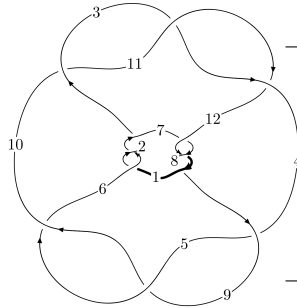
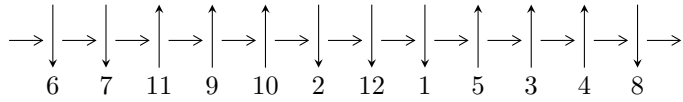


12a₁₂₈₈ (K12a₁₂₈₈)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$1,6 \xrightarrow{c_1} 2 \xrightarrow{c_6} 7 \xrightarrow{c_2} 3,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_5} 5 \xrightarrow{c_9} 9 \xrightarrow{c_4} 4 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \rightsquigarrow c_3, c_7, c_{11}$$

Ideals for irreducible components² of X_{par}

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$\begin{aligned}
I_1^u &= \langle u^{11} + u^{10} - 6u^9 - 5u^8 + 11u^7 + 5u^6 - 7u^5 + 5u^4 + 3u^3 - 4u^2 + 4b - 2u, \\
&\quad - 3u^{11} - 8u^{10} + 9u^9 + 33u^8 - 4u^7 - 30u^6 + 20u^5 - 42u^3 + u^2 + 4a + 10u - 2, \\
&\quad u^{12} + 3u^{11} - 3u^{10} - 14u^9 + u^8 + 18u^7 - 8u^6 - 6u^5 + 24u^4 - 3u^3 - 13u^2 + 6u - 2 \rangle \\
I_2^u &= \langle 1999u^{15} + 3106u^{14} + \dots + 2878b - 22827, -1627u^{15} - 1680u^{14} + \dots + 15829a + 36947, \\
&\quad u^{16} + 3u^{15} + \dots - 2u - 11 \rangle \\
I_3^u &= \langle u^7a - u^7 - 4u^5a - u^4a + 4u^5 + 4u^3a - u^4 + u^2a - 4u^3 + 2au + u^2 + 2b + a + 1, \\
&\quad - u^7a + u^6a + 2u^7 + 3u^5a - 3u^6 - 3u^4a - 7u^5 - 2u^3a + 10u^4 + 2u^2a + 7u^3 + a^2 - au - 7u^2 + a - 5, \\
&\quad u^8 - u^7 - 4u^6 + 3u^5 + 5u^4 - u^3 - u^2 - 3u - 1 \rangle \\
I_4^u &= \langle -u^{11}a - u^{11} + \dots + a + 1, \\
&\quad u^{11} - 5u^9 + u^7a - 2u^8 + 9u^7 - 2u^5a + 8u^6 - u^4a - 4u^5 - 10u^4 + u^2a - 6u^3 + a^2 + 2au + 2u^2 + a + 6u + 2, \\
&\quad u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1 \rangle \\
I_5^u &= \langle 2b - a - 1, a^2 - 3, u - 1 \rangle \\
I_6^u &= \langle 2b - u + 1, 3a - u, u^2 - 3 \rangle \\
I_7^u &= \langle b + 1, a, u - 1 \rangle \\
I_8^u &= \langle 4b^2 - 4b + 5, 2ba - 2b - 3a + 4u + 7, 2bu + 2b - 2a + u + 3, a^2 - 2a + 1, au + a - u - 1, u^2 + 2u + 1 \rangle \\
I_9^u &= \langle a - 1, u + 1 \rangle \\
I_1^v &= \langle a, b - 1, v + 1 \rangle
\end{aligned}$$

* 9 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 78 representations.

* 1 irreducible components of $\dim_{\mathbb{C}} = 1$

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle u^{11} + u^{10} + \dots + 4b - 2u, -3u^{11} - 8u^{10} + \dots + 4a - 2, u^{12} + 3u^{11} + \dots + 6u - 2 \rangle$$

