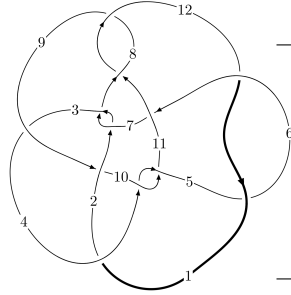
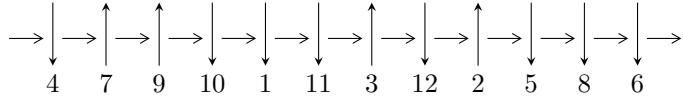


12a<sub>1056</sub> (K12a<sub>1056</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$8, 11 \xrightarrow{c_{11}} 12 \xrightarrow{c_8} 3, 9 \xrightarrow{c_3} 4 \xrightarrow{c_7} 7 \xrightarrow{c_2} 2 \xrightarrow{c_6} 6 \xrightarrow{c_{12}} 1 \xrightarrow{c_5} 5 \xrightarrow{c_{10}} 10 \rightsquigarrow c_1, c_4, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.20589 \times 10^{861} u^{169} - 1.68317 \times 10^{862} u^{168} + \dots + 3.92119 \times 10^{861} b - 1.07359 \times 10^{864}, \\ - 2.08380 \times 10^{863} u^{169} - 1.48692 \times 10^{864} u^{168} + \dots + 8.66583 \times 10^{863} a - 5.10383 \times 10^{865}, \\ u^{170} + 8u^{169} + \dots - 715u + 221 \rangle$$

$$I_2^u = \langle 2.87441 \times 10^{31} u^{46} + 1.04633 \times 10^{32} u^{45} + \dots + 3.67466 \times 10^{29} b - 6.08288 \times 10^{31}, \\ 1.01354 \times 10^{31} u^{46} + 3.82828 \times 10^{31} u^{45} + \dots + 3.67466 \times 10^{29} a - 1.99417 \times 10^{31}, u^{47} + 3u^{46} + \dots - u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 217 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -2.21 \times 10^{861} u^{169} - 1.68 \times 10^{862} u^{168} + \dots + 3.92 \times 10^{861} b - 1.07 \times 10^{864}, -2.08 \times 10^{863} u^{169} - 1.49 \times 10^{864} u^{168} + \dots + 8.67 \times 10^{863} a - 5.10 \times 10^{865}, u^{170} + 8u^{169} + \dots - 715u + 221 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.240462u^{169} + 1.71584u^{168} + \dots - 213.145u + 58.8960 \\ 0.562557u^{169} + 4.29249u^{168} + \dots - 1443.71u + 273.792 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.345473u^{169} + 2.53056u^{168} + \dots - 549.544u + 119.828 \\ 0.451916u^{169} + 3.44659u^{168} + \dots - 1148.66u + 218.467 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0758536u^{169} + 0.482857u^{168} + \dots + 31.9502u + 1.29112 \\ 0.0670230u^{169} + 0.611089u^{168} + \dots - 518.273u + 88.7818 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1.29316u^{169} + 9.38618u^{168} + \dots - 1589.87u + 368.013 \\ 0.647019u^{169} + 4.85787u^{168} + \dots - 1368.07u + 269.970 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.142877u^{169} + 1.09395u^{168} + \dots - 486.322u + 90.0730 \\ 0.0670230u^{169} + 0.611089u^{168} + \dots - 518.273u + 88.7818 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 3.05118u^{169} + 22.3493u^{168} + \dots - 4601.86u + 988.759 \\ 1.73028u^{169} + 12.7494u^{168} + \dots - 2868.52u + 600.253 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.317412u^{169} + 2.17686u^{168} + \dots - 245.983u + 62.9293 \\ -1.04715u^{169} - 7.63752u^{168} + \dots + 1595.46u - 335.601 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.896039u^{169} - 6.43983u^{168} + \dots + 1252.55u - 271.632 \\ -0.841413u^{169} - 6.23424u^{168} + \dots + 1470.83u - 307.080 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-0.513757u^{169} - 3.30789u^{168} + \dots - 410.609u + 24.5051$

(iv) u-Polynomials at the component

| Crossings     | u-Polynomials at each crossing                      |
|---------------|---|
| $c_1$         | $u^{170} - 14u^{169} + \dots + 18u - 1$             |
| $c_2, c_7$    | $u^{170} + u^{169} + \dots - 42944u + 1984$         |
| $c_3$         | $u^{170} - u^{169} + \dots - 276535005u - 23926117$ |
| $c_4, c_{10}$ | $u^{170} + u^{169} + \dots + 60040u - 6379$         |
| $c_5, c_{12}$ | $u^{170} + 2u^{169} + \dots + 6420u - 35591$        |
| $c_6$         | $u^{170} - u^{169} + \dots + 9130974u + 5572759$    |
| $c_8, c_{11}$ | $u^{170} + 8u^{169} + \dots - 715u + 221$           |
| $c_9$         | $u^{170} + 3u^{169} + \dots + 811454u + 271819$     |

