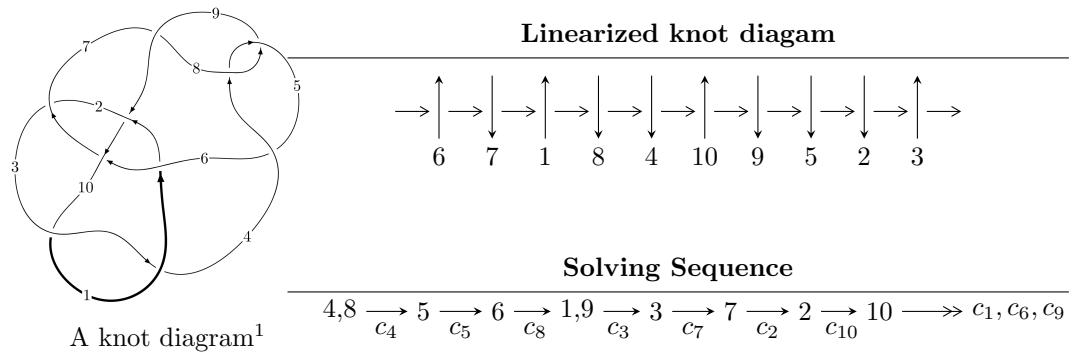


10<sub>87</sub> ( $K10a_{39}$ )



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 2225248116121u^{40} - 2393989479567u^{39} + \dots + 10297376929134b - 6012630756121, \\ - 31071718506119u^{40} + 39367206545589u^{39} + \dots + 5148688464567a - 44602733573152, \\ u^{41} - 2u^{40} + \dots - u - 1 \rangle$$

$$I_2^u = \langle b - 1, a - 1, u - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 42 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

**I.**

$$I_1^u = \langle 2.23 \times 10^{12} u^{40} - 2.39 \times 10^{12} u^{39} + \dots + 1.03 \times 10^{13} b - 6.01 \times 10^{12}, -3.11 \times 10^{13} u^{40} + 3.94 \times 10^{13} u^{39} + \dots + 5.15 \times 10^{12} a - 4.46 \times 10^{13}, u^{41} - 2u^{40} + \dots - u - 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 6.03488u^{40} - 7.64606u^{39} + \dots + 20.1260u + 8.66293 \\ -0.216099u^{40} + 0.232485u^{39} + \dots - 1.20415u + 0.583899 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 5.64438u^{40} - 7.18325u^{39} + \dots + 18.2918u + 8.93217 \\ -0.135606u^{40} + 0.0700585u^{39} + \dots - 1.18339u + 0.664403 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 4.44062u^{40} - 5.31684u^{39} + \dots + 13.7767u + 7.07457 \\ -1.46774u^{40} + 1.54335u^{39} + \dots - 6.10178u - 1.46782 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1.00290u^{40} - 1.84189u^{39} + \dots + 5.12751u + 1.12239 \\ -0.839015u^{40} + 1.67515u^{39} + \dots - 0.958478u - 0.838993 \end{pmatrix}$$

