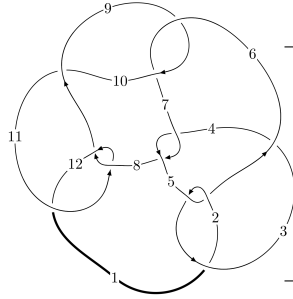
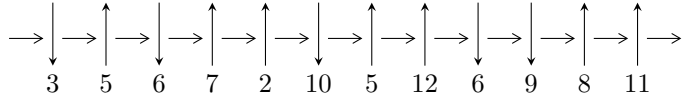


12n₀₀₂₀ (K12n₀₀₂₀)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$6, 10 \xrightarrow{c_6} 2, 7 \xrightarrow{c_5} 5 \xrightarrow{c_2} 3 \xrightarrow{c_7} 8 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_{10}} 11 \xrightarrow{c_{12}} 12 \Rightarrow c_3, c_8, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 6.15417 \times 10^{24} u^{34} + 4.90608 \times 10^{25} u^{33} + \dots + 1.32838 \times 10^{26} b - 6.91943 \times 10^{25}, \\ 1.02387 \times 10^{26} u^{34} + 2.68565 \times 10^{26} u^{33} + \dots + 1.32838 \times 10^{26} a - 3.02927 \times 10^{26}, u^{35} + 3u^{34} + \dots - 2u - 1 \rangle$$

$$I_2^u = \langle 4u^5 a + 5u^4 a + 4u^5 - 7u^3 a + 5u^4 - 14u^2 a - 7u^3 + 5au - 14u^2 + 17b + a + 5u + 1, \\ -u^5 a + 2u^3 a - 2u^4 + u^2 a - u^3 + a^2 - 2au + 2u^2 + 2u, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 47 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 6.15 \times 10^{24} u^{34} + 4.91 \times 10^{25} u^{33} + \dots + 1.33 \times 10^{26} b - 6.92 \times 10^{25}, 1.02 \times 10^{26} u^{34} + 2.69 \times 10^{26} u^{33} + \dots + 1.33 \times 10^{26} a - 3.03 \times 10^{26}, u^{35} + 3u^{34} + \dots - 2u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.770764u^{34} - 2.02174u^{33} + \dots - 4.41998u + 2.28042 \\ -0.0463282u^{34} - 0.369327u^{33} + \dots + 0.317345u + 0.520890 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1.26890u^{34} + 2.84616u^{33} + \dots - 4.14141u + 0.782118 \\ -0.0631189u^{34} - 0.437170u^{33} + \dots + 0.413577u - 0.482385 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1.55412u^{34} + 3.44078u^{33} + \dots - 4.40019u - 0.146776 \\ -0.0448946u^{34} - 0.427369u^{33} + \dots + 0.806983u - 0.450739 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.690375u^{34} + 2.08177u^{33} + \dots - 1.15296u - 2.07734 \\ 0.00686562u^{34} + 0.115030u^{33} + \dots - 0.332383u - 0.172479 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.700744u^{34} + 1.98651u^{33} + \dots - 0.108902u - 1.89421 \\ 0.0103696u^{34} - 0.0952592u^{33} + \dots + 1.04406u + 0.183128 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1.59901u^{34} + 3.86815u^{33} + \dots - 5.20717u + 0.303962 \\ -0.0448946u^{34} - 0.427369u^{33} + \dots + 0.806983u - 0.450739 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.743963u^{34} + 2.07828u^{33} + \dots - 0.147237u - 1.89598 \\ 0.0883859u^{34} + 0.102670u^{33} + \dots + 1.52166u + 0.0975759 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{138501011022536071388354471}{22139732193931699544465805} u^{34} + \frac{368226358523013848196048853}{22139732193931699544465805} u^{33} + \dots - \frac{423513858408885950087940661}{44279464387863399088931610} u - \frac{130309672706343830288860133}{14759821462621133029643870}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{35} + 5u^{34} + \dots + 6u - 1$
c_2, c_5	$u^{35} + 7u^{34} + \dots - 6u - 1$
c_3	$u^{35} - 7u^{34} + \dots - 25346u - 337$
c_4, c_7	$u^{35} + 3u^{34} + \dots + 16384u + 4096$
c_6, c_9	$u^{35} + 3u^{34} + \dots - 2u - 1$
c_8, c_{11}	$u^{35} + 3u^{34} + \dots + 2u - 1$
c_{10}	$u^{35} + 3u^{34} + \dots - 2u + 1$