I. $I_1^u =$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{3}{4}u^{11} + 2u^{10} + \dots - \frac{5}{2}u + \frac{1}{2} \\ -\frac{1}{4}u^{11} - \frac{1}{4}u^{10} + \dots + u^2 + \frac{1}{2}u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{4}u^{11} + u^{10} + \dots - \frac{7}{2}u + \frac{1}{2} \\ -\frac{1}{4}u^{10} - \frac{3}{4}u^9 + \dots + \frac{3}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{4}u^{11} - u^{10} + \dots + \frac{3}{2}u - \frac{1}{2} \\ -\frac{1}{4}u^{11} - \frac{1}{4}u^{10} + \dots + u^2 + \frac{1}{2}u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{1}{2}u^{10} - \frac{3}{2}u^9 + \dots - \frac{15}{2}u^2 - 1 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{4}u^{11} + \frac{7}{4}u^9 + \dots - \frac{3}{2}u + \frac{3}{2} \\ -u^{11} - \frac{7}{4}u^{10} + \dots - \frac{5}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -\frac{1}{2}u^{10} - \frac{3}{2}u^9 + \dots + u - 1 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{1}{2}u^{11} + \frac{3}{2}u^{10} + \dots + u + 1 \\ -u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{1}{2}u^{11} + u^{10} - \frac{3}{2}u^9 - \frac{1}{2}u^8 + 3u^7 - 13u^6 - 8u^5 + 22u^4 - 11u^3 - \frac{19}{2}u^2 + 32u - 7$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	$u^{12} - 3u^{11} + \dots - 6u - 2$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	$u^{12} + 3u^{11} + \dots + 6u - 2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3	
c_4, c_5, c_6	$y^{12} - 15y^{11} + \dots + 16y + 4$
c_7, c_8, c_9	
c_{10}, c_{11}, c_{12}	

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.369891 + 0.895594I$ $a = -0.40167 + 1.49298I$ $b = -0.02653 - 1.85453I$	$11.33630 - 5.25212I$	$7.30257 + 4.65184I$
$u = 0.369891 - 0.895594I$ $a = -0.40167 - 1.49298I$ $b = -0.02653 + 1.85453I$	$11.33630 + 5.25212I$	$7.30257 - 4.65184I$
$u = 1.22438$ $a = -1.51331$ $b = -1.43561$	8.64658	-5.83920
$u = 0.740748$ $a = 2.25319$ $b = 0.277533$	10.7798	10.0010
$u = -1.48568 + 0.19251I$ $a = -0.168040 - 0.624592I$ $b = -0.695418 + 0.595170I$	$-11.33630 + 5.25212I$	$-7.30257 - 4.65184I$
$u = -1.48568 - 0.19251I$ $a = -0.168040 + 0.624592I$ $b = -0.695418 - 0.595170I$	$-11.33630 - 5.25212I$	$-7.30257 + 4.65184I$
$u = -1.46094 + 0.44342I$ $a = 0.831296 + 0.555829I$ $b = 1.16548 - 2.08317I$	$15.2352I$	$0. - 7.62682I$
$u = -1.46094 - 0.44342I$ $a = 0.831296 - 0.555829I$ $b = 1.16548 + 2.08317I$	$- 15.2352I$	$0. + 7.62682I$
$u = 0.186071 + 0.332496I$ $a = -0.523030 - 0.852314I$ $b = 0.072588 + 0.300683I$	$- 0.761015I$	$0. + 9.12858I$
$u = 0.186071 - 0.332496I$ $a = -0.523030 + 0.852314I$ $b = 0.072588 - 0.300683I$	$0.761015I$	$0. - 9.12858I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.66904$ $a = 0.443816$ $b = 0.958809$	-10.7798	-10.0010
$u = -1.85286$ $a = -0.660804$ $b = -0.832979$	-8.64658	5.83920

