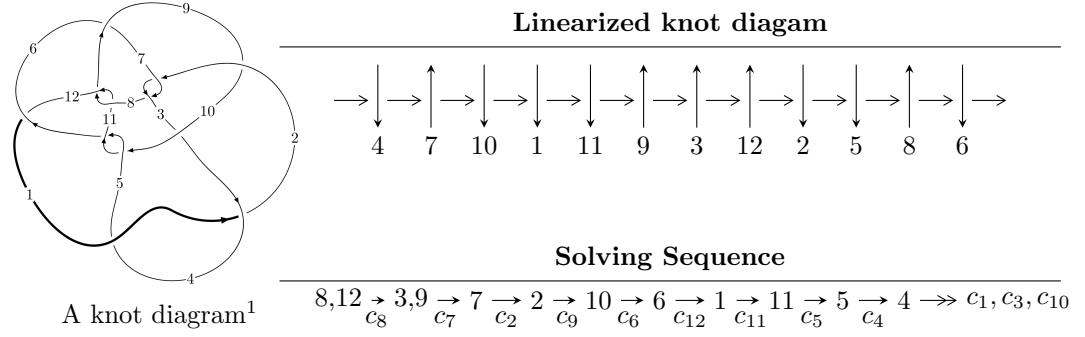


$12a_{1091}$  ( $K12a_{1091}$ )



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -6.39310 \times 10^{837} u^{160} + 4.58819 \times 10^{837} u^{159} + \dots + 1.25873 \times 10^{837} b + 1.99542 \times 10^{842}, \\ 1.45185 \times 10^{842} u^{160} - 7.32509 \times 10^{841} u^{159} + \dots + 2.86374 \times 10^{841} a - 5.38127 \times 10^{846}, \\ u^{161} - 43u^{159} + \dots + 23192u - 22751 \rangle$$

$$I_2^u = \langle -1.30052 \times 10^{27} u^{42} + 5.58534 \times 10^{27} u^{41} + \dots + 5.17611 \times 10^{24} b - 1.73362 \times 10^{27}, \\ - 5.05339 \times 10^{27} u^{42} + 2.24625 \times 10^{28} u^{41} + \dots + 5.17611 \times 10^{24} a - 8.77138 \times 10^{27}, u^{43} - 5u^{42} + \dots + 9u - \dots \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 204 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -6.39 \times 10^{837} u^{160} + 4.59 \times 10^{837} u^{159} + \dots + 1.26 \times 10^{837} b + 2.00 \times 10^{842}, 1.45 \times 10^{842} u^{160} - 7.33 \times 10^{841} u^{159} + \dots + 2.86 \times 10^{841} a - 5.38 \times 10^{846}, u^{161} - 43u^{159} + \dots + 23192u - 22751 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -5.06979u^{160} + 2.55788u^{159} + \dots - 468625.u + 187911. \\ 5.07901u^{160} - 3.64509u^{159} + \dots + 375636.u - 158527. \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 10.6826u^{160} - 9.77082u^{159} + \dots + 576831.u - 269285. \\ -24.6702u^{160} + 21.3731u^{159} + \dots - 1.39803 \times 10^6 u + 645587. \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1.12700u^{160} - 6.54266u^{159} + \dots - 510744.u + 142501. \\ 1.25989u^{160} + 0.372663u^{159} + \dots + 244271.u - 82982.0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -80.0417u^{160} + 75.0777u^{159} + \dots - 4.05107 \times 10^6 u + 1.94173 \times 10^6 \\ 28.1384u^{160} - 23.4524u^{159} + \dots + 1.66699 \times 10^6 u - 759659. \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 26.3009u^{160} - 22.6628u^{159} + \dots + 1.50521 \times 10^6 u - 692577. \\ -35.0998u^{160} + 29.6020u^{159} + \dots - 2.05235 \times 10^6 u + 938893. \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 74.7417u^{160} - 62.5278u^{159} + \dots + 4.47416 \times 10^6 u - 2.02663 \times 10^6 \\ -45.8026u^{160} + 37.7780u^{159} + \dots - 2.80124 \times 10^6 u + 1.25943 \times 10^6 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 21.0485u^{160} - 18.9227u^{159} + \dots + 1.14409 \times 10^6 u - 534703. \\ -29.8474u^{160} + 25.8619u^{159} + \dots - 1.69123 \times 10^6 u + 781019. \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -23.3510u^{160} + 15.7838u^{159} + \dots - 1.78107 \times 10^6 u + 747855. \\ -11.4670u^{160} + 12.3883u^{159} + \dots - 382645.u + 221297. \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -357.352u^{160} + 338.730u^{159} + \dots - 1.76787 \times 10^7 u + 8.55098 \times 10^6$$

**(iv) u-Polynomials at the component**

| Crossings     | u-Polynomials at each crossing                              |
|---------------|---|
| $c_1, c_4$    | $u^{161} - 6u^{160} + \cdots - 60405u + 2525$               |
| $c_2, c_7$    | $u^{161} + u^{160} + \cdots + 62875u + 20690$               |
| $c_3$         | $u^{161} + u^{160} + \cdots + 6424407u - 1081037$           |
| $c_5, c_{10}$ | $u^{161} - 5u^{160} + \cdots - 34377u - 24287$              |
| $c_6$         | $u^{161} + 4u^{160} + \cdots + 209706558586u + 17633051719$ |
| $c_8, c_{11}$ | $u^{161} - 43u^{159} + \cdots + 23192u + 22751$             |
| $c_9$         | $u^{161} + 5u^{160} + \cdots + 5900566245u - 806431049$     |
| $c_{12}$      | $u^{161} + 2u^{160} + \cdots + 297854463u - 20528044$       |