c_{12}	$u^{35} - 23u^{34} + \dots - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{35} + 57y^{34} + \dots + 6y - 1$
c_2, c_5	$y^{35} + 5y^{34} + \dots + 6y - 1$
c_3	$y^{35} + 109y^{34} + \dots + 279652022y - 113569$
c_4, c_7	$y^{35} - 65y^{34} + \dots - 83886080y - 16777216$
c_6, c_9	$y^{35} - 3y^{34} + \dots - 2y - 1$
c_8, c_{11}	$y^{35} - 23y^{34} + \dots - 2y - 1$
c_{10}	$y^{35} + 61y^{34} + \dots + 6y - 1$
c_{12}	$y^{35} - 19y^{34} + \dots + 182y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.991966 + 0.091776I$		
$a = 0.72692 + 1.45829I$	$-2.80047 + 0.03393I$	$-4.96122 - 0.73381I$
$b = -0.068558 + 0.738981I$		
$u = -0.991966 - 0.091776I$		
$a = 0.72692 - 1.45829I$	$-2.80047 - 0.03393I$	$-4.96122 + 0.73381I$
$b = -0.068558 - 0.738981I$		
$u = 0.909482 + 0.380777I$		
$a = 0.29144 - 1.73248I$	$-1.72254 - 4.24984I$	$-2.18876 + 7.04122I$
$b = 0.014187 - 1.000160I$		
$u = 0.909482 - 0.380777I$		
$a = 0.29144 + 1.73248I$	$-1.72254 + 4.24984I$	$-2.18876 - 7.04122I$
$b = 0.014187 + 1.000160I$		
$u = 0.576907 + 0.754246I$		
$a = 0.591225 + 0.311198I$	$2.25585 + 1.15466I$	$4.96533 - 0.29519I$
$b = -0.377861 - 0.131381I$		
$u = 0.576907 - 0.754246I$		
$a = 0.591225 - 0.311198I$	$2.25585 - 1.15466I$	$4.96533 + 0.29519I$
$b = -0.377861 + 0.131381I$		
$u = -1.010040 + 0.446446I$		
$a = 0.650598 - 0.883449I$	$-1.67432 + 1.71265I$	$-0.948963 + 0.233573I$
$b = -0.388281 - 0.417527I$		
$u = -1.010040 - 0.446446I$		
$a = 0.650598 + 0.883449I$	$-1.67432 - 1.71265I$	$-0.948963 - 0.233573I$
$b = -0.388281 + 0.417527I$		
$u = -0.438128 + 0.690005I$		
$a = -0.45748 + 1.41127I$	$2.97461 + 5.04238I$	$7.52995 - 7.92929I$
$b = 0.70266 + 1.26431I$		
$u = -0.438128 - 0.690005I$		
$a = -0.45748 - 1.41127I$	$2.97461 - 5.04238I$	$7.52995 + 7.92929I$
$b = 0.70266 - 1.26431I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.125324 + 0.796091I$ $a = 0.172538 - 0.306733I$ $b = 1.204060 - 0.564978I$	$5.45936 - 1.99795I$	$12.38801 + 3.24689I$
$u = 0.125324 - 0.796091I$ $a = 0.172538 + 0.306733I$ $b = 1.204060 + 0.564978I$	$5.45936 + 1.99795I$	$12.38801 - 3.24689I$
$u = 1.114360 + 0.664977I$ $a = 0.458155 + 0.916311I$ $b = -0.612297 + 0.465157I$	$0.69794 - 6.72088I$	$4.01525 + 3.80549I$
$u = 1.114360 - 0.664977I$ $a = 0.458155 - 0.916311I$ $b = -0.612297 - 0.465157I$	$0.69794 + 6.72088I$	$4.01525 - 3.80549I$
$u = 0.675945$ $a = 2.49935$ $b = 0.470215$	2.49299	1.75040
$u = -0.019593 + 0.666979I$ $a = 0.386507 - 0.586859I$ $b = 0.438826 + 0.519059I$	$0.93795 + 1.36112I$	$3.65858 - 4.50590I$
$u = -0.019593 - 0.666979I$ $a = 0.386507 + 0.586859I$ $b = 0.438826 - 0.519059I$	$0.93795 - 1.36112I$	$3.65858 + 4.50590I$
$u = -0.000172 + 0.620501I$ $a = 0.266778 - 1.045710I$ $b = 0.458461 + 0.655103I$	$0.93048 + 1.37281I$	$3.33756 - 4.46340I$
$u = -0.000172 - 0.620501I$ $a = 0.266778 + 1.045710I$ $b = 0.458461 - 0.655103I$	$0.93048 - 1.37281I$	$3.33756 + 4.46340I$
$u = 0.428622 + 0.434204I$ $a = -1.22891 - 2.28547I$ $b = 0.489459 - 1.005660I$	$-0.28045 - 2.82979I$	$1.83395 + 3.29320I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.428622 - 0.434204I$ $a = -1.22891 + 2.28547I$ $b = 0.489459 + 1.005660I$	$-0.28045 + 2.82979I$	$1.83395 - 3.29320I$
