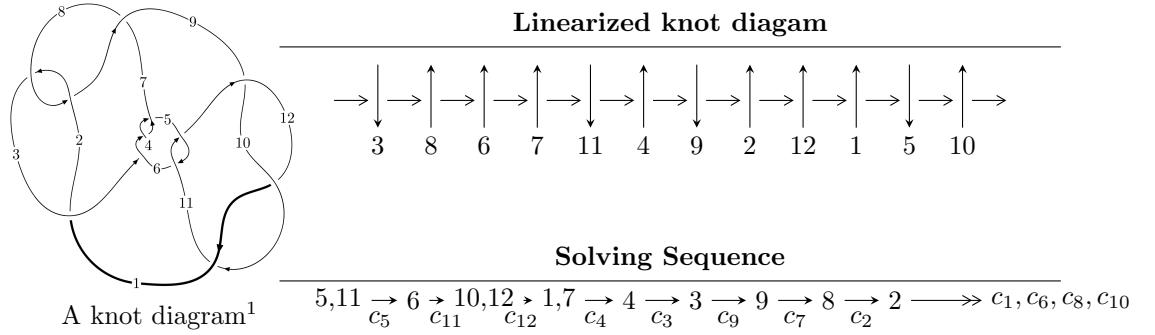


$12a_{0693}$ ($K12a_{0693}$)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 3.03402 \times 10^{43}u^{32} - 2.41482 \times 10^{44}u^{31} + \dots + 8.30969 \times 10^{46}d - 2.35468 \times 10^{45}, \\ - 1.63168 \times 10^{45}u^{32} + 5.79263 \times 10^{45}u^{31} + \dots + 1.66194 \times 10^{47}c + 8.26721 \times 10^{46}, \\ 2.98338 \times 10^{44}u^{32} - 6.07211 \times 10^{44}u^{31} + \dots + 8.30969 \times 10^{46}b + 2.51360 \times 10^{46}, \\ 1.47168 \times 10^{44}u^{32} - 3.80823 \times 10^{44}u^{31} + \dots + 1.66194 \times 10^{47}a - 1.40982 \times 10^{47}, u^{33} - 3u^{32} + \dots - 32u + 3 \rangle$$

$$I_2^u = \langle -43643176926349u^{24} - 6533209487727u^{23} + \dots + 36953350808552d - 173010685681858, \\ - 25166501522073u^{24}a + 34404839224211u^{24} + \dots - 99103984064754a + 136057334873306, \\ - 18554983719311u^{24}a + 8394493620023u^{24} + \dots + 50333003044146a - 30523951539978, \\ - 86505342840929u^{24}a + 33387065157365u^{24} + \dots + 716188465355062a - 526188833960766, \\ u^{25} + u^{24} + \dots + 4u - 4 \rangle$$

$$I_1^v = \langle a, d, c - v, b + 1, v^2 - v + 1 \rangle$$

$$I_2^v = \langle c, d + v - 1, b, a - 1, v^2 - v + 1 \rangle$$

$$I_3^v = \langle a, d + 1, c - a + 1, b + 1, v + 1 \rangle$$

$$I_4^v = \langle a, a^2d + c^2v - 2v^2c + v^3 + 2ca + cv - 2av - v^2 + a + v, dv - 1, \\ c^2v^2 - 2v^3c + v^4 + 2cav + v^2c - 2v^2a - v^3 + a^2 + av + v^2, b + 1 \rangle$$

* 5 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 88 representations.

* 1 irreducible components of $\dim_{\mathbb{C}} = 1$

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew (<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose (<https://github.com/CATsTAILs/LinksPainter>).

$$\text{I. } I_1^u = \langle 3.03 \times 10^{43}u^{32} - 2.41 \times 10^{44}u^{31} + \cdots + 8.31 \times 10^{46}d - 2.35 \times 10^{45}, -1.63 \times 10^{45}u^{32} + 5.79 \times 10^{45}u^{31} + \cdots + 1.66 \times 10^{47}c + 8.27 \times 10^{46}, 2.98 \times 10^{44}u^{32} - 6.07 \times 10^{44}u^{31} + \cdots + 8.31 \times 10^{46}b + 2.51 \times 10^{46}, 1.47 \times 10^{44}u^{32} - 3.81 \times 10^{44}u^{31} + \cdots + 1.66 \times 10^{47}a - 1.41 \times 10^{47}, u^{33} - 3u^{32} + \cdots - 32u + 32 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.00981792u^{32} - 0.0348547u^{31} + \cdots + 1.28086u - 0.497444 \\ -0.000365118u^{32} + 0.00290603u^{31} + \cdots + 0.819964u + 0.0283366 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.00945281u^{32} + 0.0319487u^{31} + \cdots - 2.10082u + 0.469107 \\ -0.000365118u^{32} + 0.00290603u^{31} + \cdots + 0.819964u + 0.0283366 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.000885519u^{32} + 0.00229144u^{31} + \cdots - 0.0914785u + 0.848301 \\ -0.00359025u^{32} + 0.00730726u^{31} + \cdots - 0.166618u - 0.302490 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.000885519u^{32} + 0.00229144u^{31} + \cdots - 0.0914785u + 0.848301 \\ 0.00540092u^{32} - 0.0113739u^{31} + \cdots + 0.183270u + 0.314174 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.00447577u^{32} + 0.00959870u^{31} + \cdots - 0.258096u + 0.545811 \\ 0.00661052u^{32} - 0.0132031u^{31} + \cdots + 0.187327u + 0.425005 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.0132814u^{32} - 0.0464547u^{31} + \cdots + 1.69824u - 0.612332 \\ -0.00382860u^{32} + 0.0145061u^{31} + \cdots + 0.402587u + 0.143225 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.0199599u^{32} + 0.0470707u^{31} + \cdots - 1.09062u + 0.264873 \\ 0.00406824u^{32} - 0.00955037u^{31} + \cdots - 0.124182u - 0.479897 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0149968u^{32} + 0.0409221u^{31} + \cdots - 2.43207u + 0.604078 \\ -0.0128090u^{32} + 0.0440976u^{31} + \cdots - 0.373843u + 0.638717 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $0.0605080u^{32} - 0.0513753u^{31} + \cdots - 7.44134u + 11.1534$

