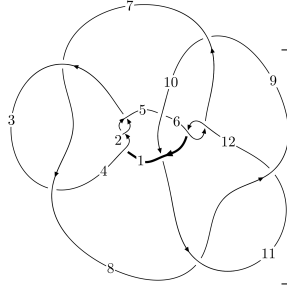
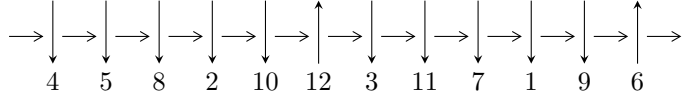


12a₀₈₂₉ (K12a₀₈₂₉)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$3, 8 \xrightarrow{c_3} 4, 11 \xrightarrow{c_8} 9 \xrightarrow{c_{11}} 12 \xrightarrow{c_7} 7 \xrightarrow{c_9} 10 \xrightarrow{c_6} 6 \xrightarrow{c_{12}} 1 \xrightarrow{c_5} 5 \xrightarrow{c_2} 2 \twoheadrightarrow c_1, c_4, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 7.15195 \times 10^{399} u^{106} - 8.59095 \times 10^{399} u^{105} + \dots + 3.48006 \times 10^{400} b - 4.32470 \times 10^{402}, \\ 3.78913 \times 10^{398} u^{106} - 5.25909 \times 10^{398} u^{105} + \dots + 4.09419 \times 10^{399} a - 3.05225 \times 10^{401}, \\ u^{107} - 2u^{106} + \dots - 512u + 512 \rangle$$

$$I_2^u = \langle 22u^2 + 17b + 2u + 40, u^2 + a - u + 2, u^3 - u^2 + 2u - 1 \rangle$$

$$I_1^v = \langle a, 14536v^8 + 40690v^7 + \dots + 11959b + 36034, \\ v^9 + 3v^8 - 2v^7 - 9v^6 + 11v^5 + 25v^4 + 6v^3 - 2v^2 + 3v + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 119 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 7.15 \times 10^{399} u^{106} - 8.59 \times 10^{399} u^{105} + \dots + 3.48 \times 10^{400} b - 4.32 \times 10^{402}, 3.79 \times 10^{398} u^{106} - 5.26 \times 10^{398} u^{105} + \dots + 4.09 \times 10^{399} a - 3.05 \times 10^{401}, u^{107} - 2u^{106} + \dots - 512u + 512 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0925491u^{106} + 0.128453u^{105} + \dots + 27.8911u + 74.5508 \\ -0.205512u^{106} + 0.246862u^{105} + \dots + 10.0191u + 124.271 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.141762u^{106} + 0.160044u^{105} + \dots - 13.9980u + 76.5882 \\ -0.0579410u^{106} + 0.0583727u^{105} + \dots - 24.6379u + 21.0757 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.225565u^{106} + 0.289473u^{105} + \dots + 48.0564u + 157.554 \\ -0.280106u^{106} + 0.347672u^{105} + \dots + 48.3843u + 184.903 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.192530u^{106} + 0.222762u^{105} + \dots - 4.85824u + 110.365 \\ -0.108709u^{106} + 0.121091u^{105} + \dots - 15.4981u + 54.8520 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.151786u^{106} - 0.171743u^{105} + \dots + 15.7215u - 78.5804 \\ 0.00714381u^{106} - 0.00235302u^{105} + \dots + 22.5669u + 5.72998 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0917504u^{106} - 0.139578u^{105} + \dots - 54.8541u - 83.2245 \\ -0.0193726u^{106} + 0.0291699u^{105} + \dots + 7.73340u + 16.5814 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.125588u^{106} + 0.200162u^{105} + \dots + 87.0752u + 122.294 \\ -0.0338377u^{106} + 0.0605837u^{105} + \dots + 32.2211u + 39.0699 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.125588u^{106} - 0.200162u^{105} + \dots - 87.0752u - 122.294 \\ -0.0267303u^{106} + 0.0296535u^{105} + \dots - 5.96052u + 12.9504 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $0.991312u^{106} - 1.30501u^{105} + \dots - 366.569u - 745.449$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------|---|
| c_1, c_2, c_4 | $u^{107} - 11u^{106} + \dots - u - 1$ |
| c_3, c_7 | $u^{107} - 2u^{106} + \dots - 512u + 512$ |
