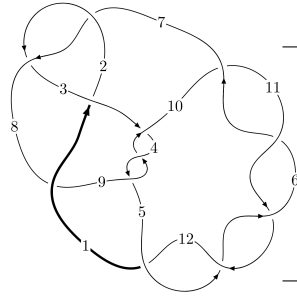
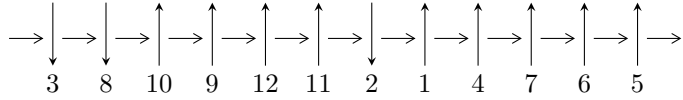


12a<sub>0753</sub> (K12a<sub>0753</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,9 \xrightarrow{c_4} 4 \xrightarrow{c_9} 10 \xrightarrow{c_3} 1,3 \xrightarrow{c_8} 8 \xrightarrow{c_2} 2 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 12 \xrightarrow{c_5} 6 \xrightarrow{c_{11}} 11 \rightsquigarrow c_1, c_6, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 3.47678 \times 10^{21} u^{49} - 1.33799 \times 10^{21} u^{48} + \dots + 1.34820 \times 10^{22} b - 3.88891 \times 10^{22}, \\ 2.21158 \times 10^{21} u^{49} - 1.62283 \times 10^{21} u^{48} + \dots + 1.34820 \times 10^{22} a - 4.79098 \times 10^{22}, u^{50} - u^{49} + \dots - 4u + 4 \rangle \\ I_2^u = \langle b^2 - bu + 1, a^2 + a + 1, u^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 58 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 3.48 \times 10^{21} u^{49} - 1.34 \times 10^{21} u^{48} + \dots + 1.35 \times 10^{22} b - 3.89 \times 10^{22}, 2.21 \times 10^{21} u^{49} - 1.62 \times 10^{21} u^{48} + \dots + 1.35 \times 10^{22} a - 4.79 \times 10^{22}, u^{50} - u^{49} + \dots - 4u + 4 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.164040u^{49} + 0.120370u^{48} + \dots + 8.84293u + 3.55361 \\ -0.257882u^{49} + 0.0992428u^{48} + \dots + 2.87776u + 2.88452 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.570562u^{49} - 0.676764u^{48} + \dots - 8.50993u - 2.63929 \\ 0.00372260u^{49} + 0.222580u^{48} + \dots - 6.74010u - 1.68097 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.137529u^{49} - 0.0400013u^{48} + \dots + 4.53679u + 1.15498 \\ -0.233430u^{49} + 0.0703666u^{48} + \dots + 1.46685u + 2.29315 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.836099u^{49} - 0.448168u^{48} + \dots - 24.1572u - 6.13765 \\ -0.144284u^{49} + 0.0267194u^{48} + \dots - 0.748206u - 1.92710 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0938429u^{49} + 0.0211270u^{48} + \dots + 5.96518u + 0.669092 \\ -0.257882u^{49} + 0.0992428u^{48} + \dots + 2.87776u + 2.88452 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.122630u^{49} - 0.215276u^{48} + \dots - 0.518300u - 8.94249 \\ 0.297613u^{49} - 0.201245u^{48} + \dots - 3.06461u + 0.521412 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0377076u^{49} - 0.204943u^{48} + \dots - 5.37290u - 2.05267 \\ -0.215869u^{49} + 0.420688u^{48} + \dots + 7.63220u + 1.46112 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{6041655765283033164853}{3370503149641393660032} u^{49} - \frac{2696370501616779290413}{1685251574820696830016} u^{48} + \dots - \frac{15380340131345433270079}{421312893705174207504} u - \frac{15926907601216017826235}{842625787410348415008}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{50} + 27u^{49} + \dots + 131u + 25$
$c_2, c_7$	$u^{50} + u^{49} + \dots + u + 5$
$c_3, c_4, c_9$	$u^{50} + u^{49} + \dots + 4u + 4$
$c_5, c_6, c_{10}$ $c_{11}, c_{12}$	$u^{50} - u^{49} + \dots + 9u + 1$
