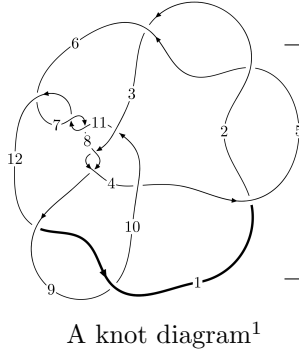
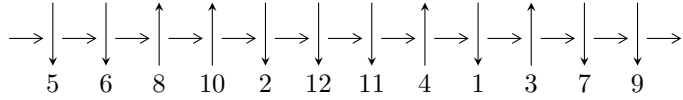


12a₁₂₂₄ (K12a₁₂₂₄)



Linearized knot diagram



Solving Sequence

$$1,5 \xrightarrow{c_1} 2 \xrightarrow{c_5} 6 \xrightarrow{c_2} 3,10 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \xrightarrow{c_6} 7 \xrightarrow{c_{11}} 11 \rightsquigarrow c_3, c_7, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 1.21800 \times 10^{175} u^{86} + 1.10072 \times 10^{176} u^{85} + \dots + 5.56542 \times 10^{175} b + 9.38658 \times 10^{176}, \\ - 2.03509 \times 10^{176} u^{86} + 9.22272 \times 10^{176} u^{85} + \dots + 5.56542 \times 10^{175} a + 3.49997 \times 10^{177}, \\ u^{87} - 5u^{86} + \dots - 31u - 1 \rangle$$

$$I_2^u = \langle 3u^{20} - 5u^{19} + \dots + b - 2, -3u^{20} + 4u^{19} + \dots + a + 4, u^{21} - 14u^{19} + \dots + u - 1 \rangle$$

$$I_3^u = \langle b + 1, -u^5 + 2u^4 + 2u^3 - 4u^2 + a - u + 1, u^6 - 3u^5 + 6u^3 - 4u^2 + 1 \rangle$$