| c_5 | $u^{107} + 2u^{106} + \dots - 10404u + 2312$ |
| c_6, c_{12} | $u^{107} + 3u^{106} + \dots - 3u - 1$ |
| c_8, c_{11} | $u^{107} - 5u^{106} + \dots - 5466u - 289$ |
| c_9 | $17(17u^{107} + 96u^{106} + \dots - 2.67194 \times 10^8 u + 4.35330 \times 10^7)$ |
| c_{10} | $17(17u^{107} + 61u^{106} + \dots + 4.98410 \times 10^7 u - 2813417)$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------|---|
| c_1, c_2, c_4 | $y^{107} - 99y^{106} + \dots - 29y - 1$ |
| c_3, c_7 | $y^{107} - 54y^{106} + \dots + 7340032y - 262144$ |
| c_5 | $y^{107} - 18y^{106} + \dots + 277740560y - 5345344$ |
| c_6, c_{12} | $y^{107} + 73y^{106} + \dots + 55y - 1$ |
| c_8, c_{11} | $y^{107} - 81y^{106} + \dots + 6093612y - 83521$ |
| c_9 | $289(289y^{107} - 19076y^{106} + \dots + 8.77063 \times 10^{16}y - 1.89512 \times 10^{15})$ |
| c_{10} | 289 $\cdot (289y^{107} - 7971y^{106} + \dots + 1153422073109755y - 7915315215889)$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.931265 + 0.406170I$ | $-2.30486 + 1.44330I$ | 0 |
| $a = 0.180524 + 0.102775I$ | | |
| $b = -0.628756 + 1.070630I$ | | |
| $u = -0.931265 - 0.406170I$ | $-2.30486 - 1.44330I$ | 0 |
| $a = 0.180524 - 0.102775I$ | | |
| $b = -0.628756 - 1.070630I$ | | |
| $u = 0.976707 + 0.115936I$ | $-3.84509 + 1.95256I$ | 0 |
| $a = 0.599235 + 0.941304I$ | | |
| $b = 0.698962 - 0.236650I$ | | |
| $u = 0.976707 - 0.115936I$ | $-3.84509 - 1.95256I$ | 0 |
| $a = 0.599235 - 0.941304I$ | | |
| $b = 0.698962 + 0.236650I$ | | |
| $u = -0.356416 + 0.955461I$ | $-1.66924 - 1.97469I$ | 0 |
| $a = -0.592799 + 0.220178I$ | | |
| $b = -0.938545 + 0.461272I$ | | |
| $u = -0.356416 - 0.955461I$ | $-1.66924 + 1.97469I$ | 0 |
| $a = -0.592799 - 0.220178I$ | | |
| $b = -0.938545 - 0.461272I$ | | |
| $u = -1.012720 + 0.132824I$ | $-7.33756 + 0.07613I$ | 0 |
| $a = 1.54325 + 0.67120I$ | | |
| $b = 2.50954 + 0.63542I$ | | |
| $u = -1.012720 - 0.132824I$ | $-7.33756 - 0.07613I$ | 0 |
| $a = 1.54325 - 0.67120I$ | | |
| $b = 2.50954 - 0.63542I$ | | |
| $u = -0.971497 + 0.327337I$ | $-2.56341 + 2.94691I$ | 0 |
| $a = 1.094850 + 0.029360I$ | | |
| $b = 2.56859 + 0.95662I$ | | |
| $u = -0.971497 - 0.327337I$ | $-2.56341 - 2.94691I$ | 0 |
| $a = 1.094850 - 0.029360I$ | | |
| $b = 2.56859 - 0.95662I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.088254 + 0.953155I$ | | |
| $a = 0.143294 + 1.178500I$ | $-4.79638 + 0.98699I$ | 0 |
| $b = 1.132480 - 0.334989I$ | | |
| $u = 0.088254 - 0.953155I$ | | |
| $a = 0.143294 - 1.178500I$ | $-4.79638 - 0.98699I$ | 0 |
| $b = 1.132480 + 0.334989I$ | | |
| $u = 0.933039 + 0.143215I$ | | |
| $a = -0.494644 - 1.048140I$ | $-3.78091 - 2.99219I$ | 0 |
| $b = -0.343321 - 1.127840I$ | | |
| $u = 0.933039 - 0.143215I$ | | |
| $a = -0.494644 + 1.048140I$ | $-3.78091 + 2.99219I$ | 0 |
| $b = -0.343321 + 1.127840I$ | | |
| $u = -0.431800 + 0.976154I$ | | |
| $a = -0.668560 - 0.913554I$ | $-3.77986 + 4.80948I$ | 0 |
| $b = -0.428460 + 0.364883I$ | | |
| $u = -0.431800 - 0.976154I$ | | |
| $a = -0.668560 + 0.913554I$ | $-3.77986 - 4.80948I$ | 0 |
| $b = -0.428460 - 0.364883I$ | | |
| $u = 0.228518 + 0.892361I$ | | |
