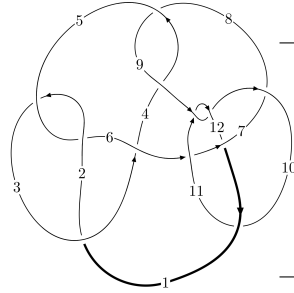
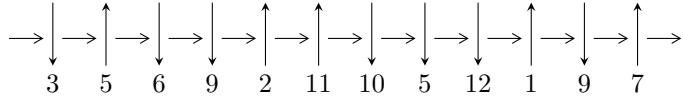


12n<sub>0027</sub> (K12n<sub>0027</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,8 \xrightarrow{c_8} 9,12 \xrightarrow{c_9} 10 \xrightarrow{c_4} 4 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 1 \xrightarrow{c_{11}} 11 \xrightarrow{c_6} 6 \xrightarrow{c_3} 3 \xrightarrow{c_2} 2 \twoheadrightarrow c_1, c_5, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 4.63893 \times 10^{317} u^{76} + 6.90082 \times 10^{317} u^{75} + \dots + 1.25294 \times 10^{321} b + 1.60645 \times 10^{321}, \\ -1.19015 \times 10^{318} u^{76} - 3.51549 \times 10^{318} u^{75} + \dots + 2.50588 \times 10^{321} a - 2.87281 \times 10^{322}, \\ u^{77} + 2u^{76} + \dots + 20480u + 4096 \rangle$$

$$I_2^u = \langle 2u^3 + 2u^2 + b + 5u + 1, -u^3 - 3u^2 + a - 3u - 6, u^4 + u^3 + 3u^2 + 2u + 1 \rangle$$

$$I_1^v = \langle a, 309980v^{11} + 790238v^{10} + \dots + 707733b + 1249018, \\ v^{12} + 3v^{11} + 3v^{10} + 18v^9 + 31v^8 - 29v^7 - 31v^6 - 9v^5 + 19v^4 + 5v^3 - 4v^2 + v + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 93 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 4.64 \times 10^{317} u^{76} + 6.90 \times 10^{317} u^{75} + \dots + 1.25 \times 10^{321} b + 1.61 \times 10^{321}, -1.19 \times 10^{318} u^{76} - 3.52 \times 10^{318} u^{75} + \dots + 2.51 \times 10^{321} a - 2.87 \times 10^{322}, u^{77} + 2u^{76} + \dots + 20480u + 4096 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.000474943u^{76} + 0.00140290u^{75} + \dots + 19.8888u + 11.4642 \\ -0.000370243u^{76} - 0.000550769u^{75} + \dots - 12.5316u - 1.28214 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.000502182u^{76} + 0.00148228u^{75} + \dots + 18.5669u + 11.5558 \\ -0.000400721u^{76} - 0.000628200u^{75} + \dots - 14.2062u - 2.01128 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.00403445u^{76} + 0.00701135u^{75} + \dots + 135.801u + 30.0505 \\ 0.000251477u^{76} + 0.000675536u^{75} + \dots + 18.8283u + 6.76857 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.000316716u^{76} + 0.000548963u^{75} + \dots + 6.03001u + 1.86087 \\ -8.61974 \times 10^{-6} u^{76} - 0.0000450420u^{75} + \dots - 2.08710u - 0.369176 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.000443453u^{76} + 0.00138924u^{75} + \dots + 18.5802u + 12.0376 \\ -0.000400972u^{76} - 0.000579591u^{75} + \dots - 13.4129u - 1.48420 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.000325336u^{76} + 0.000594005u^{75} + \dots + 8.11710u + 2.23004 \\ 0.0000255950u^{76} + 0.0000821978u^{75} + \dots + 1.91504u + 0.601280 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.0000229625u^{76} - 0.000118674u^{75} + \dots - 2.05186u - 1.28107 \\ 0.0000158254u^{76} + 0.0000361796u^{75} + \dots + 2.94000u + 0.422511 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0000229625u^{76} - 0.000118674u^{75} + \dots - 2.05186u - 1.28107 \\ 0.0000353440u^{76} + 0.0000721239u^{75} + \dots + 4.52395u + 0.720490 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $0.000265127u^{76} + 0.00273732u^{75} + \dots + 71.8347u + 33.0070$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{77} + 42u^{76} + \dots - 173u - 1$
