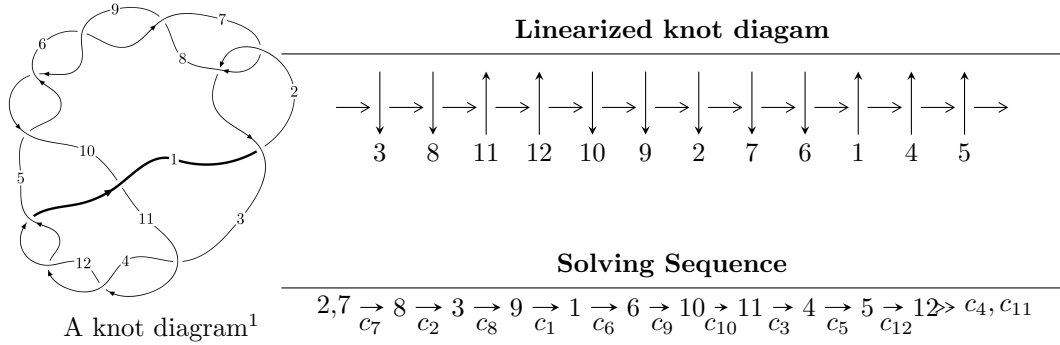


12a<sub>0791</sub> (K12a<sub>0791</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{31} - u^{30} + \dots - 2u^2 + 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 31 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle u^{31} - u^{30} + \dots - 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^4 - u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^6 + u^4 - 2u^2 + 1 \\ u^6 + u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^{14} - u^{12} + 4u^{10} - 3u^8 + 2u^6 - 2u^2 + 1 \\ u^{16} - 2u^{14} + 6u^{12} - 8u^{10} + 10u^8 - 6u^6 + 4u^4 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{27} - 2u^{25} + \dots + 12u^5 - 5u^3 \\ u^{29} - 3u^{27} + \dots - u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^8 - u^6 + 3u^4 - 2u^2 + 1 \\ -u^8 - 2u^4 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{21} + 2u^{19} + \dots + 6u^3 - u \\ u^{21} - u^{19} + 7u^{17} - 6u^{15} + 16u^{13} - 11u^{11} + 13u^9 - 6u^7 + 3u^5 - u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= 4u^{30} - 12u^{28} + 4u^{27} + 60u^{26} - 8u^{25} - 136u^{24} + 44u^{23} + 344u^{22} - 72u^{21} - 592u^{20} + 184u^{19} + 960u^{18} - 240u^{17} - 1232u^{16} + 372u^{15} + 1356u^{14} - 376u^{13} - 1232u^{12} + 388u^{11} + 896u^{10} - 300u^9 - 504u^8 + 204u^7 + 204u^6 - 112u^5 - 40u^4 + 40u^3 - 12u - 2$$

(iv) u-Polynomials at the component

| Crossings                      | u-Polynomials at each crossing           |
|--------------------------------|--|
| $c_1, c_5, c_6$<br>$c_8, c_9$  | $u^{31} + 5u^{30} + \dots + 4u + 1$      |
| $c_2, c_7$                     | $u^{31} + u^{30} + \dots + 2u^2 - 1$     |
| $c_3, c_4, c_{11}$<br>$c_{12}$ | $u^{31} - u^{30} + \dots - 2u - 1$       |
| $c_{10}$                       | $u^{31} + 11u^{30} + \dots + 904u + 329$ |