$$\text{II. } I_2^u = \langle 1999u^{15} + 3106u^{14} + \dots + 2878b - 22827, -1627u^{15} - 1680u^{14} + \dots + 15829a + 36947, u^{16} + 3u^{15} + \dots - 2u - 11 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.102786u^{15} + 0.106134u^{14} + \dots - 0.0633647u - 2.33413 \\ -0.694580u^{15} - 1.07922u^{14} + \dots - 5.24913u + 7.93155 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0812433u^{15} + 0.190220u^{14} + \dots + 0.503696u + 0.181502 \\ -1.01355u^{15} - 1.80195u^{14} + \dots - 3.62717u + 5.92113 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0504138u^{15} - 0.0794744u^{14} + \dots + 1.94864u + 1.81092 \\ 0.312370u^{15} + 0.280751u^{14} + \dots + 1.27762u - 4.97672 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.503254u^{15} + 0.504896u^{14} + \dots + 3.85571u - 3.97524 \\ -0.594163u^{15} - 0.777623u^{14} + \dots - 6.03753u + 4.15705 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.434645u^{15} + 0.605534u^{14} + \dots + 2.21884u - 1.80814 \\ 0.0309243u^{15} - 0.298124u^{14} + \dots + 0.944058u - 3.69180 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.0909091u^{15} - 0.272727u^{14} + \dots - 2.18182u + 0.181818 \\ -0.594163u^{15} - 0.777623u^{14} + \dots - 6.03753u + 4.15705 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.377914u^{15} + 0.539579u^{14} + \dots + 1.33679u - 5.79335 \\ 1.00486u^{15} + 1.85198u^{14} + \dots + 2.96873u - 7.53579 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{3610}{1439}u^{15} - \frac{5684}{1439}u^{14} + \dots - \frac{43398}{1439}u + \frac{24298}{1439}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	$u^{16} - 3u^{15} + \dots + 2u - 11$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	$(u^8 - u^7 - 4u^6 + 3u^5 + 5u^4 - u^3 - u^2 - 3u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	$y^{16} - 13y^{15} + \dots - 532y + 121$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	$(y^8 - 9y^7 + 32y^6 - 53y^5 + 31y^4 + 15y^3 - 15y^2 - 7y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.694226 + 0.667719I$ $a = 1.12920 - 1.08608I$ $b = 0.276681 + 1.311520I$	10.1546	$6.33746 + 0.I$
$u = 0.694226 - 0.667719I$ $a = 1.12920 + 1.08608I$ $b = 0.276681 - 1.311520I$	10.1546	$6.33746 + 0.I$
$u = 0.262333 + 1.058630I$ $a = 0.019128 - 1.343770I$ $b = 0.19190 + 2.13545I$	$5.44991 - 9.88301I$	$3.28252 + 6.06963I$
$u = 0.262333 - 1.058630I$ $a = 0.019128 + 1.343770I$ $b = 0.19190 - 2.13545I$	$5.44991 + 9.88301I$	$3.28252 - 6.06963I$
$u = 1.15427$ $a = -0.296909$ $b = -0.236501$	-2.57083	2.16010
$u = 0.524313 + 0.657146I$ $a = 0.513557 + 0.640043I$ $b = -0.598451 - 0.154997I$	$-4.77492 - 2.26376I$	$-6.05872 + 4.53378I$
$u = 0.524313 - 0.657146I$ $a = 0.513557 - 0.640043I$ $b = -0.598451 + 0.154997I$	$-4.77492 + 2.26376I$	$-6.05872 - 4.53378I$
$u = -1.345930 + 0.090134I$ $a = 0.078599 + 0.505339I$ $b = 0.329421 - 1.036490I$	$-4.77492 + 2.26376I$	$-6.05872 - 4.53378I$
$u = -1.345930 - 0.090134I$ $a = 0.078599 - 0.505339I$ $b = 0.329421 + 1.036490I$	$-4.77492 - 2.26376I$	$-6.05872 + 4.53378I$
$u = 1.125920 + 0.800303I$ $a = -0.889080 + 0.447838I$ $b = -0.77247 - 1.44681I$	$2.93531 + 3.55755I$	$2.52739 - 2.62489I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.125920 - 0.800303I$ $a = -0.889080 - 0.447838I$ $b = -0.77247 + 1.44681I$	$2.93531 - 3.55755I$	$2.52739 + 2.62489I$
$u = -0.604309$ $a = 0.567118$ $b = 1.07322$	-2.57083	2.16010
$u = -1.47759 + 0.37462I$ $a = -0.854231 - 0.441448I$ $b = -0.72115 + 1.92612I$	$5.44991 + 9.88301I$	$3.28252 - 6.06963I$
$u = -1.47759 - 0.37462I$ $a = -0.854231 + 0.441448I$ $b = -0.72115 - 1.92612I$	$5.44991 - 9.88301I$	$3.28252 + 6.06963I$
$u = -1.55826 + 0.27885I$ $a = 0.822270 + 0.280177I$ $b = 0.375716 - 1.326680I$	$2.93531 + 3.55755I$	$2.52739 - 2.62489I$
$u = -1.55826 - 0.27885I$ $a = 0.822270 - 0.280177I$ $b = 0.375716 + 1.326680I$	$2.93531 - 3.55755I$	$2.52739 + 2.62489I$