$c_2, c_5$	$u^{77} + 8u^{76} + \dots + 3u + 1$
$c_3$	$u^{77} - 8u^{76} + \dots + 2520u + 1732$
$c_4, c_8$	$u^{77} + 2u^{76} + \dots + 20480u + 4096$
$c_6$	$u^{77} - u^{76} + \dots + 7631854u - 2351327$
$c_7$	$u^{77} - 7u^{76} + \dots - 18228u - 7979$
$c_9, c_{11}$	$u^{77} - 7u^{76} + \dots - 65u + 1$
$c_{10}$	$u^{77} + 13u^{76} + \dots - 200u - 16$
$c_{12}$	$u^{77} + 4u^{76} + \dots - 3u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{77} - 6y^{76} + \dots + 13671y - 1$
$c_2, c_5$	$y^{77} + 42y^{76} + \dots - 173y - 1$
$c_3$	$y^{77} - 54y^{76} + \dots - 552548680y - 2999824$
$c_4, c_8$	$y^{77} - 60y^{76} + \dots + 234881024y - 16777216$
$c_6$	$y^{77} - 9y^{76} + \dots - 135685107448604y - 5528738660929$
$c_7$	$y^{77} - 77y^{76} + \dots + 2964755496y - 63664441$
$c_9, c_{11}$	$y^{77} - 63y^{76} + \dots - 2399y - 1$
$c_{10}$	$y^{77} + 21y^{76} + \dots + 15168y - 256$
$c_{12}$	$y^{77} + 2y^{76} + \dots - 29y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.021202 + 0.991505I$		
$a = 0.85015 + 1.14174I$	$-1.29984 - 4.81871I$	$-3.73970 + 8.31831I$
$b = -0.435122 - 0.281974I$		
$u = -0.021202 - 0.991505I$		
$a = 0.85015 - 1.14174I$	$-1.29984 + 4.81871I$	$-3.73970 - 8.31831I$
$b = -0.435122 + 0.281974I$		
$u = 0.350174 + 0.870277I$		
$a = 0.183615 + 1.203250I$	$-4.26262 - 2.29968I$	$-11.37943 + 4.09375I$
$b = 0.621978 - 0.404845I$		
$u = 0.350174 - 0.870277I$		
$a = 0.183615 - 1.203250I$	$-4.26262 + 2.29968I$	$-11.37943 - 4.09375I$
$b = 0.621978 + 0.404845I$		
$u = 0.552031 + 0.673417I$		
$a = 0.538939 - 0.192540I$	$-3.26120 + 0.96418I$	$-9.85344 - 3.05224I$
$b = 1.155460 - 0.244632I$		
$u = 0.552031 - 0.673417I$		
$a = 0.538939 + 0.192540I$	$-3.26120 - 0.96418I$	$-9.85344 + 3.05224I$
$b = 1.155460 + 0.244632I$		
$u = 0.801656 + 0.115028I$		
$a = 0.100644 - 1.215600I$	$0.77686 - 3.97780I$	$-2.71090 + 8.29234I$
$b = 0.407413 - 0.043467I$		
$u = 0.801656 - 0.115028I$		
$a = 0.100644 + 1.215600I$	$0.77686 + 3.97780I$	$-2.71090 - 8.29234I$
$b = 0.407413 + 0.043467I$		
$u = -0.742333 + 0.323629I$		
$a = 0.674206 - 0.258407I$	$0.963117 - 0.556760I$	$-4.97972 - 0.27994I$
$b = -0.517206 - 1.155410I$		
$u = -0.742333 - 0.323629I$		
$a = 0.674206 + 0.258407I$	$0.963117 + 0.556760I$	$-4.97972 + 0.27994I$
$b = -0.517206 + 1.155410I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.000355 + 0.774042I$ $a = 2.07113 - 0.25770I$ $b = -0.849623 + 0.308056I$	$-1.18097 + 1.51108I$	$-2.56147 - 1.04285I$