$c_8$	$u^{50} + 3u^{49} + \dots + 519u + 345$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{50} - 3y^{49} + \dots + 89y + 625$
$c_2, c_7$	$y^{50} - 27y^{49} + \dots - 131y + 25$
$c_3, c_4, c_9$	$y^{50} + 53y^{49} + \dots - 8y + 16$
$c_5, c_6, c_{10}$ $c_{11}, c_{12}$	$y^{50} + 69y^{49} + \dots - 39y + 1$
$c_8$	$y^{50} + 33y^{49} + \dots - 1916391y + 119025$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.825284 + 0.564850I$ $a = 1.018290 - 0.857226I$ $b = 0.03252 - 1.72373I$	$-12.07120 - 2.72832I$	$1.32353 + 2.43193I$
$u = -0.825284 - 0.564850I$ $a = 1.018290 + 0.857226I$ $b = 0.03252 + 1.72373I$	$-12.07120 + 2.72832I$	$1.32353 - 2.43193I$
$u = -0.084210 + 1.043320I$ $a = -0.384445 - 0.811272I$ $b = -0.178045 + 0.054788I$	$-1.54403 - 2.06175I$	$7.89718 + 4.27454I$
$u = -0.084210 - 1.043320I$ $a = -0.384445 + 0.811272I$ $b = -0.178045 - 0.054788I$	$-1.54403 + 2.06175I$	$7.89718 - 4.27454I$
$u = -0.650825 + 0.686901I$ $a = -0.574983 + 0.899543I$ $b = -0.001959 + 1.082170I$	$-5.77062 + 1.33212I$	$-3.10818 - 0.66099I$
$u = -0.650825 - 0.686901I$ $a = -0.574983 - 0.899543I$ $b = -0.001959 - 1.082170I$	$-5.77062 - 1.33212I$	$-3.10818 + 0.66099I$
$u = -0.798083 + 0.491554I$ $a = -1.12468 + 0.88964I$ $b = -0.227660 + 1.067050I$	$-5.13290 - 6.35349I$	$-1.14202 + 7.17760I$
$u = -0.798083 - 0.491554I$ $a = -1.12468 - 0.88964I$ $b = -0.227660 - 1.067050I$	$-5.13290 + 6.35349I$	$-1.14202 - 7.17760I$
$u = 0.267440 + 1.044800I$ $a = -0.170870 + 0.254106I$ $b = -0.227134 + 0.746761I$	$-3.70325 + 0.50512I$	$-4.05141 + 0.I$
$u = 0.267440 - 1.044800I$ $a = -0.170870 - 0.254106I$ $b = -0.227134 - 0.746761I$	$-3.70325 - 0.50512I$	$-4.05141 + 0.I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.981288 + 0.514013I$ $a = -0.96413 - 1.07465I$ $b = -0.05777 - 1.74519I$	$-15.2476 + 7.5356I$	0
$u = 0.981288 - 0.514013I$ $a = -0.96413 + 1.07465I$ $b = -0.05777 + 1.74519I$	$-15.2476 - 7.5356I$	0
$u = 0.872961 + 0.773969I$ $a = -0.729263 - 0.828003I$ $b = 0.00151 - 1.74975I$	$-16.0293 - 1.3459I$	0
$u = 0.872961 - 0.773969I$ $a = -0.729263 + 0.828003I$ $b = 0.00151 + 1.74975I$	$-16.0293 + 1.3459I$	0
$u = -0.233208 + 1.157960I$ $a = 0.103022 - 0.205335I$ $b = -0.06216 - 1.60924I$	$-11.81320 + 0.61087I$	0
$u = -0.233208 - 1.157960I$ $a = 0.103022 + 0.205335I$ $b = -0.06216 + 1.60924I$	$-11.81320 - 0.61087I$	0
$u = 0.626871 + 0.455302I$ $a = 1.027610 + 0.620239I$ $b = 0.151543 + 0.964779I$	$-2.39825 + 2.03419I$	$2.27060 - 4.05066I$
$u = 0.626871 - 0.455302I$ $a = 1.027610 - 0.620239I$ $b = 0.151543 - 0.964779I$	$-2.39825 - 2.03419I$	$2.27060 + 4.05066I$
$u = 0.500054 + 0.432744I$ $a = -1.58264 - 0.45958I$ $b = -0.429197 - 0.273799I$	$-0.92587 + 4.11077I$	$5.01065 - 8.99779I$
$u = 0.500054 - 0.432744I$ $a = -1.58264 + 0.45958I$ $b = -0.429197 + 0.273799I$	$-0.92587 - 4.11077I$	$5.01065 + 8.99779I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.037819 + 1.343840I$ $a = -0.297542 + 1.152810I$ $b = -0.056382 - 1.024380I$	$-5.06538 + 2.73318I$	0