(v) Riley Polynomials at the component

| Crossings     | Riley Polynomials at each crossing                                   |
|---------------|--|
| $c_1$         | $y^{170} + 6y^{169} + \dots - 760y + 1$                              |
| $c_2, c_7$    | $y^{170} - 93y^{169} + \dots - 827236352y + 3936256$                 |
| $c_3$         | $y^{170} - 41y^{169} + \dots - 46800698030178335y + 572459074697689$ |
| $c_4, c_{10}$ | $y^{170} - 113y^{169} + \dots - 1618495822y + 40691641$              |
| $c_5, c_{12}$ | $y^{170} + 118y^{169} + \dots + 25027873906y + 1266719281$           |
| $c_6$         | $y^{170} - 9y^{169} + \dots + 1788240547802984y + 31055642872081$    |
| $c_8, c_{11}$ | $y^{170} - 88y^{169} + \dots + 1304511y + 48841$                     |
| $c_9$         | $y^{170} + 43y^{169} + \dots + 6707969409918y + 73885568761$         |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 0.806491 + 0.602217I$<br>$a = -0.642128 + 0.983618I$<br>$b = 0.19143 - 1.76020I$  | $7.48922 - 0.81335I$                  | 0          |
| $u = 0.806491 - 0.602217I$<br>$a = -0.642128 - 0.983618I$<br>$b = 0.19143 + 1.76020I$  | $7.48922 + 0.81335I$                  | 0          |
| $u = -0.923484 + 0.347149I$<br>$a = 1.12852 - 1.00215I$<br>$b = -0.674725 + 0.109848I$ | $-5.16258 - 1.55018I$                 | 0          |
| $u = -0.923484 - 0.347149I$<br>$a = 1.12852 + 1.00215I$<br>$b = -0.674725 - 0.109848I$ | $-5.16258 + 1.55018I$                 | 0          |
| $u = 0.141671 + 0.976038I$<br>$a = -0.488385 + 1.125170I$<br>$b = -0.03831 - 1.42440I$ | $3.36613 + 3.99327I$                  | 0          |
| $u = 0.141671 - 0.976038I$<br>$a = -0.488385 - 1.125170I$<br>$b = -0.03831 + 1.42440I$ | $3.36613 - 3.99327I$                  | 0          |
| $u = 0.956886 + 0.364577I$<br>$a = 1.035210 - 0.734016I$<br>$b = -0.30003 + 2.40004I$  | $2.92615 - 8.39267I$                  | 0          |
| $u = 0.956886 - 0.364577I$<br>$a = 1.035210 + 0.734016I$<br>$b = -0.30003 - 2.40004I$  | $2.92615 + 8.39267I$                  | 0          |
| $u = 0.798269 + 0.554483I$<br>$a = -1.29539 + 0.66106I$<br>$b = -0.907230 - 0.822265I$ | $7.53091 - 3.76031I$                  | 0          |
| $u = 0.798269 - 0.554483I$<br>$a = -1.29539 - 0.66106I$<br>$b = -0.907230 + 0.822265I$ | $7.53091 + 3.76031I$                  | 0          |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -0.831602 + 0.494310I$<br>$a = -1.48201 - 0.73010I$<br>$b = -0.840353 + 1.057020I$ | $4.31538 + 8.41906I$                  | 0          |
| $u = -0.831602 - 0.494310I$<br>$a = -1.48201 + 0.73010I$<br>$b = -0.840353 - 1.057020I$ | $4.31538 - 8.41906I$                  | 0          |
| $u = -0.338787 + 0.978329I$<br>$a = -0.007267 - 0.513671I$<br>$b = -0.80769 + 1.41151I$ | $3.70858 + 2.48023I$                  | 0          |
| $u = -0.338787 - 0.978329I$<br>$a = -0.007267 + 0.513671I$<br>$b = -0.80769 - 1.41151I$ | $3.70858 - 2.48023I$                  | 0          |
| $u = -0.802710 + 0.530461I$<br>$a = -0.947896 - 1.022750I$<br>$b = 0.15648 + 1.76490I$  | $4.38227 - 4.26234I$                  | 0          |
| $u = -0.802710 - 0.530461I$<br>$a = -0.947896 + 1.022750I$<br>$b = 0.15648 - 1.76490I$  | $4.38227 + 4.26234I$                  | 0          |
| $u = -1.044890 + 0.163904I$<br>$a = -0.738916 - 0.484622I$<br>$b = -0.99773 + 1.59669I$ | $-1.66846 + 0.48444I$                 | 0          |
| $u = -1.044890 - 0.163904I$<br>$a = -0.738916 + 0.484622I$<br>$b = -0.99773 - 1.59669I$ | $-1.66846 - 0.48444I$                 | 0          |
| $u = -0.414758 + 0.845908I$<br>$a = 0.183797 - 1.029530I$<br>$b = 0.40704 + 1.83699I$   | $0.96077 + 6.50241I$                  | 0          |
| $u = -0.414758 - 0.845908I$<br>$a = 0.183797 + 1.029530I$<br>$b = 0.40704 - 1.83699I$   | $0.96077 - 6.50241I$                  | 0          |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = -0.158664 + 1.046010I$<br>$a = -0.605569 - 1.030360I$<br>$b = 0.236176 + 1.351120I$ | $-0.85216 - 7.75918I$                 | 0          |
| $u = -0.158664 - 1.046010I$<br>$a = -0.605569 + 1.030360I$<br>$b = 0.236176 - 1.351120I$ | $-0.85216 + 7.75918I$                 | 0          |
| $u = 0.834299 + 0.650852I$<br>$a = -0.098909 + 1.187020I$<br>$b = -1.35369 - 1.59644I$   | $-3.52491 - 5.82721I$                 | 0          |
| $u = 0.834299 - 0.650852I$<br>$a = -0.098909 - 1.187020I$<br>$b = -1.35369 + 1.59644I$   | $-3.52491 + 5.82721I$                 | 0          |
| $u = -1.018280 + 0.313229I$<br>$a = 0.828726 + 0.572675I$<br>$b = -1.02081 - 1.92324I$   | $4.88864 + 3.76517I$                  | 0          |
| $u = -1.018280 - 0.313229I$<br>$a = 0.828726 - 0.572675I$<br>$b = -1.02081 + 1.92324I$   | $4.88864 - 3.76517I$                  | 0          |
| $u = 0.224394 + 0.906655I$<br>$a = -0.559436 - 0.349460I$<br>$b = 0.096076 + 0.954016I$  | $4.22731 + 2.52538I$                  | 0          |
| $u = 0.224394 - 0.906655I$<br>$a = -0.559436 + 0.349460I$<br>$b = 0.096076 - 0.954016I$  | $4.22731 - 2.52538I$                  | 0          |
| $u = 1.036580 + 0.282285I$<br>$a = -0.811496 + 0.728701I$<br>$b = -1.43074 - 1.60823I$   | $-6.33389 - 5.42778I$                 | 0          |
| $u = 1.036580 - 0.282285I$<br>$a = -0.811496 - 0.728701I$<br>$b = -1.43074 + 1.60823I$   | $-6.33389 + 5.42778I$                 | 0          |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -0.366311 + 1.028260I$<br>$a = -0.601079 - 0.608587I$<br>$b = -0.376946 + 0.702967I$ | $1.11850 + 2.49775I$                  | 0          |
| $u = -0.366311 - 1.028260I$<br>$a = -0.601079 + 0.608587I$<br>$b = -0.376946 - 0.702967I$ | $1.11850 - 2.49775I$                  | 0          |
| $u = 0.955413 + 0.535542I$<br>$a = -1.031710 - 0.527843I$<br>$b = 0.492943 - 0.739556I$   | $-4.00039 + 1.13083I$                 | 0          |
| $u = 0.955413 - 0.535542I$<br>$a = -1.031710 + 0.527843I$<br>$b = 0.492943 + 0.739556I$   | $-4.00039 - 1.13083I$                 | 0          |
| $u = 1.085970 + 0.244696I$<br>$a = 0.996060 + 0.557928I$<br>$b = -0.051939 + 0.187299I$   | $-2.66025 + 2.54993I$                 | 0          |
| $u = 1.085970 - 0.244696I$<br>$a = 0.996060 - 0.557928I$<br>$b = -0.051939 - 0.187299I$   | $-2.66025 - 2.54993I$                 | 0          |
| $u = 0.874696 + 0.133073I$<br>$a = 0.774374 + 1.094520I$<br>$b = -0.046872 - 0.469309I$   | $-1.30487 + 1.72427I$                 | 0          |
| $u = 0.874696 - 0.133073I$<br>$a = 0.774374 - 1.094520I$<br>$b = -0.046872 + 0.469309I$   | $-1.30487 - 1.72427I$                 | 0          |
| $u = -0.497941 + 0.729795I$<br>$a = 1.165820 + 0.629819I$<br>$b = 0.006520 - 0.998511I$   | $-2.03235 - 1.15583I$                 | 0          |
| $u = -0.497941 - 0.729795I$<br>$a = 1.165820 - 0.629819I$<br>$b = 0.006520 + 0.998511I$   | $-2.03235 + 1.15583I$                 | 0          |



| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 1.061980 + 0.362119I$<br>$a = -0.528626 - 0.797838I$<br>$b = 0.149722 + 0.444329I$  | $-2.90057 - 3.69809I$                 | 0          |
| $u = 1.061980 - 0.362119I$<br>$a = -0.528626 + 0.797838I$<br>$b = 0.149722 - 0.444329I$  | $-2.90057 + 3.69809I$                 | 0          |
| $u = -1.002390 + 0.507253I$<br>$a = -0.775875 - 0.405924I$<br>$b = 0.36366 + 1.97753I$   | $2.66744 + 2.88124I$                  | 0          |
| $u = -1.002390 - 0.507253I$<br>$a = -0.775875 + 0.405924I$<br>$b = 0.36366 - 1.97753I$   | $2.66744 - 2.88124I$                  | 0          |
| $u = 1.039130 + 0.442035I$<br>$a = -0.012302 - 0.813686I$<br>$b = 0.719743 + 1.063800I$  | $-4.03539 - 3.56778I$                 | 0          |
| $u = 1.039130 - 0.442035I$<br>$a = -0.012302 + 0.813686I$<br>$b = 0.719743 - 1.063800I$  | $-4.03539 + 3.56778I$                 | 0          |
| $u = -1.090030 + 0.319356I$<br>$a = -0.276890 + 0.948683I$<br>$b = 0.701189 - 0.427324I$ | $-4.85761 + 3.45164I$                 | 0          |
| $u = -1.090030 - 0.319356I$<br>$a = -0.276890 - 0.948683I$<br>$b = 0.701189 + 0.427324I$ | $-4.85761 - 3.45164I$                 | 0          |
| $u = -1.078490 + 0.389234I$<br>$a = -0.787230 + 0.880471I$<br>$b = 0.048133 - 0.220752I$ | $-6.77478 + 6.50412I$                 | 0          |
| $u = -1.078490 - 0.389234I$<br>$a = -0.787230 - 0.880471I$<br>$b = 0.048133 + 0.220752I$ | $-6.77478 - 6.50412I$                 | 0          |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.264729 + 0.810062I$ |                                       |            |
| $a = -0.919199 + 0.505820I$ | $-0.28815 - 8.54272I$                 | 0          |
| $b = 0.468141 - 0.933035I$  |                                       |            |
| $u = -0.264729 - 0.810062I$ |                                       |            |
| $a = -0.919199 - 0.505820I$ | $-0.28815 + 8.54272I$                 | 0          |
| $b = 0.468141 + 0.933035I$  |                                       |            |
| $u = 1.074410 + 0.405058I$  |                                       |            |
| $a = -0.271488 - 0.968396I$ | $-1.51684 - 6.06281I$                 | 0          |
| $b = 0.076752 + 0.262131I$  |                                       |            |
| $u = 1.074410 - 0.405058I$  |                                       |            |
| $a = -0.271488 + 0.968396I$ | $-1.51684 + 6.06281I$                 | 0          |
| $b = 0.076752 - 0.262131I$  |                                       |            |
| $u = 0.770082 + 0.363667I$  |                                       |            |
| $a = 1.69569 - 0.51875I$    | $3.56946 + 5.26691I$                  | 0          |
| $b = 1.41698 + 1.21974I$    |                                       |            |
| $u = 0.770082 - 0.363667I$  |                                       |            |
| $a = 1.69569 + 0.51875I$    | $3.56946 - 5.26691I$                  | 0          |
| $b = 1.41698 - 1.21974I$    |                                       |            |
| $u = -1.087010 + 0.390708I$ |                                       |            |
| $a = 0.564034 + 1.103930I$  | $1.73688 + 5.19821I$                  | 0          |
| $b = 0.049728 - 0.981981I$  |                                       |            |
| $u = -1.087010 - 0.390708I$ |                                       |            |
| $a = 0.564034 - 1.103930I$  | $1.73688 - 5.19821I$                  | 0          |
| $b = 0.049728 + 0.981981I$  |                                       |            |
| $u = -1.014070 + 0.566273I$ |                                       |            |
| $a = 0.511883 + 1.128890I$  | $-3.51186 + 6.09555I$                 | 0          |
| $b = 0.85240 - 1.71737I$    |                                       |            |
| $u = -1.014070 - 0.566273I$ |                                       |            |
| $a = 0.511883 - 1.128890I$  | $-3.51186 - 6.09555I$                 | 0          |
| $b = 0.85240 + 1.71737I$    |                                       |            |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 1.085820 + 0.418233I$<br>$a = 0.798553 - 1.006530I$<br>$b = 0.222149 + 1.264500I$  | $1.81434 - 3.63679I$                  | 0          |
| $u = 1.085820 - 0.418233I$<br>$a = 0.798553 + 1.006530I$<br>$b = 0.222149 - 1.264500I$  | $1.81434 + 3.63679I$                  | 0          |
| $u = 1.032740 + 0.540789I$<br>$a = -0.639624 + 0.255097I$<br>$b = 0.64336 - 1.81774I$   | $3.05780 - 1.58165I$                  | 0          |
| $u = 1.032740 - 0.540789I$<br>$a = -0.639624 - 0.255097I$<br>$b = 0.64336 + 1.81774I$   | $3.05780 + 1.58165I$                  | 0          |
| $u = -1.172030 + 0.110315I$<br>$a = 0.546361 - 0.282163I$<br>$b = 0.338652 - 0.023447I$ | $-1.85244 - 0.13124I$                 | 0          |
| $u = -1.172030 - 0.110315I$<br>$a = 0.546361 + 0.282163I$<br>$b = 0.338652 + 0.023447I$ | $-1.85244 + 0.13124I$                 | 0          |
| $u = 0.206943 + 0.792165I$<br>$a = -0.77995 + 1.43503I$<br>$b = -0.23213 - 1.55337I$    | $3.35332 + 3.66686I$                  | 0          |
| $u = 0.206943 - 0.792165I$<br>$a = -0.77995 - 1.43503I$<br>$b = -0.23213 + 1.55337I$    | $3.35332 - 3.66686I$                  | 0          |
| $u = 1.073230 + 0.497941I$<br>$a = 0.718078 - 0.898766I$<br>$b = 0.56627 + 1.47951I$    | $1.19048 - 4.34256I$                  | 0          |
| $u = 1.073230 - 0.497941I$<br>$a = 0.718078 + 0.898766I$<br>$b = 0.56627 - 1.47951I$    | $1.19048 + 4.34256I$                  | 0          |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = -0.386200 + 0.716926I$<br>$a = -1.23518 - 1.03634I$<br>$b = -0.09588 + 1.72609I$     | $1.62100 - 4.92629I$                  | 0          |
| $u = -0.386200 - 0.716926I$<br>$a = -1.23518 + 1.03634I$<br>$b = -0.09588 - 1.72609I$     | $1.62100 + 4.92629I$                  | 0          |
| $u = -1.087760 + 0.478529I$<br>$a = -0.398562 + 0.536807I$<br>$b = -0.090742 + 0.198724I$ | $1.11222 + 2.21408I$                  | 0          |
| $u = -1.087760 - 0.478529I$<br>$a = -0.398562 - 0.536807I$<br>$b = -0.090742 - 0.198724I$ | $1.11222 - 2.21408I$                  | 0          |
| $u = 0.720394 + 0.363656I$<br>$a = 0.1003940 - 0.0876140I$<br>$b = 0.09773 + 1.62111I$    | $-4.26294 - 3.88455I$                 | 0          |
| $u = 0.720394 - 0.363656I$<br>$a = 0.1003940 + 0.0876140I$<br>$b = 0.09773 - 1.62111I$    | $-4.26294 + 3.88455I$                 | 0          |
| $u = -0.751811 + 0.261150I$<br>$a = 1.67265 + 0.26483I$<br>$b = 1.79961 - 0.35379I$       | $5.89546 - 1.20354I$                  | 0          |
| $u = -0.751811 - 0.261150I$<br>$a = 1.67265 - 0.26483I$<br>$b = 1.79961 + 0.35379I$       | $5.89546 + 1.20354I$                  | 0          |
| $u = 1.077970 + 0.559514I$<br>$a = 0.528140 - 0.647463I$<br>$b = 1.59630 + 1.38440I$      | $-5.68088 - 0.47001I$                 | 0          |
| $u = 1.077970 - 0.559514I$<br>$a = 0.528140 + 0.647463I$<br>$b = 1.59630 - 1.38440I$      | $-5.68088 + 0.47001I$                 | 0          |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 1.141460 + 0.436982I$  |                                       |            |