**(v) Riley Polynomials at the component**

| Crossings     | Riley Polynomials at each crossing   |
|---------------|--|
| $c_1, c_4$    | $y^{161} + 104y^{160} + \dots - 44901925y - 6375625$                       |
| $c_2, c_7$    | $y^{161} - 95y^{160} + \dots + 56848574785y - 428076100$                   |
| $c_3$         | $y^{161} + 13y^{160} + \dots - 81817610068445y - 1168640995369$            |
| $c_5, c_{10}$ | $y^{161} - 71y^{160} + \dots - 8324930855y - 589858369$                    |
| $c_6$         | $y^{161} - 44y^{160} + \dots + 4.98 \times 10^{21}y - 3.11 \times 10^{20}$ |
| $c_8, c_{11}$ | $y^{161} - 86y^{160} + \dots + 30379536528y - 517608001$                   |
| $c_9$         | $y^{161} + 29y^{160} + \dots - 3.95 \times 10^{19}y - 6.50 \times 10^{17}$ |
| $c_{12}$      | $y^{161} + 36y^{160} + \dots - 326855592628287y - 421400590465936$         |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.950374 + 0.325702I$ |                                       |            |
| $a = 0.393996 - 0.385326I$  | $1.60788 - 1.20779I$                  | 0          |
| $b = 0.169698 + 0.056372I$  |                                       |            |
| $u = -0.950374 - 0.325702I$ |                                       |            |
| $a = 0.393996 + 0.385326I$  | $1.60788 + 1.20779I$                  | 0          |
| $b = 0.169698 - 0.056372I$  |                                       |            |
| $u = -0.072510 + 0.991759I$ |                                       |            |
| $a = -0.559105 - 0.563435I$ | $6.47296 - 7.82720I$                  | 0          |
| $b = 1.205640 - 0.484119I$  |                                       |            |
| $u = -0.072510 - 0.991759I$ |                                       |            |
| $a = -0.559105 + 0.563435I$ | $6.47296 + 7.82720I$                  | 0          |
| $b = 1.205640 + 0.484119I$  |                                       |            |
| $u = -0.993352 + 0.197972I$ |                                       |            |
| $a = 2.56889 + 0.55840I$    | $0.61248 - 4.81440I$                  | 0          |
| $b = -1.30419 + 0.69007I$   |                                       |            |
| $u = -0.993352 - 0.197972I$ |                                       |            |
| $a = 2.56889 - 0.55840I$    | $0.61248 + 4.81440I$                  | 0          |
| $b = -1.30419 - 0.69007I$   |                                       |            |
| $u = 0.902874 + 0.463441I$  |                                       |            |
| $a = 1.336050 - 0.193210I$  | $-0.08463 + 5.13600I$                 | 0          |
| $b = -0.871684 - 0.901749I$ |                                       |            |
| $u = 0.902874 - 0.463441I$  |                                       |            |
| $a = 1.336050 + 0.193210I$  | $-0.08463 - 5.13600I$                 | 0          |
| $b = -0.871684 + 0.901749I$ |                                       |            |
| $u = -0.955013 + 0.229039I$ |                                       |            |
| $a = -2.93997 - 0.42458I$   | $3.79930 - 8.84455I$                  | 0          |
| $b = 1.50313 - 0.49893I$    |                                       |            |
| $u = -0.955013 - 0.229039I$ |                                       |            |
| $a = -2.93997 + 0.42458I$   | $3.79930 + 8.84455I$                  | 0          |
| $b = 1.50313 + 0.49893I$    |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.173656 + 0.965528I$ |                                       |            |
| $a = 0.467423 + 0.277205I$  | $1.90577 - 4.13490I$                  | 0          |
| $b = -1.156730 + 0.326183I$ |                                       |            |
| $u = -0.173656 - 0.965528I$ |                                       |            |
| $a = 0.467423 - 0.277205I$  | $1.90577 + 4.13490I$                  | 0          |
| $b = -1.156730 - 0.326183I$ |                                       |            |
| $u = 0.363651 + 0.909552I$  |                                       |            |
| $a = 0.282299 - 0.406949I$  | $-1.77610 - 2.50851I$                 | 0          |
| $b = -0.623074 - 0.340925I$ |                                       |            |
| $u = 0.363651 - 0.909552I$  |                                       |            |
| $a = 0.282299 + 0.406949I$  | $-1.77610 + 2.50851I$                 | 0          |
| $b = -0.623074 + 0.340925I$ |                                       |            |
| $u = -0.133671 + 0.967135I$ |                                       |            |
| $a = 0.363269 + 0.968622I$  | $-0.48025 + 8.06330I$                 | 0          |
| $b = -0.060760 + 1.024230I$ |                                       |            |
| $u = -0.133671 - 0.967135I$ |                                       |            |
| $a = 0.363269 - 0.968622I$  | $-0.48025 - 8.06330I$                 | 0          |
| $b = -0.060760 - 1.024230I$ |                                       |            |
| $u = -0.923789 + 0.443969I$ |                                       |            |
| $a = 0.26507 + 1.48143I$    | $4.76381 + 0.13098I$                  | 0          |
| $b = -0.951484 - 0.034762I$ |                                       |            |
| $u = -0.923789 - 0.443969I$ |                                       |            |
| $a = 0.26507 - 1.48143I$    | $4.76381 - 0.13098I$                  | 0          |
| $b = -0.951484 + 0.034762I$ |                                       |            |
| $u = 0.794847 + 0.656611I$  |                                       |            |
| $a = 0.210662 + 0.974229I$  | $6.86027 + 2.36778I$                  | 0          |
| $b = -0.875222 + 0.010488I$ |                                       |            |
| $u = 0.794847 - 0.656611I$  |                                       |            |
| $a = 0.210662 - 0.974229I$  | $6.86027 - 2.36778I$                  | 0          |
| $b = -0.875222 - 0.010488I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.990904 + 0.328079I$  |                                       |            |
| $a = 0.276707 + 0.562545I$  | $-2.70689 + 1.93033I$                 | 0          |
| $b = -0.696982 + 0.658755I$ |                                       |            |
| $u = 0.990904 - 0.328079I$  |                                       |            |
| $a = 0.276707 - 0.562545I$  | $-2.70689 - 1.93033I$                 | 0          |
| $b = -0.696982 - 0.658755I$ |                                       |            |
| $u = 0.955110 + 0.432923I$  |                                       |            |
| $a = -0.730781 - 0.042302I$ | $0.31187 + 3.75114I$                  | 0          |
| $b = 0.519570 + 0.834793I$  |                                       |            |
| $u = 0.955110 - 0.432923I$  |                                       |            |
| $a = -0.730781 + 0.042302I$ | $0.31187 - 3.75114I$                  | 0          |
| $b = 0.519570 - 0.834793I$  |                                       |            |
| $u = 1.023370 + 0.258291I$  |                                       |            |
| $a = -0.437416 - 1.185920I$ | $1.01774 + 6.80120I$                  | 0          |
| $b = 0.685995 - 0.525139I$  |                                       |            |
| $u = 1.023370 - 0.258291I$  |                                       |            |
| $a = -0.437416 + 1.185920I$ | $1.01774 - 6.80120I$                  | 0          |
| $b = 0.685995 + 0.525139I$  |                                       |            |
| $u = 0.836063 + 0.420493I$  |                                       |            |
| $a = -1.70373 + 0.81945I$   | $1.31743 + 5.01058I$                  | 0          |
| $b = 0.969989 + 0.648626I$  |                                       |            |
| $u = 0.836063 - 0.420493I$  |                                       |            |
| $a = -1.70373 - 0.81945I$   | $1.31743 - 5.01058I$                  | 0          |
| $b = 0.969989 - 0.648626I$  |                                       |            |
| $u = 0.633559 + 0.685378I$  |                                       |            |
| $a = -0.527296 - 0.412378I$ | $-3.10634 - 1.77812I$                 | 0          |
| $b = -0.933157 + 0.296491I$ |                                       |            |
| $u = 0.633559 - 0.685378I$  |                                       |            |
| $a = -0.527296 + 0.412378I$ | $-3.10634 + 1.77812I$                 | 0          |
| $b = -0.933157 - 0.296491I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.048950 + 0.218293I$ | $-1.32350 - 3.70585I$                 | 0          |
| $a = 1.050050 + 0.088161I$  |                                       |            |
| $b = -0.710613 + 1.195320I$ |                                       |            |
| $u = -1.048950 - 0.218293I$ | $-1.32350 + 3.70585I$                 | 0          |
| $a = 1.050050 - 0.088161I$  |                                       |            |
| $b = -0.710613 - 1.195320I$ |                                       |            |
| $u = -0.926103 + 0.043767I$ | $3.09316 - 2.11983I$                  | 0          |
| $a = -2.15843 + 4.41436I$   |                                       |            |
| $b = -0.854807 + 0.525279I$ |                                       |            |
| $u = -0.926103 - 0.043767I$ | $3.09316 + 2.11983I$                  | 0          |
| $a = -2.15843 - 4.41436I$   |                                       |            |
| $b = -0.854807 - 0.525279I$ |                                       |            |
| $u = -1.066240 + 0.148110I$ | $3.77843 - 2.44545I$                  | 0          |
| $a = -3.43481 - 1.07592I$   |                                       |            |
| $b = 1.010390 - 0.473750I$  |                                       |            |
| $u = -1.066240 - 0.148110I$ | $3.77843 + 2.44545I$                  | 0          |
| $a = -3.43481 + 1.07592I$   |                                       |            |
| $b = 1.010390 + 0.473750I$  |                                       |            |
| $u = 0.944602 + 0.520467I$  | $1.82846 + 10.45490I$                 | 0          |
| $a = 0.167943 + 1.200010I$  |                                       |            |
| $b = 0.965227 + 0.370418I$  |                                       |            |
| $u = 0.944602 - 0.520467I$  | $1.82846 - 10.45490I$                 | 0          |
| $a = 0.167943 - 1.200010I$  |                                       |            |
| $b = 0.965227 - 0.370418I$  |                                       |            |
| $u = 0.946178 + 0.536677I$  | $-2.15295 + 6.49551I$                 | 0          |
| $a = 0.370509 - 0.948938I$  |                                       |            |
| $b = -0.880008 - 0.511022I$ |                                       |            |
| $u = 0.946178 - 0.536677I$  | $-2.15295 - 6.49551I$                 | 0          |
| $a = 0.370509 + 0.948938I$  |                                       |            |
| $b = -0.880008 + 0.511022I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.662436 + 0.623903I$  |                                       |            |
| $a = 1.028290 + 0.834059I$  | $0.96205 - 5.94168I$                  | 0          |
| $b = 1.059350 - 0.145601I$  |                                       |            |
| $u = 0.662436 - 0.623903I$  |                                       |            |
| $a = 1.028290 - 0.834059I$  | $0.96205 + 5.94168I$                  | 0          |
| $b = 1.059350 + 0.145601I$  |                                       |            |
| $u = -1.087020 + 0.168140I$ |                                       |            |
| $a = 0.436478 + 0.788002I$  | $3.59860 + 0.07650I$                  | 0          |
| $b = -0.183843 + 0.032853I$ |                                       |            |
| $u = -1.087020 - 0.168140I$ |                                       |            |
| $a = 0.436478 - 0.788002I$  | $3.59860 - 0.07650I$                  | 0          |
| $b = -0.183843 - 0.032853I$ |                                       |            |
| $u = -1.049320 + 0.371160I$ |                                       |            |
| $a = -0.222543 - 0.140301I$ | $-0.000052 + 0.961895I$               | 0          |
| $b = 0.202947 - 0.964642I$  |                                       |            |
| $u = -1.049320 - 0.371160I$ |                                       |            |
| $a = -0.222543 + 0.140301I$ | $-0.000052 - 0.961895I$               | 0          |
| $b = 0.202947 + 0.964642I$  |                                       |            |
| $u = -0.875918 + 0.103730I$ |                                       |            |
| $a = 2.03283 - 1.31093I$    | $3.04543 + 1.62804I$                  | 0          |
| $b = 0.799114 + 0.511328I$  |                                       |            |
| $u = -0.875918 - 0.103730I$ |                                       |            |
