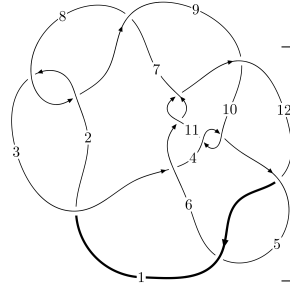
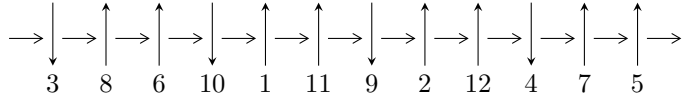


12a<sub>0702</sub> (K12a<sub>0702</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$4,10 \xrightarrow{c_4} 5 \xrightarrow{c_{10}} 7,11 \xrightarrow{c_{11}} 12 \xrightarrow{c_{12}} 1 \xrightarrow{c_6} 6 \xrightarrow{c_3} 3 \xrightarrow{c_9} 9 \xrightarrow{c_7} 8 \xrightarrow{c_2} 2 \rightsquigarrow c_1, c_5, c_8$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -1.19038 \times 10^{83} u^{40} + 4.26853 \times 10^{83} u^{39} + \dots + 1.55480 \times 10^{86} b - 1.07861 \times 10^{86}, \\ - 5.72981 \times 10^{85} u^{40} + 1.60933 \times 10^{86} u^{39} + \dots + 3.88699 \times 10^{87} a - 9.00245 \times 10^{87}, \\ u^{41} - 3u^{40} + \dots - 434u + 50 \rangle$$

$$I_2^u = \langle -u^2 a + b + 1, -2u^{26} a - 2u^{25} a + \dots - 3a + 6, u^{27} + u^{26} + \dots + 2u - 1 \rangle$$

$$I_3^u = \langle u^3 - u^2 + 5b + 2u + 3, 3u^3 + 2u^2 + 10a - 14u - 6, u^4 - 2u^2 + 2 \rangle$$

$$I_4^u = \langle b + a - 1, 8a^3 + 4a^2 u - 12a^2 - 4au + 2a + 1, u^2 + 1 \rangle$$

