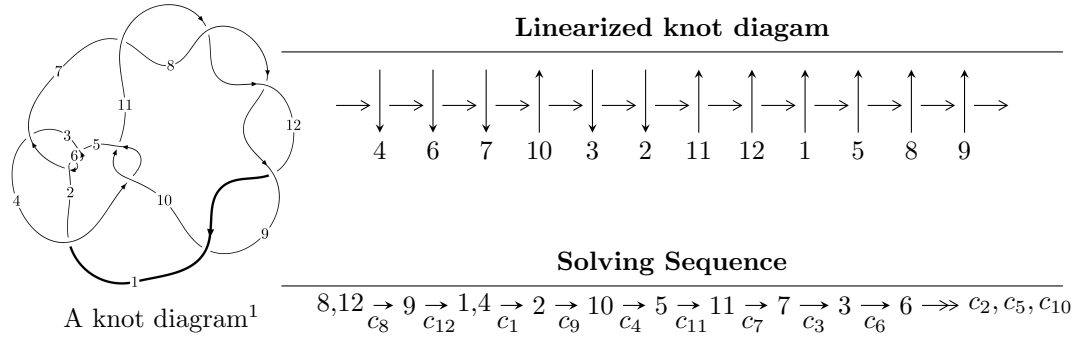


12a<sub>0881</sub> (K12a<sub>0881</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 30u^{49} + 63u^{48} + \dots + 4b + 19, 7u^{48} + 15u^{47} + \dots + 4a - 3, u^{50} + 4u^{49} + \dots - u + 1 \rangle$$

$$I_2^u = \langle b + a, a^3 + a^2 - 1, u^2 - u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 56 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle 30u^{49} + 63u^{48} + \dots + 4b + 19, 7u^{48} + 15u^{47} + \dots + 4a - 3, u^{50} + 4u^{49} + \dots - u + 1 \rangle$$

I.  $I_1^u =$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{7}{4}u^{48} - \frac{15}{4}u^{47} + \dots - \frac{7}{2}u + \frac{3}{4} \\ -\frac{15}{2}u^{49} - \frac{63}{4}u^{48} + \dots + 6u - \frac{19}{4} \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{4}u^{49} + \frac{3}{4}u^{48} + \dots + \frac{23}{4}u + 1 \\ -\frac{1}{4}u^{49} - \frac{3}{4}u^{48} + \dots - 5u^2 + \frac{1}{4}u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -20u^{49} - \frac{185}{4}u^{48} + \dots + \frac{29}{2}u - \frac{43}{4} \\ \frac{51}{2}u^{49} + \frac{233}{4}u^{48} + \dots - 23u + \frac{55}{4} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{111}{4}u^{49} - 65u^{48} + \dots + \frac{85}{4}u - \frac{63}{4} \\ 34.7500u^{49} + 81.2500u^{48} + \dots - 32.7500u + 19.5000 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{9}{2}u^{49} - \frac{21}{2}u^{48} + \dots + 4u - 2 \\ \frac{21}{4}u^{49} + \frac{51}{4}u^{48} + \dots - \frac{19}{4}u + 3 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $25u^{49} + 59u^{48} + \dots - \frac{83}{2}u + \frac{25}{2}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{50} - 9u^{49} + \dots + 1832u + 113$
$c_2, c_5, c_6$	$u^{50} - 3u^{49} + \dots - 10u + 1$
$c_3$	$u^{50} + 3u^{49} + \dots - 2392u + 241$
$c_4, c_{10}$	$u^{50} - u^{49} + \dots - 96u + 64$
$c_7, c_8, c_9$ $c_{11}, c_{12}$	$u^{50} - 4u^{49} + \dots + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{50} + 31y^{49} + \dots - 5984830y + 12769$
$c_2, c_5, c_6$	$y^{50} + 47y^{49} + \dots - 54y + 1$
$c_3$	$y^{50} + 11y^{49} + \dots - 2239214y + 58081$
$c_4, c_{10}$	$y^{50} - 35y^{49} + \dots - 54272y + 4096$
$c_7, c_8, c_9$ $c_{11}, c_{12}$	$y^{50} - 68y^{49} + \dots + 9y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.952202 + 0.085743I$ $a = 0.263868 + 0.811802I$ $b = 0.109466 + 1.005260I$	$1.99660 - 1.56126I$	$0. + 4.54210I$
$u = -0.952202 - 0.085743I$ $a = 0.263868 - 0.811802I$ $b = 0.109466 - 1.005260I$	$1.99660 + 1.56126I$	$0. - 4.54210I$
$u = -1.051590 + 0.116393I$ $a = -0.460087 - 1.130740I$ $b = 0.029530 - 1.139970I$	$7.55680 - 4.35419I$	0
