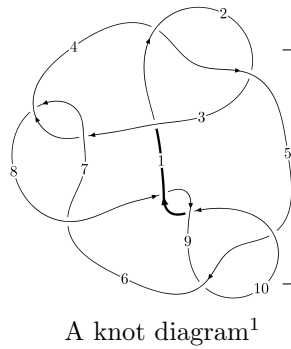
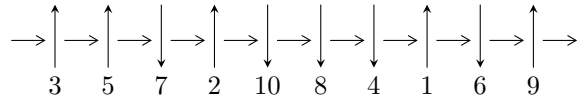


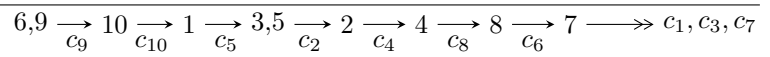
10<sub>71</sub> (K10a<sub>10</sub>)



**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{27} + 5u^{25} + \dots + b + u, -u^{39} - u^{38} + \dots + a - 4u, u^{40} + 2u^{39} + \dots + 4u^2 + 1 \rangle$$

$$I_2^u = \langle b + u + 1, a, u^2 + u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 42 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{27} + 5u^{25} + \dots + b + u, -u^{39} - u^{38} + \dots + a - 4u, u^{40} + 2u^{39} + \dots + 4u^2 + 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{39} + u^{38} + \dots - 5u^2 + 4u \\ -u^{27} - 5u^{25} + \dots + 4u^2 - u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{21} + 4u^{19} + \dots - 4u^2 + 3u \\ -u^{39} - 2u^{38} + \dots - u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{39} - u^{38} + \dots + 3u - 1 \\ -2u^{39} - 4u^{38} + \dots - 4u^2 - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^4 + u^2 + 1 \\ u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^9 - 2u^7 - 3u^5 - 2u^3 - u \\ -u^9 - u^7 - u^5 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= u^{39} + 9u^{38} + 17u^{37} + 66u^{36} + 94u^{35} + 285u^{34} + 329u^{33} + 852u^{32} + 826u^{31} + 1962u^{30} + 1576u^{29} + 3630u^{28} + 2362u^{27} + 5577u^{26} + 2755u^{25} + 7286u^{24} + 2421u^{23} + 8227u^{22} + 1323u^{21} + 8198u^{20} - 136u^{19} + 7289u^{18} - 1361u^{17} + 5878u^{16} - 1976u^{15} + 4322u^{14} - 1882u^{13} + 2864u^{12} - 1394u^{11} + 1700u^{10} - 826u^9 + 838u^8 - 385u^7 + 329u^6 - 157u^5 + 92u^4 - 42u^3 + 7u^2 - 5u + 6$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{40} - 21u^{39} + \dots - 3u + 1$
$c_2, c_4$	$u^{40} + 3u^{39} + \dots + 3u + 1$
$c_3, c_7$	$u^{40} + u^{39} + \dots - 8u + 4$
$c_5, c_9$	$u^{40} - 2u^{39} + \dots + 4u^2 + 1$
$c_6$	$u^{40} + 15u^{39} + \dots + 120u + 16$
$c_8, c_{10}$	$u^{40} - 14u^{39} + \dots - 8u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{40} - y^{39} + \dots + 17y + 1$
$c_2, c_4$	$y^{40} - 21y^{39} + \dots - 3y + 1$
$c_3, c_7$	$y^{40} - 15y^{39} + \dots - 120y + 16$
$c_5, c_9$	$y^{40} + 14y^{39} + \dots + 8y + 1$
$c_6$	$y^{40} + 17y^{39} + \dots + 2016y + 256$
$c_8, c_{10}$	$y^{40} + 26y^{39} + \dots + 44y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.725993 + 0.653238I$ $a = -1.77855 + 1.81598I$ $b = -2.56295 - 0.04821I$	$0.63968 + 1.74616I$	$0.044303 - 1.257582I$
$u = 0.725993 - 0.653238I$ $a = -1.77855 - 1.81598I$ $b = -2.56295 + 0.04821I$	$0.63968 - 1.74616I$	$0.044303 + 1.257582I$
$u = 0.657117 + 0.787048I$ $a = 1.66831 + 0.40061I$ $b = 0.89334 + 1.41707I$	$-1.07354 - 2.17702I$	$-2.16670 + 4.43587I$
$u = 0.657117 - 0.787048I$ $a = 1.66831 - 0.40061I$ $b = 0.89334 - 1.41707I$	$-1.07354 + 2.17702I$	$-2.16670 - 4.43587I$
$u = 0.096376 + 1.028080I$ $a = 0.442341 + 0.052565I$ $b = -0.722317 + 0.146557I$	$2.32493 - 2.41163I$	$2.33571 + 3.34704I$
$u = 0.096376 - 1.028080I$ $a = 0.442341 - 0.052565I$ $b = -0.722317 - 0.146557I$	$2.32493 + 2.41163I$	$2.33571 - 3.34704I$