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_7	$u^{33} + 11u^{32} + \cdots + 8u - 16$
c_2, c_8	$u^{33} + u^{32} + \cdots - 12u + 4$
c_3, c_4, c_6 c_9, c_{10}, c_{12}	$u^{33} + 5u^{32} + \cdots - 7u^2 - 1$
c_5, c_{11}	$u^{33} - 3u^{32} + \cdots - 32u + 32$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_7	$y^{33} + 23y^{32} + \cdots - 14304y - 256$
c_2, c_8	$y^{33} + 11y^{32} + \cdots + 8y - 16$
c_3, c_4, c_6 c_9, c_{10}, c_{12}	$y^{33} - 39y^{32} + \cdots - 14y - 1$
c_5, c_{11}	$y^{33} + 15y^{32} + \cdots - 6144y - 1024$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.979372 + 0.273800I$ $a = 0.431028 - 0.024061I$ $b = -1.312830 - 0.129109I$ $c = -1.70621 + 0.13086I$ $d = 0.428725 + 0.094450I$	$4.01193 + 3.40996I$	$6.93635 - 3.61829I$
$u = 0.979372 - 0.273800I$ $a = 0.431028 + 0.024061I$ $b = -1.312830 + 0.129109I$ $c = -1.70621 - 0.13086I$ $d = 0.428725 - 0.094450I$	$4.01193 - 3.40996I$	$6.93635 + 3.61829I$
$u = 0.581985 + 0.777781I$ $a = 0.666890 + 0.389948I$ $b = -0.117441 + 0.653397I$ $c = 0.381291 - 0.245865I$ $d = 0.084826 + 0.745638I$	$-3.19812 - 2.28214I$	$-2.55468 + 4.65224I$
$u = 0.581985 - 0.777781I$ $a = 0.666890 - 0.389948I$ $b = -0.117441 - 0.653397I$ $c = 0.381291 + 0.245865I$ $d = 0.084826 - 0.745638I$	$-3.19812 + 2.28214I$	$-2.55468 - 4.65224I$
$u = -0.342726 + 1.062970I$ $a = 0.557825 - 0.285941I$ $b = -0.419652 - 0.727712I$ $c = -0.617597 - 0.133391I$ $d = 0.112766 + 0.690951I$	$2.46500 + 1.75021I$	$7.36804 - 3.35767I$
$u = -0.342726 - 1.062970I$ $a = 0.557825 + 0.285941I$ $b = -0.419652 + 0.727712I$ $c = -0.617597 + 0.133391I$ $d = 0.112766 - 0.690951I$	$2.46500 - 1.75021I$	$7.36804 + 3.35767I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.16826$		
$a = 0.415930$		
$b = -1.40425$	7.47395	12.4850
$c = 1.68792$		
$d = -0.485914$		
$u = 0.464136 + 1.103860I$		
$a = 0.545028 + 0.324179I$		
$b = -0.355294 + 0.806119I$	1.74788 - 7.33440I	5.47919 + 8.14278I
$c = 0.610442 - 0.217661I$		
$d = -0.104881 + 0.752097I$		
$u = 0.464136 - 1.103860I$		
$a = 0.545028 - 0.324179I$		
$b = -0.355294 - 0.806119I$	1.74788 + 7.33440I	5.47919 - 8.14278I
$c = 0.610442 + 0.217661I$		
$d = -0.104881 - 0.752097I$		
$u = 0.635877 + 0.397843I$		
$a = 0.923878 + 0.490787I$		
$b = 0.155830 + 0.448444I$	-0.42221 + 2.98824I	-0.68495 - 3.66701I
$c = 0.101013 - 0.282995I$		
$d = 0.392216 + 0.679638I$		
$u = 0.635877 - 0.397843I$		
$a = 0.923878 - 0.490787I$		
$b = 0.155830 - 0.448444I$	-0.42221 - 2.98824I	-0.68495 + 3.66701I
$c = 0.101013 + 0.282995I$		
$d = 0.392216 - 0.679638I$		
$u = -0.239228 + 0.607577I$		
$a = 0.750526 - 0.191152I$		
$b = -0.251234 - 0.318679I$	0.292144 + 0.942663I	5.66111 - 7.03214I
$c = -0.249740 + 0.035069I$		
$d = -0.063407 + 0.501731I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.239228 - 0.607577I$ $a = 0.750526 + 0.191152I$ $b = -0.251234 + 0.318679I$ $c = -0.249740 - 0.035069I$ $d = -0.063407 - 0.501731I$	$0.292144 - 0.942663I$	$5.66111 + 7.03214I$
$u = 0.351447 + 1.312440I$ $a = -1.87607 - 0.66709I$ $b = 1.47320 - 0.16826I$ $c = -0.05533 + 1.61726I$ $d = 0.21618 - 2.69668I$	$9.06107 - 0.86504I$	$11.01805 + 0.17133I$
$u = 0.351447 - 1.312440I$ $a = -1.87607 + 0.66709I$ $b = 1.47320 + 0.16826I$ $c = -0.05533 - 1.61726I$ $d = 0.21618 + 2.69668I$	$9.06107 + 0.86504I$	$11.01805 - 0.17133I$
