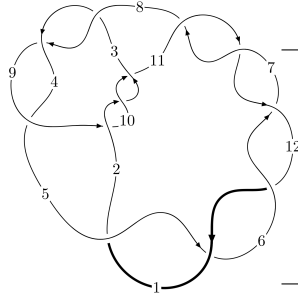
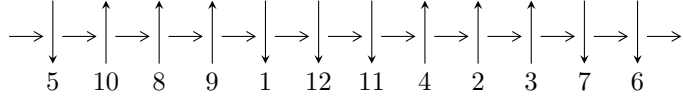


12a₁₂₈₆ (K12a₁₂₈₆)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$3,8 \xrightarrow{c_3} 4 \xrightarrow{c_8} 9 \xrightarrow{c_4} 5,11 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 12 \xrightarrow{c_6} 6 \xrightarrow{c_{10}} 10 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \twoheadrightarrow c_5, c_9, c_{12}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle b - u, -u^{12} + u^{11} + 8u^{10} - 7u^9 - 23u^8 + 15u^7 + 26u^6 - 6u^5 - 8u^4 - 4u^3 + 2u^2 + 4a - 11u, \\ u^{13} - u^{12} - 9u^{11} + 8u^{10} + 31u^9 - 22u^8 - 49u^7 + 21u^6 + 34u^5 - 2u^4 - 10u^3 + 3u^2 + 2u + 1 \rangle$$

$$I_2^u = \langle 5u^{13} + u^{12} - 28u^{11} - 14u^{10} + 50u^9 + 49u^8 - 41u^7 - 68u^6 + 68u^5 + 70u^4 - 87u^3 - 79u^2 + 6b + 18u + 30, \\ 17u^{13} + 7u^{12} + \dots + 24a + 105, \\ u^{14} - u^{13} - 6u^{12} + 4u^{11} + 14u^{10} - 2u^9 - 21u^8 - 5u^7 + 31u^6 - u^5 - 35u^4 + 3u^3 + 23u^2 + 5u - 8 \rangle$$