| $a = -0.264082 + 0.338861I$ | $-4.76982 - 0.36186I$ | 0 |
| $b = 0.70974 + 1.40915I$ | | |
| $u = 0.228518 - 0.892361I$ | | |
| $a = -0.264082 - 0.338861I$ | $-4.76982 + 0.36186I$ | 0 |
| $b = 0.70974 - 1.40915I$ | | |
| $u = -0.092471 + 1.078070I$ | | |
| $a = -0.44549 + 1.54366I$ | $-9.17182 - 2.19773I$ | 0 |
| $b = -0.620069 + 0.456648I$ | | |
| $u = -0.092471 - 1.078070I$ | | |
| $a = -0.44549 - 1.54366I$ | $-9.17182 + 2.19773I$ | 0 |
| $b = -0.620069 - 0.456648I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 0.889247 + 0.203541I$ $a = -1.189030 + 0.430620I$ $b = -2.69411 - 0.64847I$ | $-2.97691 - 0.95326I$ | 0 |
| $u = 0.889247 - 0.203541I$ $a = -1.189030 - 0.430620I$ $b = -2.69411 + 0.64847I$ | $-2.97691 + 0.95326I$ | 0 |
| $u = -0.242919 + 0.867268I$ $a = 0.10892 - 1.53983I$ $b = 0.090572 + 0.409338I$ | $-4.39157 - 8.45275I$ | 0 |
| $u = -0.242919 - 0.867268I$ $a = 0.10892 + 1.53983I$ $b = 0.090572 - 0.409338I$ | $-4.39157 + 8.45275I$ | 0 |
| $u = 1.061410 + 0.301435I$ $a = -1.53828 - 0.25745I$ $b = -2.67895 + 0.02396I$ | $-6.91732 - 4.41662I$ | 0 |
| $u = 1.061410 - 0.301435I$ $a = -1.53828 + 0.25745I$ $b = -2.67895 - 0.02396I$ | $-6.91732 + 4.41662I$ | 0 |
| $u = 0.304573 + 1.063250I$ $a = 0.997292 + 0.520611I$ $b = 1.080310 + 0.440969I$ | $-5.05564 + 5.39819I$ | 0 |
| $u = 0.304573 - 1.063250I$ $a = 0.997292 - 0.520611I$ $b = 1.080310 - 0.440969I$ | $-5.05564 - 5.39819I$ | 0 |
| $u = -0.870663 + 0.176776I$ $a = -0.973907 + 0.679642I$ $b = -0.531737 - 0.185116I$ | $-0.72189 + 2.74860I$ | 0 |
| $u = -0.870663 - 0.176776I$ $a = -0.973907 - 0.679642I$ $b = -0.531737 + 0.185116I$ | $-0.72189 - 2.74860I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 1.015450 + 0.504665I$ $a = -0.241834 - 0.639622I$ $b = -0.171049 - 0.300765I$ | $1.09835 - 3.92237I$ | 0 |
| $u = 1.015450 - 0.504665I$ $a = -0.241834 + 0.639622I$ $b = -0.171049 + 0.300765I$ | $1.09835 + 3.92237I$ | 0 |
| $u = 0.526835 + 0.664073I$ $a = 0.813713 + 0.084744I$ $b = 0.649668 + 0.235899I$ | $2.60177 - 0.62792I$ | 0 |
| $u = 0.526835 - 0.664073I$ $a = 0.813713 - 0.084744I$ $b = 0.649668 - 0.235899I$ | $2.60177 + 0.62792I$ | 0 |
| $u = -1.076720 + 0.464977I$ $a = 0.552748 - 0.958127I$ $b = 0.796377 - 0.842288I$ | $-2.37272 + 7.54825I$ | 0 |
| $u = -1.076720 - 0.464977I$ $a = 0.552748 + 0.958127I$ $b = 0.796377 + 0.842288I$ | $-2.37272 - 7.54825I$ | 0 |
| $u = -0.733065 + 0.330340I$ $a = 0.064198 - 0.514775I$ $b = -0.374792 - 0.363000I$ | $-0.769990 - 0.237218I$ | $-8.00000 - 1.04777I$ |
| $u = -0.733065 - 0.330340I$ $a = 0.064198 + 0.514775I$ $b = -0.374792 + 0.363000I$ | $-0.769990 + 0.237218I$ | $-8.00000 + 1.04777I$ |
| $u = 0.716753 + 0.360053I$ $a = -1.124690 + 0.448670I$ $b = 3.46273 - 0.61131I$ | $-3.50386 - 1.66896I$ | $-16.6348 - 15.7652I$ |
| $u = 0.716753 - 0.360053I$ $a = -1.124690 - 0.448670I$ $b = 3.46273 + 0.61131I$ | $-3.50386 + 1.66896I$ | $-16.6348 + 15.7652I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.092779 + 0.786586I$ $a = -0.268044 - 1.184120I$ $b = -0.075212 + 0.508676I$ | $0.99398 + 2.92097I$ | $-2.14055 - 8.38546I$ |