$u = 0.611782 + 1.268620I$ $a = -1.54743 - 1.00939I$ $b = 1.45334 - 0.29571I$ $c = -0.07474 + 1.55998I$ $d = 0.33385 - 2.58063I$	$7.09875 - 9.27148I$	$8.26421 + 6.23171I$
$u = 0.611782 - 1.268620I$ $a = -1.54743 + 1.00939I$ $b = 1.45334 + 0.29571I$ $c = -0.07474 - 1.55998I$ $d = 0.33385 + 2.58063I$	$7.09875 + 9.27148I$	$8.26421 - 6.23171I$
$u = 0.053785 + 0.584876I$ $a = 0.567133 - 0.028165I$ $b = -0.758918 - 0.087353I$ $c = -0.313400 + 0.942882I$ $d = 0.046976 + 0.330187I$	$2.76296 + 2.31801I$	$12.30250 - 4.19824I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.053785 - 0.584876I$		
$a = 0.567133 + 0.028165I$		
$b = -0.758918 + 0.087353I$	$2.76296 - 2.31801I$	$12.30250 + 4.19824I$
$c = -0.313400 - 0.942882I$		
$d = 0.046976 - 0.330187I$		
$u = -1.38673 + 0.43185I$		
$a = 0.395798 + 0.032608I$		
$b = -1.50951 + 0.20675I$	$11.58920 - 2.62797I$	$12.22236 + 0.42879I$
$c = 1.59758 + 0.04740I$		
$d = -0.562946 + 0.125707I$		
$u = -1.38673 - 0.43185I$		
$a = 0.395798 - 0.032608I$		
$b = -1.50951 - 0.20675I$	$11.58920 + 2.62797I$	$12.22236 - 0.42879I$
$c = 1.59758 - 0.04740I$		
$d = -0.562946 - 0.125707I$		
$u = -0.489796 + 0.230188I$		
$a = 1.111610 - 0.308664I$		
$b = 0.164799 - 0.231913I$	$0.15528 + 1.56621I$	$-1.22779 - 2.98994I$
$c = 0.015550 - 0.148753I$		
$d = -0.473411 + 0.407061I$		
$u = -0.489796 - 0.230188I$		
$a = 1.111610 + 0.308664I$		
$b = 0.164799 + 0.231913I$	$0.15528 - 1.56621I$	$-1.22779 + 2.98994I$
$c = 0.015550 + 0.148753I$		
$d = -0.473411 - 0.407061I$		
$u = 1.35730 + 0.53891I$		
$a = 0.396350 - 0.041125I$		
$b = -1.49615 - 0.25900I$	$10.79550 + 8.72073I$	$10.94592 - 5.35160I$
$c = -1.57777 + 0.05545I$		
$d = 0.560127 + 0.157777I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.35730 - 0.53891I$		
$a = 0.396350 + 0.041125I$		
$b = -1.49615 + 0.25900I$	$10.79550 - 8.72073I$	$10.94592 + 5.35160I$
$c = -1.57777 - 0.05545I$		
$d = 0.560127 - 0.157777I$		
$u = -0.48684 + 1.39736I$		
$a = -1.61091 + 0.72954I$		
$b = 1.51512 + 0.23328I$	$12.10590 + 5.85939I$	$13.7252 - 3.8290I$
$c = 0.04717 + 1.58742I$		
$d = -0.23517 - 2.60619I$		
$u = -0.48684 - 1.39736I$		
$a = -1.61091 - 0.72954I$		
$b = 1.51512 - 0.23328I$	$12.10590 - 5.85939I$	$13.7252 + 3.8290I$
$c = 0.04717 - 1.58742I$		
$d = -0.23517 + 2.60619I$		
$u = 0.82581 + 1.33817I$		
$a = -1.22197 - 0.99602I$		
$b = 1.49169 - 0.40077I$	$13.4411 - 16.4286I$	$10.77382 + 8.75984I$
$c = -0.04243 + 1.51660I$		
$d = 0.32373 - 2.45773I$		
$u = 0.82581 - 1.33817I$		
$a = -1.22197 + 0.99602I$		
$b = 1.49169 + 0.40077I$	$13.4411 + 16.4286I$	$10.77382 - 8.75984I$
$c = -0.04243 - 1.51660I$		
$d = 0.32373 + 2.45773I$		
$u = -0.77347 + 1.38729I$		
$a = -1.27234 + 0.92357I$		
$b = 1.51473 + 0.37364I$	$14.7439 + 10.2508I$	$12.57547 - 4.19472I$
$c = 0.03820 + 1.53196I$		
$d = -0.29714 - 2.47946I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.77347 - 1.38729I$		
$a = -1.27234 - 0.92357I$		
$b = 1.51473 - 0.37364I$	$14.7439 - 10.2508I$	$12.57547 + 4.19472I$
$c = 0.03820 - 1.53196I$		
$d = -0.29714 + 2.47946I$		
$u = -0.05858 + 1.69521I$		
$a = -1.52532 + 0.06419I$		
$b = 1.65444 + 0.02754I$	$-19.6551 + 3.2714I$	$13.9526 - 2.4448I$
$c = 0.00202 + 1.61414I$		
$d = -0.01947 - 2.58949I$		
$u = -0.05858 - 1.69521I$		
$a = -1.52532 - 0.06419I$		
$b = 1.65444 - 0.02754I$	$-19.6551 - 3.2714I$	$13.9526 + 2.4448I$
$c = 0.00202 - 1.61414I$		
$d = -0.01947 + 2.58949I$		