$$I_3^u = \langle b - 1, a^2 + 3, u + 1 \rangle$$

$$I_4^u = \langle b + 1, a^2 + 1, u - 1 \rangle$$

$$I_5^u = \langle b - 1, a, u + 1 \rangle$$

* 5 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 32 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } \Gamma_1^u = \langle b - u, -u^{12} + u^{11} + \dots + 4a - 11u, u^{13} - u^{12} + \dots + 2u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{4}u^{12} - \frac{1}{4}u^{11} + \dots - \frac{1}{2}u^2 + \frac{11}{4}u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{2}u^{12} - \frac{3}{4}u^{11} + \dots - \frac{1}{2}u + \frac{1}{4} \\ \frac{1}{4}u^{12} - \frac{1}{4}u^{11} + \dots - \frac{1}{2}u^2 + \frac{3}{4}u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}u^{12} - \frac{1}{2}u^{11} + \dots + 2u + \frac{1}{2} \\ \frac{1}{4}u^{12} - \frac{1}{2}u^{11} + \dots + \frac{3}{4}u + \frac{1}{4} \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{4}u^{12} + \frac{3}{4}u^{11} + \dots - 2u^2 - \frac{7}{4}u \\ \frac{1}{4}u^{12} - \frac{9}{4}u^{10} + \dots + \frac{1}{4}u + \frac{1}{4} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{4}u^{12} - \frac{1}{4}u^{11} + \dots - \frac{1}{2}u^2 + \frac{7}{4}u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{4}u^{11} - \frac{1}{4}u^{10} + \dots - \frac{1}{2}u + \frac{3}{4} \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{4}u^{11} - \frac{1}{4}u^{10} + \dots - \frac{1}{2}u + \frac{3}{4} \\ -\frac{1}{4}u^{11} + \frac{1}{4}u^{10} + \dots + \frac{1}{2}u + \frac{1}{4} \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{5}{2}u^{12} - \frac{9}{2}u^{11} - 21u^{10} + \frac{75}{2}u^9 + \frac{131}{2}u^8 - \frac{225}{2}u^7 - 91u^6 + 136u^5 + 59u^4 - 55u^3 - 26u^2 + \frac{45}{2}u + 7$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	$u^{13} + 3u^{12} + \dots + 12u + 2$
c_2, c_3, c_4 c_8, c_9, c_{10}	$u^{13} + u^{12} + \dots + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	$y^{13} + 19y^{12} + \dots - 36y - 4$
c_2, c_3, c_4 c_8, c_9, c_{10}	$y^{13} - 19y^{12} + \dots - 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.640373 + 0.415565I$ $a = -1.25824 + 1.93661I$ $b = -0.640373 + 0.415565I$	$15.1852 - 1.4688I$	$6.47409 + 4.73042I$
$u = -0.640373 - 0.415565I$ $a = -1.25824 - 1.93661I$ $b = -0.640373 - 0.415565I$	$15.1852 + 1.4688I$	$6.47409 - 4.73042I$
$u = 0.481196 + 0.382474I$ $a = 1.09706 + 1.46655I$ $b = 0.481196 + 0.382474I$	$4.66648 + 1.38672I$	$6.13236 - 5.06598I$
$u = 0.481196 - 0.382474I$ $a = 1.09706 - 1.46655I$ $b = 0.481196 - 0.382474I$	$4.66648 - 1.38672I$	$6.13236 + 5.06598I$
$u = -1.60418$ $a = 0.434953$ $b = -1.60418$	10.2165	6.80950
$u = 1.61970 + 0.12491I$ $a = -0.311845 + 0.455641I$ $b = 1.61970 + 0.12491I$	$12.32310 + 4.09027I$	$9.54540 - 4.06441I$
$u = 1.61970 - 0.12491I$ $a = -0.311845 - 0.455641I$ $b = 1.61970 - 0.12491I$	$12.32310 - 4.09027I$	$9.54540 + 4.06441I$
$u = -0.187914 + 0.306655I$ $a = -0.476417 + 0.917350I$ $b = -0.187914 + 0.306655I$	$0.020555 - 0.726577I$	$0.71558 + 9.62371I$
$u = -0.187914 - 0.306655I$ $a = -0.476417 - 0.917350I$ $b = -0.187914 - 0.306655I$	$0.020555 + 0.726577I$	$0.71558 - 9.62371I$
$u = -1.65131 + 0.26273I$ $a = 0.042681 + 0.832421I$ $b = -1.65131 + 0.26273I$	$19.0260 - 7.1684I$	$11.29845 + 3.79891I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.65131 - 0.26273I$	$19.0260 + 7.1684I$	$11.29845 - 3.79891I$
$a = 0.042681 - 0.832421I$		
$b = -1.65131 - 0.26273I$		
$u = 1.68079 + 0.37590I$	$-8.62649 + 8.95936I$	$11.42936 - 3.31793I$
$a = 0.189278 + 1.048750I$		
$b = 1.68079 + 0.37590I$		
$u = 1.68079 - 0.37590I$	$-8.62649 - 8.95936I$	$11.42936 + 3.31793I$
$a = 0.189278 - 1.048750I$		
$b = 1.68079 - 0.37590I$		

$$\langle 5u^{13} + u^{12} + \dots + 6b + 30, 17u^{13} + 7u^{12} + \dots + 24a + 105, u^{14} - u^{13} + \dots + 5u - 8 \rangle$$