| $a = 2.03283 + 1.31093I$    | $3.04543 - 1.62804I$                  | 0          |
| $b = 0.799114 - 0.511328I$  |                                       |            |
| $u = -0.841656 + 0.044934I$ |                                       |            |
| $a = 0.16926 + 1.84266I$    | $-2.50794 + 2.48803I$                 | 0          |
| $b = -0.38662 - 1.39931I$   |                                       |            |
| $u = -0.841656 - 0.044934I$ |                                       |            |
| $a = 0.16926 - 1.84266I$    | $-2.50794 - 2.48803I$                 | 0          |
| $b = -0.38662 + 1.39931I$   |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.796866 + 0.244137I$ |                                       |            |
| $a = -1.061210 + 0.068995I$ | $3.30258 + 6.67390I$                  | 0          |
| $b = 1.257450 + 0.612779I$  |                                       |            |
| $u = -0.796866 - 0.244137I$ |                                       |            |
| $a = -1.061210 - 0.068995I$ | $3.30258 - 6.67390I$                  | 0          |
| $b = 1.257450 - 0.612779I$  |                                       |            |
| $u = 0.814659 + 0.159634I$  |                                       |            |
| $a = -0.871559 + 0.272351I$ | $0.94128 - 1.98249I$                  | 0          |
| $b = 0.807308 - 0.821539I$  |                                       |            |
| $u = 0.814659 - 0.159634I$  |                                       |            |
| $a = -0.871559 - 0.272351I$ | $0.94128 + 1.98249I$                  | 0          |
| $b = 0.807308 + 0.821539I$  |                                       |            |
| $u = 0.252024 + 1.147930I$  |                                       |            |
| $a = -0.038822 - 0.459122I$ | $3.97747 + 2.64873I$                  | 0          |
| $b = 1.39368 - 0.48426I$    |                                       |            |
| $u = 0.252024 - 1.147930I$  |                                       |            |
| $a = -0.038822 + 0.459122I$ | $3.97747 - 2.64873I$                  | 0          |
| $b = 1.39368 + 0.48426I$    |                                       |            |
| $u = -1.114150 + 0.402874I$ |                                       |            |
| $a = 2.58183 + 1.28478I$    | $9.37549 - 4.01193I$                  | 0          |
| $b = -1.226860 + 0.255437I$ |                                       |            |
| $u = -1.114150 - 0.402874I$ |                                       |            |
| $a = 2.58183 - 1.28478I$    | $9.37549 + 4.01193I$                  | 0          |
| $b = -1.226860 - 0.255437I$ |                                       |            |
| $u = -0.791974 + 0.157432I$ |                                       |            |
| $a = 0.265101 + 0.320836I$  | $-0.11674 + 3.08623I$                 | 0          |
| $b = -1.030410 - 0.730490I$ |                                       |            |
| $u = -0.791974 - 0.157432I$ |                                       |            |
| $a = 0.265101 - 0.320836I$  | $-0.11674 - 3.08623I$                 | 0          |
| $b = -1.030410 + 0.730490I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.014317 + 0.799111I$  |                                       |            |
| $a = -0.676822 + 0.294373I$ | $4.16113 - 3.92910I$                  | 0          |
| $b = 1.241560 - 0.201321I$  |                                       |            |
| $u = 0.014317 - 0.799111I$  |                                       |            |
| $a = -0.676822 - 0.294373I$ | $4.16113 + 3.92910I$                  | 0          |
| $b = 1.241560 + 0.201321I$  |                                       |            |
| $u = -1.097850 + 0.496437I$ |                                       |            |
| $a = -0.808536 - 0.037056I$ | $6.15852 - 1.21053I$                  | 0          |
| $b = -0.169521 - 0.579602I$ |                                       |            |
| $u = -1.097850 - 0.496437I$ |                                       |            |
| $a = -0.808536 + 0.037056I$ | $6.15852 + 1.21053I$                  | 0          |
| $b = -0.169521 + 0.579602I$ |                                       |            |
| $u = 0.033762 + 0.791489I$  |                                       |            |
| $a = -0.79759 - 1.72609I$   | $-5.45941 + 1.36823I$                 | 0          |
| $b = -0.117292 - 0.771044I$ |                                       |            |
| $u = 0.033762 - 0.791489I$  |                                       |            |
| $a = -0.79759 + 1.72609I$   | $-5.45941 - 1.36823I$                 | 0          |
| $b = -0.117292 + 0.771044I$ |                                       |            |
| $u = 0.785570 + 0.051564I$  |                                       |            |
| $a = -4.81959 - 0.73771I$   | $-0.30806 - 5.16477I$                 | 0          |
| $b = 0.828167 - 0.031471I$  |                                       |            |
| $u = 0.785570 - 0.051564I$  |                                       |            |
| $a = -4.81959 + 0.73771I$   | $-0.30806 + 5.16477I$                 | 0          |
| $b = 0.828167 + 0.031471I$  |                                       |            |
| $u = -1.184560 + 0.266383I$ |                                       |            |
| $a = -2.57917 - 0.56752I$   | $4.24337 - 3.13114I$                  | 0          |
| $b = 1.106790 - 0.256566I$  |                                       |            |
| $u = -1.184560 - 0.266383I$ |                                       |            |
| $a = -2.57917 + 0.56752I$   | $4.24337 + 3.13114I$                  | 0          |
| $b = 1.106790 + 0.256566I$  |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.275379 + 1.183100I$ |                                       |            |
| $a = 0.367775 - 0.409936I$  | $3.41290 + 13.66070I$                 | 0          |
| $b = -1.31774 - 0.54177I$   |                                       |            |
| $u = -0.275379 - 1.183100I$ |                                       |            |
| $a = 0.367775 + 0.409936I$  | $3.41290 - 13.66070I$                 | 0          |
| $b = -1.31774 + 0.54177I$   |                                       |            |
| $u = 0.784212$              |                                       |            |
| $a = 4.93069$               | -4.42162                              | 0          |
| $b = -0.828307$             |                                       |            |
| $u = 1.194880 + 0.268287I$  |                                       |            |
| $a = -0.356072 - 0.444064I$ | $1.95698 + 3.36078I$                  | 0          |
| $b = 0.014716 + 1.171310I$  |                                       |            |
| $u = 1.194880 - 0.268287I$  |                                       |            |
| $a = -0.356072 + 0.444064I$ | $1.95698 - 3.36078I$                  | 0          |
| $b = 0.014716 - 1.171310I$  |                                       |            |
| $u = 0.750525 + 0.971488I$  |                                       |            |
| $a = -0.423895 + 0.819516I$ | -1.87142 + 1.91362I                   | 0          |
| $b = 0.889804 + 0.129233I$  |                                       |            |
| $u = 0.750525 - 0.971488I$  |                                       |            |
| $a = -0.423895 - 0.819516I$ | -1.87142 - 1.91362I                   | 0          |
| $b = 0.889804 - 0.129233I$  |                                       |            |
| $u = -0.249738 + 0.717625I$ |                                       |            |
| $a = 1.70201 + 0.75465I$    | -2.54043 - 4.81653I                   | 0          |
| $b = -0.143646 + 0.490394I$ |                                       |            |
| $u = -0.249738 - 0.717625I$ |                                       |            |
| $a = 1.70201 - 0.75465I$    | -2.54043 + 4.81653I                   | 0          |
| $b = -0.143646 - 0.490394I$ |                                       |            |
| $u = 1.057840 + 0.659438I$  |                                       |            |
| $a = 1.49849 - 1.64923I$    | $7.74010 + 2.88014I$                  | 0          |
| $b = -1.069830 - 0.095667I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 1.057840 - 0.659438I$  |                                       |            |
| $a = 1.49849 + 1.64923I$    | $7.74010 - 2.88014I$                  | 0          |
| $b = -1.069830 + 0.095667I$ |                                       |            |
| $u = -0.691215 + 0.294815I$ |                                       |            |
| $a = 0.289608 - 1.087610I$  | $1.38946 - 1.66923I$                  | 0          |
| $b = 0.819546 - 0.317304I$  |                                       |            |
| $u = -0.691215 - 0.294815I$ |                                       |            |
| $a = 0.289608 + 1.087610I$  | $1.38946 + 1.66923I$                  | 0          |
| $b = 0.819546 + 0.317304I$  |                                       |            |
| $u = -0.086248 + 0.741503I$ |                                       |            |
| $a = -0.246964 + 0.667509I$ | $3.30597 - 3.17657I$                  | 0          |
| $b = 0.141184 + 0.757421I$  |                                       |            |
| $u = -0.086248 - 0.741503I$ |                                       |            |
| $a = -0.246964 - 0.667509I$ | $3.30597 + 3.17657I$                  | 0          |
| $b = 0.141184 - 0.757421I$  |                                       |            |
| $u = 1.051730 + 0.682378I$  |                                       |            |
| $a = -0.200801 + 0.021955I$ | $-0.72570 + 4.16457I$                 | 0          |
| $b = 0.629989 - 0.128704I$  |                                       |            |
| $u = 1.051730 - 0.682378I$  |                                       |            |
| $a = -0.200801 - 0.021955I$ | $-0.72570 - 4.16457I$                 | 0          |
| $b = 0.629989 + 0.128704I$  |                                       |            |
| $u = 0.542256 + 1.134990I$  |                                       |            |
| $a = -0.888463 - 0.217508I$ | $-1.79231 + 0.58528I$                 | 0          |
| $b = 0.928594 - 0.125798I$  |                                       |            |
| $u = 0.542256 - 1.134990I$  |                                       |            |
| $a = -0.888463 + 0.217508I$ | $-1.79231 - 0.58528I$                 | 0          |
| $b = 0.928594 + 0.125798I$  |                                       |            |
| $u = 0.538354 + 0.507318I$  |                                       |            |
| $a = -0.187718 - 0.615248I$ | $-1.07550 - 1.11618I$                 | 0          |
| $b = -0.505655 + 0.830666I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 0.538354 - 0.507318I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = -0.187718 + 0.615248I$ | $-1.07550 + 1.11618I$                 | 0          |
| $b = -0.505655 - 0.830666I$ |                                       |            |
| $u = 0.141501 + 1.253470I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 0.924660 + 0.167727I$  | $-1.23918 - 4.98850I$                 | 0          |
| $b = -0.925758 + 0.178230I$ |                                       |            |
| $u = 0.141501 - 1.253470I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 0.924660 - 0.167727I$  | $-1.23918 + 4.98850I$                 | 0          |
| $b = -0.925758 - 0.178230I$ |                                       |            |
| $u = 1.227100 + 0.388147I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 0.386210 + 0.443945I$  | $7.19910 + 7.20219I$                  | 0          |
| $b = 0.142871 - 1.021830I$  |                                       |            |
| $u = 1.227100 - 0.388147I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 0.386210 - 0.443945I$  | $7.19910 - 7.20219I$                  | 0          |
| $b = 0.142871 + 1.021830I$  |                                       |            |
| $u = 1.283860 + 0.197190I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 1.85782 - 0.24238I$    | $12.15770 + 2.16342I$                 | 0          |
| $b = -1.39271 + 0.39227I$   |                                       |            |
| $u = 1.283860 - 0.197190I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 1.85782 + 0.24238I$    | $12.15770 - 2.16342I$                 | 0          |
| $b = -1.39271 - 0.39227I$   |                                       |            |
| $u = 1.163390 + 0.588438I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 0.094949 - 0.291251I$  | $0.72346 + 7.97520I$                  | 0          |
| $b = -0.427811 + 0.447608I$ |                                       |            |
| $u = 1.163390 - 0.588438I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = 0.094949 + 0.291251I$  | $0.72346 - 7.97520I$                  | 0          |
| $b = -0.427811 - 0.447608I$ |                                       |            |