$$I_1^v = \langle a, b + 1, v + 1 \rangle$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 106 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -1.19 \times 10^{83} u^{40} + 4.27 \times 10^{83} u^{39} + \dots + 1.55 \times 10^{86} b - 1.08 \times 10^{86}, -5.73 \times 10^{85} u^{40} + 1.61 \times 10^{86} u^{39} + \dots + 3.89 \times 10^{87} a - 9.00 \times 10^{87}, u^{41} - 3u^{40} + \dots - 434u + 50 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0147410u^{40} - 0.0414030u^{39} + \dots + 31.9284u + 2.31605 \\ 0.000765620u^{40} - 0.00274539u^{39} + \dots + 1.07683u + 0.693733 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0115033u^{40} - 0.0353806u^{39} + \dots + 46.5023u - 6.32310 \\ 0.00230652u^{40} - 0.00672063u^{39} + \dots + 8.78658u - 0.731794 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0138747u^{40} - 0.0423896u^{39} + \dots + 56.2419u - 7.09843 \\ 0.00281990u^{40} - 0.00776945u^{39} + \dots + 8.71363u - 0.737049 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.0146359u^{40} - 0.0416011u^{39} + \dots + 31.6745u + 2.43461 \\ 0.000870716u^{40} - 0.00254730u^{39} + \dots + 1.33067u + 0.575165 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.0128297u^{40} - 0.0366995u^{39} + \dots + 28.5656u + 1.49810 \\ 0.00113437u^{40} - 0.00267356u^{39} + \dots + 2.04755u + 0.246021 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.00492043u^{40} - 0.0158956u^{39} + \dots + 24.8003u - 4.18302 \\ 0.00178970u^{40} - 0.00537829u^{39} + \dots + 7.06620u - 0.641486 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.000300319u^{40} + 0.00224674u^{39} + \dots - 9.20295u + 3.52338 \\ -0.00108526u^{40} + 0.00257937u^{39} + \dots - 2.40758u + 0.183564 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.00367128u^{40} - 0.00992859u^{39} + \dots + 5.43318u + 0.814239 \\ 0.00134579u^{40} - 0.00361819u^{39} + \dots + 3.39304u + 0.0150160 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-0.0228051u^{40} + 0.0718802u^{39} + \dots - 38.8520u + 4.20733$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u^{41} + 13u^{40} + \dots - 1260u - 100$
$c_2, c_8$	$u^{41} + 3u^{40} + \dots - 10u + 10$
$c_3, c_9$	$64(64u^{41} + 256u^{40} + \dots - 13u^2 - 1)$
$c_4, c_{10}$	$u^{41} - 3u^{40} + \dots - 434u + 50$
$c_5, c_6, c_{11}$ $c_{12}$	$u^{41} - u^{40} + \dots + 14u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$y^{41} + 33y^{40} + \dots - 489200y - 10000$
$c_2, c_8$	$y^{41} + 13y^{40} + \dots - 1260y - 100$
$c_3, c_9$	$4096(4096y^{41} - 147456y^{40} + \dots - 26y - 1)$
$c_4, c_{10}$	$y^{41} + 25y^{40} + \dots - 199044y - 2500$
$c_5, c_6, c_{11}$ $c_{12}$	$y^{41} - 31y^{40} + \dots - 96y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.455951 + 0.852881I$ $a = 0.728739 + 0.291805I$ $b = 0.139910 - 0.558255I$	$0.86494 + 1.62805I$	$5.67415 - 3.58289I$
$u = 0.455951 - 0.852881I$ $a = 0.728739 - 0.291805I$ $b = 0.139910 + 0.558255I$	$0.86494 - 1.62805I$	$5.67415 + 3.58289I$
$u = -0.021368 + 1.036750I$ $a = 1.161860 + 0.121316I$ $b = -1.236090 - 0.167032I$	$4.65548 + 2.80230I$	$13.48887 - 2.99820I$
$u = -0.021368 - 1.036750I$ $a = 1.161860 - 0.121316I$ $b = -1.236090 + 0.167032I$	$4.65548 - 2.80230I$	$13.48887 + 2.99820I$
$u = -0.850702 + 0.604796I$ $a = 1.089290 - 0.351516I$ $b = -0.364276 + 0.545866I$	$-0.16962 + 2.89326I$	$2.19290 - 0.10248I$
$u = -0.850702 - 0.604796I$ $a = 1.089290 + 0.351516I$ $b = -0.364276 - 0.545866I$	$-0.16962 - 2.89326I$	$2.19290 + 0.10248I$
$u = -0.471844 + 0.764313I$ $a = -0.121231 + 0.155243I$ $b = 0.127637 - 0.862325I$	$1.00547 + 1.41725I$	$6.32483 - 4.75240I$
$u = -0.471844 - 0.764313I$ $a = -0.121231 - 0.155243I$ $b = 0.127637 + 0.862325I$	$1.00547 - 1.41725I$	$6.32483 + 4.75240I$
$u = 0.676505 + 0.580935I$ $a = -0.636641 + 0.057470I$ $b = 0.388189 + 0.860067I$	$-0.01909 - 5.83785I$	$3.11476 + 10.68510I$
$u = 0.676505 - 0.580935I$ $a = -0.636641 - 0.057470I$ $b = 0.388189 - 0.860067I$	$-0.01909 + 5.83785I$	$3.11476 - 10.68510I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.106757 + 1.119200I$		
$a = 0.407888 + 0.094333I$	$-0.743392 - 0.853731I$	$8.26894 + 8.56558I$
$b = 0.707134 - 0.209548I$		
$u = 0.106757 - 1.119200I$		
$a = 0.407888 - 0.094333I$	$-0.743392 + 0.853731I$	$8.26894 - 8.56558I$
$b = 0.707134 + 0.209548I$		
$u = -0.135573 + 0.750401I$		
$a = 0.497918 + 0.003694I$	$0.517216 + 0.980568I$	$7.41204 - 7.03124I$
$b = -0.087550 - 0.403450I$		
$u = -0.135573 - 0.750401I$		
$a = 0.497918 - 0.003694I$	$0.517216 - 0.980568I$	$7.41204 + 7.03124I$
$b = -0.087550 + 0.403450I$		
$u = 0.015207 + 1.271930I$		
$a = 0.258817 + 0.015105I$	$4.96111 - 3.02863I$	$13.36303 + 2.94764I$
$b = 1.052190 - 0.036306I$		
$u = 0.015207 - 1.271930I$		
$a = 0.258817 - 0.015105I$	$4.96111 + 3.02863I$	$13.36303 - 2.94764I$
$b = 1.052190 + 0.036306I$		
$u = 1.267430 + 0.165148I$		
$a = -1.57147 - 0.04495I$	$10.5970 - 11.3672I$	$9.96311 + 7.10557I$
$b = 0.523699 + 0.462735I$		
$u = 1.267430 - 0.165148I$		
$a = -1.57147 + 0.04495I$	$10.5970 + 11.3672I$	$9.96311 - 7.10557I$
$b = 0.523699 - 0.462735I$		
$u = -1.303430 + 0.145939I$		
$a = -1.59455 + 0.04931I$	$11.47150 + 4.79100I$	$11.44614 - 2.44954I$
$b = 0.546188 - 0.390643I$		
$u = -1.303430 - 0.145939I$		
$a = -1.59455 - 0.04931I$	$11.47150 - 4.79100I$	$11.44614 + 2.44954I$
$b = 0.546188 + 0.390643I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.48598$ $a = -1.70628$ $b = 0.809440$	6.30192	14.4050
$u = 0.346910 + 0.359461I$ $a = -0.044452 + 0.984431I$ $b = 0.444124 + 0.546475I$	$-2.78156 - 0.97104I$	$-4.60139 + 3.38415I$
$u = 0.346910 - 0.359461I$ $a = -0.044452 - 0.984431I$ $b = 0.444124 - 0.546475I$	$-2.78156 + 0.97104I$	$-4.60139 - 3.38415I$
$u = 1.54269 + 0.18278I$ $a = -1.72780 - 0.12223I$ $b = 0.941440 + 0.289062I$	$2.02994 - 4.70447I$	$11.23439 + 5.82932I$
$u = 1.54269 - 0.18278I$ $a = -1.72780 + 0.12223I$ $b = 0.941440 - 0.289062I$	$2.02994 + 4.70447I$	$11.23439 - 5.82932I$
$u = 0.52762 + 1.47752I$ $a = -0.21972 + 1.74763I$ $b = 0.20870 - 2.77021I$	$15.8147 - 17.6250I$	0
$u = 0.52762 - 1.47752I$ $a = -0.21972 - 1.74763I$ $b = 0.20870 + 2.77021I$	$15.8147 + 17.6250I$	0
$u = -0.53754 + 1.48742I$ $a = -0.19175 - 1.71682I$ $b = 0.21292 + 2.73453I$	$16.6893 + 11.2011I$	0
$u = -0.53754 - 1.48742I$ $a = -0.19175 + 1.71682I$ $b = 0.21292 - 2.73453I$	$16.6893 - 11.2011I$	0
$u = 0.50522 + 1.54544I$ $a = -0.04761 + 1.80771I$ $b = 0.06833 - 2.69458I$	$7.92273 - 11.59880I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.50522 - 1.54544I$ $a = -0.04761 - 1.80771I$ $b = 0.06833 + 2.69458I$	$7.92273 + 11.59880I$	0
$u = -0.56045 + 1.56650I$ $a = 0.03187 - 1.69887I$ $b = 0.08948 + 2.57599I$	$11.62590 + 7.27779I$	0
$u = -0.56045 - 1.56650I$ $a = 0.03187 + 1.69887I$ $b = 0.08948 - 2.57599I$	$11.62590 - 7.27779I$	0
$u = -0.68168 + 1.55704I$ $a = 0.25317 - 1.45413I$ $b = 0.08907 + 2.25581I$	$15.8034 + 2.5637I$	0
$u = -0.68168 - 1.55704I$ $a = 0.25317 + 1.45413I$ $b = 0.08907 - 2.25581I$	$15.8034 - 2.5637I$	0
$u = 0.71972 + 1.54565I$ $a = 0.34306 + 1.40038I$ $b = 0.04686 - 2.15261I$	$14.6951 + 4.0355I$	0
$u = 0.71972 - 1.54565I$ $a = 0.34306 - 1.40038I$ $b = 0.04686 + 2.15261I$	$14.6951 - 4.0355I$	0
$u = 0.58769 + 1.64814I$ $a = 0.20254 + 1.74524I$ $b = -0.04962 - 2.50192I$	$7.14307 - 3.31046I$	0
$u = 0.58769 - 1.64814I$ $a = 0.20254 - 1.74524I$ $b = -0.04962 + 2.50192I$	$7.14307 + 3.31046I$	0
$u = 0.053861 + 0.132763I$ $a = 4.65323 + 2.55602I$ $b = 0.746943 + 0.099019I$	$1.42567 + 2.78320I$	$0.79755 - 2.69383I$



	Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u =$	$0.053861 - 0.132763I$		
$a =$	$4.65323 - 2.55602I$	$1.42567 - 2.78320I$	$0.79755 + 2.69383I$
$b =$	$0.746943 - 0.099019I$		

**II.**

$$I_2^u = \langle -u^2a + b + 1, -2u^{26}a - 2u^{25}a + \dots - 3a + 6, u^{27} + u^{26} + \dots + 2u - 1 \rangle$$

**(i) Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} a \\ u^2a - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u^{26} + 3u^{25} + \dots + 2au - 4u \\ -2u^{25} - 2u^{24} + \dots - u + 2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^{26} + 3u^{25} + \dots + au - 2u \\ -2u^{25} - 2u^{24} + \dots - u + 2 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^4a - u^2a + u^2 + a \\ u^4a + 2u^2a - u^2 - 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -2u^{26}a + 4u^{26} + \dots - a + 5 \\ 2u^{26}a - 2u^{26} + \dots + 8u - 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 2u^{25}a - 3u^{26} + \dots - 2a + 2 \\ -2u^{25}a + 2u^{26} + \dots + 2a - 2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -2u^{26}a + 4u^{26} + \dots + a + 3 \\ 2u^{26}a - 2u^{26} + \dots + 8u - 3 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 2u^{25}a - u^{26} + \dots - 2a + 6 \\ -2u^{25}a + 2u^{26} + \dots + 2a - 2 \end{pmatrix} \end{aligned}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes**  $= -4u^{25} - 4u^{24} - 44u^{23} - 40u^{22} - 208u^{21} - 168u^{20} - 536u^{19} - 372u^{18} - 772u^{17} - 432u^{16} - 508u^{15} - 184u^{14} + 100u^{13} + 92u^{12} + 340u^{11} + 72u^{10} + 68u^9 - 48u^8 - 144u^7 - 28u^6 - 76u^5 + 12u^4 + 16u^3 + 20u + 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$(u^{27} + 7u^{26} + \dots - 2u - 1)^2$
$c_2, c_8$	$(u^{27} - u^{26} + \dots - u^2 - 1)^2$
$c_3, c_9$	$u^{54} - 7u^{53} + \dots - 168722854u - 19874761$
$c_4, c_{10}$	$(u^{27} + u^{26} + \dots + 2u - 1)^2$
$c_5, c_6, c_{11}$ $c_{12}$	$u^{54} - u^{53} + \dots - 532u - 53$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$(y^{27} + 27y^{26} + \dots + 14y - 1)^2$
$c_2, c_8$	$(y^{27} + 7y^{26} + \dots - 2y - 1)^2$
$c_3, c_9$	$y^{54} - 37y^{53} + \dots - 8208746653844232y + 395006124807121$
$c_4, c_{10}$	$(y^{27} + 23y^{26} + \dots - 2y - 1)^2$
$c_5, c_6, c_{11}$ $c_{12}$	$y^{54} - 41y^{53} + \dots - 143528y + 2809$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.278071 + 0.956556I$ $a = 2.36487 + 0.60631I$ $b = -2.65845 - 1.76596I$	$7.99009 - 3.05015I$	$9.08831 + 1.99178I$
$u = -0.278071 + 0.956556I$ $a = -0.31543 + 2.83300I$ $b = 0.77133 - 2.20533I$	$7.99009 - 3.05015I$	$9.08831 + 1.99178I$
$u = -0.278071 - 0.956556I$ $a = 2.36487 - 0.60631I$ $b = -2.65845 + 1.76596I$	$7.99009 + 3.05015I$	$9.08831 - 1.99178I$
$u = -0.278071 - 0.956556I$ $a = -0.31543 - 2.83300I$ $b = 0.77133 + 2.20533I$	$7.99009 + 3.05015I$	$9.08831 - 1.99178I$
$u = 0.260338 + 0.833668I$ $a = 2.60824 + 0.53025I$ $b = -2.86613 + 0.79958I$	$8.16912 - 2.83072I$	$9.79804 + 3.74350I$
$u = 0.260338 + 0.833668I$ $a = 0.66908 - 3.18206I$ $b = -0.03843 + 2.28630I$	$8.16912 - 2.83072I$	$9.79804 + 3.74350I$
$u = 0.260338 - 0.833668I$ $a = 2.60824 - 0.53025I$ $b = -2.86613 - 0.79958I$	$8.16912 + 2.83072I$	$9.79804 - 3.74350I$
$u = 0.260338 - 0.833668I$ $a = 0.66908 + 3.18206I$ $b = -0.03843 - 2.28630I$	$8.16912 + 2.83072I$	$9.79804 - 3.74350I$
$u = -0.768863 + 0.186622I$ $a = 0.767167 - 0.556376I$ $b = -0.732874 - 0.529681I$	$5.58232 + 7.02686I$	$5.81546 - 6.08794I$
$u = -0.768863 + 0.186622I$ $a = 1.47566 + 0.78554I$ $b = 0.0463708 + 0.0135400I$	$5.58232 + 7.02686I$	$5.81546 - 6.08794I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.768863 - 0.186622I$ $a = 0.767167 + 0.556376I$ $b = -0.732874 + 0.529681I$	$5.58232 - 7.02686I$	$5.81546 + 6.08794I$