$u = -0.000355 - 0.774042I$ $a = 2.07113 + 0.25770I$ $b = -0.849623 - 0.308056I$	$-1.18097 - 1.51108I$	$-2.56147 + 1.04285I$
$u = -1.241430 + 0.227325I$ $a = 0.236549 - 0.474818I$ $b = 0.342053 - 1.260670I$	$-2.68140 + 1.19053I$	0
$u = -1.241430 - 0.227325I$ $a = 0.236549 + 0.474818I$ $b = 0.342053 + 1.260670I$	$-2.68140 - 1.19053I$	0
$u = 0.116220 + 0.707665I$ $a = 1.044990 - 0.550262I$ $b = -0.426152 - 0.182747I$	$1.17719 + 1.40870I$	$3.29231 - 3.00363I$
$u = 0.116220 - 0.707665I$ $a = 1.044990 + 0.550262I$ $b = -0.426152 + 0.182747I$	$1.17719 - 1.40870I$	$3.29231 + 3.00363I$
$u = -0.715312 + 0.028489I$ $a = 0.85434 + 1.29507I$ $b = 0.556271 + 0.176958I$	$0.648909 - 0.975553I$	$-3.60474 - 0.46426I$
$u = -0.715312 - 0.028489I$ $a = 0.85434 - 1.29507I$ $b = 0.556271 - 0.176958I$	$0.648909 + 0.975553I$	$-3.60474 + 0.46426I$
$u = -0.378806 + 0.592823I$ $a = -0.74970 + 4.36413I$ $b = 3.08806 - 0.53632I$	$-1.97793 + 1.35936I$	$-28.8056 - 39.0048I$
$u = -0.378806 - 0.592823I$ $a = -0.74970 - 4.36413I$ $b = 3.08806 + 0.53632I$	$-1.97793 - 1.35936I$	$-28.8056 + 39.0048I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.556381 + 0.425890I$ $a = 0.709325 - 0.442191I$ $b = -0.056823 - 0.605176I$	$1.65009 + 1.91270I$	$-1.87415 + 0.42405I$
$u = 0.556381 - 0.425890I$ $a = 0.709325 + 0.442191I$ $b = -0.056823 + 0.605176I$	$1.65009 - 1.91270I$	$-1.87415 - 0.42405I$
$u = -1.33114$ $a = -3.12813$ $b = -4.38293$	$-4.62840$	$0$
$u = 0.615724 + 0.225295I$ $a = 0.442606 + 0.279319I$ $b = -1.027400 + 0.849451I$	$-0.50082 + 7.43088I$	$-9.83588 - 3.06441I$
$u = 0.615724 - 0.225295I$ $a = 0.442606 - 0.279319I$ $b = -1.027400 - 0.849451I$	$-0.50082 - 7.43088I$	$-9.83588 + 3.06441I$
$u = -0.377234 + 0.508733I$ $a = 0.910926 + 0.090831I$ $b = -0.080814 - 0.346857I$	$-0.22325 + 1.43278I$	$-1.54695 - 5.02383I$
$u = -0.377234 - 0.508733I$ $a = 0.910926 - 0.090831I$ $b = -0.080814 + 0.346857I$	$-0.22325 - 1.43278I$	$-1.54695 + 5.02383I$
$u = -0.481913 + 0.382313I$ $a = 0.472417 + 0.298979I$ $b = -0.844793 + 0.392938I$	$-0.04977 + 4.23277I$	$-3.74018 - 11.43224I$
$u = -0.481913 - 0.382313I$ $a = 0.472417 - 0.298979I$ $b = -0.844793 - 0.392938I$	$-0.04977 - 4.23277I$	$-3.74018 + 11.43224I$
$u = 1.38453 + 0.33788I$ $a = -0.331549 - 0.202544I$ $b = -0.197769 + 0.616102I$	$-2.94680 - 5.49032I$	$0$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.38453 - 0.33788I$ $a = -0.331549 + 0.202544I$ $b = -0.197769 - 0.616102I$	$-2.94680 + 5.49032I$	0
$u = -0.13459 + 1.43811I$ $a = 0.510736 + 0.169564I$ $b = -2.29528 - 0.29972I$	$-3.00179 + 4.56266I$	0
$u = -0.13459 - 1.43811I$ $a = 0.510736 - 0.169564I$ $b = -2.29528 + 0.29972I$	$-3.00179 - 4.56266I$	0
$u = 1.45101 + 0.03574I$ $a = 0.081914 - 0.620709I$ $b = 0.71394 - 1.81215I$	$-6.59261 - 2.90185I$	0