$u = -1.051590 - 0.116393I$ $a = -0.460087 + 1.130740I$ $b = 0.029530 + 1.139970I$	$7.55680 + 4.35419I$	0
$u = 0.926369 + 0.110294I$ $a = -0.951862 + 0.190261I$ $b = 1.207080 - 0.506059I$	$4.83990 + 3.67287I$	$11.52712 - 5.42395I$
$u = 0.926369 - 0.110294I$ $a = -0.951862 - 0.190261I$ $b = 1.207080 + 0.506059I$	$4.83990 - 3.67287I$	$11.52712 + 5.42395I$
$u = 0.926358$ $a = 1.08741$ $b = -1.30017$	1.12359	7.78030
$u = 1.075460 + 0.335893I$ $a = 0.318078 + 0.440056I$ $b = 0.173538 + 1.100140I$	$5.70451 + 6.74184I$	0
$u = 1.075460 - 0.335893I$ $a = 0.318078 - 0.440056I$ $b = 0.173538 - 1.100140I$	$5.70451 - 6.74184I$	0
$u = 1.101720 + 0.265116I$ $a = -0.631574 - 0.369790I$ $b = 0.069190 - 0.623696I$	$6.52824 + 2.59024I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.101720 - 0.265116I$ $a = -0.631574 + 0.369790I$ $b = 0.069190 + 0.623696I$	$6.52824 - 2.59024I$	0
$u = 1.091080 + 0.380456I$ $a = -0.163597 - 0.625898I$ $b = -0.536851 - 1.297450I$	$11.5454 + 10.2862I$	0
$u = 1.091080 - 0.380456I$ $a = -0.163597 + 0.625898I$ $b = -0.536851 + 1.297450I$	$11.5454 - 10.2862I$	0
$u = -0.740193 + 0.295777I$ $a = -0.361219 - 0.137662I$ $b = -0.870973 - 0.536080I$	$4.15678 - 0.49764I$	$9.03893 + 1.33769I$
$u = -0.740193 - 0.295777I$ $a = -0.361219 + 0.137662I$ $b = -0.870973 + 0.536080I$	$4.15678 + 0.49764I$	$9.03893 - 1.33769I$
$u = 1.199130 + 0.267015I$ $a = 0.903623 + 0.631411I$ $b = 0.208467 + 0.051458I$	$13.08760 + 0.25307I$	0
$u = 1.199130 - 0.267015I$ $a = 0.903623 - 0.631411I$ $b = 0.208467 - 0.051458I$	$13.08760 - 0.25307I$	0
$u = -0.470779 + 0.592707I$ $a = 0.805640 - 0.073631I$ $b = -0.525112 + 1.088250I$	$7.73029 + 2.70190I$	$9.92902 - 0.03562I$
$u = -0.470779 - 0.592707I$ $a = 0.805640 + 0.073631I$ $b = -0.525112 - 1.088250I$	$7.73029 - 2.70190I$	$9.92902 + 0.03562I$
$u = -0.301413 + 0.651199I$ $a = -1.27352 + 0.89636I$ $b = -0.537119 - 0.669077I$	$7.21081 - 6.77625I$	$8.31083 + 6.21335I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.301413 - 0.651199I$ $a = -1.27352 - 0.89636I$ $b = -0.537119 + 0.669077I$	$7.21081 + 6.77625I$	$8.31083 - 6.21335I$
$u = -0.295790 + 0.583078I$ $a = 0.912564 - 0.926539I$ $b = 0.190072 + 0.467950I$	$1.43056 - 3.60804I$	$4.24958 + 7.07743I$
$u = -0.295790 - 0.583078I$ $a = 0.912564 + 0.926539I$ $b = 0.190072 - 0.467950I$	$1.43056 + 3.60804I$	$4.24958 - 7.07743I$
$u = -0.405535 + 0.509845I$ $a = -0.537103 + 0.460008I$ $b = 0.355378 - 0.582565I$	$1.81710 + 0.00783I$	$6.28682 + 0.01976I$
$u = -0.405535 - 0.509845I$ $a = -0.537103 - 0.460008I$ $b = 0.355378 + 0.582565I$	$1.81710 - 0.00783I$	$6.28682 - 0.01976I$