| $u = 0.092779 - 0.786586I$ $a = -0.268044 + 1.184120I$ $b = -0.075212 - 0.508676I$ | $0.99398 - 2.92097I$ | $-2.14055 + 8.38546I$ |
| $u = 0.758308 + 0.133029I$ $a = -0.372777 + 0.723023I$ $b = 0.63345 + 1.29744I$ | $-3.58750 + 2.31232I$ | $-15.8918 - 2.7555I$ |
| $u = 0.758308 - 0.133029I$ $a = -0.372777 - 0.723023I$ $b = 0.63345 - 1.29744I$ | $-3.58750 - 2.31232I$ | $-15.8918 + 2.7555I$ |
| $u = 0.722730 + 0.161926I$ $a = 1.58847 + 0.40979I$ $b = 0.337724 - 0.130488I$ | $-5.80226 - 7.40735I$ | $-18.9937 + 9.1512I$ |
| $u = 0.722730 - 0.161926I$ $a = 1.58847 - 0.40979I$ $b = 0.337724 + 0.130488I$ | $-5.80226 + 7.40735I$ | $-18.9937 - 9.1512I$ |
| $u = 1.232030 + 0.307377I$ $a = -0.310429 + 0.667179I$ $b = 0.154826 - 0.286118I$ | $-6.76847 - 1.51759I$ | 0 |
| $u = 1.232030 - 0.307377I$ $a = -0.310429 - 0.667179I$ $b = 0.154826 + 0.286118I$ | $-6.76847 + 1.51759I$ | 0 |
| $u = -0.393537 + 0.609625I$ $a = -1.165490 + 0.721828I$ $b = -0.669946 + 0.274768I$ | $-0.31883 - 3.28324I$ | $-5.60431 + 3.66597I$ |
| $u = -0.393537 - 0.609625I$ $a = -1.165490 - 0.721828I$ $b = -0.669946 - 0.274768I$ | $-0.31883 + 3.28324I$ | $-5.60431 - 3.66597I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -1.212990 + 0.397926I$ $a = 0.623595 + 0.309847I$ $b = -0.39774 - 2.98122I$ | $-8.99268 + 4.16407I$ | 0 |
| $u = -1.212990 - 0.397926I$ $a = 0.623595 - 0.309847I$ $b = -0.39774 + 2.98122I$ | $-8.99268 - 4.16407I$ | 0 |
| $u = 1.242800 + 0.298457I$ $a = 1.168920 + 0.075796I$ $b = 2.89703 + 0.03063I$ | $-9.14754 - 8.24261I$ | 0 |
| $u = 1.242800 - 0.298457I$ $a = 1.168920 - 0.075796I$ $b = 2.89703 - 0.03063I$ | $-9.14754 + 8.24261I$ | 0 |
| $u = -0.141063 + 1.304170I$ $a = -0.115873 - 0.757239I$ $b = -0.172892 + 0.880125I$ | $1.38178 + 2.91494I$ | 0 |
| $u = -0.141063 - 1.304170I$ $a = -0.115873 + 0.757239I$ $b = -0.172892 - 0.880125I$ | $1.38178 - 2.91494I$ | 0 |
| $u = 1.204720 + 0.538302I$ $a = -0.224257 - 0.099675I$ $b = 0.245011 + 1.036330I$ | $-7.84058 - 4.80609I$ | 0 |
| $u = 1.204720 - 0.538302I$ $a = -0.224257 + 0.099675I$ $b = 0.245011 - 1.036330I$ | $-7.84058 + 4.80609I$ | 0 |
| $u = -1.309760 + 0.270121I$ $a = 0.371792 + 1.058620I$ $b = 0.086820 + 0.488872I$ | $-10.74750 - 1.26365I$ | 0 |
| $u = -1.309760 - 0.270121I$ $a = 0.371792 - 1.058620I$ $b = 0.086820 - 0.488872I$ | $-10.74750 + 1.26365I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 1.271700 + 0.434265I$ | $-8.58798 + 4.36356I$ | 0 |
| $a = 0.883155 - 0.416545I$ | | |
| $b = 2.30508 - 0.40191I$ | | |
| $u = 1.271700 - 0.434265I$ | $-8.58798 - 4.36356I$ | 0 |
| $a = 0.883155 + 0.416545I$ | | |
| $b = 2.30508 + 0.40191I$ | | |
| $u = -1.275970 + 0.428836I$ | $-9.07128 + 3.71874I$ | 0 |
| $a = 0.870350 + 0.396090I$ | | |
| $b = 2.57554 - 0.73466I$ | | |
| $u = -1.275970 - 0.428836I$ | $-9.07128 - 3.71874I$ | 0 |
| $a = 0.870350 - 0.396090I$ | | |
| $b = 2.57554 + 0.73466I$ | | |
| $u = 0.441267 + 1.276080I$ | $-10.4011 + 11.2730I$ | 0 |
| $a = 0.010079 - 1.136560I$ | | |
| $b = -0.075031 + 0.587350I$ | | |
| $u = 0.441267 - 1.276080I$ | $-10.4011 - 11.2730I$ | 0 |
| $a = 0.010079 + 1.136560I$ | | |
| $b = -0.075031 - 0.587350I$ | | |