$u = -0.824710 + 0.626683I$ $a = -1.67414 - 1.41541I$ $b = -2.39518 + 0.13829I$	$-1.20323 - 7.65538I$	$-1.63964 + 4.86252I$
$u = -0.824710 - 0.626683I$ $a = -1.67414 + 1.41541I$ $b = -2.39518 - 0.13829I$	$-1.20323 + 7.65538I$	$-1.63964 - 4.86252I$
$u = -0.789408 + 0.675423I$ $a = 1.235380 + 0.007261I$ $b = 1.156310 - 0.509552I$	$-3.72005 - 2.44717I$	$-4.96365 + 1.04542I$
$u = -0.789408 - 0.675423I$ $a = 1.235380 - 0.007261I$ $b = 1.156310 + 0.509552I$	$-3.72005 + 2.44717I$	$-4.96365 - 1.04542I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.386153 + 0.965172I$ $a = -0.238506 + 0.455641I$ $b = -0.397991 + 0.639039I$	$0.74845 - 2.81821I$	$-1.95524 + 6.55211I$
$u = 0.386153 - 0.965172I$ $a = -0.238506 - 0.455641I$ $b = -0.397991 - 0.639039I$	$0.74845 + 2.81821I$	$-1.95524 - 6.55211I$
$u = -0.023616 + 1.041760I$ $a = -1.087150 - 0.838239I$ $b = 0.393277 - 1.005930I$	$6.00686 + 1.32070I$	$7.28134 - 0.72610I$
$u = -0.023616 - 1.041760I$ $a = -1.087150 + 0.838239I$ $b = 0.393277 + 1.005930I$	$6.00686 - 1.32070I$	$7.28134 + 0.72610I$
$u = -0.650732 + 0.672523I$ $a = 0.172779 + 0.250083I$ $b = -0.359504 - 0.987978I$	$1.25887 + 0.68759I$	$-0.543601 + 0.759704I$
$u = -0.650732 - 0.672523I$ $a = 0.172779 - 0.250083I$ $b = -0.359504 + 0.987978I$	$1.25887 - 0.68759I$	$-0.543601 - 0.759704I$
$u = 0.095598 + 1.116440I$ $a = -0.834103 + 0.849030I$ $b = 0.370183 + 0.684126I$	$5.21580 - 6.90989I$	$5.24227 + 6.39245I$
$u = 0.095598 - 1.116440I$ $a = -0.834103 - 0.849030I$ $b = 0.370183 - 0.684126I$	$5.21580 + 6.90989I$	$5.24227 - 6.39245I$
$u = 0.639866 + 0.934630I$ $a = -0.19632 + 1.43499I$ $b = -1.28155 + 0.60102I$	$-0.60920 - 2.86826I$	$-1.22261 + 1.95241I$
$u = 0.639866 - 0.934630I$ $a = -0.19632 - 1.43499I$ $b = -1.28155 - 0.60102I$	$-0.60920 + 2.86826I$	$-1.22261 - 1.95241I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.777168 + 0.837928I$		
$a = -0.91272 - 1.60741I$	$-6.21108 + 0.22925I$	$-5.84725 + 0.24543I$
$b = -2.00597 - 0.19942I$		
$u = -0.777168 - 0.837928I$		
$a = -0.91272 + 1.60741I$	$-6.21108 - 0.22925I$	$-5.84725 - 0.24543I$
$b = -2.00597 + 0.19942I$		
$u = -0.762796 + 0.899428I$		
$a = 1.74060 + 0.53261I$	$-6.02457 + 5.56367I$	$-5.18066 - 6.01609I$
$b = 2.07413 - 1.05941I$		
$u = -0.762796 - 0.899428I$		
$a = 1.74060 - 0.53261I$	$-6.02457 - 5.56367I$	$-5.18066 + 6.01609I$
$b = 2.07413 + 1.05941I$		
$u = -0.651476 + 0.987984I$		
$a = 0.197553 + 0.008658I$	$2.21178 + 4.43619I$	$1.72906 - 5.48285I$
$b = -0.673463 - 1.012420I$		
$u = -0.651476 - 0.987984I$		
$a = 0.197553 - 0.008658I$	$2.21178 - 4.43619I$	$1.72906 + 5.48285I$
$b = -0.673463 + 1.012420I$		
$u = 0.559538 + 1.043730I$		
$a = 0.204110 + 0.051194I$	$2.37466 + 0.03317I$	$2.30074 - 1.92960I$
$b = -0.743272 + 0.884629I$		
$u = 0.559538 - 1.043730I$		
$a = 0.204110 - 0.051194I$	$2.37466 - 0.03317I$	$2.30074 + 1.92960I$
$b = -0.743272 - 0.884629I$		
$u = 0.674430 + 1.003370I$		
$a = 1.99901 - 1.47152I$	$1.68055 - 7.12390I$	$1.84913 + 6.13601I$
$b = 3.05304 + 1.06309I$		