$$I_4^u = \langle b + 1, a - 1, u + 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 115 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 1.22 \times 10^{175} u^{86} + 1.10 \times 10^{176} u^{85} + \dots + 5.57 \times 10^{175} b + 9.39 \times 10^{176}, -2.04 \times 10^{176} u^{86} + 9.22 \times 10^{176} u^{85} + \dots + 5.57 \times 10^{175} a + 3.50 \times 10^{177}, u^{87} - 5u^{86} + \dots - 31u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 3.65668u^{86} - 16.5715u^{85} + \dots - 1025.07u - 62.8879 \\ -0.218852u^{86} - 1.97778u^{85} + \dots - 412.229u - 16.8659 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -20.1258u^{86} + 100.004u^{85} + \dots + 3106.06u + 123.163 \\ 1.01692u^{86} - 6.75872u^{85} + \dots - 461.880u - 22.8410 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 3.43783u^{86} - 18.5492u^{85} + \dots - 1437.30u - 79.7538 \\ -0.218852u^{86} - 1.97778u^{85} + \dots - 412.229u - 16.8659 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 20.7323u^{86} - 106.664u^{85} + \dots - 4060.99u - 176.355 \\ -1.96351u^{86} + 8.22272u^{85} + \dots + 158.487u + 9.66986 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -21.5377u^{86} + 114.337u^{85} + \dots + 5556.14u + 273.143 \\ 1.30331u^{86} - 0.885320u^{85} + \dots + 627.672u + 26.9509 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -3.73334u^{86} + 32.1426u^{85} + \dots + 2150.24u + 65.7851 \\ 8.70129u^{86} - 35.1065u^{85} + \dots - 562.970u - 33.7329 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 3.49067u^{86} - 18.8111u^{85} + \dots - 1445.83u - 79.7310 \\ 0.510581u^{86} - 4.63816u^{85} + \dots - 407.668u - 16.8546 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-3.04694u^{86} + 31.0771u^{85} + \dots + 2704.70u + 109.774$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------|---|
| c_1, c_2, c_5 | $u^{87} + 5u^{86} + \dots - 31u + 1$ |
| c_3, c_8 | $u^{87} + 2u^{86} + \dots + 1867u - 1459$ |
| c_4 | $u^{87} - u^{86} + \dots - 108842u + 15817$ |
| c_6, c_7, c_{11} | $u^{87} + 2u^{86} + \dots - 36u + 7$ |
| c_9, c_{12} | $u^{87} - 9u^{86} + \dots + 784u - 8$ |
| c_{10} | $u^{87} + 3u^{86} + \dots + 619168u + 590297$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------|---|
| c_1, c_2, c_5 | $y^{87} - 91y^{86} + \dots + 301y - 1$ |
| c_3, c_8 | $y^{87} - 64y^{86} + \dots + 35213103y - 2128681$ |
| c_4 | $y^{87} + 33y^{86} + \dots + 197455366y - 250177489$ |
| c_6, c_7, c_{11} | $y^{87} + 90y^{86} + \dots + 2206y - 49$ |
| c_9, c_{12} | $y^{87} - 59y^{86} + \dots + 638432y - 64$ |
| c_{10} | $y^{87} - 25y^{86} + \dots + 7264616979632y - 348450548209$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 0.919570 + 0.341269I$ $a = -0.230219 - 1.291490I$ $b = 1.018910 + 0.767688I$ | $4.92914 - 3.18573I$ | 0 |
| $u = 0.919570 - 0.341269I$ $a = -0.230219 + 1.291490I$ $b = 1.018910 - 0.767688I$ | $4.92914 + 3.18573I$ | 0 |
| $u = 0.643376 + 0.795200I$ $a = -0.443359 - 0.859364I$ $b = 1.129980 + 0.180708I$ | $-3.41783 - 2.87585I$ | 0 |
| $u = 0.643376 - 0.795200I$ $a = -0.443359 + 0.859364I$ $b = 1.129980 - 0.180708I$ | $-3.41783 + 2.87585I$ | 0 |
| $u = -0.801927 + 0.529130I$ $a = -1.221220 - 0.403028I$ $b = -0.518441 + 0.530723I$ | $8.78928 - 2.20079I$ | 0 |