| $u = -1.230600 + 0.564328I$ | $-7.4189 + 13.7965I$ | 0 |
| $a = -1.137020 - 0.087814I$ | | |
| $b = -2.86197 - 0.20383I$ | | |
| $u = -1.230600 - 0.564328I$ | $-7.4189 - 13.7965I$ | 0 |
| $a = -1.137020 + 0.087814I$ | | |
| $b = -2.86197 + 0.20383I$ | | |
| $u = -1.323420 + 0.286711I$ | $-4.18081 + 2.37986I$ | 0 |
| $a = -0.914417 - 0.024510I$ | | |
| $b = -2.58390 + 0.00153I$ | | |
| $u = -1.323420 - 0.286711I$ | $-4.18081 - 2.37986I$ | 0 |
| $a = -0.914417 + 0.024510I$ | | |
| $b = -2.58390 - 0.00153I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 1.278700 + 0.503687I$ $a = -0.908905 + 0.010734I$ $b = -2.44601 + 0.82010I$ | $-8.52536 - 6.22901I$ | 0 |
| $u = 1.278700 - 0.503687I$ $a = -0.908905 - 0.010734I$ $b = -2.44601 - 0.82010I$ | $-8.52536 + 6.22901I$ | 0 |
| $u = -1.232670 + 0.616020I$ $a = 0.285190 - 0.632161I$ $b = 0.364306 - 0.134856I$ | $-4.44227 + 7.78550I$ | 0 |
| $u = -1.232670 - 0.616020I$ $a = 0.285190 + 0.632161I$ $b = 0.364306 + 0.134856I$ | $-4.44227 - 7.78550I$ | 0 |
| $u = 1.267260 + 0.549056I$ $a = 0.938331 - 0.109314I$ $b = 2.60437 - 0.08018I$ | $-2.55413 - 8.13238I$ | 0 |
| $u = 1.267260 - 0.549056I$ $a = 0.938331 + 0.109314I$ $b = 2.60437 + 0.08018I$ | $-2.55413 + 8.13238I$ | 0 |
| $u = -0.613234$ $a = 0.343678$ $b = -0.360765$ | -0.940432 | -9.73200 |
| $u = -0.429164 + 1.329720I$ $a = -0.068472 - 0.921024I$ $b = -0.098161 + 0.749867I$ | $-5.51395 - 5.51248I$ | 0 |
| $u = -0.429164 - 1.329720I$ $a = -0.068472 + 0.921024I$ $b = -0.098161 - 0.749867I$ | $-5.51395 + 5.51248I$ | 0 |
| $u = -0.397402 + 0.438020I$ $a = 1.19302 + 1.61741I$ $b = 0.57156 + 4.09559I$ | $-5.90093 - 0.77524I$ | $-7.20009 - 8.79210I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -0.397402 - 0.438020I$ $a = 1.19302 - 1.61741I$ $b = 0.57156 - 4.09559I$ | $-5.90093 + 0.77524I$ | $-7.20009 + 8.79210I$ |
| $u = 1.349340 + 0.415520I$ $a = -1.217360 + 0.693262I$ $b = -2.01551 + 0.42109I$ | $-13.9537 - 2.9601I$ | 0 |
| $u = 1.349340 - 0.415520I$ $a = -1.217360 - 0.693262I$ $b = -2.01551 - 0.42109I$ | $-13.9537 + 2.9601I$ | 0 |
| $u = 1.27824 + 0.62370I$ $a = -0.527044 - 0.887663I$ $b = -0.860085 - 0.585152I$ | $-8.16809 - 11.50410I$ | 0 |
| $u = 1.27824 - 0.62370I$ $a = -0.527044 + 0.887663I$ $b = -0.860085 + 0.585152I$ | $-8.16809 + 11.50410I$ | 0 |
| $u = -0.288463 + 0.497708I$ $a = 0.665687 - 0.559774I$ $b = -0.203916 + 0.598819I$ | $-0.62747 + 1.89102I$ | $-3.97049 - 2.88595I$ |
| $u = -0.288463 - 0.497708I$ $a = 0.665687 + 0.559774I$ $b = -0.203916 - 0.598819I$ | $-0.62747 - 1.89102I$ | $-3.97049 + 2.88595I$ |
| $u = -1.33200 + 0.52311I$ $a = 1.312210 - 0.185097I$ $b = 2.36998 + 0.15644I$ | $-13.1732 + 7.9062I$ | 0 |
| $u = -1.33200 - 0.52311I$ $a = 1.312210 + 0.185097I$ $b = 2.36998 - 0.15644I$ | $-13.1732 - 7.9062I$ | 0 |
| $u = 0.55234 + 1.32267I$ $a = 0.388265 - 0.819153I$ $b = 0.481113 + 0.580917I$ | $-9.67010 - 1.15397I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.55234 - 1.32267I$ | | |
| $a = 0.388265 + 0.819153I$ | $-9.67010 + 1.15397I$ | 0 |
| $b = 0.481113 - 0.580917I$ | | |
| $u = -1.29769 + 0.65667I$ | | |
| $a = -0.767810 - 0.380695I$ | $-6.46600 + 1.47782I$ | 0 |
