060I$
$u = 0.446265 + 1.170890I$ $a = -0.083115 - 0.736096I$ $b = -0.476825 + 0.306143I$	$6.49035 - 4.18968I$	$0. + 3.85017I$
$u = 0.446265 + 1.170890I$ $a = -0.98672 - 1.45431I$ $b = 1.58085 + 1.38043I$	$6.49035 - 4.18968I$	$0. + 3.85017I$
$u = 0.446265 - 1.170890I$ $a = -0.083115 + 0.736096I$ $b = -0.476825 - 0.306143I$	$6.49035 + 4.18968I$	$0. - 3.85017I$
$u = 0.446265 - 1.170890I$ $a = -0.98672 + 1.45431I$ $b = 1.58085 - 1.38043I$	$6.49035 + 4.18968I$	$0. - 3.85017I$



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.480714 + 1.157280I$ $a = 0.095453 - 0.746494I$ $b = 0.492941 + 0.284502I$	$4.61322 + 9.27115I$	$0. - 8.56343I$
$u = -0.480714 + 1.157280I$ $a = -1.51091 + 1.78770I$ $b = 2.70589 - 1.57781I$	$4.61322 + 9.27115I$	$0. - 8.56343I$
$u = -0.480714 - 1.157280I$ $a = 0.095453 + 0.746494I$ $b = 0.492941 - 0.284502I$	$4.61322 - 9.27115I$	$0. + 8.56343I$
$u = -0.480714 - 1.157280I$ $a = -1.51091 - 1.78770I$ $b = 2.70589 + 1.57781I$	$4.61322 - 9.27115I$	$0. + 8.56343I$
$u = 0.560382 + 1.148160I$ $a = 1.090810 + 0.445231I$ $b = -1.33863 + 0.58110I$	$-1.67798 - 10.01170I$	$0. + 7.22646I$
$u = 0.560382 + 1.148160I$ $a = 1.23542 + 1.62075I$ $b = -2.46031 - 1.43171I$	$-1.67798 - 10.01170I$	$0. + 7.22646I$
$u = 0.560382 - 1.148160I$ $a = 1.090810 - 0.445231I$ $b = -1.33863 - 0.58110I$	$-1.67798 + 10.01170I$	$0. - 7.22646I$
$u = 0.560382 - 1.148160I$ $a = 1.23542 - 1.62075I$ $b = -2.46031 + 1.43171I$	$-1.67798 + 10.01170I$	$0. - 7.22646I$
$u = 0.711517$ $a = -0.542111 + 0.968090I$ $b = 0.832272 + 0.025706I$	$3.18095$	$-0.237640$
$u = 0.711517$ $a = -0.542111 - 0.968090I$ $b = 0.832272 - 0.025706I$	$3.18095$	$-0.237640$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.340404 + 1.242800I$ $a = 0.032335 - 0.731892I$ $b = 0.385344 + 0.365827I$	$5.03718 - 3.41596I$	0
$u = -0.340404 + 1.242800I$ $a = 0.235290 + 0.372209I$ $b = -1.019910 + 0.456338I$	$5.03718 - 3.41596I$	0
$u = -0.340404 - 1.242800I$ $a = 0.032335 + 0.731892I$ $b = 0.385344 - 0.365827I$	$5.03718 + 3.41596I$	0
$u = -0.340404 - 1.242800I$ $a = 0.235290 - 0.372209I$ $b = -1.019910 - 0.456338I$	$5.03718 + 3.41596I$	0
$u = -0.686238 + 0.096964I$ $a = 0.491955 + 1.019840I$ $b = -0.841799 + 0.092164I$	$1.63501 - 4.89218I$	$-3.21822 + 5.35953I$
$u = -0.686238 + 0.096964I$ $a = -0.28294 + 1.99860I$ $b = 1.098800 - 0.134459I$	$1.63501 - 4.89218I$	$-3.21822 + 5.35953I$
$u = -0.686238 - 0.096964I$ $a = 0.491955 - 1.019840I$ $b = -0.841799 - 0.092164I$	$1.63501 + 4.89218I$	$-3.21822 - 5.35953I$
$u = -0.686238 - 0.096964I$ $a = -0.28294 - 1.99860I$ $b = 1.098800 + 0.134459I$	$1.63501 + 4.89218I$	$-3.21822 - 5.35953I$
$u = -0.541068 + 1.196610I$ $a = 0.98556 - 1.26327I$ $b = -1.60448 + 1.12233I$	$3.60464 + 12.44580I$	0
$u = -0.541068 + 1.196610I$ $a = -1.39332 + 1.52484I$ $b = 2.59851 - 1.34576I$	$3.60464 + 12.44580I$	0

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.541068 - 1.196610I$ $a = 0.98556 + 1.26327I$ $b = -1.60448 - 1.12233I$	$3.60464 - 12.44580I$	0
$u = -0.541068 - 1.196610I$ $a = -1.39332 - 1.52484I$ $b = 2.59851 + 1.34576I$	$3.60464 - 12.44580I$	0
$u = -0.224537 + 0.568559I$ $a = -0.490715 + 0.741336I$ $b = -0.871940 + 0.351164I$	$0.002055 + 0.400940I$	$-7.16201 - 2.06092I$
$u = -0.224537 + 0.568559I$ $a = 2.13564 + 2.59121I$ $b = -0.47847 - 1.91301I$	$0.002055 + 0.400940I$	$-7.16201 - 2.06092I$
$u = -0.224537 - 0.568559I$ $a = -0.490715 - 0.741336I$ $b = -0.871940 - 0.351164I$	$0.002055 - 0.400940I$	$-7.16201 + 2.06092I$
$u = -0.224537 - 0.568559I$ $a = 2.13564 - 2.59121I$ $b = -0.47847 + 1.91301I$	$0.002055 - 0.400940I$	$-7.16201 + 2.06092I$
$u = 0.543576$ $a = -0.11878 + 2.32451I$ $b = -1.052670 - 0.226855I$	0.437519	-5.45100
$u = 0.543576$ $a = -0.11878 - 2.32451I$ $b = -1.052670 + 0.226855I$	0.437519	-5.45100