$u = -0.768863 - 0.186622I$ $a = 1.47566 - 0.78554I$ $b = 0.0463708 - 0.0135400I$	$5.58232 - 7.02686I$	$5.81546 + 6.08794I$
$u = 0.738973 + 0.201195I$ $a = 0.724890 + 0.569525I$ $b = -0.802846 + 0.503503I$	$6.04391 - 0.96140I$	$6.72916 + 1.18503I$
$u = 0.738973 + 0.201195I$ $a = 1.55361 - 0.82203I$ $b = 0.0299440 + 0.0463562I$	$6.04391 - 0.96140I$	$6.72916 + 1.18503I$
$u = 0.738973 - 0.201195I$ $a = 0.724890 - 0.569525I$ $b = -0.802846 - 0.503503I$	$6.04391 + 0.96140I$	$6.72916 - 1.18503I$
$u = 0.738973 - 0.201195I$ $a = 1.55361 + 0.82203I$ $b = 0.0299440 - 0.0463562I$	$6.04391 + 0.96140I$	$6.72916 - 1.18503I$
$u = -0.291604 + 1.207020I$ $a = -0.661099 + 0.685256I$ $b = 0.389321 - 0.474702I$	$2.46677 + 0.98697I$	$3.17341 + 0.25321I$
$u = -0.291604 + 1.207020I$ $a = 0.48769 + 1.53601I$ $b = -0.58778 - 2.45051I$	$2.46677 + 0.98697I$	$3.17341 + 0.25321I$
$u = -0.291604 - 1.207020I$ $a = -0.661099 - 0.685256I$ $b = 0.389321 + 0.474702I$	$2.46677 - 0.98697I$	$3.17341 - 0.25321I$
$u = -0.291604 - 1.207020I$ $a = 0.48769 - 1.53601I$ $b = -0.58778 + 2.45051I$	$2.46677 - 0.98697I$	$3.17341 - 0.25321I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.750412 + 0.064416I$ $a = 0.856575 - 0.332457I$ $b = -0.553343 - 0.268644I$	$-1.00899 + 2.79673I$	$-0.25981 - 4.61920I$
$u = -0.750412 + 0.064416I$ $a = 1.42141 + 0.41171I$ $b = -0.165674 + 0.092715I$	$-1.00899 + 2.79673I$	$-0.25981 - 4.61920I$
$u = -0.750412 - 0.064416I$ $a = 0.856575 + 0.332457I$ $b = -0.553343 + 0.268644I$	$-1.00899 - 2.79673I$	$-0.25981 + 4.61920I$
$u = -0.750412 - 0.064416I$ $a = 1.42141 - 0.41171I$ $b = -0.165674 - 0.092715I$	$-1.00899 - 2.79673I$	$-0.25981 + 4.61920I$
$u = 0.082485 + 1.285040I$ $a = -1.23688 + 0.88472I$ $b = 0.84651 - 1.71714I$	$7.63181 - 2.01066I$	$12.08108 + 3.90758I$
$u = 0.082485 + 1.285040I$ $a = -0.56330 - 1.80575I$ $b = 0.30916 + 2.85016I$	$7.63181 - 2.01066I$	$12.08108 + 3.90758I$
$u = 0.082485 - 1.285040I$ $a = -1.23688 - 0.88472I$ $b = 0.84651 + 1.71714I$	$7.63181 + 2.01066I$	$12.08108 - 3.90758I$
$u = 0.082485 - 1.285040I$ $a = -0.56330 + 1.80575I$ $b = 0.30916 - 2.85016I$	$7.63181 + 2.01066I$	$12.08108 - 3.90758I$
$u = 0.257867 + 1.292320I$ $a = -0.657719 - 0.061377I$ $b = 0.095618 - 0.339940I$	$5.83412 - 3.27708I$	$11.27794 + 2.87566I$
$u = 0.257867 + 1.292320I$ $a = 0.16467 - 1.58727I$ $b = -0.20616 + 2.65508I$	$5.83412 - 3.27708I$	$11.27794 + 2.87566I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.257867 - 1.292320I$ $a = -0.657719 + 0.061377I$ $b = 0.095618 + 0.339940I$	$5.83412 + 3.27708I$	$11.27794 - 2.87566I$
$u = 0.257867 - 1.292320I$ $a = 0.16467 + 1.58727I$ $b = -0.20616 - 2.65508I$	$5.83412 + 3.27708I$	$11.27794 - 2.87566I$
$u = -0.317436 + 1.304880I$ $a = 0.20283 + 1.46123I$ $b = -0.11439 - 2.50885I$	$3.27233 + 6.65682I$	$5.19788 - 7.22011I$
$u = -0.317436 + 1.304880I$ $a = -0.350883 + 0.118774I$ $b = -0.339506 + 0.100412I$	$3.27233 + 6.65682I$	$5.19788 - 7.22011I$
$u = -0.317436 - 1.304880I$ $a = 0.20283 - 1.46123I$ $b = -0.11439 + 2.50885I$	$3.27233 - 6.65682I$	$5.19788 + 7.22011I$
$u = -0.317436 - 1.304880I$ $a = -0.350883 - 0.118774I$ $b = -0.339506 - 0.100412I$	$3.27233 - 6.65682I$	$5.19788 + 7.22011I$
$u = 0.649647$ $a = 0.553820$ $b = -0.766265$	$1.77816$	$5.74170$
$u = 0.649647$ $a = 1.85261$ $b = -0.218123$	$1.77816$	$5.74170$
$u = 0.307012 + 1.374630I$ $a = 0.11853 - 1.41160I$ $b = -0.02134 + 2.63436I$	$11.02600 - 4.75862I$	$11.32590 + 2.41055I$
$u = 0.307012 + 1.374630I$ $a = -0.301203 + 0.156502I$ $b = -0.591333 - 0.535207I$	$11.02600 - 4.75862I$	$11.32590 + 2.41055I$



Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.307012 - 1.374630I$ $a = 0.11853 + 1.41160I$ $b = -0.02134 - 2.63436I$	$11.02600 + 4.75862I$	$11.32590 - 2.41055I$
$u = 0.307012 - 1.374630I$ $a = -0.301203 - 0.156502I$ $b = -0.591333 + 0.535207I$	$11.02600 + 4.75862I$	$11.32590 - 2.41055I$
$u = -0.322115 + 1.372980I$ $a = 0.135135 + 1.402660I$ $b = -0.00005 - 2.61810I$	$10.5129 + 10.9775I$	$10.31167 - 7.27184I$
$u = -0.322115 + 1.372980I$ $a = -0.257057 - 0.132543I$ $b = -0.659339 + 0.463470I$	$10.5129 + 10.9775I$	$10.31167 - 7.27184I$
$u = -0.322115 - 1.372980I$ $a = 0.135135 - 1.402660I$ $b = -0.00005 + 2.61810I$	$10.5129 - 10.9775I$	$10.31167 + 7.27184I$
$u = -0.322115 - 1.372980I$ $a = -0.257057 + 0.132543I$ $b = -0.659339 - 0.463470I$	$10.5129 - 10.9775I$	$10.31167 + 7.27184I$
$u = 0.01000 + 1.42794I$ $a = -0.476092 + 1.070440I$ $b = -0.05987 - 2.19612I$	$15.0119 - 3.1530I$	$13.82291 + 2.60032I$
$u = 0.01000 + 1.42794I$ $a = -0.447560 - 1.123330I$ $b = -0.05538 + 2.27757I$	$15.0119 - 3.1530I$	$13.82291 + 2.60032I$
$u = 0.01000 - 1.42794I$ $a = -0.476092 - 1.070440I$ $b = -0.05987 + 2.19612I$	$15.0119 + 3.1530I$	$13.82291 - 2.60032I$
$u = 0.01000 - 1.42794I$ $a = -0.447560 + 1.123330I$ $b = -0.05538 - 2.27757I$	$15.0119 + 3.1530I$	$13.82291 - 2.60032I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.247000 + 0.300914I$		
$a = 0.24147 + 2.21936I$	$2.93764 - 0.95364I$	$5.76719 + 7.10310I$
$b = -1.337040 - 0.029666I$		
$u = 0.247000 + 0.300914I$		
$a = 2.77217 - 2.52780I$	$2.93764 - 0.95364I$	$5.76719 + 7.10310I$
$b = -0.706130 + 0.486758I$		
$u = 0.247000 - 0.300914I$		
$a = 0.24147 - 2.21936I$	$2.93764 + 0.95364I$	$5.76719 - 7.10310I$
$b = -1.337040 + 0.029666I$		
$u = 0.247000 - 0.300914I$		
$a = 2.77217 + 2.52780I$	$2.93764 + 0.95364I$	$5.76719 - 7.10310I$
$b = -0.706130 - 0.486758I$		