(ii) **Obstruction class = -1**

(iii) **Cusp Shapes**

$$= \frac{23238917313784}{1716229488189} u^{40} - \frac{10481023528134}{572076496063} u^{39} + \dots + \frac{28692506559598}{572076496063} u + \frac{39302820789020}{1716229488189}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{41} + 8u^{39} + \cdots + 687u + 229$
$c_2$	$u^{41} + 2u^{40} + \cdots - 97u + 29$
$c_3, c_{10}$	$u^{41} + 2u^{40} + \cdots + 9u + 1$
$c_4, c_8$	$u^{41} + 2u^{40} + \cdots - u + 1$
$c_5, c_7$	$u^{41} + 12u^{40} + \cdots + 5u + 1$
$c_6$	$u^{41} + 4u^{40} + \cdots + u + 1$
$c_9$	$u^{41} - 7u^{40} + \cdots + 6u - 2$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{41} + 16y^{40} + \cdots + 1271637y - 52441$
$c_2$	$y^{41} + 48y^{40} + \cdots - 7063y - 841$
$c_3, c_{10}$	$y^{41} - 32y^{40} + \cdots + 141y - 1$
$c_4, c_8$	$y^{41} - 12y^{40} + \cdots + 5y - 1$
$c_5, c_7$	$y^{41} + 36y^{40} + \cdots + 5y - 1$
$c_6$	$y^{41} - 8y^{40} + \cdots + 5y - 1$
$c_9$	$y^{41} + 9y^{40} + \cdots - 16y - 4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.903206 + 0.396002I$		
$a = 1.211920 + 0.667053I$	$-1.94008 - 1.34771I$	$-7.61480 + 3.42502I$
$b = -0.408078 + 0.420450I$		
$u = 0.903206 - 0.396002I$		
$a = 1.211920 - 0.667053I$	$-1.94008 + 1.34771I$	$-7.61480 - 3.42502I$
$b = -0.408078 - 0.420450I$		
$u = -0.952455 + 0.222261I$		
$a = -0.211328 + 0.932061I$	$-2.78156 + 3.84619I$	$-6.97849 - 6.75687I$
$b = -0.096162 + 0.914015I$		
$u = -0.952455 - 0.222261I$		
$a = -0.211328 - 0.932061I$	$-2.78156 - 3.84619I$	$-6.97849 + 6.75687I$
$b = -0.096162 - 0.914015I$		
$u = -0.821825 + 0.760247I$		
$a = 0.450451 - 0.306050I$	$3.49362 + 1.78935I$	$0.87448 - 4.34492I$
$b = 0.335334 - 0.324976I$		
$u = -0.821825 - 0.760247I$		
$a = 0.450451 + 0.306050I$	$3.49362 - 1.78935I$	$0.87448 + 4.34492I$
$b = 0.335334 + 0.324976I$		
$u = 0.866850$		
$a = 0.639506$	$-1.43130$	$-6.87200$
$b = -0.0835204$		
$u = 0.798878 + 0.810698I$		
$a = 0.377223 - 0.719870I$	$3.76974 + 2.25598I$	$1.50138 - 3.41744I$
$b = 0.265202 + 1.192170I$		
$u = 0.798878 - 0.810698I$		
$a = 0.377223 + 0.719870I$	$3.76974 - 2.25598I$	$1.50138 + 3.41744I$
$b = 0.265202 - 1.192170I$		
$u = -1.102330 + 0.334587I$		
$a = 0.338270 - 1.284530I$	$0.85372 + 8.63849I$	$-1.84811 - 8.19635I$
$b = -1.253450 - 0.430907I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.102330 - 0.334587I$		
$a = 0.338270 + 1.284530I$	$0.85372 - 8.63849I$	$-1.84811 + 8.19635I$
$b = -1.253450 + 0.430907I$		
$u = -0.058442 + 0.843545I$		
$a = 1.57943 - 0.15589I$	$4.36449 - 4.62926I$	$4.68493 + 4.91932I$
$b = -1.284700 + 0.271028I$		
$u = -0.058442 - 0.843545I$		
$a = 1.57943 + 0.15589I$	$4.36449 + 4.62926I$	$4.68493 - 4.91932I$
$b = -1.284700 - 0.271028I$		
$u = -0.883648 + 0.770325I$		
$a = -3.62989 + 1.11022I$	$5.18095 + 2.90757I$	$-15.8800 + 0.I$
$b = 1.134150 + 0.025263I$		
$u = -0.883648 - 0.770325I$		
$a = -3.62989 - 1.11022I$	$5.18095 - 2.90757I$	$-15.8800 + 0.I$
$b = 1.134150 - 0.025263I$		
$u = 0.760286 + 0.907829I$		
$a = 1.73221 + 0.34788I$	$9.17940 + 7.97252I$	$3.27060 - 3.71618I$
$b = -1.45266 - 0.46932I$		
$u = 0.760286 - 0.907829I$		
$a = 1.73221 - 0.34788I$	$9.17940 - 7.97252I$	$3.27060 + 3.71618I$
$b = -1.45266 + 0.46932I$		
$u = 0.866672 + 0.809557I$		
$a = -1.56395 - 1.02120I$	$7.77351 - 0.87153I$	$6.95024 - 0.30904I$
$b = 1.60494 + 0.57469I$		
$u = 0.866672 - 0.809557I$		
$a = -1.56395 + 1.02120I$	$7.77351 + 0.87153I$	$6.95024 + 0.30904I$
$b = 1.60494 - 0.57469I$		
$u = -0.929908 + 0.739442I$		
$a = 0.037024 + 0.508793I$	$3.15987 + 3.90045I$	$-0.31532 - 1.57295I$
$b = 0.197100 + 0.379729I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.929908 - 0.739442I$		
$a = 0.037024 - 0.508793I$	$3.15987 - 3.90045I$	$-0.31532 + 1.57295I$
$b = 0.197100 - 0.379729I$		
$u = -0.744475 + 0.942248I$		
$a = 1.62214 - 0.18187I$	$8.52020 + 0.56768I$	$6.81847 - 0.32338I$
$b = -1.310630 + 0.070763I$		
$u = -0.744475 - 0.942248I$		
$a = 1.62214 + 0.18187I$	$8.52020 - 0.56768I$	$6.81847 + 0.32338I$
$b = -1.310630 - 0.070763I$		
$u = -0.739440 + 0.286658I$		
$a = 0.11659 + 1.68574I$	$1.56831 + 2.54987I$	$1.57226 - 7.77175I$
$b = 1.073000 + 0.545709I$		
$u = -0.739440 - 0.286658I$		
$a = 0.11659 - 1.68574I$	$1.56831 - 2.54987I$	$1.57226 + 7.77175I$
$b = 1.073000 - 0.545709I$		
$u = 0.913744 + 0.795988I$		
$a = -2.19807 - 1.07996I$	$7.62795 - 5.14257I$	$6.43416 + 5.95767I$
$b = 1.55855 - 0.65970I$		
$u = 0.913744 - 0.795988I$		
$a = -2.19807 + 1.07996I$	$7.62795 + 5.14257I$	$6.43416 - 5.95767I$
$b = 1.55855 + 0.65970I$		
$u = 1.191150 + 0.227807I$		
$a = -0.076211 + 0.412771I$	$0.067811 + 0.953358I$	$2.02910 - 7.42558I$
$b = -1.116560 - 0.153454I$		
$u = 1.191150 - 0.227807I$		
$a = -0.076211 - 0.412771I$	$0.067811 - 0.953358I$	$2.02910 + 7.42558I$
$b = -1.116560 + 0.153454I$		
$u = 0.960612 + 0.767884I$		
$a = -1.113770 + 0.253317I$	$3.27367 - 8.18385I$	$0. + 8.35233I$
$b = 0.163245 - 1.244780I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.960612 - 0.767884I$		
$a = -1.113770 - 0.253317I$	$3.27367 + 8.18385I$	$0. - 8.35233I$
$b = 0.163245 + 1.244780I$		
$u = 0.748657 + 0.093307I$		
$a = 0.47886 - 4.75552I$	$0.431185 - 0.284475I$	$13.1815 - 15.1990I$
$b = 0.938830 - 0.044980I$		
$u = 0.748657 - 0.093307I$		
$a = 0.47886 + 4.75552I$	$0.431185 + 0.284475I$	$13.1815 + 15.1990I$
$b = 0.938830 + 0.044980I$		
$u = 1.022750 + 0.797628I$		
$a = 1.90383 + 1.42431I$	$8.3544 - 14.2736I$	$0. + 8.33140I$
$b = -1.44670 + 0.51890I$		
$u = 1.022750 - 0.797628I$		
$a = 1.90383 - 1.42431I$	$8.3544 + 14.2736I$	$0. - 8.33140I$
$b = -1.44670 - 0.51890I$		
$u = -1.045230 + 0.812235I$		
$a = 1.41367 - 1.18781I$	$7.57848 + 5.87702I$	$0. - 5.65225I$
$b = -1.277530 - 0.155370I$		
$u = -1.045230 - 0.812235I$		
$a = 1.41367 + 1.18781I$	$7.57848 - 5.87702I$	$0. + 5.65225I$
$b = -1.277530 + 0.155370I$		
$u = 0.039502 + 0.458105I$		
$a = 0.880104 + 0.384951I$	$0.05414 - 1.50218I$	$0.18723 + 4.24532I$
$b = 0.142705 - 0.550416I$		
$u = 0.039502 - 0.458105I$		
$a = 0.880104 - 0.384951I$	$0.05414 + 1.50218I$	$0.18723 - 4.24532I$
$b = 0.142705 + 0.550416I$		
$u = -0.361128 + 0.264161I$		
$a = -0.168271 + 0.663616I$	$2.56290 - 0.10225I$	$4.38337 - 2.22967I$
$b = 1.275180 - 0.127224I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.361128 - 0.264161I$		
$a = -0.168271 - 0.663616I$	$2.56290 + 0.10225I$	$4.38337 + 2.22967I$
$b = 1.275180 + 0.127224I$		