$u = 0.037819 - 1.343840I$ $a = -0.297542 - 1.152810I$ $b = -0.056382 + 1.024380I$	$-5.06538 - 2.73318I$	0
$u = -0.07762 + 1.41592I$ $a = -0.839838 - 0.126193I$ $b = -0.589212 + 0.356243I$	$-4.18150 - 1.91267I$	0
$u = -0.07762 - 1.41592I$ $a = -0.839838 + 0.126193I$ $b = -0.589212 - 0.356243I$	$-4.18150 + 1.91267I$	0
$u = -0.04588 + 1.49852I$ $a = -0.286588 - 1.290620I$ $b = -0.01350 + 1.73889I$	$-15.0633 - 3.0141I$	0
$u = -0.04588 - 1.49852I$ $a = -0.286588 + 1.290620I$ $b = -0.01350 - 1.73889I$	$-15.0633 + 3.0141I$	0
$u = -0.04118 + 1.50695I$ $a = 0.857242 + 0.055781I$ $b = 0.641940 + 0.482037I$	$-7.87180 - 2.16186I$	0
$u = -0.04118 - 1.50695I$ $a = 0.857242 - 0.055781I$ $b = 0.641940 - 0.482037I$	$-7.87180 + 2.16186I$	0
$u = 0.20411 + 1.49822I$ $a = -0.995020 + 0.295616I$ $b = -0.332774 - 1.115340I$	$-8.78560 + 5.06490I$	0
$u = 0.20411 - 1.49822I$ $a = -0.995020 - 0.295616I$ $b = -0.332774 + 1.115340I$	$-8.78560 - 5.06490I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.15926 + 1.50725I$ $a = 0.985140 - 0.130046I$ $b = 0.692157 + 0.316900I$	$-7.37205 + 6.50901I$	0
$u = 0.15926 - 1.50725I$ $a = 0.985140 + 0.130046I$ $b = 0.692157 - 0.316900I$	$-7.37205 - 6.50901I$	0
$u = -0.453530 + 0.155768I$ $a = 1.294160 - 0.225533I$ $b = 0.381984 - 0.104645I$	$0.863945 - 0.260084I$	$11.81001 + 2.51028I$
$u = -0.453530 - 0.155768I$ $a = 1.294160 + 0.225533I$ $b = 0.381984 + 0.104645I$	$0.863945 + 0.260084I$	$11.81001 - 2.51028I$
$u = 0.002331 + 0.475435I$ $a = -1.31229 - 1.31457I$ $b = -0.222613 - 0.360188I$	$-1.29560 - 1.71128I$	$3.62337 - 0.57980I$
$u = 0.002331 - 0.475435I$ $a = -1.31229 + 1.31457I$ $b = -0.222613 + 0.360188I$	$-1.29560 + 1.71128I$	$3.62337 + 0.57980I$
$u = -0.10985 + 1.56287I$ $a = 0.745097 + 0.121175I$ $b = 0.305737 - 1.232150I$	$-13.35830 - 1.13064I$	0
$u = -0.10985 - 1.56287I$ $a = 0.745097 - 0.121175I$ $b = 0.305737 + 1.232150I$	$-13.35830 + 1.13064I$	0
$u = -0.26983 + 1.54338I$ $a = 1.117940 + 0.149645I$ $b = 0.408507 - 1.113900I$	$-11.8242 - 10.2576I$	0
$u = -0.26983 - 1.54338I$ $a = 1.117940 - 0.149645I$ $b = 0.408507 + 1.113900I$	$-11.8242 + 10.2576I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.28876 + 1.56911I$ $a = -1.116410 - 0.382260I$ $b = -0.08858 + 1.75569I$	$-19.0611 - 6.8576I$	0
$u = -0.28876 - 1.56911I$ $a = -1.116410 + 0.382260I$ $b = -0.08858 - 1.75569I$	$-19.0611 + 6.8576I$	0
$u = 0.36007 + 1.57989I$ $a = 1.221070 - 0.154749I$ $b = 0.11163 + 1.75687I$	$17.4391 + 12.4733I$	0
$u = 0.36007 - 1.57989I$ $a = 1.221070 + 0.154749I$ $b = 0.11163 - 1.75687I$	$17.4391 - 12.4733I$	0
$u = 0.329455 + 0.007485I$ $a = 2.30065 - 0.55846I$ $b = 0.177809 - 0.666151I$	$-0.77656 - 1.82163I$	$4.80979 + 5.42360I$
$u = 0.329455 - 0.007485I$ $a = 2.30065 + 0.55846I$ $b = 0.177809 + 0.666151I$	$-0.77656 + 1.82163I$	$4.80979 - 5.42360I$
$u = 0.22272 + 1.66105I$ $a = 0.730785 - 0.308803I$ $b = 0.06984 + 1.78630I$	$15.1658 + 2.7485I$	0