| $b = -2.13616 - 0.22858I$ | | |
| $u = -1.29769 - 0.65667I$ | | |
| $a = -0.767810 + 0.380695I$ | $-6.46600 - 1.47782I$ | 0 |
| $b = -2.13616 + 0.22858I$ | | |
| $u = 1.31949 + 0.75319I$ | | |
| $a = 1.044930 - 0.147670I$ | $-13.2708 - 18.4610I$ | 0 |
| $b = 2.73164 - 0.27623I$ | | |
| $u = 1.31949 - 0.75319I$ | | |
| $a = 1.044930 + 0.147670I$ | $-13.2708 + 18.4610I$ | 0 |
| $b = 2.73164 + 0.27623I$ | | |
| $u = -1.34268 + 0.75552I$ | | |
| $a = -0.894702 - 0.162317I$ | $-8.5253 + 12.8531I$ | 0 |
| $b = -2.54796 - 0.12017I$ | | |
| $u = -1.34268 - 0.75552I$ | | |
| $a = -0.894702 + 0.162317I$ | $-8.5253 - 12.8531I$ | 0 |
| $b = -2.54796 + 0.12017I$ | | |
| $u = -0.399946 + 0.214162I$ | | |
| $a = 1.30736 + 1.02540I$ | $-1.063250 - 0.043134I$ | $-7.94611 - 1.24147I$ |
| $b = -0.415975 + 0.038938I$ | | |
| $u = -0.399946 - 0.214162I$ | | |
| $a = 1.30736 - 1.02540I$ | $-1.063250 + 0.043134I$ | $-7.94611 + 1.24147I$ |
| $b = -0.415975 - 0.038938I$ | | |
| $u = 0.149223 + 0.396575I$ | | |
| $a = 0.01530 + 3.13817I$ | $-4.49140 + 1.51008I$ | $-9.81598 - 1.55694I$ |
| $b = 0.294661 + 0.448912I$ | | |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.149223 - 0.396575I$ $a = 0.01530 - 3.13817I$ $b = 0.294661 - 0.448912I$ | $-4.49140 - 1.51008I$ | $-9.81598 + 1.55694I$ |
| $u = 1.35595 + 0.81241I$ $a = 0.749963 - 0.331925I$ $b = 2.15867 - 0.11610I$ | $-12.32240 - 6.52710I$ | 0 |
| $u = 1.35595 - 0.81241I$ $a = 0.749963 + 0.331925I$ $b = 2.15867 + 0.11610I$ | $-12.32240 + 6.52710I$ | 0 |
| $u = -1.61146 + 0.03604I$ $a = -0.948244 - 0.190754I$ $b = -2.56392 - 0.11689I$ | $-18.4193 - 6.1353I$ | 0 |
| $u = -1.61146 - 0.03604I$ $a = -0.948244 + 0.190754I$ $b = -2.56392 + 0.11689I$ | $-18.4193 + 6.1353I$ | 0 |
| $u = 1.65879$ $a = 0.839440$ $b = 2.53074$ | -13.8071 | 0 |
| $u = 0.315785$ $a = -2.96408$ $b = -4.94665$ | -3.02083 | -69.6120 |

$$\text{II. } I_2^u = \langle 22u^2 + 17b + 2u + 40, u^2 + a - u + 2, u^3 - u^2 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + u - 2 \\ -\frac{22}{17}u^2 - \frac{2}{17}u - \frac{40}{17} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + u - 2 \\ -\frac{22}{17}u^2 + \frac{15}{17}u - \frac{40}{17} \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{14}{17}u^2 + \frac{8}{17}u - \frac{27}{17} \\ -\frac{19}{17}u^2 + \frac{6}{17}u - \frac{33}{17} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u^2 - u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 2u - 1 \\ u^2 - 2u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u^2 - u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = \frac{2667}{289}u^2 - \frac{10925}{289}u + \frac{2721}{289}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------|--------------------------------|
| c_1, c_2 | $u^3 + u^2 - 1$ |
| c_3 | $u^3 - u^2 + 2u - 1$ |
| c_4 | $u^3 - u^2 + 1$ |
| c_5 | u^3 |
| c_6 | $u^3 - 3u^2 + 2u + 1$ |
| c_7 | $u^3 + u^2 + 2u + 1$ |
| c_8 | $(u - 1)^3$ |
| c_9 | $17(17u^3 + 10u^2 - u - 1)$ |
| c_{10} | $17(17u^3 - 23u^2 + 8u - 1)$ |
| c_{11} | $(u + 1)^3$ |
| c_{12} | $u^3 + 3u^2 + 2u - 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------|------------------------------------|