II.

$$I_2^u = \langle -4.36 \times 10^{13}u^{24} - 6.53 \times 10^{12}u^{23} + \dots + 3.70 \times 10^{13}d - 1.73 \times 10^{14}, -2.52 \times 10^{13}au^{24} + 3.44 \times 10^{13}u^{24} + \dots - 9.91 \times 10^{13}a + 1.36 \times 10^{14}, -1.86 \times 10^{13}au^{24} + 8.39 \times 10^{12}u^{24} + \dots + 5.03 \times 10^{13}a - 3.05 \times 10^{13}, -8.65 \times 10^{13}au^{24} + 3.34 \times 10^{13}u^{24} + \dots + 7.16 \times 10^{14}a - 5.26 \times 10^{14}, u^{25} + u^{24} + \dots + 4u - 4 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.681034au^{24} - 0.931034u^{24} + \dots + 2.68187a - 3.68187 \\ 1.18103u^{24} + 0.176796u^{23} + \dots - 14.3723u + 4.68187 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.681034au^{24} - 0.250000u^{24} + \dots - 2.68187a - 1 \\ 1.18103u^{24} + 0.176796u^{23} + \dots - 14.3723u + 4.68187 \end{pmatrix} \\ a_7 &= \begin{pmatrix} a \\ 1.00424au^{24} - 0.454329u^{24} + \dots - 2.72414a + 1.65203 \end{pmatrix} \\ a_4 &= \begin{pmatrix} a \\ -1.00424au^{24} + 0.454329u^{24} + \dots + 2.72414a - 1.65203 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1.00424au^{24} - 0.454329u^{24} + \dots - 1.72414a + 1.65203 \\ -1.99712au^{24} + 0.930056u^{24} + \dots + 4.50730a - 3.40772 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 1.12683au^{24} - 0.931034u^{24} + \dots + 6.69882a - 3.68187 \\ -0.445792au^{24} + 1.18103u^{24} + \dots - 4.01695a + 4.68187 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -2.44203au^{24} + 1.16427u^{24} + \dots + 6.39909a + 0.185751 \\ 2.42063au^{24} - 1.33567u^{24} + \dots - 6.29543a - 3.15467 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -1.57386au^{24} + 0.195792u^{24} + \dots - 7.91615a + 3.01695 \\ 0.638749au^{24} + 0.561007u^{24} + \dots + 9.76810a - 3.30659 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes**