$u = 1.45101 - 0.03574I$ $a = 0.081914 + 0.620709I$ $b = 0.71394 + 1.81215I$	$-6.59261 + 2.90185I$	0
$u = 1.46452 + 0.10406I$ $a = -1.48734 + 0.15258I$ $b = -1.59100 + 0.52581I$	$-7.24514 - 2.22253I$	0
$u = 1.46452 - 0.10406I$ $a = -1.48734 - 0.15258I$ $b = -1.59100 - 0.52581I$	$-7.24514 + 2.22253I$	0
$u = 1.47132 + 0.00598I$ $a = 1.74208 - 0.11100I$ $b = 2.41570 + 0.08447I$	$-3.93524 + 7.62228I$	0
$u = 1.47132 - 0.00598I$ $a = 1.74208 + 0.11100I$ $b = 2.41570 - 0.08447I$	$-3.93524 - 7.62228I$	0
$u = 1.41409 + 0.41604I$ $a = 0.106381 + 0.389440I$ $b = -0.08739 + 1.42927I$	$-5.83012 - 5.98154I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41409 - 0.41604I$ $a = 0.106381 - 0.389440I$ $b = -0.08739 - 1.42927I$	$-5.83012 + 5.98154I$	0
$u = -0.13878 + 1.48672I$ $a = 0.755838 + 0.008269I$ $b = -2.60237 - 0.35998I$	$5.24362 + 3.10833I$	0
$u = -0.13878 - 1.48672I$ $a = 0.755838 - 0.008269I$ $b = -2.60237 + 0.35998I$	$5.24362 - 3.10833I$	0
$u = 0.424249 + 0.248865I$ $a = -1.60490 + 7.51402I$ $b = -0.626376 + 0.383358I$	$-2.15277 + 2.70026I$	$-9.88811 + 8.45872I$
$u = 0.424249 - 0.248865I$ $a = -1.60490 - 7.51402I$ $b = -0.626376 - 0.383358I$	$-2.15277 - 2.70026I$	$-9.88811 - 8.45872I$
$u = -0.345743 + 0.345351I$ $a = 5.23140 - 9.13487I$ $b = -1.17665 - 1.19040I$	$-1.72233 + 1.49478I$	$-0.6746 - 41.0959I$
$u = -0.345743 - 0.345351I$ $a = 5.23140 + 9.13487I$ $b = -1.17665 + 1.19040I$	$-1.72233 - 1.49478I$	$-0.6746 + 41.0959I$
$u = -1.50984 + 0.22948I$ $a = 1.55997 + 0.33556I$ $b = 2.38243 - 0.51571I$	$-3.74678 - 1.39146I$	0
$u = -1.50984 - 0.22948I$ $a = 1.55997 - 0.33556I$ $b = 2.38243 + 0.51571I$	$-3.74678 + 1.39146I$	0
$u = 1.52087 + 0.23706I$ $a = -2.41757 + 0.56218I$ $b = -4.64875 - 0.40405I$	$-8.26886 - 4.60408I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.52087 - 0.23706I$ $a = -2.41757 - 0.56218I$ $b = -4.64875 + 0.40405I$	$-8.26886 + 4.60408I$	0
$u = -1.56389 + 0.08723I$ $a = -0.166301 + 0.131482I$ $b = 0.044542 - 0.990744I$	$-7.30971 + 1.30866I$	0
$u = -1.56389 - 0.08723I$ $a = -0.166301 - 0.131482I$ $b = 0.044542 + 0.990744I$	$-7.30971 - 1.30866I$	0
$u = -1.50572 + 0.51745I$ $a = -0.379639 + 0.074193I$ $b = -0.510768 - 0.673818I$	$-6.14031 + 10.62530I$	0
$u = -1.50572 - 0.51745I$ $a = -0.379639 - 0.074193I$ $b = -0.510768 + 0.673818I$	$-6.14031 - 10.62530I$	0
$u = -0.16466 + 1.59990I$ $a = 0.464159 - 0.164254I$ $b = -2.70309 - 0.17160I$	$-6.96276 - 9.17383I$	0
$u = -0.16466 - 1.59990I$ $a = 0.464159 + 0.164254I$ $b = -2.70309 + 0.17160I$	$-6.96276 + 9.17383I$	0
$u = -1.64354 + 0.14674I$ $a = -1.243040 - 0.088377I$ $b = -1.59369 + 0.94791I$	$-11.25600 + 2.45702I$	0
$u = -1.64354 - 0.14674I$ $a = -1.243040 + 0.088377I$ $b = -1.59369 - 0.94791I$	$-11.25600 - 2.45702I$	0
$u = -1.61779 + 0.33663I$ $a = -1.260540 - 0.374517I$ $b = -1.91931 - 0.36768I$	$-10.89770 + 7.17611I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.61779 - 0.33663I$ $a = -1.260540 + 0.374517I$ $b = -1.91931 + 0.36768I$	$-10.89770 - 7.17611I$	0