$u = -0.98049 + 1.10389I$ $a = -0.491542 + 0.320489I$ $b = -1.14756 + 0.89148I$	$16.2670 + 5.6984I$	$6.10259 - 2.75484I$
$u = -0.98049 - 1.10389I$ $a = -0.491542 - 0.320489I$ $b = -1.14756 - 0.89148I$	$16.2670 - 5.6984I$	$6.10259 + 2.75484I$
$u = 0.99399 + 1.11491I$ $a = -0.412944 - 0.428999I$ $b = -1.046520 - 0.943327I$	$11.73730 - 0.22593I$	0
$u = 0.99399 - 1.11491I$ $a = -0.412944 + 0.428999I$ $b = -1.046520 + 0.943327I$	$11.73730 + 0.22593I$	0
$u = -1.10793 + 1.00267I$ $a = 0.35872 - 1.51332I$ $b = -1.04229 - 1.00409I$	$15.8086 + 2.0235I$	$5.61504 + 0.I$
$u = -1.10793 - 1.00267I$ $a = 0.35872 + 1.51332I$ $b = -1.04229 + 1.00409I$	$15.8086 - 2.0235I$	$5.61504 + 0.I$
$u = -1.08711 + 1.02841I$ $a = 0.53533 - 1.58797I$ $b = -0.94816 - 1.13708I$	$15.3839 + 13.3033I$	$4.97161 - 6.77945I$
$u = -1.08711 - 1.02841I$ $a = 0.53533 + 1.58797I$ $b = -0.94816 + 1.13708I$	$15.3839 - 13.3033I$	$4.97161 + 6.77945I$
$u = -1.01043 + 1.10512I$ $a = -0.436340 + 0.546687I$ $b = -1.01525 + 1.03906I$	$15.6838 - 5.5084I$	$5.51943 + 2.85249I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.01043 - 1.10512I$ $a = -0.436340 - 0.546687I$ $b = -1.01525 - 1.03906I$	$15.6838 + 5.5084I$	$5.51943 - 2.85249I$
$u = 1.10529 + 1.02256I$ $a = 0.46909 + 1.51898I$ $b = -0.96358 + 1.05901I$	$11.33260 - 7.58418I$	$0. + 4.10781I$
$u = 1.10529 - 1.02256I$ $a = 0.46909 - 1.51898I$ $b = -0.96358 - 1.05901I$	$11.33260 + 7.58418I$	$0. - 4.10781I$
$u = -0.446086 + 0.207143I$ $a = 5.87024 - 1.44569I$ $b = 0.567586 - 0.882988I$	$1.99036 - 2.28427I$	$-9.4417 - 11.9389I$
$u = -0.446086 - 0.207143I$ $a = 5.87024 + 1.44569I$ $b = 0.567586 + 0.882988I$	$1.99036 + 2.28427I$	$-9.4417 + 11.9389I$

II.

$$I_2^u = \langle 4u^5a + 4u^5 + \dots + a + 1, -u^5a - 2u^4 + \dots + a^2 + 2u, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a \\ -0.235294au^5 - 0.235294u^5 + \dots - 0.0588235a - 0.0588235 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.235294au^5 - 0.764706u^5 + \dots + 1.05882a + 0.0588235 \\ -0.235294au^5 - 0.235294u^5 + \dots - 0.0588235a - 1.05882 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^5 + 2u^3 + u^2 + a - 2u - 1 \\ -0.235294au^5 - 0.235294u^5 + \dots - 0.0588235a - 1.05882 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.235294au^5 - 0.764706u^5 + \dots + 1.05882a + 0.0588235 \\ -0.235294au^5 - 0.235294u^5 + \dots - 0.0588235a - 1.05882 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^5 - 2u^3 + u \\ u^5 + u^4 - 2u^3 - u^2 + u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= \frac{33}{17}u^5a + \frac{3}{17}u^4a + \frac{33}{17}u^5 - \frac{62}{17}u^3a + \frac{88}{17}u^4 - \frac{56}{17}u^2a - \frac{62}{17}u^3 + \frac{54}{17}au - \frac{124}{17}u^2 + \frac{4}{17}a - \frac{14}{17}u + \frac{106}{17}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3, c_5	$(u^2 - u + 1)^6$
c_2	$(u^2 + u + 1)^6$
c_4, c_7	u^{12}
c_6, c_{11}	$(u^6 + u^5 - u^4 - 2u^3 + u + 1)^2$
c_8, c_9	$(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$
c_{10}	$(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^2$
c_{12}	$(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3 c_5	$(y^2 + y + 1)^6$
c_4, c_7	y^{12}
c_6, c_8, c_9 c_{11}	$(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$