$u = -0.512306$ $a = 0.313006$ $b = 0.321368$	$0.766149$	$13.4410$
$u = -0.033821 + 0.416681I$ $a = -0.02102 + 1.94574I$ $b = 0.405990 + 0.159838I$	$2.06372 - 1.98561I$	$1.75080 + 4.13320I$
$u = -0.033821 - 0.416681I$ $a = -0.02102 - 1.94574I$ $b = 0.405990 - 0.159838I$	$2.06372 + 1.98561I$	$1.75080 - 4.13320I$
$u = 1.59708$ $a = -0.845107$ $b = 1.07699$	$8.19154$	$0$
$u = 1.61144 + 0.05910I$ $a = 1.25524 - 0.79623I$ $b = -1.80165 + 0.80672I$	$12.23120 + 1.76270I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.61144 - 0.05910I$ $a = 1.25524 + 0.79623I$ $b = -1.80165 - 0.80672I$	$12.23120 - 1.76270I$	0
$u = 0.267156 + 0.194860I$ $a = 0.14623 + 2.75307I$ $b = 0.727620 - 0.740672I$	$3.42049 + 3.22954I$	$-0.37490 - 5.13369I$
$u = 0.267156 - 0.194860I$ $a = 0.14623 - 2.75307I$ $b = 0.727620 + 0.740672I$	$3.42049 - 3.22954I$	$-0.37490 + 5.13369I$
$u = -1.71592$ $a = 0.726622$ $b = -0.423053$	10.6526	0
$u = -1.71698 + 0.02280I$ $a = -0.638945 - 0.755487I$ $b = 0.367724 + 1.082380I$	$14.3705 - 4.1609I$	0
$u = -1.71698 - 0.02280I$ $a = -0.638945 + 0.755487I$ $b = 0.367724 - 1.082380I$	$14.3705 + 4.1609I$	0
$u = 1.71834 + 0.01659I$ $a = -0.32264 + 2.56462I$ $b = 0.69393 - 4.29665I$	$11.59990 + 1.93326I$	0
$u = 1.71834 - 0.01659I$ $a = -0.32264 - 2.56462I$ $b = 0.69393 + 4.29665I$	$11.59990 - 1.93326I$	0
$u = 1.74020 + 0.02935I$ $a = 0.58408 - 2.98539I$ $b = -1.34410 + 5.19321I$	$17.6233 + 4.9552I$	0
$u = 1.74020 - 0.02935I$ $a = 0.58408 + 2.98539I$ $b = -1.34410 - 5.19321I$	$17.6233 - 4.9552I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.102654 + 0.234461I$ $a = -0.48752 - 2.52124I$ $b = -0.550472 + 0.258801I$	$-1.186530 + 0.460043I$	$-6.06013 - 1.97452I$
$u = 0.102654 - 0.234461I$ $a = -0.48752 + 2.52124I$ $b = -0.550472 - 0.258801I$	$-1.186530 - 0.460043I$	$-6.06013 + 1.97452I$
$u = -1.74331 + 0.08919I$ $a = -0.36769 + 2.41491I$ $b = 0.37187 - 4.07506I$	$15.7539 - 8.5170I$	0
$u = -1.74331 - 0.08919I$ $a = -0.36769 - 2.41491I$ $b = 0.37187 + 4.07506I$	$15.7539 + 8.5170I$	0
$u = -1.74805 + 0.07009I$ $a = 0.42579 - 1.94514I$ $b = -0.80402 + 3.33285I$	$16.7378 - 4.0067I$	0
$u = -1.74805 - 0.07009I$ $a = 0.42579 + 1.94514I$ $b = -0.80402 - 3.33285I$	$16.7378 + 4.0067I$	0
$u = -1.74828 + 0.10270I$ $a = 0.50895 - 2.70608I$ $b = -0.35501 + 4.68791I$	$-17.8318 - 12.3199I$	0
$u = -1.74828 - 0.10270I$ $a = 0.50895 + 2.70608I$ $b = -0.35501 - 4.68791I$	$-17.8318 + 12.3199I$	0
$u = -1.77321 + 0.06163I$ $a = -1.04826 + 1.68240I$ $b = 2.07789 - 3.22013I$	$-15.6447 - 1.6429I$	0