| $u = -0.801927 - 0.529130I$ $a = -1.221220 + 0.403028I$ $b = -0.518441 - 0.530723I$ | $8.78928 + 2.20079I$ | 0 |
| $u = -0.605395 + 0.915337I$ $a = 0.449296 - 1.181010I$ $b = -1.230940 + 0.562762I$ | $6.97761 + 12.04090I$ | 0 |
| $u = -0.605395 - 0.915337I$ $a = 0.449296 + 1.181010I$ $b = -1.230940 - 0.562762I$ | $6.97761 - 12.04090I$ | 0 |
| $u = -0.524939 + 0.728503I$ $a = -0.50181 + 1.52469I$ $b = 1.221130 - 0.467400I$ | $0.17465 + 8.23740I$ | 0 |
| $u = -0.524939 - 0.728503I$ $a = -0.50181 - 1.52469I$ $b = 1.221130 + 0.467400I$ | $0.17465 - 8.23740I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------|
| $u = 1.146280 + 0.016740I$ $a = -0.218153 + 1.254070I$ $b = 0.883487 - 0.824717I$ | $5.16086 + 3.06951I$ | 0 |
| $u = 1.146280 - 0.016740I$ $a = -0.218153 - 1.254070I$ $b = 0.883487 + 0.824717I$ | $5.16086 - 3.06951I$ | 0 |
| $u = -0.421925 + 0.731310I$ $a = -0.889218 + 0.084686I$ $b = 1.110590 + 0.288943I$ | $0.35974 - 3.47491I$ | 0 |
| $u = -0.421925 - 0.731310I$ $a = -0.889218 - 0.084686I$ $b = 1.110590 - 0.288943I$ | $0.35974 + 3.47491I$ | 0 |
| $u = 0.073826 + 0.813368I$ $a = -1.60062 + 0.49196I$ $b = 0.899591 - 0.403821I$ | $7.79839 - 0.95510I$ | 0 |
| $u = 0.073826 - 0.813368I$ $a = -1.60062 - 0.49196I$ $b = 0.899591 + 0.403821I$ | $7.79839 + 0.95510I$ | 0 |
| $u = 1.20375$ $a = 0.466459$ $b = 0.00998561$ | -2.53324 | 0 |
| $u = -0.635177 + 1.044370I$ $a = 0.662353 - 0.064701I$ $b = -1.059810 - 0.347777I$ | $7.02919 - 5.71442I$ | 0 |
| $u = -0.635177 - 1.044370I$ $a = 0.662353 + 0.064701I$ $b = -1.059810 + 0.347777I$ | $7.02919 + 5.71442I$ | 0 |
| $u = 0.509200 + 1.127410I$ $a = 0.472655 + 0.551529I$ $b = -1.195790 - 0.258865I$ | $1.51094 - 5.10157I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.509200 - 1.127410I$ $a = 0.472655 - 0.551529I$ $b = -1.195790 + 0.258865I$ | $1.51094 + 5.10157I$ | 0 |
| $u = -0.365776 + 0.653749I$ $a = -0.081284 + 1.401450I$ $b = -0.287242 - 1.062190I$ | $10.02620 + 6.30984I$ | 0 |
| $u = -0.365776 - 0.653749I$ $a = -0.081284 - 1.401450I$ $b = -0.287242 + 1.062190I$ | $10.02620 - 6.30984I$ | 0 |
| $u = 0.129351 + 0.704209I$ $a = -0.679190 - 0.828173I$ $b = 0.103762 + 0.686088I$ | $5.33081 - 1.86604I$ | $0. + 3.90648I$ |
| $u = 0.129351 - 0.704209I$ $a = -0.679190 + 0.828173I$ $b = 0.103762 - 0.686088I$ | $5.33081 + 1.86604I$ | $0. - 3.90648I$ |
| $u = 1.223970 + 0.401442I$ $a = -0.462473 - 0.267648I$ $b = -0.073035 - 0.139352I$ | $2.07456 - 2.27551I$ | 0 |
| $u = 1.223970 - 0.401442I$ $a = -0.462473 + 0.267648I$ $b = -0.073035 + 0.139352I$ | $2.07456 + 2.27551I$ | 0 |
| $u = -1.263230 + 0.374502I$ $a = -0.746639 + 0.577828I$ $b = 0.860702 + 0.092884I$ | $3.67205 + 5.24598I$ | 0 |
| $u = -1.263230 - 0.374502I$ $a = -0.746639 - 0.577828I$ $b = 0.860702 - 0.092884I$ | $3.67205 - 5.24598I$ | 0 |
| $u = -0.266580 + 0.588131I$ $a = 1.35207 - 2.09086I$ $b = -1.122390 + 0.353863I$ | $0.18453 + 2.81647I$ | $-0.56699 - 5.14375I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -0.266580 - 0.588131I$ $a = 1.35207 + 2.09086I$ $b = -1.122390 - 0.353863I$ | $0.18453 - 2.81647I$ | $-0.56699 + 5.14375I$ |
| $u = -0.383725 + 0.510780I$ $a = -0.35311 - 1.52762I$ $b = 0.127056 + 0.881304I$ | $3.55177 + 3.39819I$ | $0.84018 - 6.92415I$ |