$u = -0.230559 + 0.235592I$ $a = 2.01640 - 0.20890I$ $b = 0.988240 - 0.430122I$	$-1.89908 + 0.79590I$	$-4.83770 + 0.82015I$
$u = -0.230559 - 0.235592I$ $a = 2.01640 + 0.20890I$ $b = 0.988240 + 0.430122I$	$-1.89908 - 0.79590I$	$-4.83770 - 0.82015I$
$u = 1.55975 + 0.62424I$ $a = 1.44242 - 0.64185I$ $b = 2.71325 + 0.97362I$	$-8.2935 - 11.7637I$	0
$u = 1.55975 - 0.62424I$ $a = 1.44242 + 0.64185I$ $b = 2.71325 - 0.97362I$	$-8.2935 + 11.7637I$	0
$u = 0.33491 + 1.65140I$ $a = 0.521990 - 0.114366I$ $b = -2.61863 + 0.78521I$	$-6.64004 + 0.42401I$	0
$u = 0.33491 - 1.65140I$ $a = 0.521990 + 0.114366I$ $b = -2.61863 - 0.78521I$	$-6.64004 - 0.42401I$	0
$u = -1.55571 + 0.78921I$ $a = 1.30436 + 0.75861I$ $b = 2.70847 - 1.25612I$	$-11.3053 + 17.4741I$	0
$u = -1.55571 - 0.78921I$ $a = 1.30436 - 0.75861I$ $b = 2.70847 + 1.25612I$	$-11.3053 - 17.4741I$	0
$u = -1.62516 + 0.70906I$ $a = 1.218970 + 0.523530I$ $b = 2.46724 - 1.50899I$	$-7.62809 + 3.43602I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.62516 - 0.70906I$		
$a = 1.218970 - 0.523530I$	$-7.62809 - 3.43602I$	0
$b = 2.46724 + 1.50899I$		
$u = 1.60150 + 0.85618I$		
$a = 1.146330 - 0.596908I$	$-10.63730 - 9.31613I$	0
$b = 2.37731 + 1.76533I$		
$u = 1.60150 - 0.85618I$		
$a = 1.146330 + 0.596908I$	$-10.63730 + 9.31613I$	0
$b = 2.37731 - 1.76533I$		
$u = -1.79507 + 0.49521I$		
$a = 1.331820 + 0.400074I$	$-13.6570 + 7.5061I$	0
$b = 3.11758 - 0.72547I$		
$u = -1.79507 - 0.49521I$		
$a = 1.331820 - 0.400074I$	$-13.6570 - 7.5061I$	0
$b = 3.11758 + 0.72547I$		
$u = 1.83627 + 0.59317I$		
$a = 1.180040 - 0.374782I$	$-13.24420 + 0.87431I$	0
$b = 2.90054 + 1.35306I$		
$u = 1.83627 - 0.59317I$		
$a = 1.180040 + 0.374782I$	$-13.24420 - 0.87431I$	0
$b = 2.90054 - 1.35306I$		

**II.**

$$I_2^u = \langle 2u^3 + 2u^2 + b + 5u + 1, -u^3 - 3u^2 + a - 3u - 6, u^4 + u^3 + 3u^2 + 2u + 1 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^3 + 3u^2 + 3u + 6 \\ -2u^3 - 2u^2 - 5u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 + 3u^2 + 3u + 7 \\ -2u^3 - u^2 - 5u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 11u^3 + 4u^2 + 27u + 5 \\ 3u^3 + 4u^2 + 8u + 8 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 - 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^3 + 3u^2 + 3u + 7 \\ -2u^3 - u^2 - 5u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 + 2u \\ u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 + 2u \\ u^3 + u^2 + 2u + 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

$$\text{(iii) Cusp Shapes} = -23u^3 - 11u^2 - 70u - 48$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^4 - u^3 + 3u^2 - 2u + 1$
$c_2$	$u^4 - u^3 + u^2 + 1$
$c_3$	$u^4 + u^3 + 5u^2 - u + 2$
$c_5$	$u^4 + u^3 + u^2 + 1$