$$\text{III. } I_3^u = \langle u^7 a - u^7 + \cdots + a + 1, -u^7 a + 2u^7 + \cdots + a - 5, u^8 - u^7 - 4u^6 + 3u^5 + 5u^4 - u^3 - u^2 - 3u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -\frac{1}{2}u^7 a + \frac{1}{2}u^7 + \cdots - \frac{1}{2}a - \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^7 - 4u^5 - u^3 a + 4u^3 + au + a + u \\ -\frac{1}{2}u^7 a + \frac{1}{2}u^7 + \cdots - \frac{1}{2}a - \frac{1}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^6 a - u^7 + \cdots - a + 2 \\ -\frac{1}{2}u^7 a + \frac{1}{2}u^7 + \cdots - \frac{1}{2}a - \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + 1 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^7 a - u^7 + \cdots - a + 2 \\ -\frac{1}{2}u^7 a + \frac{1}{2}u^7 + \cdots - \frac{1}{2}a - \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^6 - u^5 - 3u^4 + 2u^3 + 2u^2 + u + 1 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^7 + u^6 + 3u^5 - 2u^4 - 2u^3 - u^2 - u + 1 \\ -u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-2u^6 - 2u^5 + 10u^4 + 8u^3 - 12u^2 - 10u - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	$(u^8 + u^7 - 4u^6 - 3u^5 + 5u^4 + u^3 - u^2 + 3u - 1)^2$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	$u^{16} + 3u^{15} + \dots - 2u - 11$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	$(y^8 - 9y^7 + 32y^6 - 53y^5 + 31y^4 + 15y^3 - 15y^2 - 7y + 1)^2$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	$y^{16} - 13y^{15} + \dots - 532y + 121$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.151337 + 0.673064I$ $a = 0.762637 - 0.950471I$ $b = 0.076801 + 0.408443I$	$4.77492 + 2.26376I$	$6.05872 - 4.53378I$
$u = -0.151337 + 0.673064I$ $a = 0.30052 + 1.93213I$ $b = -0.06507 - 1.92874I$	$4.77492 + 2.26376I$	$6.05872 - 4.53378I$
$u = -0.151337 - 0.673064I$ $a = 0.762637 + 0.950471I$ $b = 0.076801 - 0.408443I$	$4.77492 - 2.26376I$	$6.05872 + 4.53378I$
$u = -0.151337 - 0.673064I$ $a = 0.30052 - 1.93213I$ $b = -0.06507 + 1.92874I$	$4.77492 - 2.26376I$	$6.05872 + 4.53378I$
$u = -1.359440 + 0.207304I$ $a = -0.897134 + 0.451895I$ $b = -0.592239 - 0.125436I$	$-2.93531 + 3.55755I$	$-2.52739 - 2.62489I$
$u = -1.359440 + 0.207304I$ $a = 1.089640 + 0.371279I$ $b = 1.80045 - 1.27064I$	$-2.93531 + 3.55755I$	$-2.52739 - 2.62489I$
$u = -1.359440 - 0.207304I$ $a = -0.897134 - 0.451895I$ $b = -0.592239 + 0.125436I$	$-2.93531 - 3.55755I$	$-2.52739 + 2.62489I$
$u = -1.359440 - 0.207304I$ $a = 1.089640 - 0.371279I$ $b = 1.80045 + 1.27064I$	$-2.93531 - 3.55755I$	$-2.52739 + 2.62489I$
$u = 1.42757 + 0.33227I$ $a = -0.923905 + 0.477454I$ $b = -1.51269 - 1.88228I$	$-5.44991 - 9.88301I$	$-3.28252 + 6.06963I$
$u = 1.42757 + 0.33227I$ $a = 0.010591 - 0.744025I$ $b = 0.534351 + 0.711339I$	$-5.44991 - 9.88301I$	$-3.28252 + 6.06963I$