$$= -\frac{6062761600965}{9238337702138}u^{24} + \frac{3225176474347}{9238337702138}u^{23} + \dots + \frac{61042729884201}{9238337702138}u + \frac{27155343409896}{4619168851069}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_7	$(u^{25} + 8u^{24} + \cdots + 11u - 1)^2$
c_2	$(u^{25} + 2u^{24} + \cdots + 3u + 1)^2$
c_3, c_4, c_9	$u^{50} + 3u^{49} + \cdots + 24u - 16$
c_5	$(u^{25} + u^{24} + \cdots + 4u - 4)^2$
c_6, c_{10}, c_{12}	$-u^{50} + 3u^{49} + \cdots + 24u + 16$
c_8	$(u^{25} - 2u^{24} + \cdots + 3u - 1)^2$
c_{11}	$(u^{25} - u^{24} + \cdots + 4u + 4)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_7	$(y^{25} + 20y^{24} + \cdots + 251y - 1)^2$
c_2, c_8	$(y^{25} + 8y^{24} + \cdots + 11y - 1)^2$
c_3, c_4, c_6 c_9, c_{10}, c_{12}	$y^{50} - 39y^{49} + \cdots - 3872y + 256$
c_5, c_{11}	$(y^{25} + 15y^{24} + \cdots - 88y - 16)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.111975 + 0.962557I$		
$a = 0.567856 - 0.205094I$		
$b = -0.557801 - 0.562636I$	$3.08820 + 2.66172I$	$9.28523 - 3.57661I$
$c = 0.819383 + 0.216893I$		
$d = -0.206986 + 0.489964I$		
$u = -0.111975 + 0.962557I$		
$a = 0.526908 + 0.153743I$		
$b = -0.748963 + 0.510317I$	$3.08820 + 2.66172I$	$9.28523 - 3.57661I$
$c = -0.644034 + 0.069293I$		
$d = 0.133829 + 0.569559I$		
$u = -0.111975 - 0.962557I$		
$a = 0.567856 + 0.205094I$		
$b = -0.557801 + 0.562636I$	$3.08820 - 2.66172I$	$9.28523 + 3.57661I$
$c = 0.819383 - 0.216893I$		
$d = -0.206986 - 0.489964I$		
$u = -0.111975 - 0.962557I$		
$a = 0.526908 - 0.153743I$		
$b = -0.748963 - 0.510317I$	$3.08820 - 2.66172I$	$9.28523 + 3.57661I$
$c = -0.644034 - 0.069293I$		
$d = 0.133829 - 0.569559I$		
$u = 1.061780 + 0.135314I$		
$a = 0.707086 + 1.072640I$		
$b = 0.571600 + 0.649877I$	$4.81480 - 0.43356I$	$8.91196 - 0.04506I$
$c = -1.71425 + 0.05535I$		
$d = 0.452395 + 0.045198I$		
$u = 1.061780 + 0.135314I$		
$a = 0.424600 - 0.011543I$		
$b = -1.353420 - 0.063981I$	$4.81480 - 0.43356I$	$8.91196 - 0.04506I$
$c = 0.000864 - 0.699820I$		
$d = 0.605628 + 1.234590I$		

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.061780 - 0.135314I$		
$a = 0.707086 - 1.072640I$		
$b = 0.571600 - 0.649877I$	$4.81480 + 0.43356I$	$8.91196 + 0.04506I$
$c = -1.71425 - 0.05535I$		
$d = 0.452395 - 0.045198I$		
$u = 1.061780 - 0.135314I$		
$a = 0.424600 + 0.011543I$		
$b = -1.353420 + 0.063981I$	$4.81480 + 0.43356I$	$8.91196 + 0.04506I$
$c = 0.000864 + 0.699820I$		
$d = 0.605628 - 1.234590I$		
$u = -0.465035 + 1.033020I$		
$a = 0.568091 - 0.326292I$		
$b = -0.323623 - 0.760243I$	$1.37392 + 5.41987I$	$4.64303 - 6.54919I$
$c = 0.14931 + 1.61347I$		
$d = -0.45403 - 2.76996I$		
$u = -0.465035 + 1.033020I$		
$a = -2.06507 + 1.36916I$		
$b = 1.336380 + 0.223022I$	$1.37392 + 5.41987I$	$4.64303 - 6.54919I$
$c = -0.567551 - 0.202618I$		
$d = 0.072882 + 0.738584I$		
$u = -0.465035 - 1.033020I$		
$a = 0.568091 + 0.326292I$		
$b = -0.323623 + 0.760243I$	$1.37392 - 5.41987I$	$4.64303 + 6.54919I$
$c = 0.14931 - 1.61347I$		
$d = -0.45403 + 2.76996I$		
$u = -0.465035 - 1.033020I$		
$a = -2.06507 - 1.36916I$		
$b = 1.336380 - 0.223022I$	$1.37392 - 5.41987I$	$4.64303 + 6.54919I$
$c = -0.567551 + 0.202618I$		
$d = 0.072882 - 0.738584I$		