| $a = 0.719505 - 0.582562I$  | $-2.77969 - 9.91991I$                 | 0          |
| $b = 1.79355 + 2.15528I$    |                                       |            |
| $u = 1.141460 - 0.436982I$  |                                       |            |
| $a = 0.719505 + 0.582562I$  | $-2.77969 + 9.91991I$                 | 0          |
| $b = 1.79355 - 2.15528I$    |                                       |            |
| $u = -0.412691 + 1.159020I$ |                                       |            |
| $a = 0.751366 + 0.779719I$  | $2.83336 - 13.74430I$                 | 0          |
| $b = 0.13006 - 1.68933I$    |                                       |            |
| $u = -0.412691 - 1.159020I$ |                                       |            |
| $a = 0.751366 - 0.779719I$  | $2.83336 + 13.74430I$                 | 0          |
| $b = 0.13006 + 1.68933I$    |                                       |            |
| $u = -0.759159 + 0.077930I$ |                                       |            |
| $a = 0.27620 + 1.61746I$    | $-4.43746 + 4.02048I$                 | 0          |
| $b = 0.358040 - 0.701749I$  |                                       |            |
| $u = -0.759159 - 0.077930I$ |                                       |            |
| $a = 0.27620 - 1.61746I$    | $-4.43746 - 4.02048I$                 | 0          |
| $b = 0.358040 + 0.701749I$  |                                       |            |
| $u = 1.218450 + 0.215306I$  |                                       |            |
| $a = -0.492939 + 0.554272I$ | $-5.11241 + 5.14848I$                 | 0          |
| $b = -1.21497 - 1.07752I$   |                                       |            |
| $u = 1.218450 - 0.215306I$  |                                       |            |
| $a = -0.492939 - 0.554272I$ | $-5.11241 - 5.14848I$                 | 0          |
| $b = -1.21497 + 1.07752I$   |                                       |            |
| $u = -1.103990 + 0.569699I$ |                                       |            |
| $a = -0.767471 - 0.982847I$ | $-0.49000 + 9.86610I$                 | 0          |
| $b = -1.20004 + 2.17363I$   |                                       |            |
| $u = -1.103990 - 0.569699I$ |                                       |            |
| $a = -0.767471 + 0.982847I$ | $-0.49000 - 9.86610I$                 | 0          |
| $b = -1.20004 - 2.17363I$   |                                       |            |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 0.453656 + 1.178900I$<br>$a = -0.531767 + 0.782266I$<br>$b = -0.08702 - 1.78565I$  | $5.39447 + 4.87671I$                  | 0          |
| $u = 0.453656 - 1.178900I$<br>$a = -0.531767 - 0.782266I$<br>$b = -0.08702 + 1.78565I$  | $5.39447 - 4.87671I$                  | 0          |
| $u = -0.730425$<br>$a = 0.666694$<br>$b = 0.382456$                                     | $-1.46358$                            | 0          |
| $u = -1.086450 + 0.664366I$<br>$a = 0.482956 + 0.569224I$<br>$b = 0.96455 - 1.58617I$   | $-1.16037 + 2.89712I$                 | 0          |
| $u = -1.086450 - 0.664366I$<br>$a = 0.482956 - 0.569224I$<br>$b = 0.96455 + 1.58617I$   | $-1.16037 - 2.89712I$                 | 0          |
| $u = 0.499069 + 0.527627I$<br>$a = -0.88297 + 1.37264I$<br>$b = -1.43447 - 0.40397I$    | $4.65459 - 2.82623I$                  | 0          |
| $u = 0.499069 - 0.527627I$<br>$a = -0.88297 - 1.37264I$<br>$b = -1.43447 + 0.40397I$    | $4.65459 + 2.82623I$                  | 0          |
| $u = -1.161360 + 0.525226I$<br>$a = 0.754007 + 0.654124I$<br>$b = 0.688330 - 1.215040I$ | $-0.390599 + 1.111860I$               | 0          |
| $u = -1.161360 - 0.525226I$<br>$a = 0.754007 - 0.654124I$<br>$b = 0.688330 + 1.215040I$ | $-0.390599 - 1.111860I$               | 0          |
| $u = -0.608042 + 0.394118I$<br>$a = -1.44804 - 1.10655I$<br>$b = -1.46064 + 0.72845I$   | $3.98560 + 1.07651I$                  | 0          |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = -0.608042 - 0.394118I$<br>$a = -1.44804 + 1.10655I$<br>$b = -1.46064 - 0.72845I$    | $3.98560 - 1.07651I$                  | 0          |
| $u = 1.151370 + 0.560793I$<br>$a = -0.779456 + 0.840590I$<br>$b = -0.89795 - 2.16549I$   | $0.68066 - 8.67829I$                  | 0          |
| $u = 1.151370 - 0.560793I$<br>$a = -0.779456 - 0.840590I$<br>$b = -0.89795 + 2.16549I$   | $0.68066 + 8.67829I$                  | 0          |
| $u = -1.158310 + 0.565107I$<br>$a = 0.651043 - 0.728404I$<br>$b = -0.379605 + 0.088246I$ | $-2.91077 + 13.64960I$                | 0          |
| $u = -1.158310 - 0.565107I$<br>$a = 0.651043 + 0.728404I$<br>$b = -0.379605 - 0.088246I$ | $-2.91077 - 13.64960I$                | 0          |
| $u = -0.259853 + 1.266720I$<br>$a = 0.080496 + 0.743006I$<br>$b = 0.08175 - 1.53457I$    | $2.98324 + 4.47610I$                  | 0          |
| $u = -0.259853 - 1.266720I$<br>$a = 0.080496 - 0.743006I$<br>$b = 0.08175 + 1.53457I$    | $2.98324 - 4.47610I$                  | 0          |
| $u = -0.420304 + 1.229010I$<br>$a = 0.408093 + 0.560897I$<br>$b = 0.63897 - 1.98417I$    | $2.83986 + 2.69706I$                  | 0          |
| $u = -0.420304 - 1.229010I$<br>$a = 0.408093 - 0.560897I$<br>$b = 0.63897 + 1.98417I$    | $2.83986 - 2.69706I$                  | 0          |
| $u = 1.308170 + 0.087102I$<br>$a = -0.422502 - 0.416698I$<br>$b = 0.371850 + 0.107744I$  | $-7.93701 - 1.01267I$                 | 0          |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 1.308170 - 0.087102I$<br>$a = -0.422502 + 0.416698I$<br>$b = 0.371850 - 0.107744I$   | $-7.93701 + 1.01267I$                 | 0          |
| $u = 1.176760 + 0.579739I$<br>$a = 0.569992 + 0.583963I$<br>$b = -0.188102 - 0.147284I$   | $1.43457 - 7.87964I$                  | 0          |
| $u = 1.176760 - 0.579739I$<br>$a = 0.569992 - 0.583963I$<br>$b = -0.188102 + 0.147284I$   | $1.43457 + 7.87964I$                  | 0          |
| $u = 0.663821 + 0.163673I$<br>$a = 1.47918 + 0.96656I$<br>$b = 0.116724 - 1.086720I$      | $0.37077 + 3.23302I$                  | 0          |
| $u = 0.663821 - 0.163673I$<br>$a = 1.47918 - 0.96656I$<br>$b = 0.116724 + 1.086720I$      | $0.37077 - 3.23302I$                  | 0          |
| $u = 0.285135 + 0.610380I$<br>$a = 0.92416 - 1.60790I$<br>$b = -0.050637 + 0.924680I$     | $3.32659 + 0.00720I$                  | 0          |
| $u = 0.285135 - 0.610380I$<br>$a = 0.92416 + 1.60790I$<br>$b = -0.050637 - 0.924680I$     | $3.32659 - 0.00720I$                  | 0          |
| $u = 0.489942 + 1.238200I$<br>$a = 0.662960 - 0.648185I$<br>$b = 0.32328 + 1.65794I$      | $6.77832 + 6.88044I$                  | 0          |
| $u = 0.489942 - 1.238200I$<br>$a = 0.662960 + 0.648185I$<br>$b = 0.32328 - 1.65794I$      | $6.77832 - 6.88044I$                  | 0          |
| $u = -0.224321 + 0.627904I$<br>$a = -0.015286 - 0.524588I$<br>$b = -0.697858 - 0.367055I$ | $1.46936 + 3.06749I$                  | 0          |



| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape       |
|---|---------------------------------------|------------------|
| $u = -0.224321 - 0.627904I$<br>$a = -0.015286 + 0.524588I$<br>$b = -0.697858 + 0.367055I$ | $1.46936 - 3.06749I$                  | 0                |
| $u = -1.239430 + 0.548102I$<br>$a = 0.594663 + 0.527662I$<br>$b = 1.28662 - 1.99516I$     | $-0.44375 + 3.54352I$                 | 0                |
| $u = -1.239430 - 0.548102I$<br>$a = 0.594663 - 0.527662I$<br>$b = 1.28662 + 1.99516I$     | $-0.44375 - 3.54352I$                 | 0                |
| $u = 1.237470 + 0.568808I$<br>$a = -0.627057 + 0.775924I$<br>$b = -0.73911 - 1.78795I$    | $0.06510 - 9.48183I$                  | 0                |
| $u = 1.237470 - 0.568808I$<br>$a = -0.627057 - 0.775924I$<br>$b = -0.73911 + 1.78795I$    | $0.06510 + 9.48183I$                  | 0                |
| $u = -0.793060 + 1.121730I$<br>$a = -0.603634 - 0.489180I$<br>$b = -0.30687 + 1.65575I$   | $5.39327 + 0.10507I$                  | 0                |
| $u = -0.793060 - 1.121730I$<br>$a = -0.603634 + 0.489180I$<br>$b = -0.30687 - 1.65575I$   | $5.39327 - 0.10507I$                  | 0                |
| $u = 0.082693 + 0.619395I$<br>$a = 1.330360 - 0.139633I$<br>$b = -0.567613 + 0.202043I$   | $-1.43472 - 0.22373I$                 | $-6.30972 + 0.I$ |
| $u = 0.082693 - 0.619395I$<br>$a = 1.330360 + 0.139633I$<br>$b = -0.567613 - 0.202043I$   | $-1.43472 + 0.22373I$                 | $-6.30972 + 0.I$ |
| $u = -1.339410 + 0.321709I$<br>$a = 0.442287 - 0.111362I$<br>$b = 0.236354 + 0.185662I$   | $-1.88503 + 0.69044I$                 | 0                |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = -1.339410 - 0.321709I$<br>$a = 0.442287 + 0.111362I$<br>$b = 0.236354 - 0.185662I$   | $-1.88503 - 0.69044I$                 | 0                     |
| $u = -0.596396 + 0.171044I$<br>$a = 2.62171 - 0.18103I$<br>$b = 0.374303 + 0.234488I$     | $3.70485 - 2.31607I$                  | $8.00942 + 10.51133I$ |
| $u = -0.596396 - 0.171044I$<br>$a = 2.62171 + 0.18103I$<br>$b = 0.374303 - 0.234488I$     | $3.70485 + 2.31607I$                  | $8.00942 - 10.51133I$ |
| $u = -1.126100 + 0.806514I$<br>$a = -0.486449 - 0.786512I$<br>$b = -1.14253 + 1.78471I$   | $4.11605 + 6.88628I$                  | 0                     |
| $u = -1.126100 - 0.806514I$<br>$a = -0.486449 + 0.786512I$<br>$b = -1.14253 - 1.78471I$   | $4.11605 - 6.88628I$                  | 0                     |
| $u = -1.257770 + 0.586925I$<br>$a = -0.594375 - 0.866892I$<br>$b = -0.84456 + 1.64543I$   | $-4.2304 + 13.5113I$                  | 0                     |
| $u = -1.257770 - 0.586925I$<br>$a = -0.594375 + 0.866892I$<br>$b = -0.84456 - 1.64543I$   | $-4.2304 - 13.5113I$                  | 0                     |
| $u = -0.602834 + 0.059909I$<br>$a = 1.236460 - 0.344801I$<br>$b = 0.54829 + 2.39941I$     | $3.83155 + 1.06583I$                  | $-4.00000 + 2.27970I$ |
| $u = -0.602834 - 0.059909I$<br>$a = 1.236460 + 0.344801I$<br>$b = 0.54829 - 2.39941I$     | $3.83155 - 1.06583I$                  | $-4.00000 - 2.27970I$ |
| $u = -1.358310 + 0.338934I$<br>$a = -0.645718 + 0.311033I$<br>$b = -0.788077 - 0.481250I$ | $-2.67108 - 0.80743I$                 | 0                     |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = -1.358310 - 0.338934I$<br>$a = -0.645718 - 0.311033I$<br>$b = -0.788077 + 0.481250I$ | $-2.67108 + 0.80743I$                 | 0                     |
| $u = -1.41244 + 0.09773I$<br>$a = -0.540708 - 0.306582I$<br>$b = -0.025817 + 0.713256I$   | $-1.86249 + 2.87351I$                 | 0                     |
| $u = -1.41244 - 0.09773I$<br>$a = -0.540708 + 0.306582I$<br>$b = -0.025817 - 0.713256I$   | $-1.86249 - 2.87351I$                 | 0                     |
| $u = 1.37826 + 0.32789I$<br>$a = 0.455189 + 0.134338I$<br>$b = -0.486035 - 0.133376I$     | $-4.44501 - 6.89655I$                 | 0                     |
| $u = 1.37826 - 0.32789I$<br>$a = 0.455189 - 0.134338I$<br>$b = -0.486035 + 0.133376I$     | $-4.44501 + 6.89655I$                 | 0                     |
| $u = 1.22258 + 0.71942I$<br>$a = -0.621398 + 0.775987I$<br>$b = -1.07203 - 1.78504I$      | $2.89560 - 11.55240I$                 | 0                     |
| $u = 1.22258 - 0.71942I$<br>$a = -0.621398 - 0.775987I$<br>$b = -1.07203 + 1.78504I$      | $2.89560 + 11.55240I$                 | 0                     |
| $u = -1.25219 + 0.71084I$<br>$a = 0.543757 + 0.865900I$<br>$b = 1.04106 - 2.08031I$       | $0.1443 + 20.3788I$                   | 0                     |
| $u = -1.25219 - 0.71084I$<br>$a = 0.543757 - 0.865900I$<br>$b = 1.04106 + 2.08031I$       | $0.1443 - 20.3788I$                   | 0                     |
| $u = 0.534851 + 0.132966I$<br>$a = 1.121550 - 0.197616I$<br>$b = 0.35022 + 3.10796I$      | $-0.19642 + 6.85043I$                 | $-1.84550 + 2.67603I$ |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = 0.534851 - 0.132966I$<br>$a = 1.121550 + 0.197616I$<br>$b = 0.35022 - 3.10796I$  | $-0.19642 - 6.85043I$                 | $-1.84550 - 2.67603I$ |
| $u = -1.33846 + 0.58648I$<br>$a = -0.443468 - 0.617881I$<br>$b = -0.49859 + 1.62161I$ | $-2.08247 + 3.93238I$                 | 0                     |
| $u = -1.33846 - 0.58648I$<br>$a = -0.443468 + 0.617881I$<br>$b = -0.49859 - 1.62161I$ | $-2.08247 - 3.93238I$                 | 0                     |
| $u = 1.26749 + 0.74633I$<br>$a = 0.492857 - 0.802095I$<br>$b = 0.98971 + 2.07463I$    | $4.1866 - 13.8875I$                   | 0                     |
| $u = 1.26749 - 0.74633I$<br>$a = 0.492857 + 0.802095I$<br>$b = 0.98971 - 2.07463I$    | $4.1866 + 13.8875I$                   | 0                     |
| $u = 0.446362 + 0.272843I$<br>$a = 2.69827 - 1.07449I$<br>$b = 0.160409 + 0.341725I$  | $3.88766 + 0.27154I$                  | $5.15604 + 5.66364I$  |
| $u = 0.446362 - 0.272843I$<br>$a = 2.69827 + 1.07449I$<br>$b = 0.160409 - 0.341725I$  | $3.88766 - 0.27154I$                  | $5.15604 - 5.66364I$  |
| $u = -1.26094 + 0.77132I$<br>$a = 0.673439 - 0.161979I$<br>$b = 0.400369 - 0.223005I$ | $-2.70929 + 1.16729I$                 | 0                     |
| $u = -1.26094 - 0.77132I$<br>$a = 0.673439 + 0.161979I$<br>$b = 0.400369 + 0.223005I$ | $-2.70929 - 1.16729I$                 | 0                     |
| $u = -1.15098 + 1.00543I$<br>$a = 0.179396 + 0.754151I$<br>$b = 0.75282 - 2.03006I$   | $-1.98794 + 6.58061I$                 | 0                     |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -1.15098 - 1.00543I$<br>$a = 0.179396 - 0.754151I$<br>$b = 0.75282 + 2.03006I$    | $-1.98794 - 6.58061I$                 | 0                     |
| $u = 1.53401 + 0.01399I$<br>$a = -0.558959 - 0.287533I$<br>$b = -0.340586 + 0.213226I$ | $-4.77758 + 9.26085I$                 | 0                     |
| $u = 1.53401 - 0.01399I$<br>$a = -0.558959 + 0.287533I$<br>$b = -0.340586 - 0.213226I$ | $-4.77758 - 9.26085I$                 | 0                     |
| $u = 1.50727 + 0.33979I$<br>$a = 0.540012 + 0.063785I$<br>$b = 0.123494 + 0.461332I$   | $-6.33708 + 2.52064I$                 | 0                     |
| $u = 1.50727 - 0.33979I$<br>$a = 0.540012 - 0.063785I$<br>$b = 0.123494 - 0.461332I$   | $-6.33708 - 2.52064I$                 | 0                     |
| $u = -1.67875$<br>$a = 0.472938$<br>$b = 0.657377$                                     | $-2.97193$                            | 0                     |
| $u = -0.061501 + 0.315308I$<br>$a = 1.35388 - 0.54162I$<br>$b = -0.015852 - 0.379706I$ | $-0.235966 + 0.960167I$               | $-4.61956 - 6.69387I$ |
| $u = -0.061501 - 0.315308I$<br>$a = 1.35388 + 0.54162I$<br>$b = -0.015852 + 0.379706I$ | $-0.235966 - 0.960167I$               | $-4.61956 + 6.69387I$ |
| $u = 0.0646493 + 0.1162420I$<br>$a = 3.68249 + 3.57533I$<br>$b = 0.256926 + 1.011690I$ | $-4.19477 - 3.63377I$                 | $-8.37769 + 3.26370I$ |
| $u = 0.0646493 - 0.1162420I$<br>$a = 3.68249 - 3.57533I$<br>$b = 0.256926 - 1.011690I$ | $-4.19477 + 3.63377I$                 | $-8.37769 - 3.26370I$ |