| $u = 1.218890 + 0.469664I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ |            |
| $a = -2.09340 + 0.77780I$   | $7.68884 + 8.51436I$                  | 0          |
| $b = 1.45635 + 0.24580I$    |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = 1.218890 - 0.469664I$  |                                       |            |
| $a = -2.09340 - 0.77780I$   | $7.68884 - 8.51436I$                  | 0          |
| $b = 1.45635 - 0.24580I$    |                                       |            |
| $u = 0.488312 + 0.487819I$  |                                       |            |
| $a = 0.549771 + 0.405455I$  | $-0.976204 + 0.110519I$               | 0          |
| $b = 0.070979 - 0.755869I$  |                                       |            |
| $u = 0.488312 - 0.487819I$  |                                       |            |
| $a = 0.549771 - 0.405455I$  | $-0.976204 - 0.110519I$               | 0          |
| $b = 0.070979 + 0.755869I$  |                                       |            |
| $u = -1.225560 + 0.463896I$ |                                       |            |
| $a = -1.67421 - 1.18222I$   | $7.75605 - 0.60215I$                  | 0          |
| $b = 1.246410 - 0.082879I$  |                                       |            |
| $u = -1.225560 - 0.463896I$ |                                       |            |
| $a = -1.67421 + 1.18222I$   | $7.75605 + 0.60215I$                  | 0          |
| $b = 1.246410 + 0.082879I$  |                                       |            |
| $u = 1.237590 + 0.437420I$  |                                       |            |
| $a = 2.01148 - 0.66167I$    | $6.37169 + 8.20229I$                  | 0          |
| $b = -1.46536 - 0.39893I$   |                                       |            |
| $u = 1.237590 - 0.437420I$  |                                       |            |
| $a = 2.01148 + 0.66167I$    | $6.37169 - 8.20229I$                  | 0          |
| $b = -1.46536 + 0.39893I$   |                                       |            |
| $u = -0.067862 + 0.681199I$ |                                       |            |
| $a = 0.176085 - 0.260940I$  | $2.58142 - 4.00230I$                  | 0          |
| $b = -1.176730 + 0.387839I$ |                                       |            |
| $u = -0.067862 - 0.681199I$ |                                       |            |
| $a = 0.176085 + 0.260940I$  | $2.58142 + 4.00230I$                  | 0          |
| $b = -1.176730 - 0.387839I$ |                                       |            |
| $u = -0.940533 + 0.941896I$ |                                       |            |
| $a = -0.277371 - 0.435324I$ | $6.24717 - 0.29908I$                  | 0          |
| $b = -0.988739 - 0.802148I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -0.940533 - 0.941896I$ |                                       |            |
| $a = -0.277371 + 0.435324I$ | $6.24717 + 0.29908I$                  | 0          |
| $b = -0.988739 + 0.802148I$ |                                       |            |
| $u = -0.283208 + 1.306100I$ |                                       |            |
| $a = 0.390236 + 0.305867I$  | $1.63786 - 4.30834I$                  | 0          |
| $b = -1.294480 + 0.218177I$ |                                       |            |
| $u = -0.283208 - 1.306100I$ |                                       |            |
| $a = 0.390236 - 0.305867I$  | $1.63786 + 4.30834I$                  | 0          |
| $b = -1.294480 - 0.218177I$ |                                       |            |
| $u = -0.392797 + 1.286680I$ |                                       |            |
| $a = -0.267809 + 0.366326I$ | $-0.76603 + 6.89558I$                 | 0          |
| $b = 1.34240 + 0.55580I$    |                                       |            |
| $u = -0.392797 - 1.286680I$ |                                       |            |
| $a = -0.267809 - 0.366326I$ | $-0.76603 - 6.89558I$                 | 0          |
| $b = 1.34240 - 0.55580I$    |                                       |            |
| $u = -0.327204 + 0.555531I$ |                                       |            |
| $a = 0.636996 - 1.229940I$  | $7.00072 + 0.30811I$                  | 0          |
| $b = -1.111360 - 0.326258I$ |                                       |            |
| $u = -0.327204 - 0.555531I$ |                                       |            |
| $a = 0.636996 + 1.229940I$  | $7.00072 - 0.30811I$                  | 0          |
| $b = -1.111360 + 0.326258I$ |                                       |            |
| $u = 1.376410 + 0.069310I$  |                                       |            |
| $a = -1.71327 + 0.08014I$   | $6.96615 - 2.50132I$                  | 0          |
| $b = 1.43509 - 0.41398I$    |                                       |            |
| $u = 1.376410 - 0.069310I$  |                                       |            |
| $a = -1.71327 - 0.08014I$   | $6.96615 + 2.50132I$                  | 0          |
| $b = 1.43509 + 0.41398I$    |                                       |            |
| $u = -1.269100 + 0.552397I$ |                                       |            |
| $a = -0.523171 + 0.253472I$ | $3.00122 - 13.54100I$                 | 0          |
| $b = -0.194441 - 1.243000I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.269100 - 0.552397I$ |                                       |            |
| $a = -0.523171 - 0.253472I$ | $3.00122 + 13.54100I$                 | 0          |
| $b = -0.194441 + 1.243000I$ |                                       |            |
| $u = 1.308780 + 0.465341I$  |                                       |            |
| $a = 1.83742 - 0.78805I$    | $6.33671 + 9.08273I$                  | 0          |
| $b = -1.34417 - 0.51184I$   |                                       |            |
| $u = 1.308780 - 0.465341I$  |                                       |            |
| $a = 1.83742 + 0.78805I$    | $6.33671 - 9.08273I$                  | 0          |
| $b = -1.34417 + 0.51184I$   |                                       |            |
| $u = 1.306810 + 0.475630I$  |                                       |            |
| $a = -1.89328 + 0.92128I$   | $10.7154 + 12.9263I$                  | 0          |
| $b = 1.286200 + 0.577959I$  |                                       |            |
| $u = 1.306810 - 0.475630I$  |                                       |            |
| $a = -1.89328 - 0.92128I$   | $10.7154 - 12.9263I$                  | 0          |
| $b = 1.286200 - 0.577959I$  |                                       |            |
| $u = -1.352590 + 0.377037I$ |                                       |            |
| $a = -1.48051 - 0.51240I$   | $9.28418 - 7.57796I$                  | 0          |
| $b = 1.59871 + 0.29351I$    |                                       |            |
| $u = -1.352590 - 0.377037I$ |                                       |            |
| $a = -1.48051 + 0.51240I$   | $9.28418 + 7.57796I$                  | 0          |
| $b = 1.59871 - 0.29351I$    |                                       |            |
| $u = 1.36189 + 0.38376I$    |                                       |            |
| $a = 0.327869 + 0.177645I$  | $4.22039 - 3.23688I$                  | 0          |
| $b = 0.309449 - 1.229080I$  |                                       |            |
| $u = 1.36189 - 0.38376I$    |                                       |            |
| $a = 0.327869 - 0.177645I$  | $4.22039 + 3.23688I$                  | 0          |
| $b = 0.309449 + 1.229080I$  |                                       |            |
| $u = -1.40996 + 0.21702I$   |                                       |            |
| $a = 1.87955 + 0.05582I$    | $5.05593 - 0.34565I$                  | 0          |
| $b = -1.003870 + 0.065130I$ |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.40996 - 0.21702I$   |                                       |            |
| $a = 1.87955 - 0.05582I$    | $5.05593 + 0.34565I$                  | 0          |
| $b = -1.003870 - 0.065130I$ |                                       |            |
| $u = -1.32026 + 0.58348I$   |                                       |            |
| $a = 0.429953 - 0.159621I$  | $-1.06924 - 7.01836I$                 | 0          |
| $b = 0.314367 + 1.291950I$  |                                       |            |
| $u = -1.32026 - 0.58348I$   |                                       |            |
| $a = 0.429953 + 0.159621I$  | $-1.06924 + 7.01836I$                 | 0          |
| $b = 0.314367 - 1.291950I$  |                                       |            |
| $u = 1.27599 + 0.67937I$    |                                       |            |
| $a = -1.58847 + 0.91676I$   | $0.81247 + 6.07654I$                  | 0          |
| $b = 1.059540 + 0.231478I$  |                                       |            |
| $u = 1.27599 - 0.67937I$    |                                       |            |
| $a = -1.58847 - 0.91676I$   | $0.81247 - 6.07654I$                  | 0          |
| $b = 1.059540 - 0.231478I$  |                                       |            |
| $u = 1.33885 + 0.58073I$    |                                       |            |
| $a = 1.76165 - 0.76077I$    | $2.70539 + 11.25400I$                 | 0          |
| $b = -1.076530 - 0.340845I$ |                                       |            |
| $u = 1.33885 - 0.58073I$    |                                       |            |
| $a = 1.76165 + 0.76077I$    | $2.70539 - 11.25400I$                 | 0          |
| $b = -1.076530 + 0.340845I$ |                                       |            |
| $u = -1.30757 + 0.65669I$   |                                       |            |
| $a = 1.58455 + 1.05180I$    | $6.7085 - 20.1549I$                   | 0          |
| $b = -1.35553 + 0.64430I$   |                                       |            |
| $u = -1.30757 - 0.65669I$   |                                       |            |
| $a = 1.58455 - 1.05180I$    | $6.7085 + 20.1549I$                   | 0          |
| $b = -1.35553 - 0.64430I$   |                                       |            |
| $u = -1.37349 + 0.51903I$   |                                       |            |
| $a = -1.311600 - 0.480971I$ | $10.47850 + 2.18356I$                 | 0          |
| $b = 1.259940 + 0.325657I$  |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|------------|
| $u = -1.37349 - 0.51903I$   |                                       |            |
| $a = -1.311600 + 0.480971I$ | $10.47850 - 2.18356I$                 | 0          |
| $b = 1.259940 - 0.325657I$  |                                       |            |
| $u = -1.37819 + 0.50716I$   |                                       |            |
| $a = 1.44237 + 0.63470I$    | $5.55494 - 1.82210I$                  | 0          |
| $b = -1.221120 + 0.079457I$ |                                       |            |
| $u = -1.37819 - 0.50716I$   |                                       |            |
| $a = 1.44237 - 0.63470I$    | $5.55494 + 1.82210I$                  | 0          |
| $b = -1.221120 - 0.079457I$ |                                       |            |
| $u = -0.22057 + 1.45474I$   |                                       |            |
| $a = -0.127654 - 1.048490I$ | $-5.07831 + 0.54261I$                 | 0          |
| $b = 0.15390 - 1.45082I$    |                                       |            |
| $u = -0.22057 - 1.45474I$   |                                       |            |
| $a = -0.127654 + 1.048490I$ | $-5.07831 - 0.54261I$                 | 0          |
| $b = 0.15390 + 1.45082I$    |                                       |            |
| $u = -1.42771 + 0.44318I$   |                                       |            |
| $a = 1.40615 + 0.46494I$    | $6.18667 - 2.09350I$                  | 0          |
| $b = -1.42123 - 0.11571I$   |                                       |            |
| $u = -1.42771 - 0.44318I$   |                                       |            |
| $a = 1.40615 - 0.46494I$    | $6.18667 + 2.09350I$                  | 0          |
| $b = -1.42123 + 0.11571I$   |                                       |            |
| $u = -1.32376 + 0.69830I$   |                                       |            |
| $a = -1.44255 - 1.02867I$   | $2.36737 - 13.86820I$                 | 0          |
| $b = 1.34377 - 0.66711I$    |                                       |            |
| $u = -1.32376 - 0.69830I$   |                                       |            |
| $a = -1.44255 + 1.02867I$   | $2.36737 + 13.86820I$                 | 0          |
| $b = 1.34377 + 0.66711I$    |                                       |            |
| $u = -1.24712 + 0.84386I$   |                                       |            |
| $a = 1.08987 + 1.19487I$    | $7.40283 - 6.91839I$                  | 0          |
| $b = -1.24793 + 0.76502I$   |                                       |            |