$u = -1.77321 - 0.06163I$ $a = -1.04826 - 1.68240I$ $b = 2.07789 + 3.22013I$	$-15.6447 + 1.6429I$	0

$$\text{II. } I_2^u = \langle b + a, a^3 + a^2 - 1, u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u \\ -u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -a \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a^2 + u \\ -a^2 - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ -a \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} au + a \\ -au - 2a \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a^2u + a^2 + a - u - 1 \\ -a^2u - 2a^2 - a + u + 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $a^2u - 2a^2 - au - 5a - u + 5$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u^3 + u^2 - 1)^2$
$c_2$	$(u^3 - u^2 + 2u - 1)^2$
$c_4, c_{10}$	$u^6$
$c_5, c_6$	$(u^3 + u^2 + 2u + 1)^2$
$c_7, c_8, c_9$	$(u^2 - u - 1)^3$
$c_{11}, c_{12}$	$(u^2 + u - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$(y^3 - y^2 + 2y - 1)^2$
$c_2, c_5, c_6$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_4, c_{10}$	$y^6$
$c_7, c_8, c_9$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.618034$ $a = -0.877439 + 0.744862I$ $b = 0.877439 - 0.744862I$	$4.01109 + 2.82812I$	$8.89985 + 0.15818I$
$u = -0.618034$ $a = -0.877439 - 0.744862I$ $b = 0.877439 + 0.744862I$	$4.01109 - 2.82812I$	$8.89985 - 0.15818I$
$u = -0.618034$ $a = 0.754878$ $b = -0.754878$	$-0.126494$	$0.818320$
$u = 1.61803$ $a = -0.877439 + 0.744862I$ $b = 0.877439 - 0.744862I$	$11.90680 + 2.82812I$	$9.10673 - 4.43024I$
$u = 1.61803$ $a = -0.877439 - 0.744862I$ $b = 0.877439 + 0.744862I$	$11.90680 - 2.82812I$	$9.10673 + 4.43024I$
$u = 1.61803$ $a = 0.754878$ $b = -0.754878$	$7.76919$	$-1.83150$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^3 + u^2 - 1)^2)(u^{50} - 9u^{49} + \dots + 1832u + 113)$
$c_2$	$((u^3 - u^2 + 2u - 1)^2)(u^{50} - 3u^{49} + \dots - 10u + 1)$
$c_3$	$((u^3 + u^2 - 1)^2)(u^{50} + 3u^{49} + \dots - 2392u + 241)$
$c_4, c_{10}$	$u^6(u^{50} - u^{49} + \dots - 96u + 64)$
$c_5, c_6$	$((u^3 + u^2 + 2u + 1)^2)(u^{50} - 3u^{49} + \dots - 10u + 1)$
$c_7, c_8, c_9$	$((u^2 - u - 1)^3)(u^{50} - 4u^{49} + \dots + u + 1)$
$c_{11}, c_{12}$	$((u^2 + u - 1)^3)(u^{50} - 4u^{49} + \dots + u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^3 - y^2 + 2y - 1)^2)(y^{50} + 31y^{49} + \dots - 5984830y + 12769)$
$c_2, c_5, c_6$	$((y^3 + 3y^2 + 2y - 1)^2)(y^{50} + 47y^{49} + \dots - 54y + 1)$
$c_3$	$((y^3 - y^2 + 2y - 1)^2)(y^{50} + 11y^{49} + \dots - 2239214y + 58081)$
$c_4, c_{10}$	$y^6(y^{50} - 35y^{49} + \dots - 54272y + 4096)$
$c_7, c_8, c_9$ $c_{11}, c_{12}$	$((y^2 - 3y + 1)^3)(y^{50} - 68y^{49} + \dots + 9y + 1)$