$c_6, c_7$	$u^4 - 2u^3 + 7u^2 - 5u + 1$
$c_8$	$u^4 + u^3 + 3u^2 + 2u + 1$
$c_9$	$(u - 1)^4$
$c_{10}$	$u^4$
$c_{11}$	$(u + 1)^4$
$c_{12}$	$u^4 + 5u^3 + 7u^2 + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4, c_8$	$y^4 + 5y^3 + 7y^2 + 2y + 1$
$c_2, c_5$	$y^4 + y^3 + 3y^2 + 2y + 1$
$c_3$	$y^4 + 9y^3 + 31y^2 + 19y + 4$
$c_6, c_7$	$y^4 + 10y^3 + 31y^2 - 11y + 1$
$c_9, c_{11}$	$(y - 1)^4$
$c_{10}$	$y^4$
$c_{12}$	$y^4 - 11y^3 + 31y^2 + 10y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.395123 + 0.506844I$		
$a = 4.75515 + 0.42612I$	$-1.85594 + 1.41510I$	$-24.8178 - 33.5385I$
$b = 0.69151 - 1.94753I$		
$u = -0.395123 - 0.506844I$		
$a = 4.75515 - 0.42612I$	$-1.85594 - 1.41510I$	$-24.8178 + 33.5385I$
$b = 0.69151 + 1.94753I$		
$u = -0.10488 + 1.55249I$		
$a = -0.755148 - 0.010081I$	$5.14581 + 3.16396I$	$-31.6822 - 20.2078I$
$b = 2.80849 + 0.27009I$		
$u = -0.10488 - 1.55249I$		
$a = -0.755148 + 0.010081I$	$5.14581 - 3.16396I$	$-31.6822 + 20.2078I$
$b = 2.80849 - 0.27009I$		



$$\text{III. } I_1^v = \langle a, 3.10 \times 10^5 v^{11} + 7.90 \times 10^5 v^{10} + \dots + 7.08 \times 10^5 b + 1.25 \times 10^6, v^{12} + 3v^{11} + \dots + v + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -0.437990v^{11} - 1.11658v^{10} + \dots + 0.432058v - 1.76482 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1.00827v^{11} + 2.68986v^{10} + \dots - 1.09637v + 2.28028 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1.00827v^{11} - 2.68986v^{10} + \dots + 1.09637v - 1.28028 \\ -1.62222v^{11} - 4.40786v^{10} + \dots + 1.83221v - 1.73501 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1.24751v^{11} + 3.51726v^{10} + \dots - 1.51765v + 2.58875 \\ 1.86146v^{11} + 5.23525v^{10} + \dots - 2.25349v + 3.04348 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.437990v^{11} - 1.11658v^{10} + \dots + 0.432058v - 1.76482 \\ -0.437990v^{11} - 1.11658v^{10} + \dots + 0.432058v - 1.76482 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1.24751v^{11} - 3.51726v^{10} + \dots + 1.51765v - 2.58875 \\ -1.86146v^{11} - 5.23525v^{10} + \dots + 2.25349v - 3.04348 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1.05885v^{11} + 2.76249v^{10} + \dots + 0.419689v + 2.48147 \\ 0.861460v^{11} + 2.23525v^{10} + \dots + 1.74651v + 2.04348 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.667414v^{11} + 1.61644v^{10} + \dots + 0.932022v + 2.13235 \\ 0.861460v^{11} + 2.23525v^{10} + \dots + 1.74651v + 2.04348 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = \frac{1558019}{235911}v^{11} + \frac{3765626}{235911}v^{10} + \dots - \frac{4340683}{235911}v + \frac{3615109}{235911}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_5$	$(u^2 - u + 1)^6$
$c_2$	$(u^2 + u + 1)^6$
$c_4, c_8$	$u^{12}$
$c_6, c_{10}, c_{11}$	$(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$