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.096160 + 0.296196I$ $a = 0.650082 - 0.890833I$ $b = 0.465476 - 0.732479I$ $c = 1.66469 + 0.09733I$ $d = -0.468544 + 0.097124I$	$4.43073 - 5.11531I$	$7.81745 + 5.48464I$
$u = -1.096160 + 0.296196I$ $a = 0.420667 + 0.025066I$ $b = -1.368770 + 0.141145I$ $c = -0.115286 - 0.653233I$ $d = -0.448735 + 1.169050I$	$4.43073 - 5.11531I$	$7.81745 + 5.48464I$
$u = -1.096160 - 0.296196I$ $a = 0.650082 + 0.890833I$ $b = 0.465476 + 0.732479I$ $c = 1.66469 - 0.09733I$ $d = -0.468544 - 0.097124I$	$4.43073 + 5.11531I$	$7.81745 - 5.48464I$
$u = -1.096160 - 0.296196I$ $a = 0.420667 - 0.025066I$ $b = -1.368770 - 0.141145I$ $c = -0.115286 + 0.653233I$ $d = -0.448735 - 1.169050I$	$4.43073 + 5.11531I$	$7.81745 - 5.48464I$
$u = 0.202658 + 1.122680I$ $a = 0.533156 + 0.248104I$ $b = -0.541755 + 0.717454I$ $c = -0.06617 + 1.68118I$ $d = 0.19823 - 2.88839I$	$5.39169 - 2.44039I$	$11.83401 + 3.61173I$
$u = 0.202658 + 1.122680I$ $a = -2.46070 - 0.62076I$ $b = 1.382070 - 0.096385I$ $c = 0.705023 - 0.069800I$ $d = -0.170493 + 0.648845I$	$5.39169 - 2.44039I$	$11.83401 + 3.61173I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.202658 - 1.122680I$ $a = 0.533156 - 0.248104I$ $b = -0.541755 - 0.717454I$ $c = -0.06617 - 1.68118I$ $d = 0.19823 + 2.88839I$	$5.39169 + 2.44039I$	$11.83401 - 3.61173I$
$u = 0.202658 - 1.122680I$ $a = -2.46070 + 0.62076I$ $b = 1.382070 + 0.096385I$ $c = 0.705023 + 0.069800I$ $d = -0.170493 - 0.648845I$	$5.39169 + 2.44039I$	$11.83401 - 3.61173I$
$u = -0.641188 + 0.544744I$ $a = 0.797389 - 0.461643I$ $b = 0.060728 - 0.543785I$ $c = 1.54551 + 0.43011I$ $d = -0.325741 + 0.217121I$	$-0.175498 - 1.059220I$	$0.606046 + 0.370576I$
$u = -0.641188 + 0.544744I$ $a = 0.462143 + 0.054007I$ $b = -1.134680 + 0.249465I$ $c = -0.213681 - 0.284545I$ $d = -0.259799 + 0.730373I$	$-0.175498 - 1.059220I$	$0.606046 + 0.370576I$
$u = -0.641188 - 0.544744I$ $a = 0.797389 + 0.461643I$ $b = 0.060728 + 0.543785I$ $c = 1.54551 - 0.43011I$ $d = -0.325741 - 0.217121I$	$-0.175498 + 1.059220I$	$0.606046 - 0.370576I$
$u = -0.641188 - 0.544744I$ $a = 0.462143 - 0.054007I$ $b = -1.134680 - 0.249465I$ $c = -0.213681 + 0.284545I$ $d = -0.259799 - 0.730373I$	$-0.175498 + 1.059220I$	$0.606046 - 0.370576I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.082989 + 0.805818I$ $a = 0.611223 - 0.162597I$ $b = -0.527939 - 0.406461I$ $c = 0.07908 + 1.88202I$ $d = -0.18925 - 3.40293I$	$2.66645 - 1.39976I$	$8.95722 + 0.06062I$
$u = -0.082989 + 0.805818I$ $a = -4.15470 + 0.66274I$ $b = 1.234720 + 0.037441I$ $c = -0.512649 + 0.193657I$ $d = 0.080299 + 0.506028I$	$2.66645 - 1.39976I$	$8.95722 + 0.06062I$
$u = -0.082989 - 0.805818I$ $a = 0.611223 + 0.162597I$ $b = -0.527939 + 0.406461I$ $c = 0.07908 - 1.88202I$ $d = -0.18925 + 3.40293I$	$2.66645 + 1.39976I$	$8.95722 - 0.06062I$
$u = -0.082989 - 0.805818I$ $a = -4.15470 - 0.66274I$ $b = 1.234720 - 0.037441I$ $c = -0.512649 - 0.193657I$ $d = 0.080299 - 0.506028I$	$2.66645 + 1.39976I$	$8.95722 - 0.06062I$
$u = 0.340493 + 0.559321I$ $a = 0.502139 - 0.055131I$ $b = -0.967761 - 0.216045I$ $c = -0.55582 + 1.83765I$ $d = 1.25446 - 3.40093I$	$2.95409 - 1.50728I$	$9.02072 + 4.31266I$
$u = 0.340493 + 0.559321I$ $a = -3.44021 - 4.33709I$ $b = 1.112260 - 0.141525I$ $c = -1.25214 + 0.82876I$ $d = 0.201811 + 0.262085I$	$2.95409 - 1.50728I$	$9.02072 + 4.31266I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.340493 - 0.559321I$		
$a = 0.502139 + 0.055131I$		
$b = -0.967761 + 0.216045I$	$2.95409 + 1.50728I$	$9.02072 - 4.31266I$
$c = -0.55582 - 1.83765I$		
$d = 1.25446 + 3.40093I$		
$u = 0.340493 - 0.559321I$		
$a = -3.44021 + 4.33709I$		
$b = 1.112260 + 0.141525I$	$2.95409 + 1.50728I$	$9.02072 - 4.31266I$
$c = -1.25214 - 0.82876I$		
$d = 0.201811 - 0.262085I$		
$u = -0.291960 + 1.368920I$		
$a = 0.445605 + 0.177592I$		
$b = -0.936546 + 0.771795I$	$10.21860 - 0.59688I$	$12.46758 + 1.80507I$
$c = 0.04016 + 1.62132I$		
$d = -0.16630 - 2.69033I$		
$u = -0.291960 + 1.368920I$		
$a = -1.85501 + 0.51711I$		
$b = 1.50021 + 0.13944I$	$10.21860 - 0.59688I$	$12.46758 + 1.80507I$
$c = 1.052040 - 0.018777I$		
$d = -0.373208 + 0.558147I$		
$u = -0.291960 - 1.368920I$		
$a = 0.445605 - 0.177592I$		
$b = -0.936546 - 0.771795I$	$10.21860 + 0.59688I$	$12.46758 - 1.80507I$
$c = 0.04016 - 1.62132I$		
$d = -0.16630 + 2.69033I$		
$u = -0.291960 - 1.368920I$		
$a = -1.85501 - 0.51711I$		
$b = 1.50021 - 0.13944I$	$10.21860 + 0.59688I$	$12.46758 - 1.80507I$
$c = 1.052040 + 0.018777I$		
$d = -0.373208 - 0.558147I$		