$$\text{III. } I_3^u = \langle u^3 - u^2 + 5b + 2u + 3, 3u^3 + 2u^2 + 10a - 14u - 6, u^4 - 2u^2 + 2 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{3}{10}u^3 - \frac{1}{5}u^2 + \frac{7}{5}u + \frac{3}{5} \\ -\frac{1}{5}u^3 + \frac{1}{5}u^2 - \frac{2}{5}u - \frac{3}{5} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{3}{10}u^3 - \frac{1}{5}u^2 + \frac{2}{5}u + \frac{3}{5} \\ -\frac{1}{5}u^3 + \frac{1}{5}u^2 + \frac{2}{5}u - \frac{3}{5} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{3}{10}u^3 - \frac{1}{5}u^2 + \frac{2}{5}u - \frac{2}{5} \\ -\frac{1}{5}u^3 - \frac{4}{5}u^2 + \frac{3}{5}u - \frac{3}{5} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{3}{10}u^3 - \frac{1}{5}u^2 + \frac{2}{5}u + \frac{3}{5} \\ -\frac{1}{5}u^3 + \frac{1}{5}u^2 + \frac{3}{5}u - \frac{3}{5} \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{1}{50}u^3 + \frac{4}{25}u + 1 \\ \frac{8}{25}u^3 - \frac{1}{5}u^2 - \frac{14}{25}u + \frac{3}{5} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{3}{10}u^3 + \frac{8}{25}u^2 - \frac{2}{5}u - \frac{14}{25} \\ -\frac{3}{25}u^2 + u - \frac{1}{25} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{10}u^3 - \frac{3}{25}u^2 + \frac{4}{5}u - \frac{1}{25} \\ \frac{4}{5}u^3 - \frac{2}{25}u^2 - \frac{2}{5}u - \frac{9}{25} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{9}{50}u^3 + \frac{4}{5}u^2 + \frac{11}{25}u - \frac{2}{5} \\ -\frac{3}{25}u^3 - \frac{3}{5}u^2 - \frac{1}{25}u - \frac{1}{5} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4u^2 + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$(u^2 - 2u + 2)^2$
$c_2, c_8$	$u^4 + 2u^2 + 2$
$c_3, c_9$	$25(25u^4 + 40u^3 + 12u^2 - 4u + 1)$
$c_4, c_{10}$	$u^4 - 2u^2 + 2$
$c_5, c_{11}$	$(u + 1)^4$
$c_6, c_{12}$	$(u - 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$(y^2 + 4)^2$
$c_2, c_8$	$(y^2 + 2y + 2)^2$
$c_3, c_9$	$625(625y^4 - 1000y^3 + 514y^2 + 8y + 1)$
$c_4, c_{10}$	$(y^2 - 2y + 2)^2$
$c_5, c_6, c_{11}$ $c_{12}$	$(y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.098680 + 0.455090I$	$0.82247 - 3.66386I$	$8.00000 + 4.00000I$
$a = 1.74508 - 0.02901I$		
$b = -0.968192 - 0.292791I$		
$u = 1.098680 - 0.455090I$	$0.82247 + 3.66386I$	$8.00000 - 4.00000I$
$a = 1.74508 + 0.02901I$		
$b = -0.968192 + 0.292791I$		
$u = -1.098680 + 0.455090I$	$0.82247 + 3.66386I$	$8.00000 - 4.00000I$
$a = -0.945079 + 0.370994I$		
$b = 0.168192 - 0.692791I$		
$u = -1.098680 - 0.455090I$	$0.82247 - 3.66386I$	$8.00000 + 4.00000I$
$a = -0.945079 - 0.370994I$		
$b = 0.168192 + 0.692791I$		