$$\text{III. } I_3^u = \langle -au + b + a, a^2 - a + 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ au - a \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a - u - 1 \\ au - a + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -au + a \\ au \end{pmatrix}$$

$$a_1 = \begin{pmatrix} au + a \\ -a \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -au + a + 2u - 1 \\ au - u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} au + 2a \\ -a \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $8a - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$(u^2 - u + 1)^2$
$c_2, c_5, c_6$ $c_7, c_{11}, c_{12}$	$u^4 - u^2 + 1$
$c_3$	$u^4$
$c_4, c_9$	$(u^2 + 1)^2$
$c_8$	$(u + 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$(y^2 + y + 1)^2$
$c_2, c_5, c_6$ $c_7, c_{11}, c_{12}$	$(y^2 - y + 1)^2$
$c_3$	$y^4$
$c_4, c_9$	$(y + 1)^4$
$c_8$	$(y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$ $a = 0.500000 + 0.866025I$ $b = -1.36603 - 0.36603I$	$1.64493 - 4.05977I$	$0. + 6.92820I$
$u = 1.000000I$ $a = 0.500000 - 0.866025I$ $b = 0.36603 + 1.36603I$	$1.64493 + 4.05977I$	$0. - 6.92820I$
$u = -1.000000I$ $a = 0.500000 + 0.866025I$ $b = 0.36603 - 1.36603I$	$1.64493 - 4.05977I$	$0. + 6.92820I$
$u = -1.000000I$ $a = 0.500000 - 0.866025I$ $b = -1.36603 + 0.36603I$	$1.64493 + 4.05977I$	$0. - 6.92820I$

$$\text{IV. } I_4^u = \langle au + b + a - u, a^2 - a + 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ -au - a + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u + 1 \\ -au + u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -au - a + 1 \\ au \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -au + a + u \\ -a \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -au + 2u + 1 \\ au - u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -au + 2a + u \\ -a \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$(u^2 - u + 1)^2$
$c_2, c_5, c_6$ $c_7, c_{11}, c_{12}$	$u^4 - u^2 + 1$
$c_3$	$u^4$
$c_4, c_9$	$(u^2 + 1)^2$
$c_8$	$(u + 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$(y^2 + y + 1)^2$
$c_2, c_5, c_6$ $c_7, c_{11}, c_{12}$	$(y^2 - y + 1)^2$
$c_3$	$y^4$
$c_4, c_9$	$(y + 1)^4$
$c_8$	$(y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$	1.64493	0
$a = 0.500000 + 0.866025I$		
$b = 0.366025 - 0.366025I$		
$u = 1.000000I$	1.64493	0
$a = 0.500000 - 0.866025I$		
$b = -1.36603 + 1.36603I$		
$u = -1.000000I$	1.64493	0
$a = 0.500000 + 0.866025I$		
$b = -1.36603 - 1.36603I$		
$u = -1.000000I$	1.64493	0
$a = 0.500000 - 0.866025I$		
$b = 0.366025 + 0.366025I$		

### V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_{10}$	$((u^2 - u + 1)^4)(u^{27} + 14u^{26} + \dots + 4u + 1)(u^{88} + 39u^{87} + \dots + 18u + 1)$
$c_2, c_5, c_6$ $c_{11}$	$((u^4 - u^2 + 1)^2)(u^{27} - 7u^{25} + \dots - 2u^2 + 1)(u^{88} - u^{87} + \dots - 6u + 1)$
$c_3$	$u^8(u^{27} + 5u^{26} + \dots - 320u^2 + 64)(u^{44} - 2u^{43} + \dots - 16u + 4)^2$
$c_4, c_9$	$((u^2 + 1)^4)(u^{27} - 5u^{26} + \dots - 12u + 4)(u^{44} + 2u^{43} + \dots + 2u + 1)^2$
$c_7, c_{12}$	$((u^4 - u^2 + 1)^2)(u^{27} + 5u^{25} + \dots - 2u + 3)(u^{88} - 3u^{87} + \dots - 138u + 33)$
$c_8$	$((u + 1)^8)(u^{27} - 15u^{26} + \dots + 56u + 16)(u^{44} - 24u^{43} + \dots - 4u + 1)^2$

## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_{10}$	$((y^2 + y + 1)^4)(y^{27} + 2y^{26} + \dots + 8y - 1)(y^{88} + 21y^{87} + \dots + 238y + 1)$
$c_2, c_5, c_6$ $c_{11}$	$((y^2 - y + 1)^4)(y^{27} - 14y^{26} + \dots + 4y - 1)(y^{88} - 39y^{87} + \dots - 18y + 1)$
$c_3$	$y^8(y^{27} - 13y^{26} + \dots + 40960y - 4096)$ $\cdot (y^{44} - 26y^{43} + \dots - 232y + 16)^2$
$c_4, c_9$	$((y + 1)^8)(y^{27} + 15y^{26} + \dots + 56y - 16)(y^{44} + 24y^{43} + \dots + 4y + 1)^2$
$c_7, c_{12}$	$((y^2 - y + 1)^4)(y^{27} + 10y^{26} + \dots - 20y - 9)$ $\cdot (y^{88} - 3y^{87} + \dots + 50850y + 1089)$
$c_8$	$((y - 1)^8)(y^{27} - 5y^{26} + \dots + 8480y - 256)$ $\cdot (y^{44} - 4y^{43} + \dots - 24y + 1)^2$