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.42757 - 0.33227I$ $a = -0.923905 - 0.477454I$ $b = -1.51269 + 1.88228I$	$-5.44991 + 9.88301I$	$-3.28252 - 6.06963I$
$u = 1.42757 - 0.33227I$ $a = 0.010591 + 0.744025I$ $b = 0.534351 - 0.711339I$	$-5.44991 + 9.88301I$	$-3.28252 - 6.06963I$
$u = 1.50912$ $a = 0.460021 + 0.442457I$ $b = 0.770987 - 0.303857I$	-10.1546	-6.33750
$u = 1.50912$ $a = 0.460021 - 0.442457I$ $b = 0.770987 + 0.303857I$	-10.1546	-6.33750
$u = -0.342714$ $a = 1.76330$ $b = -0.866117$	2.57083	-2.16010
$u = -0.342714$ $a = -3.36804$ $b = -0.159086$	2.57083	-2.16010

IV.

$$I_4^u = \langle -u^{11}a - u^{11} + \dots + a + 1, u^{11} - 5u^9 + \dots + a + 2, u^{12} - u^{11} + \dots + 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ u^{11}a + u^{11} + \dots - a - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^{10} + 3u^8 + u^7 - 2u^6 - 2u^5 - u^3a - 2u^4 + au + 2u^2 + a + u \\ u^{11}a - 4u^9a + \dots + u^2 - a \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^{11} - u^{10} + \dots + 2u - 1 \\ u^{11}a - u^{11} + \dots - a - u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{10} + 3u^8 + 2u^7 - 2u^6 - 4u^5 - 3u^4 + 3u^2 + 3u + 1 \\ u^{11} - 4u^9 - u^8 + 5u^7 + 3u^6 - u^5 - 2u^4 - u^3 - u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{11}a + u^{11} + \dots + 2u - 1 \\ u^{10}a - u^{11} + \dots + 5u^3 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^{11} - u^{10} - 4u^9 + 2u^8 + 7u^7 + u^6 - 5u^5 - 5u^4 - u^3 + 3u^2 + 2u \\ u^{11} - 4u^9 - u^8 + 5u^7 + 3u^6 - u^5 - 2u^4 - u^3 - u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{11} - 4u^9 - 2u^8 + 6u^7 + 6u^6 - 2u^5 - 6u^4 - 3u^3 + 2u^2 + 2u \\ u^{11} - 3u^9 - 2u^8 + 2u^7 + 4u^6 + 3u^5 - 3u^3 - 2u^2 - u - 2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-4u^8 + 12u^6 + 4u^5 - 8u^4 - 8u^3 - 4u^2 + 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	$(u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)^2$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	$(u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3	
c_4, c_5, c_6	$(y^{12} - 9y^{11} + \dots + 4y + 1)^2$
c_7, c_8, c_9	
c_{10}, c_{11}, c_{12}	

(vi) Complex Volumes and Cusp Shapes

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.895235 + 0.524661I$ $a = 1.053870 + 0.403232I$ $b = 1.02100 - 1.56444I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = -0.895235 + 0.524661I$ $a = -0.364606 + 0.330843I$ $b = 0.939757 - 0.425557I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = -0.895235 - 0.524661I$ $a = 1.053870 - 0.403232I$ $b = 1.02100 + 1.56444I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = -0.895235 - 0.524661I$ $a = -0.364606 - 0.330843I$ $b = 0.939757 + 0.425557I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = -0.282166 + 0.828798I$ $a = -0.792263 + 0.610180I$ $b = 0.383261 - 0.056485I$	$5.69302I$	$0. - 5.51057I$
$u = -0.282166 + 0.828798I$ $a = -0.20722 - 1.56570I$ $b = -0.47925 + 2.17825I$	$5.69302I$	$0. - 5.51057I$
$u = -0.282166 - 0.828798I$ $a = -0.792263 - 0.610180I$ $b = 0.383261 + 0.056485I$	$- 5.69302I$	$0. + 5.51057I$
$u = -0.282166 - 0.828798I$ $a = -0.20722 + 1.56570I$ $b = -0.47925 - 2.17825I$	$- 5.69302I$	$0. + 5.51057I$
$u = -1.155020 + 0.191936I$ $a = 0.827710 - 0.316699I$ $b = -0.087686 + 0.786615I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = -1.155020 + 0.191936I$ $a = -1.095480 - 0.303138I$ $b = -1.53926 + 1.57073I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.155020 - 0.191936I$ $a = 0.827710 + 0.316699I$ $b = -0.087686 - 0.786615I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = -1.155020 - 0.191936I$ $a = -1.095480 + 0.303138I$ $b = -1.53926 - 1.57073I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = 1.323480 + 0.139870I$ $a = -0.847918 + 0.234635I$ $b = -0.01623 - 1.47826I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = 1.323480 + 0.139870I$ $a = 0.075702 - 0.376331I$ $b = -0.831407 + 1.047810I$	$-1.89061 - 0.92430I$	$-3.71672 + 0.79423I$
$u = 1.323480 - 0.139870I$ $a = -0.847918 - 0.234635I$ $b = -0.01623 + 1.47826I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = 1.323480 - 0.139870I$ $a = 0.075702 + 0.376331I$ $b = -0.831407 - 1.047810I$	$-1.89061 + 0.92430I$	$-3.71672 - 0.79423I$
$u = 1.356120 + 0.270046I$ $a = 0.923718 - 0.383073I$ $b = 0.95599 + 1.99574I$	$-5.69302I$	$0. + 5.51057I$
$u = 1.356120 + 0.270046I$ $a = -0.083074 + 0.627698I$ $b = -0.127208 - 1.130510I$	$-5.69302I$	$0. + 5.51057I$
$u = 1.356120 - 0.270046I$ $a = 0.923718 + 0.383073I$ $b = 0.95599 - 1.99574I$	$5.69302I$	$0. - 5.51057I$
$u = 1.356120 - 0.270046I$ $a = -0.083074 - 0.627698I$ $b = -0.127208 + 1.130510I$	$5.69302I$	$0. - 5.51057I$