II.

$$I_2^u = \langle 2.87 \times 10^{31} u^{46} + 1.05 \times 10^{32} u^{45} + \dots + 3.67 \times 10^{29} b - 6.08 \times 10^{31}, 1.01 \times 10^{31} u^{46} + 3.83 \times 10^{31} u^{45} + \dots + 3.67 \times 10^{29} a - 1.99 \times 10^{31}, u^{47} + 3u^{46} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -27.5820u^{46} - 104.181u^{45} + \dots - 10.2611u + 54.2683 \\ -78.2225u^{46} - 284.743u^{45} + \dots + 69.3825u + 165.536 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -61.0684u^{46} - 225.594u^{45} + \dots + 16.0079u + 118.904 \\ -57.7069u^{46} - 209.213u^{45} + \dots + 55.6453u + 121.855 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 22.2310u^{46} + 105.841u^{45} + \dots + 82.2805u - 32.9718 \\ -31.8947u^{46} - 116.935u^{45} + \dots + 36.4035u + 61.6576 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 63.1278u^{46} + 191.176u^{45} + \dots - 181.832u - 83.3637 \\ -72.8214u^{46} - 256.230u^{45} + \dots + 83.9789u + 131.849 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -9.66367u^{46} - 11.0936u^{45} + \dots + 118.684u + 28.6858 \\ -31.8947u^{46} - 116.935u^{45} + \dots + 36.4035u + 61.6576 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 34.6423u^{46} + 73.7290u^{45} + \dots - 214.273u + 46.3463 \\ 13.3562u^{46} + 39.7678u^{45} + \dots - 49.9386u - 16.3906 \end{pmatrix} \\ a_5 &= \begin{pmatrix} -118.148u^{46} - 397.924u^{45} + \dots + 145.219u + 33.4143 \\ -4.96398u^{46} - 13.6597u^{45} + \dots + 39.6336u + 18.8281 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 76.1492u^{46} + 228.217u^{45} + \dots - 231.378u + 35.4088 \\ -54.2807u^{46} - 200.494u^{45} + \dots + 20.5694u + 98.0489 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $517.085u^{46} + 1849.01u^{45} + \dots - 396.364u - 980.572$

(iv)  $u$ -Polynomials at the component

| Crossings | u-Polynomials at each crossing          |
|-----------|---|
| $c_1$     | $u^{47} - 3u^{46} + \dots - 11u^2 + 1$  |
| $c_2$     | $u^{47} - 14u^{45} + \dots + 4u + 1$    |
| $c_3$     | $u^{47} - 6u^{45} + \dots + 297u - 27$  |
| $c_4$     | $u^{47} - 18u^{45} + \dots + 2u + 1$    |
| $c_5$     | $u^{47} - u^{46} + \dots - 20u + 1$     |
| $c_6$     | $u^{47} + 15u^{44} + \dots + 178u - 13$ |
| $c_7$     | $u^{47} - 14u^{45} + \dots + 4u - 1$    |
| $c_8$     | $u^{47} - 3u^{46} + \dots - u - 1$      |
| $c_9$     | $u^{47} + 10u^{45} + \dots + 6u - 1$    |
| $c_{10}$  | $u^{47} - 18u^{45} + \dots + 2u - 1$    |
| $c_{11}$  | $u^{47} + 3u^{46} + \dots - u + 1$      |
| $c_{12}$  | $u^{47} + u^{46} + \dots - 20u - 1$     |