| $u = -0.383725 - 0.510780I$ $a = -0.35311 + 1.52762I$ $b = 0.127056 - 0.881304I$ | $3.55177 - 3.39819I$ | $0.84018 + 6.92415I$ |
| $u = -0.631511$ $a = 0.479038$ $b = -1.15135$ | -1.55302 | -7.94170 |
| $u = 1.382990 + 0.055539I$ $a = 0.565031 - 0.732391I$ $b = -0.238430 + 0.708558I$ | $-2.35948 - 0.82108I$ | 0 |
| $u = 1.382990 - 0.055539I$ $a = 0.565031 + 0.732391I$ $b = -0.238430 - 0.708558I$ | $-2.35948 + 0.82108I$ | 0 |
| $u = -1.375540 + 0.190726I$ $a = 0.047286 + 0.731163I$ $b = 0.378703 - 1.174100I$ | $0.57233 + 4.93402I$ | 0 |
| $u = -1.375540 - 0.190726I$ $a = 0.047286 - 0.731163I$ $b = 0.378703 + 1.174100I$ | $0.57233 - 4.93402I$ | 0 |
| $u = -1.391300 + 0.009231I$ $a = 0.421080 + 0.806075I$ $b = 1.57036 - 0.71094I$ | $-2.89241 + 2.70347I$ | 0 |
| $u = -1.391300 - 0.009231I$ $a = 0.421080 - 0.806075I$ $b = 1.57036 + 0.71094I$ | $-2.89241 - 2.70347I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -0.491766 + 0.337151I$ $a = 1.52671 + 1.10854I$ $b = 0.131068 - 0.467644I$ | $3.13228 - 0.27068I$ | $1.77490 - 1.85357I$ |
| $u = -0.491766 - 0.337151I$ $a = 1.52671 - 1.10854I$ $b = 0.131068 + 0.467644I$ | $3.13228 + 0.27068I$ | $1.77490 + 1.85357I$ |
| $u = -1.41338 + 0.09716I$ $a = 1.63265 - 0.41394I$ $b = 1.024190 - 0.080144I$ | $3.14701 + 6.03465I$ | 0 |
| $u = -1.41338 - 0.09716I$ $a = 1.63265 + 0.41394I$ $b = 1.024190 + 0.080144I$ | $3.14701 - 6.03465I$ | 0 |
| $u = 1.42796 + 0.02959I$ $a = 0.701919 + 0.520870I$ $b = 1.53124 - 0.11552I$ | $-3.60289 - 2.95271I$ | 0 |
| $u = 1.42796 - 0.02959I$ $a = 0.701919 - 0.520870I$ $b = 1.53124 + 0.11552I$ | $-3.60289 + 2.95271I$ | 0 |
| $u = -1.43990 + 0.06670I$ $a = -0.012806 - 0.753944I$ $b = -0.183222 + 0.885034I$ | $-5.79294 + 2.10750I$ | 0 |
| $u = -1.43990 - 0.06670I$ $a = -0.012806 + 0.753944I$ $b = -0.183222 - 0.885034I$ | $-5.79294 - 2.10750I$ | 0 |
| $u = 1.43586 + 0.20746I$ $a = -0.41468 + 1.49380I$ $b = -1.226660 - 0.529473I$ | $-5.35379 - 5.68624I$ | 0 |
| $u = 1.43586 - 0.20746I$ $a = -0.41468 - 1.49380I$ $b = -1.226660 + 0.529473I$ | $-5.35379 + 5.68624I$ | 0 |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = 1.45502 + 0.14563I$ $a = -0.310433 + 0.637258I$ $b = 0.052332 - 1.193180I$ | $-2.41136 - 5.70802I$ | 0 |
| $u = 1.45502 - 0.14563I$ $a = -0.310433 - 0.637258I$ $b = 0.052332 + 1.193180I$ | $-2.41136 + 5.70802I$ | 0 |
| $u = 0.427368 + 0.306228I$ $a = 0.86564 + 1.62484I$ $b = -1.109570 - 0.540320I$ | $-1.27209 - 2.61374I$ | $-8.1476 + 11.5732I$ |
| $u = 0.427368 - 0.306228I$ $a = 0.86564 - 1.62484I$ $b = -1.109570 + 0.540320I$ | $-1.27209 + 2.61374I$ | $-8.1476 - 11.5732I$ |
| $u = 1.47311 + 0.21321I$ $a = 0.208305 - 0.640823I$ $b = -0.17007 + 1.45424I$ | $4.02421 - 9.40391I$ | 0 |
| $u = 1.47311 - 0.21321I$ $a = 0.208305 + 0.640823I$ $b = -0.17007 - 1.45424I$ | $4.02421 + 9.40391I$ | 0 |
| $u = 1.49510 + 0.04344I$ $a = -0.581323 + 0.412900I$ $b = -1.51105 - 0.29367I$ | $-8.12584 - 0.44534I$ | 0 |
| $u = 1.49510 - 0.04344I$ $a = -0.581323 - 0.412900I$ $b = -1.51105 + 0.29367I$ | $-8.12584 + 0.44534I$ | 0 |
| $u = -0.469577 + 0.132148I$ $a = 0.607127 + 0.383204I$ $b = 1.022440 - 0.664659I$ | $2.30869 + 3.10979I$ | $6.28767 + 0.10476I$ |