$$\text{IV. } I_4^u = \langle b + a - 1, 8a^3 + 4a^2u - 12a^2 - 4au + 2a + 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} a \\ -a + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} au - u \\ -au + 2u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} au \\ -au + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a + 1 \\ -a \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -a^2 - a + 1 \\ a^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a^2u - 2au + u \\ -a^2u + 3au - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a^2u + 2a^2 - au - \frac{5}{2}a + \frac{5}{4} \\ -a^2u - 4a^2 + au + \frac{7}{2}a - \frac{1}{4} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -4a^2u - a^2 + \frac{9}{2}au + a - \frac{3}{4}u \\ 2a^2u + a^2 - \frac{3}{2}au - a + \frac{3}{4}u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $16a^2 + 8au - 16a - 4u + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$(u^3 - u^2 + 2u - 1)^2$
$c_2, c_8$	$u^6 + u^4 + 2u^2 + 1$
$c_3, c_9$	$64(64u^6 + 192u^5 + 192u^4 + 64u^3 - 4u^2 - 4u + 1)$
$c_4, c_5, c_6$ $c_{10}, c_{11}, c_{12}$	$(u^2 + 1)^3$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_8$	$(y^3 + y^2 + 2y + 1)^2$
$c_3, c_9$	$4096(4096y^6 - 12288y^5 + 11776y^4 - 3968y^3 + 912y^2 - 24y + 1)$
$c_4, c_5, c_6$ $c_{10}, c_{11}, c_{12}$	$(y + 1)^6$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$ $a = 1.153570 - 0.107540I$ $b = -0.153571 + 0.107540I$	$3.02413 - 2.82812I$	$7.50976 + 2.97945I$
$u = 1.000000I$ $a = 0.500000 - 0.284920I$ $b = 0.500000 + 0.284920I$	$-1.11345$	$-60.980489 + 0.10I$
$u = 1.000000I$ $a = -0.153571 - 0.107540I$ $b = 1.153570 + 0.107540I$	$3.02413 + 2.82812I$	$7.50976 - 2.97945I$
$u = -1.000000I$ $a = 1.153570 + 0.107540I$ $b = -0.153571 - 0.107540I$	$3.02413 + 2.82812I$	$7.50976 - 2.97945I$
$u = -1.000000I$ $a = 0.500000 + 0.284920I$ $b = 0.500000 - 0.284920I$	$-1.11345$	$-60.980489 + 0.10I$
$u = -1.000000I$ $a = -0.153571 + 0.107540I$ $b = 1.153570 - 0.107540I$	$3.02413 - 2.82812I$	$7.50976 + 2.97945I$