$u = 0.22272 - 1.66105I$ $a = 0.730785 + 0.308803I$ $b = 0.06984 - 1.78630I$	$15.1658 - 2.7485I$	0
$u = -0.186126 + 0.264782I$ $a = 2.72769 + 2.04868I$ $b = 0.01181 - 1.64054I$	$-8.93133 - 2.25545I$	$4.66563 + 3.82510I$
$u = -0.186126 - 0.264782I$ $a = 2.72769 - 2.04868I$ $b = 0.01181 + 1.64054I$	$-8.93133 + 2.25545I$	$4.66563 - 3.82510I$

$$\text{II. } I_2^u = \langle b^2 - bu + 1, a^2 + a + 1, u^2 + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} au + u \\ -bau + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ b + a \end{pmatrix}$$

$$a_7 = \begin{pmatrix} au \\ bu \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -b + a \\ b \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -ba + bu \\ -bu + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} bau + u \\ -b - u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4a - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 - u + 1)^4$
$c_2, c_7, c_8$	$(u^4 - u^2 + 1)^2$
$c_3, c_4, c_9$	$(u^2 + 1)^4$
$c_5, c_6, c_{10}$ $c_{11}, c_{12}$	$(u^4 + 3u^2 + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 + y + 1)^4$
$c_2, c_7, c_8$	$(y^2 - y + 1)^4$
$c_3, c_4, c_9$	$(y + 1)^8$
$c_5, c_6, c_{10}$ $c_{11}, c_{12}$	$(y^2 + 3y + 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.000000I$		
$a = -0.500000 + 0.866025I$	$-2.63189 + 2.02988I$	$-2.00000 - 3.46410I$
$b = -0.618034I$		
$u = 1.000000I$		
$a = -0.500000 + 0.866025I$	$-10.52760 + 2.02988I$	$-2.00000 - 3.46410I$
$b = 1.61803I$		
$u = 1.000000I$		
$a = -0.500000 - 0.866025I$	$-2.63189 - 2.02988I$	$-2.00000 + 3.46410I$
$b = -0.618034I$		
$u = 1.000000I$		
$a = -0.500000 - 0.866025I$	$-10.52760 - 2.02988I$	$-2.00000 + 3.46410I$
$b = 1.61803I$		
$u = -1.000000I$		
$a = -0.500000 + 0.866025I$	$-2.63189 + 2.02988I$	$-2.00000 - 3.46410I$
$b = 0.618034I$		
$u = -1.000000I$		
$a = -0.500000 + 0.866025I$	$-10.52760 + 2.02988I$	$-2.00000 - 3.46410I$
$b = -1.61803I$		
$u = -1.000000I$		
$a = -0.500000 - 0.866025I$	$-2.63189 - 2.02988I$	$-2.00000 + 3.46410I$
$b = 0.618034I$		
$u = -1.000000I$		
$a = -0.500000 - 0.866025I$	$-10.52760 - 2.02988I$	$-2.00000 + 3.46410I$
$b = -1.61803I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^4)(u^{50} + 27u^{49} + \dots + 131u + 25)$
$c_2, c_7$	$((u^4 - u^2 + 1)^2)(u^{50} + u^{49} + \dots + u + 5)$
$c_3, c_4, c_9$	$((u^2 + 1)^4)(u^{50} + u^{49} + \dots + 4u + 4)$
$c_5, c_6, c_{10}$ $c_{11}, c_{12}$	$((u^4 + 3u^2 + 1)^2)(u^{50} - u^{49} + \dots + 9u + 1)$
$c_8$	$((u^4 - u^2 + 1)^2)(u^{50} + 3u^{49} + \dots + 519u + 345)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^4)(y^{50} - 3y^{49} + \dots + 89y + 625)$
$c_2, c_7$	$((y^2 - y + 1)^4)(y^{50} - 27y^{49} + \dots - 131y + 25)$
$c_3, c_4, c_9$	$((y + 1)^8)(y^{50} + 53y^{49} + \dots - 8y + 16)$
$c_5, c_6, c_{10}$ $c_{11}, c_{12}$	$((y^2 + 3y + 1)^4)(y^{50} + 69y^{49} + \dots - 39y + 1)$
$c_8$	$((y^2 - y + 1)^4)(y^{50} + 33y^{49} + \dots - 1916391y + 119025)$