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.152828 + 0.487477I$ $a = -1.50418 + 1.36489I$ $b = -0.820813 - 0.942146I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = 0.152828 + 0.487477I$ $a = 0.51374 - 2.55389I$ $b = 1.10185 + 1.67160I$	$1.89061 - 0.92430I$	$3.71672 + 0.79423I$
$u = 0.152828 - 0.487477I$ $a = -1.50418 - 1.36489I$ $b = -0.820813 + 0.942146I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$
$u = 0.152828 - 0.487477I$ $a = 0.51374 + 2.55389I$ $b = 1.10185 - 1.67160I$	$1.89061 + 0.92430I$	$3.71672 - 0.79423I$

$$V. I_5^u = \langle 2b - a - 1, a^2 - 3, u - 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ \frac{1}{2}a + \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a \\ -\frac{1}{2}a + \frac{1}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -3 \\ -\frac{1}{2}a - \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2a \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 3 \\ \frac{1}{2}a - \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2a - 1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2a \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_7 c_8	$(u - 1)^2$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	$u^2 - 3$
c_6, c_{12}	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	$(y - 1)^2$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	$(y - 3)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_5^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$ $a = 1.73205$ $b = 1.36603$	9.86960	0
$u = 1.00000$ $a = -1.73205$ $b = -0.366025$	9.86960	0

$$\text{VI. } \Gamma_6^u = \langle 2b - u + 1, 3a - u, u^2 - 3 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -2u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2 \\ -3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{1}{3}u \\ \frac{1}{2}u - \frac{1}{2} \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} \frac{1}{3}u - 2 \\ \frac{1}{2}u - \frac{7}{2} \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -\frac{1}{3}u \\ \frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{3}u \\ -\frac{1}{2}u + \frac{1}{2} \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -2 \\ -3 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	$u^2 - 3$
c_3, c_9	$(u - 1)^2$
c_4, c_5, c_{10} c_{11}	$(u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	$(y - 3)^2$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	$(y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.73205$ $a = 0.577350$ $b = 0.366025$	-9.86960	0
$u = -1.73205$ $a = -0.577350$ $b = -1.36603$	-9.86960	0

VII. $I_7^u = \langle b + 1, a, u - 1 \rangle$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

Crossings	u -Polynomials at each crossing
c_1, c_2, c_7 c_8	$u - 1$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	u
c_6, c_{12}	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	$y - 1$
c_3, c_4, c_5 c_9, c_{10}, c_{11}	y