c_{10}, c_{12}	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.002190 + 0.295542I$ $a = 0.315127 + 1.283850I$ $b = 0.500000 + 0.866025I$	$-1.89061 + 1.10558I$	$0.30406 - 2.63469I$
$u = 1.002190 + 0.295542I$ $a = -0.54572 - 1.78086I$ $b = 0.500000 - 0.866025I$	$-1.89061 - 2.95419I$	$-2.90246 + 4.54482I$
$u = 1.002190 - 0.295542I$ $a = 0.315127 - 1.283850I$ $b = 0.500000 - 0.866025I$	$-1.89061 - 1.10558I$	$0.30406 + 2.63469I$
$u = 1.002190 - 0.295542I$ $a = -0.54572 + 1.78086I$ $b = 0.500000 + 0.866025I$	$-1.89061 + 2.95419I$	$-2.90246 - 4.54482I$
$u = -0.428243 + 0.664531I$ $a = 0.431357 + 0.434984I$ $b = 0.500000 - 0.866025I$	$1.89061 - 2.95419I$	$2.82220 + 4.67955I$
$u = -0.428243 + 0.664531I$ $a = -2.09239 + 1.02210I$ $b = 0.500000 + 0.866025I$	$1.89061 + 1.10558I$	$6.66783 - 4.72351I$
$u = -0.428243 - 0.664531I$ $a = 0.431357 - 0.434984I$ $b = 0.500000 + 0.866025I$	$1.89061 + 2.95419I$	$2.82220 - 4.67955I$
$u = -0.428243 - 0.664531I$ $a = -2.09239 - 1.02210I$ $b = 0.500000 - 0.866025I$	$1.89061 - 1.10558I$	$6.66783 + 4.72351I$
$u = -1.073950 + 0.558752I$ $a = 0.179704 - 0.925804I$ $b = 0.500000 - 0.866025I$	$3.66314I$	$3.68173 - 3.33422I$
$u = -1.073950 + 0.558752I$ $a = -0.78808 + 1.48456I$ $b = 0.500000 + 0.866025I$	$7.72290I$	$-0.57335 - 9.26831I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.073950 - 0.558752I$		
$a = 0.179704 + 0.925804I$	$- 3.66314I$	$3.68173 + 3.33422I$
$b = 0.500000 + 0.866025I$		
$u = -1.073950 - 0.558752I$		
$a = -0.78808 - 1.48456I$	$- 7.72290I$	$-0.57335 + 9.26831I$
$b = 0.500000 - 0.866025I$		

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u^2 - u + 1)^6)(u^{35} + 5u^{34} + \dots + 6u - 1)$
c_2	$((u^2 + u + 1)^6)(u^{35} + 7u^{34} + \dots - 6u - 1)$
c_3	$((u^2 - u + 1)^6)(u^{35} - 7u^{34} + \dots - 25346u - 337)$
c_4, c_7	$u^{12}(u^{35} + 3u^{34} + \dots + 16384u + 4096)$
c_5	$((u^2 - u + 1)^6)(u^{35} + 7u^{34} + \dots - 6u - 1)$
c_6	$((u^6 + u^5 - u^4 - 2u^3 + u + 1)^2)(u^{35} + 3u^{34} + \dots - 2u - 1)$
c_8	$((u^6 - u^5 - u^4 + 2u^3 - u + 1)^2)(u^{35} + 3u^{34} + \dots + 2u - 1)$
c_9	$((u^6 - u^5 - u^4 + 2u^3 - u + 1)^2)(u^{35} + 3u^{34} + \dots - 2u - 1)$
c_{10}	$((u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^2)(u^{35} + 3u^{34} + \dots - 2u + 1)$
c_{11}	$((u^6 + u^5 - u^4 - 2u^3 + u + 1)^2)(u^{35} + 3u^{34} + \dots + 2u - 1)$
c_{12}	$((u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2)(u^{35} - 23u^{34} + \dots - 2u - 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y^2 + y + 1)^6)(y^{35} + 57y^{34} + \dots + 6y - 1)$
c_2, c_5	$((y^2 + y + 1)^6)(y^{35} + 5y^{34} + \dots + 6y - 1)$
c_3	$((y^2 + y + 1)^6)(y^{35} + 109y^{34} + \dots + 2.79652 \times 10^8 y - 113569)$
c_4, c_7	$y^{12}(y^{35} - 65y^{34} + \dots - 8.38861 \times 10^7 y - 1.67772 \times 10^7)$
c_6, c_9	$((y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2)(y^{35} - 3y^{34} + \dots - 2y - 1)$
c_8, c_{11}	$((y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2)(y^{35} - 23y^{34} + \dots - 2y - 1)$
c_{10}	$((y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2)(y^{35} + 61y^{34} + \dots + 6y - 1)$
c_{12}	$((y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2)(y^{35} - 19y^{34} + \dots + 182y - 1)$