| $u = -0.469577 - 0.132148I$ $a = 0.607127 - 0.383204I$ $b = 1.022440 + 0.664659I$ | $2.30869 - 3.10979I$ | $6.28767 - 0.10476I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = -1.51638 + 0.07781I$ $a = -0.311568 - 0.786453I$ $b = -1.38732 + 0.85466I$ | $-7.83146 + 3.89655I$ | 0 |
| $u = -1.51638 - 0.07781I$ $a = -0.311568 + 0.786453I$ $b = -1.38732 - 0.85466I$ | $-7.83146 - 3.89655I$ | 0 |
| $u = 1.54839 + 0.05770I$ $a = 0.443126 - 0.341427I$ $b = 1.47115 + 0.67450I$ | $-4.62587 - 3.85006I$ | 0 |
| $u = 1.54839 - 0.05770I$ $a = 0.443126 + 0.341427I$ $b = 1.47115 - 0.67450I$ | $-4.62587 + 3.85006I$ | 0 |
| $u = 1.52731 + 0.26111I$ $a = 0.475990 - 1.199960I$ $b = 1.36229 + 0.58251I$ | $-6.51610 - 11.88980I$ | 0 |
| $u = 1.52731 - 0.26111I$ $a = 0.475990 + 1.199960I$ $b = 1.36229 - 0.58251I$ | $-6.51610 + 11.88980I$ | 0 |
| $u = -1.54118 + 0.17061I$ $a = -0.318296 - 1.038990I$ $b = -1.170070 + 0.386041I$ | $-8.66512 + 2.45063I$ | 0 |
| $u = -1.54118 - 0.17061I$ $a = -0.318296 + 1.038990I$ $b = -1.170070 - 0.386041I$ | $-8.66512 - 2.45063I$ | 0 |
| $u = 0.277564 + 0.317493I$ $a = 0.560535 + 1.041500I$ $b = -0.079901 - 0.308666I$ | $-0.183792 - 0.864472I$ | $-4.29913 + 7.86972I$ |
| $u = 0.277564 - 0.317493I$ $a = 0.560535 - 1.041500I$ $b = -0.079901 + 0.308666I$ | $-0.183792 + 0.864472I$ | $-4.29913 - 7.86972I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -1.56054 + 0.25243I$ $a = 0.375410 + 0.928178I$ $b = 1.353380 - 0.393780I$ | $-10.60940 + 6.66212I$ | 0 |
| $u = -1.56054 - 0.25243I$ $a = 0.375410 - 0.928178I$ $b = 1.353380 + 0.393780I$ | $-10.60940 - 6.66212I$ | 0 |
| $u = -1.55851 + 0.35179I$ $a = -0.349517 - 0.886182I$ $b = -1.44084 + 0.41048I$ | $-5.19961 + 10.21640I$ | 0 |
| $u = -1.55851 - 0.35179I$ $a = -0.349517 + 0.886182I$ $b = -1.44084 - 0.41048I$ | $-5.19961 - 10.21640I$ | 0 |
| $u = 1.57773 + 0.32081I$ $a = -0.413286 + 1.072970I$ $b = -1.42145 - 0.65571I$ | $-0.1084 - 16.5867I$ | 0 |
| $u = 1.57773 - 0.32081I$ $a = -0.413286 - 1.072970I$ $b = -1.42145 + 0.65571I$ | $-0.1084 + 16.5867I$ | 0 |
| $u = -1.60922 + 0.08030I$ $a = 0.270773 + 0.717828I$ $b = 1.37271 - 1.07445I$ | $-3.46237 + 4.60398I$ | 0 |
| $u = -1.60922 - 0.08030I$ $a = 0.270773 - 0.717828I$ $b = 1.37271 + 1.07445I$ | $-3.46237 - 4.60398I$ | 0 |
| $u = 0.125878 + 0.322657I$ $a = 3.80205 - 2.84036I$ $b = 0.779351 + 0.457129I$ | $8.28711 - 4.58904I$ | $1.66459 + 8.40382I$ |
| $u = 0.125878 - 0.322657I$ $a = 3.80205 + 2.84036I$ $b = 0.779351 - 0.457129I$ | $8.28711 + 4.58904I$ | $1.66459 - 8.40382I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 1.55309 + 0.60898I$ $a = -0.171676 + 0.555702I$ $b = -1.234490 - 0.047231I$ | $-1.64260 - 2.30540I$ | 0 |
| $u = 1.55309 - 0.60898I$ $a = -0.171676 - 0.555702I$ $b = -1.234490 + 0.047231I$ | $-1.64260 + 2.30540I$ | 0 |
| $u = 1.64697 + 0.30699I$ $a = 0.307607 - 0.488246I$ $b = 1.146860 + 0.090509I$ | $-6.04528 - 1.09420I$ | 0 |
| $u = 1.64697 - 0.30699I$ $a = 0.307607 + 0.488246I$ $b = 1.146860 - 0.090509I$ | $-6.04528 + 1.09420I$ | 0 |
| $u = -0.124790$ $a = 13.9437$ $b = -0.470722$ | 2.89659 | 10.5150 |
| $u = -0.0876446 + 0.0176727I$ $a = 2.61863 - 7.91258I$ $b = 1.41551 - 0.34649I$ | $1.67209 + 2.65200I$ | $-6.68294 + 0.54441I$ |
| $u = -0.0876446 - 0.0176727I$ $a = 2.61863 + 7.91258I$ $b = 1.41551 + 0.34649I$ | $1.67209 - 2.65200I$ | $-6.68294 - 0.54441I$ |