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.414621 + 1.342760I$ $a = 0.438582 - 0.161155I$ $b = -1.008850 - 0.738143I$ $c = -0.05457 + 1.60297I$ $d = 0.23190 - 2.65647I$	$9.63785 - 5.44271I$	$11.50171 + 3.51350I$
$u = 0.414621 + 1.342760I$ $a = -1.75747 - 0.71538I$ $b = 1.48812 - 0.19869I$ $c = -1.111910 + 0.008864I$ $d = 0.398238 + 0.522092I$	$9.63785 - 5.44271I$	$11.50171 + 3.51350I$
$u = 0.414621 - 1.342760I$ $a = 0.438582 + 0.161155I$ $b = -1.008850 + 0.738143I$ $c = -0.05457 - 1.60297I$ $d = 0.23190 + 2.65647I$	$9.63785 + 5.44271I$	$11.50171 - 3.51350I$
$u = 0.414621 - 1.342760I$ $a = -1.75747 + 0.71538I$ $b = 1.48812 + 0.19869I$ $c = -1.111910 - 0.008864I$ $d = 0.398238 - 0.522092I$	$9.63785 + 5.44271I$	$11.50171 - 3.51350I$
$u = 0.55118 + 1.32473I$ $a = 0.481455 + 0.338042I$ $b = -0.391201 + 0.976798I$ $c = -0.06239 + 1.57516I$ $d = 0.28799 - 2.59876I$	$8.61369 - 5.36637I$	$10.46678 + 3.05337I$
$u = 0.55118 + 1.32473I$ $a = -1.59514 - 0.88109I$ $b = 1.48035 - 0.26533I$ $c = 0.706254 - 0.310872I$ $d = -0.182445 + 0.824120I$	$8.61369 - 5.36637I$	$10.46678 + 3.05337I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.55118 - 1.32473I$ $a = 0.481455 - 0.338042I$ $b = -0.391201 - 0.976798I$ $c = -0.06239 - 1.57516I$ $d = 0.28799 + 2.59876I$	$8.61369 + 5.36637I$	$10.46678 - 3.05337I$
$u = 0.55118 - 1.32473I$ $a = -1.59514 + 0.88109I$ $b = 1.48035 + 0.26533I$ $c = 0.706254 + 0.310872I$ $d = -0.182445 - 0.824120I$	$8.61369 + 5.36637I$	$10.46678 - 3.05337I$
$u = -0.64072 + 1.29917I$ $a = 0.481272 - 0.361055I$ $b = -0.329543 - 0.997435I$ $c = 0.06623 + 1.55407I$ $d = -0.32299 - 2.55800I$	$7.62261 + 11.39030I$	$8.71017 - 7.76664I$
$u = -0.64072 + 1.29917I$ $a = -1.48513 + 0.98104I$ $b = 1.46878 + 0.30967I$ $c = -0.677635 - 0.347996I$ $d = 0.160711 + 0.856587I$	$7.62261 + 11.39030I$	$8.71017 - 7.76664I$
$u = -0.64072 - 1.29917I$ $a = 0.481272 + 0.361055I$ $b = -0.329543 + 0.997435I$ $c = 0.06623 - 1.55407I$ $d = -0.32299 + 2.55800I$	$7.62261 - 11.39030I$	$8.71017 + 7.76664I$
$u = -0.64072 - 1.29917I$ $a = -1.48513 - 0.98104I$ $b = 1.46878 - 0.30967I$ $c = -0.677635 + 0.347996I$ $d = 0.160711 - 0.856587I$	$7.62261 - 11.39030I$	$8.71017 + 7.76664I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.518583$		
$a = 1.41735$		
$b = 0.294460$	2.09579	3.55620
$c = -2.39378$		
$d = 0.245289$		
$u = 0.518583$		
$a = 0.472999$		
$b = -1.11417$	2.09579	3.55620
$c = -0.167199$		
$d = 0.735015$		