| Solutions to $I_1^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -1.24712 - 0.84386I$   |                                       |                       |
| $a = 1.08987 - 1.19487I$    | $7.40283 + 6.91839I$                  | 0                     |
| $b = -1.24793 - 0.76502I$   |                                       |                       |
| $u = 1.41867 + 0.51798I$    |                                       |                       |
| $a = -1.46126 + 0.74622I$   | $8.02706 + 3.82363I$                  | 0                     |
| $b = 1.45701 + 0.63495I$    |                                       |                       |
| $u = 1.41867 - 0.51798I$    |                                       |                       |
| $a = -1.46126 - 0.74622I$   | $8.02706 - 3.82363I$                  | 0                     |
| $b = 1.45701 - 0.63495I$    |                                       |                       |
| $u = 1.51830 + 0.17387I$    |                                       |                       |
| $a = 1.51539 - 0.19146I$    | $10.05230 - 8.50067I$                 | 0                     |
| $b = -1.42599 + 0.37167I$   |                                       |                       |
| $u = 1.51830 - 0.17387I$    |                                       |                       |
| $a = 1.51539 + 0.19146I$    | $10.05230 + 8.50067I$                 | 0                     |
| $b = -1.42599 - 0.37167I$   |                                       |                       |
| $u = 0.168197 + 0.431680I$  |                                       |                       |
| $a = 0.875183 - 0.334368I$  | $-0.915726 - 0.687361I$               | 0                     |
| $b = -0.201001 - 0.533588I$ |                                       |                       |
| $u = 0.168197 - 0.431680I$  |                                       |                       |
| $a = 0.875183 + 0.334368I$  | $-0.915726 + 0.687361I$               | 0                     |
| $b = -0.201001 + 0.533588I$ |                                       |                       |
| $u = -0.343804 + 0.090921I$ |                                       |                       |
| $a = 0.94819 - 1.32544I$    | $1.45487 - 1.58972I$                  | $-2.00000 - 2.74536I$ |
| $b = 0.941762 - 0.385718I$  |                                       |                       |
| $u = -0.343804 - 0.090921I$ |                                       |                       |
| $a = 0.94819 + 1.32544I$    | $1.45487 + 1.58972I$                  | $-2.00000 + 2.74536I$ |
| $b = 0.941762 + 0.385718I$  |                                       |                       |
| $u = 0.280701 + 0.097255I$  |                                       |                       |
| $a = -0.97322 + 1.50126I$   | $0.71411 - 2.06955I$                  | $-3.17684 + 3.40929I$ |
| $b = 0.690430 - 0.592461I$  |                                       |                       |