(vi) Complex Volumes and Cusp Shapes

Solutions to I_7^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0$	-3.28987	-12.0000
$b = -1.00000$		

$$\text{VIII. } I_8^u = \langle 4b^2 - 4b + 5, 2ba + 4u + \cdots - 3a + 7, 2bu + u + \cdots - 2a + 3, a^2 - 2a + 1, au + a - u - 1, u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -2u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u \\ -2u - 2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2u + 2 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a - 2u - 2 \\ b + a - u - 3 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2a - u - 2 \\ b + \frac{1}{2}a - \frac{1}{2}u - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2a + 2u + 4 \\ u + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u + 2 \\ b + \frac{3}{2}a - \frac{1}{2}u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2a + 3u + 6 \\ u + 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2a - 4u - 6 \\ -2u - 3 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_3 c_7, c_8, c_9	$(u + 1)^4$
c_4, c_5, c_6 c_{10}, c_{11}, c_{12}	$(u - 1)^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3	$(y - 1)^4$
c_4, c_5, c_6	
c_7, c_8, c_9	
c_{10}, c_{11}, c_{12}	

(vi) Complex Volumes and Cusp Shapes

Solutions to I_g^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$ $a = 1.00000$ $b = 0.500000 + 1.000000I$	0	0
$u = -1.00000$ $a = 1.00000$ $b = 0.500000 + 1.000000I$	0	0
$u = -1.00000$ $a = 1.00000$ $b = 0.500000 - 1.000000I$	0	0
$u = -1.00000$ $a = 1.00000$ $b = 0.500000 - 1.000000I$	0	0

IX. $\Gamma_9^u = \langle a - 1, u + 1 \rangle$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ b - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ b - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ b \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) u-Polynomials at the component : It cannot be defined for a positive dimension component.

(v) Riley Polynomials at the component : It cannot be defined for a positive dimension component.

(iv) Complex Volumes and Cusp Shapes

Solution to I_9^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = \dots$		
$a = \dots$	0	0
$b = \dots$		

$$\mathbf{X. } I_1^v = \langle a, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 12

(iv) **u**-Polynomials at the component

Crossings	u -Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	u
c_3, c_9	$u - 1$
c_4, c_5, c_{10} c_{11}	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_6 c_7, c_8, c_{12}	y
c_3, c_4, c_5 c_9, c_{10}, c_{11}	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$	3.28987	12.0000
$b = 1.00000$		

XI. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1, c_2, c_7 c_8	$u(u-1)^3(u+1)^4(u^2-3)$ $\cdot (u^8 + u^7 - 4u^6 - 3u^5 + 5u^4 + u^3 - u^2 + 3u - 1)^2$ $\cdot (u^{12} - 3u^{11} + \dots - 6u - 2)$ $\cdot (u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)^2$ $\cdot (u^{16} - 3u^{15} + \dots + 2u - 11)$
c_3, c_9	$u(u-1)^3(u+1)^4(u^2-3)$ $\cdot (u^8 - u^7 - 4u^6 + 3u^5 + 5u^4 - u^3 - u^2 - 3u - 1)^2$ $\cdot (u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1)^2$ $\cdot (u^{12} + 3u^{11} + \dots + 6u - 2)(u^{16} + 3u^{15} + \dots - 2u - 11)$
c_4, c_5, c_{10} c_{11}	$u(u-1)^4(u+1)^3(u^2-3)$ $\cdot (u^8 - u^7 - 4u^6 + 3u^5 + 5u^4 - u^3 - u^2 - 3u - 1)^2$ $\cdot (u^{12} - u^{11} - 4u^{10} + 2u^9 + 7u^8 + u^7 - 5u^6 - 5u^5 - u^4 + 3u^3 + 2u^2 + 1)^2$ $\cdot (u^{12} + 3u^{11} + \dots + 6u - 2)(u^{16} + 3u^{15} + \dots - 2u - 11)$
c_6, c_{12}	$u(u-1)^4(u+1)^3(u^2-3)$ $\cdot (u^8 + u^7 - 4u^6 - 3u^5 + 5u^4 + u^3 - u^2 + 3u - 1)^2$ $\cdot (u^{12} - 3u^{11} + \dots - 6u - 2)$ $\cdot (u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)^2$ $\cdot (u^{16} - 3u^{15} + \dots + 2u - 11)$

XII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3	$y(y-3)^2(y-1)^7$
c_4, c_5, c_6	$\cdot (y^8 - 9y^7 + 32y^6 - 53y^5 + 31y^4 + 15y^3 - 15y^2 - 7y + 1)^2$
c_7, c_8, c_9	$\cdot (y^{12} - 15y^{11} + \dots + 16y + 4)(y^{12} - 9y^{11} + \dots + 4y + 1)^2$
c_{10}, c_{11}, c_{12}	$\cdot (y^{16} - 13y^{15} + \dots - 532y + 121)$