$$\text{II. } I_2^u = \langle b - 1, a - 1, u - 1 \rangle$$

(i) **Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) **Obstruction class = 1**

(iii) **Cusp Shapes = 0**

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_6, c_7$	$u - 1$
$c_5, c_8, c_{10}$	$u + 1$
$c_9$	$u$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_6$ $c_7, c_8, c_{10}$	$y - 1$
$c_9$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 1.00000$	0	0
$b = 1.00000$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)(u^{41} + 8u^{39} + \cdots + 687u + 229)$
$c_2$	$(u - 1)(u^{41} + 2u^{40} + \cdots - 97u + 29)$
$c_3$	$(u - 1)(u^{41} + 2u^{40} + \cdots + 9u + 1)$
$c_4$	$(u - 1)(u^{41} + 2u^{40} + \cdots - u + 1)$
$c_5$	$(u + 1)(u^{41} + 12u^{40} + \cdots + 5u + 1)$
$c_6$	$(u - 1)(u^{41} + 4u^{40} + \cdots + u + 1)$
$c_7$	$(u - 1)(u^{41} + 12u^{40} + \cdots + 5u + 1)$
$c_8$	$(u + 1)(u^{41} + 2u^{40} + \cdots - u + 1)$
$c_9$	$u(u^{41} - 7u^{40} + \cdots + 6u - 2)$
$c_{10}$	$(u + 1)(u^{41} + 2u^{40} + \cdots + 9u + 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y - 1)(y^{41} + 16y^{40} + \dots + 1271637y - 52441)$
$c_2$	$(y - 1)(y^{41} + 48y^{40} + \dots - 7063y - 841)$
$c_3, c_{10}$	$(y - 1)(y^{41} - 32y^{40} + \dots + 141y - 1)$
$c_4, c_8$	$(y - 1)(y^{41} - 12y^{40} + \dots + 5y - 1)$
$c_5, c_7$	$(y - 1)(y^{41} + 36y^{40} + \dots + 5y - 1)$
$c_6$	$(y - 1)(y^{41} - 8y^{40} + \dots + 5y - 1)$
$c_9$	$y(y^{41} + 9y^{40} + \dots - 16y - 4)$