| c_1, c_2, c_4 | $y^3 - y^2 + 2y - 1$ |
| c_3, c_7 | $y^3 + 3y^2 + 2y - 1$ |
| c_5 | y^3 |
| c_6, c_{12} | $y^3 - 5y^2 + 10y - 1$ |
| c_8, c_{11} | $(y - 1)^3$ |
| c_9 | $289(289y^3 - 134y^2 + 21y - 1)$ |
| c_{10} | $289(289y^3 - 257y^2 + 18y - 1)$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.215080 + 1.307140I$ $a = -0.122561 + 0.744862I$ $b = -0.226957 - 0.881437I$ | $1.37919 - 2.82812I$ | $-14.0563 - 44.2246I$ |
| $u = 0.215080 - 1.307140I$ $a = -0.122561 - 0.744862I$ $b = -0.226957 + 0.881437I$ | $1.37919 + 2.82812I$ | $-14.0563 + 44.2246I$ |
| $u = 0.569840$ $a = -1.75488$ $b = -2.84020$ | -2.75839 | -9.12970 |

III.

$$I_1^v = \langle a, 14536v^8 + 40690v^7 + \cdots + 11959b + 36034, v^9 + 3v^8 + \cdots + 3v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1.21549v^8 - 3.40246v^7 + \cdots - 0.204281v - 3.01313 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ -0.917468v^8 - 2.75040v^7 + \cdots - 1.68777v - 2.76913 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.298018v^8 + 0.652061v^7 + \cdots - 0.483485v + 0.244000 \\ -0.705410v^8 - 1.67138v^7 + \cdots + 2.87842v - 0.490008 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.109374v^8 + 0.367255v^7 + \cdots + 0.0885526v + 0.00200686 \\ -0.917468v^8 - 2.75040v^7 + \cdots - 1.68777v - 2.76913 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.120495v^8 - 0.294506v^7 + \cdots + 0.670792v + 0.0803579 \\ 0.198846v^8 + 0.759428v^7 + \cdots + 1.00962v - 0.427544 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.244000v^8 - 0.433983v^7 + \cdots - 0.633331v - 0.215486 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.244000v^8 + 0.433983v^7 + \cdots + 0.633331v + 0.215486 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.244000v^8 - 0.433983v^7 + \cdots - 0.633331v + 0.784514 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= \frac{30669}{11959}v^8 + \frac{76868}{11959}v^7 - \frac{100871}{11959}v^6 - \frac{237835}{11959}v^5 + \frac{437462}{11959}v^4 + \frac{579948}{11959}v^3 - \frac{66654}{11959}v^2 - \frac{147944}{11959}v - \frac{72837}{11959}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1, c_2 | $(u - 1)^9$ |
| c_3, c_7 | u^9 |
| c_4 | $(u + 1)^9$ |
| c_5, c_{10} | $u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$ |
| c_6 | $u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$ |
| c_8 | $u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$ |
| c_9 | $u^9 + 5u^8 + 12u^7 + 15u^6 + 9u^5 - u^4 - 4u^3 - 2u^2 + u + 1$ |
| c_{11} | $u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$ |
| c_{12} | $u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------|--|
| c_1, c_2, c_4 | $(y - 1)^9$ |
| c_3, c_7 | y^9 |
| c_5, c_{10} | $y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$ |
| c_6, c_{12} | $y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$ |
| c_8, c_{11} | $y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$ |
| c_9 | $y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^v | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $v = -0.924205 + 0.223068I$ $a = 0$ $b = -0.037875 + 0.791187I$ | $-2.26187 + 2.45442I$ | $-8.53903 - 2.82066I$ |