(v) Riley Polynomials at the component

| Crossings     | Riley Polynomials at each crossing         |
|---------------|--|
| $c_1$         | $y^{47} + 7y^{46} + \dots + 22y - 1$       |
| $c_2, c_7$    | $y^{47} - 28y^{46} + \dots + 36y - 1$      |
| $c_3$         | $y^{47} - 12y^{46} + \dots + 54837y - 729$ |
| $c_4, c_{10}$ | $y^{47} - 36y^{46} + \dots + 4y - 1$       |
| $c_5, c_{12}$ | $y^{47} + 43y^{46} + \dots + 76y - 1$      |
| $c_6$         | $y^{47} + 8y^{45} + \dots + 6490y - 169$   |
| $c_8, c_{11}$ | $y^{47} - 27y^{46} + \dots + 35y - 1$      |
| $c_9$         | $y^{47} + 20y^{46} + \dots - 16y - 1$      |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|--|---------------------------------------|------------------------|
| $u = -0.889937 + 0.430073I$<br>$a = 0.405900 + 1.090710I$<br>$b = -0.249732 - 1.338120I$ | $0.28405 + 4.81397I$                  | $-4.00000 - 6.94228I$  |
| $u = -0.889937 - 0.430073I$<br>$a = 0.405900 - 1.090710I$<br>$b = -0.249732 + 1.338120I$ | $0.28405 - 4.81397I$                  | $-4.00000 + 6.94228I$  |
| $u = 0.902904 + 0.320536I$<br>$a = 1.14702 + 0.96787I$<br>$b = -0.593652 + 0.229428I$    | $-5.10557 + 2.06707I$                 | $-11.08081 - 8.65643I$ |
| $u = 0.902904 - 0.320536I$<br>$a = 1.14702 - 0.96787I$<br>$b = -0.593652 - 0.229428I$    | $-5.10557 - 2.06707I$                 | $-11.08081 + 8.65643I$ |
| $u = 0.906781 + 0.289471I$<br>$a = -0.106618 - 1.163250I$<br>$b = 0.492570 + 1.136090I$  | $-5.05622 - 4.70892I$                 | $-13.0918 + 9.2301I$   |
| $u = 0.906781 - 0.289471I$<br>$a = -0.106618 + 1.163250I$<br>$b = 0.492570 - 1.136090I$  | $-5.05622 + 4.70892I$                 | $-13.0918 - 9.2301I$   |
| $u = 0.811557 + 0.469734I$<br>$a = 0.358509 - 1.070080I$<br>$b = 1.06125 + 1.69320I$     | $-4.71152 - 4.88182I$                 | $-10.09232 + 5.63767I$ |
| $u = 0.811557 - 0.469734I$<br>$a = 0.358509 + 1.070080I$<br>$b = 1.06125 - 1.69320I$     | $-4.71152 + 4.88182I$                 | $-10.09232 - 5.63767I$ |
| $u = -0.935762 + 0.528889I$<br>$a = -0.665153 - 0.391796I$<br>$b = 0.48565 + 2.06102I$   | $4.44804 + 2.04172I$                  | 0                      |
| $u = -0.935762 - 0.528889I$<br>$a = -0.665153 + 0.391796I$<br>$b = 0.48565 - 2.06102I$   | $4.44804 - 2.04172I$                  | 0                      |

| Solutions to $I_2^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = -0.450788 + 0.802899I$<br>$a = -0.462859 - 1.134600I$<br>$b = -0.885500 + 0.829356I$ | $5.93746 + 2.73605I$                  | $4.39597 - 4.05385I$ |
| $u = -0.450788 - 0.802899I$<br>$a = -0.462859 + 1.134600I$<br>$b = -0.885500 - 0.829356I$ | $5.93746 - 2.73605I$                  | $4.39597 + 4.05385I$ |
| $u = -1.083020 + 0.155939I$<br>$a = 0.725055 - 0.670192I$<br>$b = 0.185721 + 0.264913I$   | $-1.88772 - 1.80438I$                 | 0                    |
| $u = -1.083020 - 0.155939I$<br>$a = 0.725055 + 0.670192I$<br>$b = 0.185721 - 0.264913I$   | $-1.88772 + 1.80438I$                 | 0                    |
| $u = 0.065911 + 1.112560I$<br>$a = -0.272804 + 1.011100I$<br>$b = -0.04427 - 1.85749I$    | $4.03902 + 5.09451I$                  | 0                    |
| $u = 0.065911 - 1.112560I$<br>$a = -0.272804 - 1.011100I$<br>$b = -0.04427 + 1.85749I$    | $4.03902 - 5.09451I$                  | 0                    |
| $u = -0.501627 + 0.719259I$<br>$a = -0.580750 - 0.629272I$<br>$b = -0.27843 + 2.37718I$   | $4.45750 + 1.72614I$                  | $4.41580 - 2.99878I$ |
| $u = -0.501627 - 0.719259I$<br>$a = -0.580750 + 0.629272I$<br>$b = -0.27843 - 2.37718I$   | $4.45750 - 1.72614I$                  | $4.41580 + 2.99878I$ |
| $u = 1.094100 + 0.349905I$<br>$a = 0.740268 - 0.957578I$<br>$b = -0.091002 + 1.121130I$   | $1.80658 - 4.57967I$                  | 0                    |
| $u = 1.094100 - 0.349905I$<br>$a = 0.740268 + 0.957578I$<br>$b = -0.091002 - 1.121130I$   | $1.80658 + 4.57967I$                  | 0                    |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = -1.225190 + 0.113002I$ |                                       |                        |
| $a = 0.314375 + 0.453265I$  | $-2.10893 + 1.93292I$                 | 0                      |
| $b = 0.225773 - 0.714056I$  |                                       |                        |
| $u = -1.225190 - 0.113002I$ |                                       |                        |
| $a = 0.314375 - 0.453265I$  | $-2.10893 - 1.93292I$                 | 0                      |
| $b = 0.225773 + 0.714056I$  |                                       |                        |
| $u = 0.712750 + 0.203668I$  |                                       |                        |
| $a = 2.14518 + 0.08588I$    | $3.42656 + 2.09756I$                  | $-10.94235 + 4.10081I$ |
| $b = 0.839109 + 0.056598I$  |                                       |                        |
| $u = 0.712750 - 0.203668I$  |                                       |                        |
| $a = 2.14518 - 0.08588I$    | $3.42656 - 2.09756I$                  | $-10.94235 - 4.10081I$ |
| $b = 0.839109 - 0.056598I$  |                                       |                        |
| $u = 1.156770 + 0.531285I$  |                                       |                        |
| $a = -0.845915 + 0.797237I$ | $0.69570 - 10.11660I$                 | 0                      |
| $b = -1.03486 - 2.08640I$   |                                       |                        |
| $u = 1.156770 - 0.531285I$  |                                       |                        |
| $a = -0.845915 - 0.797237I$ | $0.69570 + 10.11660I$                 | 0                      |
| $b = -1.03486 + 2.08640I$   |                                       |                        |
| $u = -1.174330 + 0.572544I$ |                                       |                        |
| $a = 0.525061 + 0.518322I$  | $-1.24471 + 2.44194I$                 | 0                      |
| $b = 0.77309 - 1.55639I$    |                                       |                        |
| $u = -1.174330 - 0.572544I$ |                                       |                        |
| $a = 0.525061 - 0.518322I$  | $-1.24471 - 2.44194I$                 | 0                      |
| $b = 0.77309 + 1.55639I$    |                                       |                        |
| $u = -0.303390 + 1.280700I$ |                                       |                        |
| $a = 0.261705 + 0.514561I$  | $2.42673 + 3.32756I$                  | 0                      |
| $b = 0.57083 - 1.47279I$    |                                       |                        |
| $u = -0.303390 - 1.280700I$ |                                       |                        |
| $a = 0.261705 - 0.514561I$  | $2.42673 - 3.32756I$                  | 0                      |
| $b = 0.57083 + 1.47279I$    |                                       |                        |