II.

$$I_2^u = \langle 3u^{20} - 5u^{19} + \dots + b - 2, -3u^{20} + 4u^{19} + \dots + a + 4, u^{21} - 14u^{19} + \dots + u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 3u^{20} - 4u^{19} + \dots + 12u - 4 \\ -3u^{20} + 5u^{19} + \dots - 4u + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{20} - 2u^{19} + \dots - 4u + 3 \\ -4u^{20} + 5u^{19} + \dots - 5u + 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^{19} - 3u^{18} + \dots + 8u - 2 \\ -3u^{20} + 5u^{19} + \dots - 4u + 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -3u^{20} + 3u^{19} + \dots - 7u + 5 \\ u^{20} - u^{19} + \dots + 2u - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2u^{20} - 3u^{19} + \dots + 8u - 3 \\ u^{19} - u^{18} + \dots - 5u^2 - 2u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -3u^{20} + 4u^{19} + \dots - 4u + 3 \\ -u^{20} + 3u^{19} + \dots - u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -2u^{20} + 4u^{19} + \dots - 5u^2 + 5u \\ -7u^{20} + 10u^{19} + \dots - 9u + 5 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= 7u^{20} - 13u^{19} - 84u^{18} + 158u^{17} + 425u^{16} - 809u^{15} - 1168u^{14} + 2256u^{13} + 1870u^{12} - 3697u^{11} - 1742u^{10} + 3586u^9 + 919u^8 - 1994u^7 - 306u^6 + 636u^5 + 87u^4 - 158u^3 + 7u^2 + 24u - 16$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|------------|---------------------------------------|
| c_1, c_2 | $u^{21} - 14u^{19} + \dots + u - 1$ |
| c_3 | $u^{21} + u^{20} + \dots - u + 1$ |
| c_4 | $u^{21} - 2u^{19} + \dots - 2u - 1$ |
| c_5 | $u^{21} - 14u^{19} + \dots + u + 1$ |
| c_6, c_7 | $u^{21} + u^{20} + \dots - 9u^2 - 1$ |
| c_8 | $u^{21} - u^{20} + \dots - u - 1$ |
| c_9 | $u^{21} + 3u^{20} + \dots + 9u^2 - 1$ |
| c_{10} | $u^{21} + 3u^{19} + \dots - 8u^2 + 1$ |
| c_{11} | $u^{21} - u^{20} + \dots + 9u^2 + 1$ |
| c_{12} | $u^{21} - 3u^{20} + \dots - 9u^2 + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------|---------------------------------------|
| c_1, c_2, c_5 | $y^{21} - 28y^{20} + \dots + 9y - 1$ |
| c_3, c_8 | $y^{21} - 21y^{20} + \dots + 11y - 1$ |
| c_4 | $y^{21} - 4y^{20} + \dots - 10y - 1$ |
| c_6, c_7, c_{11} | $y^{21} + 21y^{20} + \dots - 18y - 1$ |
| c_9, c_{12} | $y^{21} - 17y^{20} + \dots + 18y - 1$ |
| c_{10} | $y^{21} + 6y^{20} + \dots + 16y - 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.980123 + 0.287889I$ $a = -0.202219 - 0.402737I$ $b = 0.821250 + 0.530110I$ | $1.64253 - 3.32447I$ | $-6.73227 + 3.23371I$ |
| $u = 0.980123 - 0.287889I$ $a = -0.202219 + 0.402737I$ $b = 0.821250 - 0.530110I$ | $1.64253 + 3.32447I$ | $-6.73227 - 3.23371I$ |
| $u = 1.12877$ $a = 0.459570$ $b = -0.644952$ | -3.11468 | -14.6860 |
| $u = -1.23262$ $a = 1.72801$ $b = -0.411550$ | -0.191889 | 1.35120 |
| $u = -1.267400 + 0.189837I$ $a = -1.145350 + 0.468508I$ $b = 0.372541 - 0.430174I$ | $5.01252 + 5.95890I$ | $0.38975 - 5.02691I$ |
| $u = -1.267400 - 0.189837I$ $a = -1.145350 - 0.468508I$ $b = 0.372541 + 0.430174I$ | $5.01252 - 5.95890I$ | $0.38975 + 5.02691I$ |
| $u = 0.513299 + 0.356158I$ $a = -0.298859 - 0.889580I$ $b = 1.198820 + 0.616343I$ | $1.84979 - 3.43907I$ | $-5.77787 + 8.99517I$ |
| $u = 0.513299 - 0.356158I$ $a = -0.298859 + 0.889580I$ $b = 1.198820 - 0.616343I$ | $1.84979 + 3.43907I$ | $-5.77787 - 8.99517I$ |
| $u = -0.428378 + 0.445644I$ $a = 0.59208 + 1.78035I$ $b = 0.635250 + 0.374830I$ | $8.00683 - 3.75384I$ | $-1.41538 + 0.52564I$ |
| $u = -0.428378 - 0.445644I$ $a = 0.59208 - 1.78035I$ $b = 0.635250 - 0.374830I$ | $8.00683 + 3.75384I$ | $-1.41538 - 0.52564I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = -1.50488 + 0.09457I$ $a = -0.300529 - 0.973392I$ $b = -1.25356 + 0.73428I$ | $-7.16310 + 3.43030I$ | $-3.74353 - 1.15763I$ |
| $u = -1.50488 - 0.09457I$ $a = -0.300529 + 0.973392I$ $b = -1.25356 - 0.73428I$ | $-7.16310 - 3.43030I$ | $-3.74353 + 1.15763I$ |
| $u = -1.54873 + 0.07946I$ $a = 0.337710 + 0.596656I$ $b = 1.56117 - 0.99590I$ | $-5.11343 + 4.80864I$ | $-8.81380 - 6.84118I$ |
| $u = -1.54873 - 0.07946I$ $a = 0.337710 - 0.596656I$ $b = 1.56117 + 0.99590I$ | $-5.11343 - 4.80864I$ | $-8.81380 + 6.84118I$ |
| $u = -0.428907$ $a = -3.99233$ $b = -0.611834$ | 2.58386 | -16.1200 |
| $u = 1.55858 + 0.20556I$ $a = -0.410534 + 0.603726I$ $b = -1.123510 - 0.131583I$ | $-5.66515 - 0.90405I$ | $-2.75648 - 2.17520I$ |
| $u = 1.55858 - 0.20556I$ $a = -0.410534 - 0.603726I$ $b = -1.123510 + 0.131583I$ | $-5.66515 + 0.90405I$ | $-2.75648 + 2.17520I$ |
| $u = 0.213126 + 0.328797I$ $a = 2.06155 + 1.99092I$ $b = -1.118860 - 0.369484I$ | $-1.13219 - 1.99292I$ | $-5.58755 - 0.19985I$ |
| $u = 0.213126 - 0.328797I$ $a = 2.06155 - 1.99092I$ $b = -1.118860 + 0.369484I$ | $-1.13219 + 1.99292I$ | $-5.58755 + 0.19985I$ |
| $u = 1.75063 + 0.30855I$ $a = 0.268529 - 0.284726I$ $b = 1.241070 + 0.159795I$ | $-2.01124 - 1.49085I$ | $-8.33532 + 1.09996I$ |

| | Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-------|------------------------|---------------------------------------|-----------------------|
| $u =$ | $1.75063 - 0.30855I$ | | |
| $a =$ | $0.268529 + 0.284726I$ | $-2.01124 + 1.49085I$ | $-8.33532 - 1.09996I$ |
| $b =$ | $1.241070 - 0.159795I$ | | |

$$\text{III. } I_3^u = \langle b + 1, -u^5 + 2u^4 + 2u^3 - 4u^2 + a - u + 1, u^6 - 3u^5 + 6u^3 - 4u^2 + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^5 - 2u^4 - 2u^3 + 4u^2 + u - 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^4 - 2u^3 - u^2 + 2u + 1 \\ u^5 - 2u^4 - 2u^3 + 5u^2 - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^5 - 2u^4 - 2u^3 + 4u^2 + u - 2 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 + 2u^2 - 2 \\ -u^5 + 2u^4 + u^3 - 4u^2 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^5 - 2u^4 - 2u^3 + 4u^2 + u - 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^5 + u^4 + 2u^3 - 2u^2 + 2u \\ -3u^5 + 4u^4 + 6u^3 - 7u^2 + 2u + 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|--------------------------------|---|
| c_1, c_2, c_5 | $u^6 + 3u^5 - 6u^3 - 4u^2 + 1$ |
| c_3, c_8 | $u^6 - 3u^5 + 6u^3 - 4u^2 + 1$ |
| c_4 | $u^6 + u^5 - 2u^4 + 6u^3 - 4u^2 + 2u + 1$ |
| c_6, c_7, c_{10} c_{11} | $u^6 - u^5 + 2u^4 - 2u^3 - 1$ |
| c_9, c_{12} | $(u + 1)^6$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------------|--|
| c_1, c_2, c_3 c_5, c_8 | $y^6 - 9y^5 + 28y^4 - 34y^3 + 16y^2 - 8y + 1$ |
| c_4 | $y^6 - 5y^5 - 16y^4 - 22y^3 - 12y^2 - 12y + 1$ |
| c_6, c_7, c_{10} c_{11} | $y^6 + 3y^5 - 6y^3 - 4y^2 + 1$ |
| c_9, c_{12} | $(y - 1)^6$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------|
| $u = 0.558227 + 0.461646I$ $a = 0.64026 + 1.59235I$ $b = -1.00000$ | -1.64493 | -6.00000 |
| $u = 0.558227 - 0.461646I$ $a = 0.64026 - 1.59235I$ $b = -1.00000$ | -1.64493 | -6.00000 |
| $u = -1.39152$ $a = -1.97338$ $b = -1.00000$ | -1.64493 | -6.00000 |
| $u = -0.401914$ $a = -0.688603$ $b = -1.00000$ | -1.64493 | -6.00000 |
| $u = 1.83849 + 0.16576I$ $a = -0.309272 + 0.392670I$ $b = -1.00000$ | -1.64493 | -6.00000 |
| $u = 1.83849 - 0.16576I$ $a = -0.309272 - 0.392670I$ $b = -1.00000$ | -1.64493 | -6.00000 |