| $v = -0.924205 - 0.223068I$ $a = 0$ $b = -0.037875 - 0.791187I$ | $-2.26187 - 2.45442I$ | $-8.53903 + 2.82066I$ |
| $v = 0.295822 + 0.390531I$ $a = 0$ $b = 0.80973 - 2.39258I$ | $-6.01628 + 1.33617I$ | $-16.4774 - 4.4812I$ |
| $v = 0.295822 - 0.390531I$ $a = 0$ $b = 0.80973 + 2.39258I$ | $-6.01628 - 1.33617I$ | $-16.4774 + 4.4812I$ |
| $v = -0.280601$ $a = 0$ $b = -2.94345$ | -2.84338 | -3.87310 |
| $v = 1.47927 + 0.93319I$ $a = 0$ $b = -0.218072 + 0.482572I$ | $0.13850 + 2.09337I$ | $-6.02684 - 1.69698I$ |
| $v = 1.47927 - 0.93319I$ $a = 0$ $b = -0.218072 - 0.482572I$ | $0.13850 - 2.09337I$ | $-6.02684 + 1.69698I$ |
| $v = -2.21059 + 0.69487I$ $a = 0$ $b = 0.417942 + 0.357732I$ | $-5.24306 - 7.08493I$ | $-9.02021 + 2.94778I$ |
| $v = -2.21059 - 0.69487I$ $a = 0$ $b = 0.417942 - 0.357732I$ | $-5.24306 + 7.08493I$ | $-9.02021 - 2.94778I$ |

IV. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------|--|
| c_1, c_2 | $((u-1)^9)(u^3+u^2-1)(u^{107}-11u^{106}+\dots-u-1)$ |
| c_3 | $u^9(u^3-u^2+2u-1)(u^{107}-2u^{106}+\dots-512u+512)$ |
| c_4 | $((u+1)^9)(u^3-u^2+1)(u^{107}-11u^{106}+\dots-u-1)$ |
| c_5 | $u^3(u^9+u^8+2u^7+u^6+3u^5+u^4+2u^3+u-1)$ $\cdot (u^{107}+2u^{106}+\dots-10404u+2312)$ |
| c_6 | (u^3-3u^2+2u+1) $\cdot (u^9+3u^8+8u^7+13u^6+17u^5+17u^4+12u^3+6u^2+u-1)$ $\cdot (u^{107}+3u^{106}+\dots-3u-1)$ |
| c_7 | $u^9(u^3+u^2+2u+1)(u^{107}-2u^{106}+\dots-512u+512)$ |
| c_8 | $(u-1)^3(u^9+u^8-2u^7-3u^6+u^5+3u^4+2u^3-u-1)$ $\cdot (u^{107}-5u^{106}+\dots-5466u-289)$ |
| c_9 | $289(17u^3+10u^2-u-1)$ $\cdot (u^9+5u^8+12u^7+15u^6+9u^5-u^4-4u^3-2u^2+u+1)$ $\cdot (17u^{107}+96u^{106}+\dots-267194040u+43532959)$ |
| c_{10} | $289(17u^3-23u^2+8u-1)(u^9+u^8+\dots+u-1)$ $\cdot (17u^{107}+61u^{106}+\dots+49840983u-2813417)$ |
| c_{11} | $(u+1)^3(u^9-u^8-2u^7+3u^6+u^5-3u^4+2u^3-u+1)$ $\cdot (u^{107}-5u^{106}+\dots-5466u-289)$ |
| c_{12} | (u^3+3u^2+2u-1) $\cdot (u^9-3u^8+8u^7-13u^6+17u^5-17u^4+12u^3-6u^2+u+1)$ $\cdot (u^{107}+3u^{106}+\dots-24u-1)$ |

V. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|-----------------|--|
| c_1, c_2, c_4 | $((y-1)^9)(y^3 - y^2 + 2y - 1)(y^{107} - 99y^{106} + \dots - 29y - 1)$ |
| c_3, c_7 | $y^9(y^3 + 3y^2 + 2y - 1)(y^{107} - 54y^{106} + \dots + 7340032y - 262144)$ |
| c_5 | $y^3(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)$ $\cdot (y^{107} - 18y^{106} + \dots + 277740560y - 5345344)$ |
| c_6, c_{12} | $(y^3 - 5y^2 + 10y - 1)$ $\cdot (y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)$ $\cdot (y^{107} + 73y^{106} + \dots + 55y - 1)$ |
| c_8, c_{11} | $(y-1)^3(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot (y^{107} - 81y^{106} + \dots + 6093612y - 83521)$ |
| c_9 | $83521(289y^3 - 134y^2 + 21y - 1)$ $\cdot (y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)$ $\cdot (289y^{107} - 1.91 \times 10^4 y^{106} + \dots + 8.77 \times 10^{16} y - 1.90 \times 10^{15})$ |
| c_{10} | $83521(289y^3 - 257y^2 + 18y - 1)$ $\cdot (y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)$ $\cdot (289y^{107} - 7971y^{106} + \dots + 1153422073109755y - 7915315215889)$ |