$u = 0.674430 - 1.003370I$		
$a = 1.99901 + 1.47152I$	$1.68055 + 7.12390I$	$1.84913 - 6.13601I$
$b = 3.05304 - 1.06309I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.710235 + 0.337827I$ $a = 0.496293 - 0.392962I$ $b = -0.069099 + 0.837495I$	$0.39800 - 4.72692I$	$-1.63267 + 6.05913I$
$u = 0.710235 - 0.337827I$ $a = 0.496293 + 0.392962I$ $b = -0.069099 - 0.837495I$	$0.39800 + 4.72692I$	$-1.63267 - 6.05913I$
$u = -0.705098 + 1.010600I$ $a = -0.462757 - 1.241560I$ $b = -1.290960 - 0.160212I$	$-2.70648 + 8.09252I$	$-2.94350 - 6.08172I$
$u = -0.705098 - 1.010600I$ $a = -0.462757 + 1.241560I$ $b = -1.290960 + 0.160212I$	$-2.70648 - 8.09252I$	$-2.94350 + 6.08172I$
$u = -0.703890 + 1.042830I$ $a = 1.61753 + 1.43395I$ $b = 2.91214 - 0.75501I$	$0.05370 + 13.38520I$	$0.42075 - 9.35928I$
$u = -0.703890 - 1.042830I$ $a = 1.61753 - 1.43395I$ $b = 2.91214 + 0.75501I$	$0.05370 - 13.38520I$	$0.42075 + 9.35928I$
$u = 0.566007 + 0.177460I$ $a = 0.944370 + 0.216688I$ $b = 0.239645 - 0.184623I$	$-1.47568 - 0.52119I$	$-6.28438 + 0.91978I$
$u = 0.566007 - 0.177460I$ $a = 0.944370 - 0.216688I$ $b = 0.239645 + 0.184623I$	$-1.47568 + 0.52119I$	$-6.28438 - 0.91978I$
$u = -0.222419 + 0.359701I$ $a = -0.03404 + 1.68269I$ $b = -0.589808 - 0.653481I$	$1.75548 + 0.68997I$	$4.17661 + 0.16492I$
$u = -0.222419 - 0.359701I$ $a = -0.03404 - 1.68269I$ $b = -0.589808 + 0.653481I$	$1.75548 - 0.68997I$	$4.17661 - 0.16492I$



$$\text{II. } I_2^u = \langle b + u + 1, a, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u \\ -2u - 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-4u + 1$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u + 1)^2$
$c_3, c_6, c_7$	$u^2$
$c_4$	$(u - 1)^2$
$c_5, c_{10}$	$u^2 - u + 1$
$c_8, c_9$	$u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^2$
$c_3, c_6, c_7$	$y^2$
$c_5, c_8, c_9$ $c_{10}$	$y^2 + y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$		
$a = 0$	$1.64493 + 2.02988I$	$3.00000 - 3.46410I$
$b = -0.500000 - 0.866025I$		
$u = -0.500000 - 0.866025I$		
$a = 0$	$1.64493 - 2.02988I$	$3.00000 + 3.46410I$
$b = -0.500000 + 0.866025I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u + 1)^2)(u^{40} - 21u^{39} + \dots - 3u + 1)$
$c_2$	$((u + 1)^2)(u^{40} + 3u^{39} + \dots + 3u + 1)$
$c_3, c_7$	$u^2(u^{40} + u^{39} + \dots - 8u + 4)$
$c_4$	$((u - 1)^2)(u^{40} + 3u^{39} + \dots + 3u + 1)$
$c_5$	$(u^2 - u + 1)(u^{40} - 2u^{39} + \dots + 4u^2 + 1)$
$c_6$	$u^2(u^{40} + 15u^{39} + \dots + 120u + 16)$
$c_8$	$(u^2 + u + 1)(u^{40} - 14u^{39} + \dots - 8u + 1)$
$c_9$	$(u^2 + u + 1)(u^{40} - 2u^{39} + \dots + 4u^2 + 1)$
$c_{10}$	$(u^2 - u + 1)(u^{40} - 14u^{39} + \dots - 8u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^2)(y^{40} - y^{39} + \dots + 17y + 1)$
$c_2, c_4$	$((y - 1)^2)(y^{40} - 21y^{39} + \dots - 3y + 1)$
$c_3, c_7$	$y^2(y^{40} - 15y^{39} + \dots - 120y + 16)$
$c_5, c_9$	$(y^2 + y + 1)(y^{40} + 14y^{39} + \dots + 8y + 1)$
$c_6$	$y^2(y^{40} + 17y^{39} + \dots + 2016y + 256)$
$c_8, c_{10}$	$(y^2 + y + 1)(y^{40} + 26y^{39} + \dots + 44y + 1)$