| Solutions to $I_1^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|----------------------------|---------------------------------------|-----------------------|
| $u = 0.280701 - 0.097255I$ |                                       |                       |
| $a = -0.97322 - 1.50126I$  | $0.71411 + 2.06955I$                  | $-3.17684 - 3.40929I$ |
| $b = 0.690430 + 0.592461I$ |                                       |                       |

## II.

$$I_2^u = \langle -1.30 \times 10^{27} u^{42} + 5.59 \times 10^{27} u^{41} + \dots + 5.18 \times 10^{24} b - 1.73 \times 10^{27}, -5.05 \times 10^{27} u^{42} + 2.25 \times 10^{28} u^{41} + \dots + 5.18 \times 10^{24} a - 8.77 \times 10^{27}, u^{43} - 5u^{42} + \dots + 9u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 976.290u^{42} - 4339.64u^{41} + \dots - 12563.5u + 1694.59 \\ 251.254u^{42} - 1079.06u^{41} + \dots - 2631.38u + 334.926 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 690.201u^{42} - 3223.52u^{41} + \dots - 11234.8u + 1666.48 \\ 1063.08u^{42} - 4649.80u^{41} + \dots - 12523.5u + 1690.74 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1946.84u^{42} - 8537.33u^{41} + \dots - 22943.6u + 3065.48 \\ -1757.20u^{42} + 7761.50u^{41} + \dots + 21933.8u - 3006.41 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -381.102u^{42} + 1690.92u^{41} + \dots + 4259.64u - 572.007 \\ -571.317u^{42} + 2488.17u^{41} + \dots + 6264.83u - 823.904 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -417.569u^{42} + 1685.77u^{41} + \dots + 2645.87u - 251.748 \\ 1435.87u^{42} - 6302.74u^{41} + \dots - 17081.9u + 2320.31 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -3563.78u^{42} + 15715.5u^{41} + \dots + 43934.5u - 5998.17 \\ 3561.78u^{42} - 15706.5u^{41} + \dots - 43899.5u + 5987.17 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -196.119u^{42} + 664.940u^{41} + \dots - 606.796u + 222.805 \\ 1214.42u^{42} - 5281.91u^{41} + \dots - 13829.2u + 1845.76 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -5669.06u^{42} + 25125.2u^{41} + \dots + 72661.1u - 10052.1 \\ 2770.71u^{42} - 12334.0u^{41} + \dots - 36228.9u + 5041.16 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= -\frac{39731743503703556572717582173}{5176114318849511714698289} u^{42} + \frac{176212969798214825520092916434}{5176114318849511714698289} u^{41} + \dots + \frac{528850699858818575212985731870}{5176114318849511714698289} u - \frac{73356324113368931490575946909}{5176114318849511714698289}$$

(iv) **u-Polynomials at the component**

| Crossings | u-Polynomials at each crossing        |
|-----------|---------------------------------------|
| $c_1$     | $u^{43} - 7u^{42} + \cdots + 10u - 1$ |
| $c_2$     | $u^{43} - 10u^{41} + \cdots - 4u - 1$ |
| $c_3$     | $u^{43} - 2u^{41} + \cdots + 4u - 1$  |
| $c_4$     | $u^{43} + 7u^{42} + \cdots + 10u + 1$ |
| $c_5$     | $u^{43} + 4u^{42} + \cdots - 2u - 1$  |
| $c_6$     | $u^{43} + 13u^{42} + \cdots - 7u + 1$ |
| $c_7$     | $u^{43} - 10u^{41} + \cdots - 4u + 1$ |
| $c_8$     | $u^{43} - 5u^{42} + \cdots + 9u - 1$  |
| $c_9$     | $u^{43} + 8u^{42} + \cdots - 6u + 1$  |
| $c_{10}$  | $u^{43} - 4u^{42} + \cdots - 2u + 1$  |
| $c_{11}$  | $u^{43} + 5u^{42} + \cdots + 9u + 1$  |
| $c_{12}$  | $u^{43} + u^{42} + \cdots - 4u + 1$   |