$$\text{III. } I_1^v = \langle a, d, c - v, b + 1, v^2 - v + 1 \rangle$$

(i) **Arc colorings**

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v - 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v \\ v \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes = $4v + 1$**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_7	$u^2 - u + 1$
c_3, c_4	$(u + 1)^2$
c_5, c_9, c_{10} c_{11}, c_{12}	u^2
c_6	$(u - 1)^2$
c_8	$u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_7 c_8	$y^2 + y + 1$
c_3, c_4, c_6	$(y - 1)^2$
c_5, c_9, c_{10} c_{11}, c_{12}	y^2

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.500000 + 0.866025I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0$		
$b = -1.00000$	$1.64493 - 2.02988I$	$3.00000 + 3.46410I$
$c = 0.500000 + 0.866025I$		
$d = 0$		
$v = 0.500000 - 0.866025I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0$		
$b = -1.00000$	$1.64493 + 2.02988I$	$3.00000 - 3.46410I$
$c = 0.500000 - 0.866025I$		
$d = 0$		

$$\text{IV. } I_2^v = \langle c, d+v-1, b, a-1, v^2-v+1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ -v+1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} v \\ v-1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -v \\ -v+1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ -v \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ v-1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-4v + 5$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_7, c_8	$u^2 - u + 1$
c_2	$u^2 + u + 1$
c_3, c_4, c_5 c_6, c_{11}	u^2
c_9, c_{10}	$(u + 1)^2$
c_{12}	$(u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_7 c_8	$y^2 + y + 1$
c_3, c_4, c_5 c_6, c_{11}	y^2
c_9, c_{10}, c_{12}	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.500000 + 0.866025I$		
$a = 1.00000$		
$b = 0$	$1.64493 + 2.02988I$	$3.00000 - 3.46410I$
$c = 0$		
$d = 0.500000 - 0.866025I$		
$v = 0.500000 - 0.866025I$		
$a = 1.00000$		
$b = 0$	$1.64493 - 2.02988I$	$3.00000 + 3.46410I$
$c = 0$		
$d = 0.500000 + 0.866025I$		

$$\mathbf{V}. \quad I_3^v = \langle a, d+1, c-a+1, b+1, v+1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 12

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_5 c_7, c_8, c_{11}	u
c_3, c_4, c_9 c_{10}	$u + 1$
c_6, c_{12}	$u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5 c_7, c_8, c_{11}	y
c_3, c_4, c_6 c_9, c_{10}, c_{12}	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$		
$b = -1.00000$	3.28987	12.0000
$c = -1.00000$		
$d = -1.00000$		

VI.

$$I_4^v = \langle a, -2v^2c + v^3 + \cdots + 2ca + a, dv - 1, -2v^3c + v^4 + \cdots + a^2 + av, b + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} c \\ d \end{pmatrix} \\ a_{12} &= \begin{pmatrix} v \\ 0 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -c + v \\ -d \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0 \\ -1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0 \\ 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} c - v \\ d \end{pmatrix} \\ a_8 &= \begin{pmatrix} -c + v - 1 \\ dc - 2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -c + v \\ -d - c + v \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class** = -1

(iii) **Cusp Shapes** = $d^2 + v^2 - 4c + 4v + 8$

(iv) **u-Polynomials at the component** : It cannot be defined for a positive dimension component.

(v) **Riley Polynomials at the component** : It cannot be defined for a positive dimension component.

(iv) Complex Volumes and Cusp Shapes

Solution to I_4^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = \dots$		
$a = \dots$		
$b = \dots$	$3.28987 + 2.02988I$	$11.78425 + 3.62207I$
$c = \dots$		
$d = \dots$		

VII. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1, c_7	$u(u^2 - u + 1)^2(u^{33} + 11u^{32} + \dots + 8u - 16)$
c_2, c_8	$u(u^2 - u + 1)(u^2 + u + 1)(u^{33} + u^{32} + \dots - 12u + 4)$
c_3, c_4, c_9 c_{10}	$u^2(u + 1)^3(u^{33} + 5u^{32} + \dots - 7u^2 - 1)$
c_5, c_{11}	$u^5(u^{33} - 3u^{32} + \dots - 32u + 32)$
c_6, c_{12}	$u^2(u - 1)^3(u^{33} + 5u^{32} + \dots - 7u^2 - 1)$

VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_7	$y(y^2 + y + 1)^2(y^{33} + 23y^{32} + \dots - 14304y - 256)$
c_2, c_8	$y(y^2 + y + 1)^2(y^{33} + 11y^{32} + \dots + 8y - 16)$
c_3, c_4, c_6 c_9, c_{10}, c_{12}	$y^2(y - 1)^3(y^{33} - 39y^{32} + \dots - 14y - 1)$
c_5, c_{11}	$y^5(y^{33} + 15y^{32} + \dots - 6144y - 1024)$