II. $I_2^u =$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.708333u^{13} - 0.291667u^{12} + \dots - 0.125000u - 4.37500 \\ -\frac{5}{6}u^{13} - \frac{1}{6}u^{12} + \dots - 3u - 5 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.208333u^{13} - 0.125000u^{12} + \dots - 0.458333u - 1.37500 \\ \frac{1}{2}u^{13} + \frac{1}{6}u^{12} + \dots + \frac{2}{3}u + 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{5}{12}u^{13} - \frac{1}{4}u^{12} + \dots + \frac{1}{12}u - \frac{11}{4} \\ -\frac{5}{3}u^{13} - \frac{1}{3}u^{12} + \dots - 3u - 10 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.458333u^{13} - 0.208333u^{12} + \dots - 0.541667u - 2.12500 \\ \frac{1}{3}u^{13} + \frac{1}{6}u^{12} + \dots + \frac{1}{2}u + \frac{7}{3} \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{8}u^{13} - \frac{1}{8}u^{12} + \dots + \frac{23}{8}u + \frac{5}{8} \\ -\frac{5}{6}u^{13} - \frac{1}{6}u^{12} + \dots - 3u - 5 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.625000u^{13} - 0.208333u^{12} + \dots - 1.20833u - 5.12500 \\ u^{13} + \frac{1}{3}u^{12} + \dots + \frac{5}{6}u + \frac{23}{3} \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{24}u^{13} + \frac{1}{8}u^{12} + \dots - \frac{17}{24}u - \frac{1}{8} \\ \frac{3}{2}u^{13} + \frac{1}{3}u^{12} + \dots + \frac{11}{6}u + \frac{31}{3} \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{26}{3}u^{13} - \frac{8}{3}u^{12} + 50u^{11} + 28u^{10} - 90u^9 - 92u^8 + \frac{208}{3}u^7 + \frac{392}{3}u^6 - \frac{344}{3}u^5 - 136u^4 + \frac{446}{3}u^3 + 146u^2 - \frac{46}{3}u - \frac{158}{3}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	$(u^7 - u^6 + 6u^5 - 5u^4 + 10u^3 - 6u^2 + 4u - 1)^2$
c_2, c_3, c_4 c_8, c_9, c_{10}	$u^{14} + u^{13} + \dots - 5u - 8$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	$(y^7 + 11y^6 + 46y^5 + 91y^4 + 86y^3 + 34y^2 + 4y - 1)^2$
c_2, c_3, c_4 c_8, c_9, c_{10}	$y^{14} - 13y^{13} + \dots - 393y + 64$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.648339 + 0.868507I$ $a = -0.946848 - 0.814097I$ $b = -1.49879 - 0.07472I$	$11.28970 + 2.92126I$	$9.79653 - 2.94858I$
$u = 0.648339 - 0.868507I$ $a = -0.946848 + 0.814097I$ $b = -1.49879 + 0.07472I$	$11.28970 - 2.92126I$	$9.79653 + 2.94858I$
$u = -1.15470$ $a = -0.288944$ $b = 0.577082$	2.54463	-1.98880
$u = -0.613438 + 0.507408I$ $a = 0.322269 - 0.816953I$ $b = 1.290190 - 0.016333I$	$4.55769 - 1.83261I$	$8.22558 + 5.43914I$
$u = -0.613438 - 0.507408I$ $a = 0.322269 + 0.816953I$ $b = 1.290190 + 0.016333I$	$4.55769 + 1.83261I$	$8.22558 - 5.43914I$
$u = -0.674237 + 1.068950I$ $a = 1.21462 - 0.78780I$ $b = 1.63675 - 0.11855I$	$-16.2972 - 3.4867I$	$9.97231 + 2.18600I$
$u = -0.674237 - 1.068950I$ $a = 1.21462 + 0.78780I$ $b = 1.63675 + 0.11855I$	$-16.2972 + 3.4867I$	$9.97231 - 2.18600I$
$u = 1.290190 + 0.016333I$ $a = 0.161518 - 0.517219I$ $b = -0.613438 - 0.507408I$	$4.55769 + 1.83261I$	$8.22558 - 5.43914I$
$u = 1.290190 - 0.016333I$ $a = 0.161518 + 0.517219I$ $b = -0.613438 + 0.507408I$	$4.55769 - 1.83261I$	$8.22558 + 5.43914I$
$u = 0.577082$ $a = 0.578156$ $b = -1.15470$	2.54463	-1.98880