| Solutions to $I_2^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = 1.328530 + 0.239810I$<br>$a = 0.341531 + 0.141402I$<br>$b = 0.259510 + 0.741575I$  | $-6.74158 + 1.85994I$                 | 0                     |
| $u = 1.328530 - 0.239810I$<br>$a = 0.341531 - 0.141402I$<br>$b = 0.259510 - 0.741575I$  | $-6.74158 - 1.85994I$                 | 0                     |
| $u = 1.361130 + 0.214761I$<br>$a = -0.297328 + 0.050725I$<br>$b = 0.060166 + 0.773436I$ | $-4.25106 - 7.64066I$                 | 0                     |
| $u = 1.361130 - 0.214761I$<br>$a = -0.297328 - 0.050725I$<br>$b = 0.060166 - 0.773436I$ | $-4.25106 + 7.64066I$                 | 0                     |
| $u = -0.600452 + 0.038623I$<br>$a = 2.41464 - 0.22924I$<br>$b = 0.977092 + 0.316977I$   | $3.35221 - 0.49367I$                  | $-9.49194 - 1.07798I$ |
| $u = -0.600452 - 0.038623I$<br>$a = 2.41464 + 0.22924I$<br>$b = 0.977092 - 0.316977I$   | $3.35221 + 0.49367I$                  | $-9.49194 + 1.07798I$ |
| $u = -1.066250 + 0.905397I$<br>$a = -0.205456 - 0.860858I$<br>$b = -0.84168 + 1.96246I$ | $-1.71287 + 6.36824I$                 | 0                     |
| $u = -1.066250 - 0.905397I$<br>$a = -0.205456 + 0.860858I$<br>$b = -0.84168 - 1.96246I$ | $-1.71287 - 6.36824I$                 | 0                     |
| $u = 0.570676 + 0.141826I$<br>$a = -0.854767 + 0.698128I$<br>$b = 0.11697 - 3.13616I$   | $-0.33740 - 7.25565I$                 | $-8.2236 + 14.6599I$  |
| $u = 0.570676 - 0.141826I$<br>$a = -0.854767 - 0.698128I$<br>$b = 0.11697 + 3.13616I$   | $-0.33740 + 7.25565I$                 | $-8.2236 - 14.6599I$  |

| Solutions to $I_2^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = -0.511816 + 0.218214I$<br>$a = -1.97577 - 1.00397I$<br>$b = -1.45878 - 0.53097I$   | $6.22975 + 2.31382I$                  | $2.39074 - 3.00194I$  |
| $u = -0.511816 - 0.218214I$<br>$a = -1.97577 + 1.00397I$<br>$b = -1.45878 + 0.53097I$   | $6.22975 - 2.31382I$                  | $2.39074 + 3.00194I$  |
| $u = -1.31030 + 0.63554I$<br>$a = -0.605765 + 0.229474I$<br>$b = -0.265858 - 0.061072I$ | $-2.81336 + 0.83183I$                 | 0                     |
| $u = -1.31030 - 0.63554I$<br>$a = -0.605765 - 0.229474I$<br>$b = -0.265858 + 0.061072I$ | $-2.81336 - 0.83183I$                 | 0                     |
| $u = 0.475870 + 0.171647I$<br>$a = -2.73580 + 0.77197I$<br>$b = -0.67721 - 1.52174I$    | $3.70241 + 6.31816I$                  | $-2.22797 - 7.95729I$ |
| $u = 0.475870 - 0.171647I$<br>$a = -2.73580 - 0.77197I$<br>$b = -0.67721 + 1.52174I$    | $3.70241 - 6.31816I$                  | $-2.22797 + 7.95729I$ |
| $u = -1.66828$<br>$a = 0.459483$<br>$b = 0.746478$                                      | -3.09044                              | 0                     |

### III. u-Polynomials

| Crossings | u-Polynomials at each crossing  |
|-----------|---|
| $c_1$     | $(u^{47} - 3u^{46} + \dots - 11u^2 + 1)(u^{170} - 14u^{169} + \dots + 18u - 1)$                         |
| $c_2$     | $(u^{47} - 14u^{45} + \dots + 4u + 1)(u^{170} + u^{169} + \dots - 42944u + 1984)$                       |
| $c_3$     | $(u^{47} - 6u^{45} + \dots + 297u - 27)$<br>$\cdot (u^{170} - u^{169} + \dots - 276535005u - 23926117)$ |
| $c_4$     | $(u^{47} - 18u^{45} + \dots + 2u + 1)(u^{170} + u^{169} + \dots + 60040u - 6379)$                       |
| $c_5$     | $(u^{47} - u^{46} + \dots - 20u + 1)(u^{170} + 2u^{169} + \dots + 6420u - 35591)$                       |
| $c_6$     | $(u^{47} + 15u^{44} + \dots + 178u - 13)$<br>$\cdot (u^{170} - u^{169} + \dots + 9130974u + 5572759)$   |
| $c_7$     | $(u^{47} - 14u^{45} + \dots + 4u - 1)(u^{170} + u^{169} + \dots - 42944u + 1984)$                       |
| $c_8$     | $(u^{47} - 3u^{46} + \dots - u - 1)(u^{170} + 8u^{169} + \dots - 715u + 221)$                           |
| $c_9$     | $(u^{47} + 10u^{45} + \dots + 6u - 1)(u^{170} + 3u^{169} + \dots + 811454u + 271819)$                   |
| $c_{10}$  | $(u^{47} - 18u^{45} + \dots + 2u - 1)(u^{170} + u^{169} + \dots + 60040u - 6379)$                       |
| $c_{11}$  | $(u^{47} + 3u^{46} + \dots - u + 1)(u^{170} + 8u^{169} + \dots - 715u + 221)$                           |
| $c_{12}$  | $(u^{47} + u^{46} + \dots - 20u - 1)(u^{170} + 2u^{169} + \dots + 6420u - 35591)$                       |



#### IV. Riley Polynomials

| Crossings     | Riley Polynomials at each crossing   |
|---------------|--|
| $c_1$         | $(y^{47} + 7y^{46} + \dots + 22y - 1)(y^{170} + 6y^{169} + \dots - 760y + 1)$  |
| $c_2, c_7$    | $(y^{47} - 28y^{46} + \dots + 36y - 1)$<br>$\cdot (y^{170} - 93y^{169} + \dots - 827236352y + 3936256)$                      |
| $c_3$         | $(y^{47} - 12y^{46} + \dots + 54837y - 729)$<br>$\cdot (y^{170} - 41y^{169} + \dots - 46800698030178335y + 572459074697689)$ |
| $c_4, c_{10}$ | $(y^{47} - 36y^{46} + \dots + 4y - 1)$<br>$\cdot (y^{170} - 113y^{169} + \dots - 1618495822y + 40691641)$                    |
| $c_5, c_{12}$ | $(y^{47} + 43y^{46} + \dots + 76y - 1)$<br>$\cdot (y^{170} + 118y^{169} + \dots + 25027873906y + 1266719281)$                |
| $c_6$         | $(y^{47} + 8y^{45} + \dots + 6490y - 169)$<br>$\cdot (y^{170} - 9y^{169} + \dots + 1788240547802984y + 31055642872081)$      |
| $c_8, c_{11}$ | $(y^{47} - 27y^{46} + \dots + 35y - 1)$<br>$\cdot (y^{170} - 88y^{169} + \dots + 1304511y + 48841)$                          |
| $c_9$         | $(y^{47} + 20y^{46} + \dots - 16y - 1)$<br>$\cdot (y^{170} + 43y^{169} + \dots + 6707969409918y + 73885568761)$              |