(v) Riley Polynomials at the component

| Crossings                      | Riley Polynomials at each crossing           |
|--------------------------------|--|
| $c_1, c_5, c_6$<br>$c_8, c_9$  | $y^{31} + 43y^{30} + \dots - 32y - 1$        |
| $c_2, c_7$                     | $y^{31} - 5y^{30} + \dots + 4y - 1$          |
| $c_3, c_4, c_{11}$<br>$c_{12}$ | $y^{31} - 37y^{30} + \dots + 4y - 1$         |
| $c_{10}$                       | $y^{31} - 25y^{30} + \dots - 9232y - 108241$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.791350 + 0.665692I$ | $2.77292 + 2.49031I$                  | $0.70638 - 3.36912I$  |
| $u = -0.791350 - 0.665692I$ | $2.77292 - 2.49031I$                  | $0.70638 + 3.36912I$  |
| $u = 0.734968 + 0.730997I$  | $5.22440 + 0.49349I$                  | $6.40243 - 1.42889I$  |
| $u = 0.734968 - 0.730997I$  | $5.22440 - 0.49349I$                  | $6.40243 + 1.42889I$  |
| $u = 0.862163 + 0.360448I$  | $6.88853 - 4.31158I$                  | $1.70139 + 6.75618I$  |
| $u = 0.862163 - 0.360448I$  | $6.88853 + 4.31158I$                  | $1.70139 - 6.75618I$  |
| $u = -0.720478 + 0.790919I$ | $13.50980 - 2.17197I$                 | $7.93260 + 0.27794I$  |
| $u = -0.720478 - 0.790919I$ | $13.50980 + 2.17197I$                 | $7.93260 - 0.27794I$  |
| $u = 0.861511 + 0.679212I$  | $4.80823 - 5.72178I$                  | $4.77645 + 8.09118I$  |
| $u = 0.861511 - 0.679212I$  | $4.80823 + 5.72178I$                  | $4.77645 - 8.09118I$  |
| $u = -0.906594 + 0.698694I$ | $12.8848 + 7.6593I$                   | $6.39810 - 6.24102I$  |
| $u = -0.906594 - 0.698694I$ | $12.8848 - 7.6593I$                   | $6.39810 + 6.24102I$  |
| $u = -0.853762$             | $5.04240$                             | $-2.72190$            |
| $u = -0.778513 + 0.296852I$ | $-0.36181 + 2.94393I$                 | $-1.66820 - 9.97564I$ |
| $u = -0.778513 - 0.296852I$ | $-0.36181 - 2.94393I$                 | $-1.66820 + 9.97564I$ |
| $u = 0.704905 + 0.147061I$  | $-1.148080 - 0.379484I$               | $-7.32750 + 0.54568I$ |
| $u = 0.704905 - 0.147061I$  | $-1.148080 + 0.379484I$               | $-7.32750 - 0.54568I$ |
| $u = 0.946436 + 0.923716I$  | $12.91130 - 3.39712I$                 | $2.13967 + 2.24704I$  |
| $u = 0.946436 - 0.923716I$  | $12.91130 + 3.39712I$                 | $2.13967 - 2.24704I$  |
| $u = -0.937373 + 0.934900I$ | $15.4949 - 0.4280I$                   | $6.07033 + 1.46342I$  |
| $u = -0.937373 - 0.934900I$ | $15.4949 + 0.4280I$                   | $6.07033 - 1.46342I$  |
| $u = 0.933748 + 0.947021I$  | $-15.3696 + 2.7248I$                  | $7.83122 - 0.36082I$  |
| $u = 0.933748 - 0.947021I$  | $-15.3696 - 2.7248I$                  | $7.83122 + 0.36082I$  |
| $u = -0.960199 + 0.921928I$ | $15.4193 + 7.2526I$                   | $5.88050 - 5.99908I$  |
| $u = -0.960199 - 0.921928I$ | $15.4193 - 7.2526I$                   | $5.88050 + 5.99908I$  |
| $u = 0.971666 + 0.924478I$  | $-15.4964 - 9.5974I$                  | $7.61372 + 4.81531I$  |
| $u = 0.971666 - 0.924478I$  | $-15.4964 + 9.5974I$                  | $7.61372 - 4.81531I$  |
| $u = 0.286578 + 0.593109I$  | $8.74676 + 0.94916I$                  | $8.06495 - 0.10527I$  |
| $u = 0.286578 - 0.593109I$  | $8.74676 - 0.94916I$                  | $8.06495 + 0.10527I$  |
| $u = -0.280590 + 0.401102I$ | $1.103510 - 0.348173I$                | $7.83889 + 1.08782I$  |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = -0.280590 - 0.401102I$ | $1.103510 + 0.348173I$                | $7.83889 - 1.08782I$ |

## II. u-Polynomials

| Crossings                      | u-Polynomials at each crossing           |
|--------------------------------|--|
| $c_1, c_5, c_6$<br>$c_8, c_9$  | $u^{31} + 5u^{30} + \dots + 4u + 1$      |
| $c_2, c_7$                     | $u^{31} + u^{30} + \dots + 2u^2 - 1$     |
| $c_3, c_4, c_{11}$<br>$c_{12}$ | $u^{31} - u^{30} + \dots - 2u - 1$       |
| $c_{10}$                       | $u^{31} + 11u^{30} + \dots + 904u + 329$ |

### III. Riley Polynomials

| Crossings                      | Riley Polynomials at each crossing           |
|--------------------------------|--|
| $c_1, c_5, c_6$<br>$c_8, c_9$  | $y^{31} + 43y^{30} + \dots - 32y - 1$        |
| $c_2, c_7$                     | $y^{31} - 5y^{30} + \dots + 4y - 1$          |
| $c_3, c_4, c_{11}$<br>$c_{12}$ | $y^{31} - 37y^{30} + \dots + 4y - 1$         |
| $c_{10}$                       | $y^{31} - 25y^{30} + \dots - 9232y - 108241$ |