**(v) Riley Polynomials at the component**

| Crossings     | Riley Polynomials at each crossing     |
|---------------|--|
| $c_1, c_4$    | $y^{43} + 27y^{42} + \cdots - 18y - 1$ |
| $c_2, c_7$    | $y^{43} - 20y^{42} + \cdots + 32y - 1$ |
| $c_3$         | $y^{43} - 4y^{42} + \cdots - 30y - 1$  |
| $c_5, c_{10}$ | $y^{43} - 4y^{42} + \cdots - 16y - 1$  |
| $c_6$         | $y^{43} + 15y^{42} + \cdots + 43y - 1$ |
| $c_8, c_{11}$ | $y^{43} - 15y^{42} + \cdots + 27y - 1$ |
| $c_9$         | $y^{43} - 24y^{42} + \cdots - 10y - 1$ |
| $c_{12}$      | $y^{43} + 3y^{42} + \cdots - 112y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|-----------------------------|---------------------------------------|----------------------|
| $u = 0.018036 + 1.005850I$  |                                       |                      |
| $a = -0.865587 - 0.572541I$ | $-1.55180 - 4.33690I$                 | 0                    |
| $b = 0.703586 - 0.069280I$  |                                       |                      |
| $u = 0.018036 - 1.005850I$  |                                       |                      |
| $a = -0.865587 + 0.572541I$ | $-1.55180 + 4.33690I$                 | 0                    |
| $b = 0.703586 + 0.069280I$  |                                       |                      |
| $u = -0.967617 + 0.119302I$ |                                       |                      |
| $a = -0.548131 + 0.149417I$ | $1.61658 - 2.29495I$                  | $4.61864 + 2.93274I$ |
| $b = 0.514103 - 0.815458I$  |                                       |                      |
| $u = -0.967617 - 0.119302I$ |                                       |                      |
| $a = -0.548131 - 0.149417I$ | $1.61658 + 2.29495I$                  | $4.61864 - 2.93274I$ |
| $b = 0.514103 + 0.815458I$  |                                       |                      |
| $u = -1.020430 + 0.293177I$ |                                       |                      |
| $a = 0.354342 - 0.854539I$  | $3.33625 + 1.27021I$                  | 0                    |
| $b = 0.693053 + 0.548437I$  |                                       |                      |
| $u = -1.020430 - 0.293177I$ |                                       |                      |
| $a = 0.354342 + 0.854539I$  | $3.33625 - 1.27021I$                  | 0                    |
| $b = 0.693053 - 0.548437I$  |                                       |                      |
| $u = 0.967778 + 0.438117I$  |                                       |                      |
| $a = 1.164550 - 0.206473I$  | $-1.36209 + 4.95710I$                 | 0                    |
| $b = -0.756698 - 0.918811I$ |                                       |                      |
| $u = 0.967778 - 0.438117I$  |                                       |                      |
| $a = 1.164550 + 0.206473I$  | $-1.36209 - 4.95710I$                 | 0                    |
| $b = -0.756698 + 0.918811I$ |                                       |                      |
| $u = -0.783383 + 0.470302I$ |                                       |                      |
| $a = -0.204859 - 1.011670I$ | $7.75302 - 2.17548I$                  | $9.56983 + 2.53983I$ |
| $b = -0.858982 + 0.087111I$ |                                       |                      |
| $u = -0.783383 - 0.470302I$ |                                       |                      |
| $a = -0.204859 + 1.011670I$ | $7.75302 + 2.17548I$                  | $9.56983 - 2.53983I$ |
| $b = -0.858982 - 0.087111I$ |                                       |                      |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.898121 + 0.033912I$ |                                       |                       |
| $a = -2.34558 + 3.49066I$   | $3.05821 - 2.10222I$                  | $-47.3234 - 50.9827I$ |
| $b = -0.856628 + 0.518902I$ |                                       |                       |
| $u = -0.898121 - 0.033912I$ |                                       |                       |
| $a = -2.34558 - 3.49066I$   | $3.05821 + 2.10222I$                  | $-47.3234 + 50.9827I$ |
| $b = -0.856628 - 0.518902I$ |                                       |                       |
| $u = 0.675502 + 0.929007I$  |                                       |                       |
| $a = 0.479383 - 0.025545I$  | $-2.75030 + 0.36331I$                 | 0                     |
| $b = -0.762703 + 0.350472I$ |                                       |                       |
| $u = 0.675502 - 0.929007I$  |                                       |                       |
| $a = 0.479383 + 0.025545I$  | $-2.75030 - 0.36331I$                 | 0                     |
| $b = -0.762703 - 0.350472I$ |                                       |                       |
| $u = -0.770362 + 0.201775I$ |                                       |                       |
| $a = 0.277954 - 0.244414I$  | $1.87369 - 2.08777I$                  | $5.28642 + 7.07196I$  |
| $b = 0.767500 - 0.404339I$  |                                       |                       |
| $u = -0.770362 - 0.201775I$ |                                       |                       |
| $a = 0.277954 + 0.244414I$  | $1.87369 + 2.08777I$                  | $5.28642 - 7.07196I$  |
| $b = 0.767500 + 0.404339I$  |                                       |                       |
| $u = 1.070160 + 0.552468I$  |                                       |                       |
| $a = 0.738078 - 0.337807I$  | $-1.36368 + 5.06561I$                 | 0                     |
| $b = -0.415913 - 0.621412I$ |                                       |                       |
| $u = 1.070160 - 0.552468I$  |                                       |                       |
| $a = 0.738078 + 0.337807I$  | $-1.36368 - 5.06561I$                 | 0                     |
| $b = -0.415913 + 0.621412I$ |                                       |                       |
| $u = -1.112120 + 0.484369I$ |                                       |                       |
| $a = 1.95574 + 1.34639I$    | $8.99490 - 1.86585I$                  | 0                     |
| $b = -1.139400 + 0.010371I$ |                                       |                       |
| $u = -1.112120 - 0.484369I$ |                                       |                       |
| $a = 1.95574 - 1.34639I$    | $8.99490 + 1.86585I$                  | 0                     |
| $b = -1.139400 - 0.010371I$ |                                       |                       |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape             |
|-----------------------------|---------------------------------------|------------------------|
| $u = 1.115720 + 0.510206I$  |                                       |                        |
| $a = -0.258006 + 1.066870I$ | $1.55198 + 8.82913I$                  | 0                      |
| $b = 0.490522 + 0.130491I$  |                                       |                        |
| $u = 1.115720 - 0.510206I$  |                                       |                        |
| $a = -0.258006 - 1.066870I$ | $1.55198 - 8.82913I$                  | 0                      |
| $b = 0.490522 - 0.130491I$  |                                       |                        |
| $u = 0.739430 + 0.158190I$  |                                       |                        |
| $a = 0.16306 - 1.69152I$    | $-2.87881 - 2.25807I$                 | $-11.65616 - 2.03401I$ |
| $b = -0.457958 + 1.315660I$ |                                       |                        |
| $u = 0.739430 - 0.158190I$  |                                       |                        |
| $a = 0.16306 + 1.69152I$    | $-2.87881 + 2.25807I$                 | $-11.65616 + 2.03401I$ |
| $b = -0.457958 - 1.315660I$ |                                       |                        |
| $u = 0.858125 + 0.903741I$  |                                       |                        |
| $a = -0.167400 + 0.587060I$ | $5.77802 + 0.61199I$                  | 0                      |
| $b = -1.001110 + 0.631626I$ |                                       |                        |
| $u = 0.858125 - 0.903741I$  |                                       |                        |
| $a = -0.167400 - 0.587060I$ | $5.77802 - 0.61199I$                  | 0                      |
| $b = -1.001110 - 0.631626I$ |                                       |                        |
| $u = -0.179188 + 1.256430I$ |                                       |                        |
| $a = -0.373285 - 0.110297I$ | $1.14741 - 4.73512I$                  | 0                      |
| $b = 1.260690 - 0.185553I$  |                                       |                        |
| $u = -0.179188 - 1.256430I$ |                                       |                        |
| $a = -0.373285 + 0.110297I$ | $1.14741 + 4.73512I$                  | 0                      |
| $b = 1.260690 + 0.185553I$  |                                       |                        |
| $u = 1.266850 + 0.376482I$  |                                       |                        |
| $a = -2.00362 + 0.42464I$   | $6.43713 + 9.46442I$                  | 0                      |
| $b = 1.48678 + 0.29090I$    |                                       |                        |
| $u = 1.266850 - 0.376482I$  |                                       |                        |
| $a = -2.00362 - 0.42464I$   | $6.43713 - 9.46442I$                  | 0                      |
| $b = 1.48678 - 0.29090I$    |                                       |                        |