$$\text{IV. } I_4^u = \langle b + 1, a - 1, u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) **u**-Polynomials at the component

| Crossings | u -Polynomials at each crossing |
|---|--|
| c_1, c_2, c_4 c_5 | $u - 1$ |
| c_3, c_6, c_7 c_8, c_9, c_{10} c_{11}, c_{12} | $u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--------------------------|------------------------------------|
| c_1, c_2, c_3 | $y - 1$ |
| c_4, c_5, c_6 | |
| c_7, c_8, c_9 | |
| c_{10}, c_{11}, c_{12} | |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = -1.00000$ | | |
| $a = 1.00000$ | -1.64493 | -6.00000 |
| $b = -1.00000$ | | |

V. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|------------|--|
| c_1, c_2 | $(u-1)(u^6 + 3u^5 + \dots - 4u^2 + 1)(u^{21} - 14u^{19} + \dots + u - 1)$ $\cdot (u^{87} + 5u^{86} + \dots - 31u + 1)$ |
| c_3 | $(u+1)(u^6 - 3u^5 + \dots - 4u^2 + 1)(u^{21} + u^{20} + \dots - u + 1)$ $\cdot (u^{87} + 2u^{86} + \dots + 1867u - 1459)$ |
| c_4 | $(u-1)(u^6 + u^5 + \dots + 2u + 1)(u^{21} - 2u^{19} + \dots - 2u - 1)$ $\cdot (u^{87} - u^{86} + \dots - 108842u + 15817)$ |
| c_5 | $(u-1)(u^6 + 3u^5 + \dots - 4u^2 + 1)(u^{21} - 14u^{19} + \dots + u + 1)$ $\cdot (u^{87} + 5u^{86} + \dots - 31u + 1)$ |
| c_6, c_7 | $(u+1)(u^6 - u^5 + 2u^4 - 2u^3 - 1)(u^{21} + u^{20} + \dots - 9u^2 - 1)$ $\cdot (u^{87} + 2u^{86} + \dots - 36u + 7)$ |
| c_8 | $(u+1)(u^6 - 3u^5 + \dots - 4u^2 + 1)(u^{21} - u^{20} + \dots - u - 1)$ $\cdot (u^{87} + 2u^{86} + \dots + 1867u - 1459)$ |
| c_9 | $((u+1)^7)(u^{21} + 3u^{20} + \dots + 9u^2 - 1)(u^{87} - 9u^{86} + \dots + 784u - 8)$ |
| c_{10} | $(u+1)(u^6 - u^5 + 2u^4 - 2u^3 - 1)(u^{21} + 3u^{19} + \dots - 8u^2 + 1)$ $\cdot (u^{87} + 3u^{86} + \dots + 619168u + 590297)$ |
| c_{11} | $(u+1)(u^6 - u^5 + 2u^4 - 2u^3 - 1)(u^{21} - u^{20} + \dots + 9u^2 + 1)$ $\cdot (u^{87} + 2u^{86} + \dots - 36u + 7)$ |
| c_{12} | $((u+1)^7)(u^{21} - 3u^{20} + \dots - 9u^2 + 1)(u^{87} - 9u^{86} + \dots + 784u - 8)$ |

VI. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|--------------------|---|
| c_1, c_2, c_5 | $(y-1)(y^6 - 9y^5 + 28y^4 - 34y^3 + 16y^2 - 8y + 1)$ $\cdot (y^{21} - 28y^{20} + \dots + 9y - 1)(y^{87} - 91y^{86} + \dots + 301y - 1)$ |
| c_3, c_8 | $(y-1)(y^6 - 9y^5 + 28y^4 - 34y^3 + 16y^2 - 8y + 1)$ $\cdot (y^{21} - 21y^{20} + \dots + 11y - 1)$ $\cdot (y^{87} - 64y^{86} + \dots + 35213103y - 2128681)$ |
| c_4 | $(y-1)(y^6 - 5y^5 - 16y^4 - 22y^3 - 12y^2 - 12y + 1)$ $\cdot (y^{21} - 4y^{20} + \dots - 10y - 1)$ $\cdot (y^{87} + 33y^{86} + \dots + 197455366y - 250177489)$ |
| c_6, c_7, c_{11} | $(y-1)(y^6 + 3y^5 + \dots - 4y^2 + 1)(y^{21} + 21y^{20} + \dots - 18y - 1)$ $\cdot (y^{87} + 90y^{86} + \dots + 2206y - 49)$ |
| c_9, c_{12} | $((y-1)^7)(y^{21} - 17y^{20} + \dots + 18y - 1)$ $\cdot (y^{87} - 59y^{86} + \dots + 638432y - 64)$ |
| c_{10} | $(y-1)(y^6 + 3y^5 + \dots - 4y^2 + 1)(y^{21} + 6y^{20} + \dots + 16y - 1)$ $\cdot (y^{87} - 25y^{86} + \dots + 7264616979632y - 348450548209)$ |