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.49879 + 0.07472I$ $a = -0.017211 - 0.901687I$ $b = 0.648339 - 0.868507I$	$11.28970 - 2.92126I$	$9.79653 + 2.94858I$
$u = -1.49879 - 0.07472I$ $a = -0.017211 + 0.901687I$ $b = 0.648339 + 0.868507I$	$11.28970 + 2.92126I$	$9.79653 - 2.94858I$
$u = 1.63675 + 0.11855I$ $a = -0.066458 - 1.112970I$ $b = -0.674237 - 1.068950I$	$-16.2972 + 3.4867I$	$9.97231 - 2.18600I$
$u = 1.63675 - 0.11855I$ $a = -0.066458 + 1.112970I$ $b = -0.674237 + 1.068950I$	$-16.2972 - 3.4867I$	$9.97231 + 2.18600I$

$$\text{III. } I_3^u = \langle b - 1, a^2 + 3, u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 3 \\ -a - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2a \\ a - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -3 \\ a + 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a - 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ -a + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 12

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	$u^2 + 3$
c_2, c_8	$(u - 1)^2$
c_3, c_4, c_9 c_{10}	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	$(y + 3)^2$
c_2, c_3, c_4 c_8, c_9, c_{10}	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$ $a = 1.73205I$ $b = 1.00000$	16.4493	12.0000
$u = -1.00000$ $a = -1.73205I$ $b = 1.00000$	16.4493	12.0000

$$\text{IV. } I_4^u = \langle b + 1, a^2 + 1, u - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ -a + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ a \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ -a \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a + 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -a \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -a \\ a + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 12

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	$u^2 + 1$
c_2, c_8	$(u + 1)^2$
c_3, c_4, c_9 c_{10}	$(u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	$(y + 1)^2$
c_2, c_3, c_4 c_8, c_9, c_{10}	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 1.000000I$	6.57974	12.0000
$b = -1.00000$		
$u = 1.00000$		
$a = -1.000000I$	6.57974	12.0000
$b = -1.00000$		

$$\mathbf{V}. I_5^u = \langle b - 1, a, u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 12

(iv) **u**-Polynomials at the component

Crossings	u -Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	u
c_2, c_8	$u - 1$
c_3, c_4, c_9 c_{10}	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	y
c_2, c_3, c_4 c_8, c_9, c_{10}	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_5^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 0$	3.28987	12.0000
$b = 1.00000$		

VI. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	$u(u^2 + 1)(u^2 + 3)(u^7 - u^6 + 6u^5 - 5u^4 + 10u^3 - 6u^2 + 4u - 1)^2$ $\cdot (u^{13} + 3u^{12} + \dots + 12u + 2)$
c_2, c_8	$((u - 1)^3)(u + 1)^2(u^{13} + u^{12} + \dots + 2u - 1)(u^{14} + u^{13} + \dots - 5u - 8)$
c_3, c_4, c_9 c_{10}	$((u - 1)^2)(u + 1)^3(u^{13} + u^{12} + \dots + 2u - 1)(u^{14} + u^{13} + \dots - 5u - 8)$

VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_5, c_6 c_7, c_{11}, c_{12}	$y(y+1)^2(y+3)^2$ $\cdot (y^7 + 11y^6 + 46y^5 + 91y^4 + 86y^3 + 34y^2 + 4y - 1)^2$ $\cdot (y^{13} + 19y^{12} + \dots - 36y - 4)$
c_2, c_3, c_4 c_8, c_9, c_{10}	$((y-1)^5)(y^{13} - 19y^{12} + \dots - 2y - 1)(y^{14} - 13y^{13} + \dots - 393y + 64)$