| Solutions to $I_2^u$        | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|-----------------------------|---------------------------------------|-----------------------|
| $u = 0.256468 + 0.623041I$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | $\text{Cusp shape}$   |
| $a = 0.63391 - 1.37530I$    | $-1.27564 + 4.14509I$                 | $-4.10122 - 5.10933I$ |
| $b = -1.103980 - 0.529718I$ |                                       |                       |
| $u = 0.256468 - 0.623041I$  |                                       |                       |
| $a = 0.63391 + 1.37530I$    | $-1.27564 - 4.14509I$                 | $-4.10122 + 5.10933I$ |
| $b = -1.103980 + 0.529718I$ |                                       |                       |
| $u = 0.122323 + 1.392290I$  |                                       |                       |
| $a = -0.100494 + 1.092750I$ | $-5.15083 - 0.32395I$                 | $0$                   |
| $b = 0.004112 + 1.384690I$  |                                       |                       |
| $u = 0.122323 - 1.392290I$  |                                       |                       |
| $a = -0.100494 - 1.092750I$ | $-5.15083 + 0.32395I$                 | $0$                   |
| $b = 0.004112 - 1.384690I$  |                                       |                       |
| $u = 1.247040 + 0.664885I$  |                                       |                       |
| $a = 1.49607 - 1.14603I$    | $7.37503 + 5.86162I$                  | $0$                   |
| $b = -1.34820 - 0.52760I$   |                                       |                       |
| $u = 1.247040 - 0.664885I$  |                                       |                       |
| $a = 1.49607 + 1.14603I$    | $7.37503 - 5.86162I$                  | $0$                   |
| $b = -1.34820 + 0.52760I$   |                                       |                       |
| $u = 0.581841 + 0.029202I$  |                                       |                       |
| $a = -2.60703 + 1.14090I$   | $2.92133 + 7.68807I$                  | $0.83209 - 7.89037I$  |
| $b = 1.301390 + 0.502509I$  |                                       |                       |
| $u = 0.581841 - 0.029202I$  |                                       |                       |
| $a = -2.60703 - 1.14090I$   | $2.92133 - 7.68807I$                  | $0.83209 + 7.89037I$  |
| $b = 1.301390 - 0.502509I$  |                                       |                       |
| $u = 0.522271 + 0.225026I$  |                                       |                       |
| $a = 4.03290 - 0.02892I$    | $-0.91454 - 5.09998I$                 | $-7.09887 + 2.47578I$ |
| $b = 0.537672 + 0.044936I$  |                                       |                       |
| $u = 0.522271 - 0.225026I$  |                                       |                       |
| $a = 4.03290 + 0.02892I$    | $-0.91454 + 5.09998I$                 | $-7.09887 - 2.47578I$ |
| $b = 0.537672 - 0.044936I$  |                                       |                       |

| Solutions to $I_2^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------------|---------------------------------------|------------|
| $u = -1.42156 + 0.41997I$  |                                       |            |
| $a = -1.56789 - 0.55679I$  | $5.72726 - 1.48386I$                  | 0          |
| $b = 1.201850 - 0.125310I$ |                                       |            |
| $u = -1.42156 - 0.41997I$  |                                       |            |
| $a = -1.56789 + 0.55679I$  | $5.72726 + 1.48386I$                  | 0          |
| $b = 1.201850 + 0.125310I$ |                                       |            |
| $u = 0.422479$             |                                       |            |
| $a = -5.50822$             | -4.97926                              | -11.8730   |
| $b = -0.519385$            |                                       |            |

### III. u-Polynomials

| Crossings | u-Polynomials at each crossing   |
|-----------|--|
| $c_1$     | $(u^{43} - 7u^{42} + \dots + 10u - 1)(u^{161} - 6u^{160} + \dots - 60405u + 2525)$                             |
| $c_2$     | $(u^{43} - 10u^{41} + \dots - 4u - 1)(u^{161} + u^{160} + \dots + 62875u + 20690)$                             |
| $c_3$     | $(u^{43} - 2u^{41} + \dots + 4u - 1)(u^{161} + u^{160} + \dots + 6424407u - 1081037)$                          |
| $c_4$     | $(u^{43} + 7u^{42} + \dots + 10u + 1)(u^{161} - 6u^{160} + \dots - 60405u + 2525)$                             |
| $c_5$     | $(u^{43} + 4u^{42} + \dots - 2u - 1)(u^{161} - 5u^{160} + \dots - 34377u - 24287)$                             |
| $c_6$     | $(u^{43} + 13u^{42} + \dots - 7u + 1)$<br>$\cdot (u^{161} + 4u^{160} + \dots + 209706558586u + 17633051719)$   |
| $c_7$     | $(u^{43} - 10u^{41} + \dots - 4u + 1)(u^{161} + u^{160} + \dots + 62875u + 20690)$                             |
| $c_8$     | $(u^{43} - 5u^{42} + \dots + 9u - 1)(u^{161} - 43u^{159} + \dots + 23192u + 22751)$                            |
| $c_9$     | $(u^{43} + 8u^{42} + \dots - 6u + 1)$<br>$\cdot (u^{161} + 5u^{160} + \dots + 5900566245u - 806431049)$        |
| $c_{10}$  | $(u^{43} - 4u^{42} + \dots - 2u + 1)(u^{161} - 5u^{160} + \dots - 34377u - 24287)$                             |
| $c_{11}$  | $(u^{43} + 5u^{42} + \dots + 9u + 1)(u^{161} - 43u^{159} + \dots + 23192u + 22751)$                            |
| $c_{12}$  | $(u^{43} + u^{42} + \dots - 4u + 1)$<br>$\cdot (u^{161} + 2u^{160} + \dots + {}_{32}^{297854463}u - 20528044)$ |

#### IV. Riley Polynomials

| Crossings     | Riley Polynomials at each crossing  |
|---------------|---|
| $c_1, c_4$    | $(y^{43} + 27y^{42} + \dots - 18y - 1) \\ \cdot (y^{161} + 104y^{160} + \dots - 44901925y - 6375625)$                       |
| $c_2, c_7$    | $(y^{43} - 20y^{42} + \dots + 32y - 1) \\ \cdot (y^{161} - 95y^{160} + \dots + 56848574785y - 428076100)$                   |
| $c_3$         | $(y^{43} - 4y^{42} + \dots - 30y - 1) \\ \cdot (y^{161} + 13y^{160} + \dots - 81817610068445y - 1168640995369)$             |
| $c_5, c_{10}$ | $(y^{43} - 4y^{42} + \dots - 16y - 1) \\ \cdot (y^{161} - 71y^{160} + \dots - 8324930855y - 589858369)$                     |
| $c_6$         | $(y^{43} + 15y^{42} + \dots + 43y - 1) \\ \cdot (y^{161} - 44y^{160} + \dots + 4.98 \times 10^{21}y - 3.11 \times 10^{20})$ |
| $c_8, c_{11}$ | $(y^{43} - 15y^{42} + \dots + 27y - 1) \\ \cdot (y^{161} - 86y^{160} + \dots + 30379536528y - 517608001)$                   |
| $c_9$         | $(y^{43} - 24y^{42} + \dots - 10y - 1) \\ \cdot (y^{161} + 29y^{160} + \dots - 3.95 \times 10^{19}y - 6.50 \times 10^{17})$ |
| $c_{12}$      | $(y^{43} + 3y^{42} + \dots - 112y - 1) \\ \cdot (y^{161} + 36y^{160} + \dots - 32685559262828287y - 421400590465936)$       |