$$\mathbf{V. } I_1^v = \langle a, b + 1, v + 1 \rangle$$

**(i) Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes = 12**

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_4$ $c_7, c_8, c_{10}$	$u$
$c_3, c_6, c_9$ $c_{12}$	$u + 1$
$c_5, c_{11}$	$u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_7, c_8, c_{10}$	$y$
$c_3, c_5, c_6$ $c_9, c_{11}, c_{12}$	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$	3.28987	12.0000
$b = -1.00000$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_7$	$u(u^2 - 2u + 2)^2(u^3 - u^2 + 2u - 1)^2(u^{27} + 7u^{26} + \dots - 2u - 1)^2$ $\cdot (u^{41} + 13u^{40} + \dots - 1260u - 100)$
$c_2, c_8$	$u(u^4 + 2u^2 + 2)(u^6 + u^4 + 2u^2 + 1)(u^{27} - u^{26} + \dots - u^2 - 1)^2$ $\cdot (u^{41} + 3u^{40} + \dots - 10u + 10)$
$c_3, c_9$	$102400(u + 1)(25u^4 + 40u^3 + 12u^2 - 4u + 1)$ $\cdot (64u^6 + 192u^5 + 192u^4 + 64u^3 - 4u^2 - 4u + 1)$ $\cdot (64u^{41} + 256u^{40} + \dots - 13u^2 - 1)$ $\cdot (u^{54} - 7u^{53} + \dots - 168722854u - 19874761)$
$c_4, c_{10}$	$u(u^2 + 1)^3(u^4 - 2u^2 + 2)(u^{27} + u^{26} + \dots + 2u - 1)^2$ $\cdot (u^{41} - 3u^{40} + \dots - 434u + 50)$
$c_5, c_{11}$	$(u - 1)(u + 1)^4(u^2 + 1)^3(u^{41} - u^{40} + \dots + 14u - 1)$ $\cdot (u^{54} - u^{53} + \dots - 532u - 53)$
$c_6, c_{12}$	$((u - 1)^4)(u + 1)(u^2 + 1)^3(u^{41} - u^{40} + \dots + 14u - 1)$ $\cdot (u^{54} - u^{53} + \dots - 532u - 53)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_7$	$y(y^2 + 4)^2(y^3 + 3y^2 + 2y - 1)^2(y^{27} + 27y^{26} + \dots + 14y - 1)^2$ $\cdot (y^{41} + 33y^{40} + \dots - 489200y - 10000)$
$c_2, c_8$	$y(y^2 + 2y + 2)^2(y^3 + y^2 + 2y + 1)^2(y^{27} + 7y^{26} + \dots - 2y - 1)^2$ $\cdot (y^{41} + 13y^{40} + \dots - 1260y - 100)$
$c_3, c_9$	$10485760000(y - 1)(625y^4 - 1000y^3 + 514y^2 + 8y + 1)$ $\cdot (4096y^6 - 12288y^5 + 11776y^4 - 3968y^3 + 912y^2 - 24y + 1)$ $\cdot (4096y^{41} - 147456y^{40} + \dots - 26y - 1)$ $\cdot (y^{54} - 37y^{53} + \dots - 8208746653844232y + 395006124807121)$
$c_4, c_{10}$	$y(y + 1)^6(y^2 - 2y + 2)^2(y^{27} + 23y^{26} + \dots - 2y - 1)^2$ $\cdot (y^{41} + 25y^{40} + \dots - 199044y - 2500)$
$c_5, c_6, c_{11}$ $c_{12}$	$((y - 1)^5)(y + 1)^6(y^{41} - 31y^{40} + \dots - 96y - 1)$ $\cdot (y^{54} - 41y^{53} + \dots - 143528y + 2809)$