$c_7, c_{12}$	$(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$
$c_9$	$(u^6 + u^5 - u^4 - 2u^3 + u + 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5$	$(y^2 + y + 1)^6$
$c_4, c_8$	$y^{12}$
$c_6, c_9, c_{10}$ $c_{11}$	$(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$
$c_7, c_{12}$	$(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.834826 + 0.083652I$ $a = 0$ $b = -0.428243 + 0.664531I$	$1.89061 + 1.10558I$	$3.79900 - 2.81207I$
$v = 0.834826 - 0.083652I$ $a = 0$ $b = -0.428243 - 0.664531I$	$1.89061 - 1.10558I$	$3.79900 + 2.81207I$
$v = -0.489858 + 0.681154I$ $a = 0$ $b = -0.428243 + 0.664531I$	$1.89061 - 2.95419I$	$1.04064 + 4.93773I$
$v = -0.489858 - 0.681154I$ $a = 0$ $b = -0.428243 - 0.664531I$	$1.89061 + 2.95419I$	$1.04064 - 4.93773I$
$v = -0.458424 + 0.081263I$ $a = 0$ $b = -1.073950 - 0.558752I$	$-7.72290I$	$2.53591 + 10.48596I$
$v = -0.458424 - 0.081263I$ $a = 0$ $b = -1.073950 + 0.558752I$	$7.72290I$	$2.53591 - 10.48596I$
$v = 0.299588 + 0.356375I$ $a = 0$ $b = -1.073950 - 0.558752I$	$-3.66314I$	$-2.83009 - 2.28483I$
$v = 0.299588 - 0.356375I$ $a = 0$ $b = -1.073950 + 0.558752I$	$3.66314I$	$-2.83009 + 2.28483I$
$v = -2.51133 + 0.49706I$ $a = 0$ $b = 1.002190 - 0.295542I$	$-1.89061 + 2.95419I$	$0.48408 - 6.69677I$
$v = -2.51133 - 0.49706I$ $a = 0$ $b = 1.002190 + 0.295542I$	$-1.89061 - 2.95419I$	$0.48408 + 6.69677I$

Solutions to $I_1^v$		$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v =$	$0.82520 + 2.42341I$	$-1.89061 + 1.10558I$	$-11.02954 + 1.23660I$
$a =$	$0$		
$b =$	$1.002190 + 0.295542I$		
$v =$	$0.82520 - 2.42341I$	$-1.89061 - 1.10558I$	$-11.02954 - 1.23660I$
$a =$	$0$		
$b =$	$1.002190 - 0.295542I$		

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u^2 - u + 1)^6)(u^4 - u^3 + 3u^2 - 2u + 1)(u^{77} + 42u^{76} + \dots - 173u - 1)$
$c_2$	$((u^2 + u + 1)^6)(u^4 - u^3 + u^2 + 1)(u^{77} + 8u^{76} + \dots + 3u + 1)$
$c_3$	$((u^2 - u + 1)^6)(u^4 + u^3 + 5u^2 - u + 2)(u^{77} - 8u^{76} + \dots + 2520u + 1732)$
$c_4$	$u^{12}(u^4 - u^3 + 3u^2 - 2u + 1)(u^{77} + 2u^{76} + \dots + 20480u + 4096)$
$c_5$	$((u^2 - u + 1)^6)(u^4 + u^3 + u^2 + 1)(u^{77} + 8u^{76} + \dots + 3u + 1)$
$c_6$	$(u^4 - 2u^3 + 7u^2 - 5u + 1)(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$ $\cdot (u^{77} - u^{76} + \dots + 7631854u - 2351327)$
$c_7$	$(u^4 - 2u^3 + 7u^2 - 5u + 1)(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$ $\cdot (u^{77} - 7u^{76} + \dots - 18228u - 7979)$
$c_8$	$u^{12}(u^4 + u^3 + 3u^2 + 2u + 1)(u^{77} + 2u^{76} + \dots + 20480u + 4096)$
$c_9$	$((u - 1)^4)(u^6 + u^5 + \dots + u + 1)^2(u^{77} - 7u^{76} + \dots - 65u + 1)$
$c_{10}$	$u^4(u^6 - u^5 + \dots - u + 1)^2(u^{77} + 13u^{76} + \dots - 200u - 16)$
$c_{11}$	$((u + 1)^4)(u^6 - u^5 + \dots - u + 1)^2(u^{77} - 7u^{76} + \dots - 65u + 1)$
$c_{12}$	$(u^4 + 5u^3 + 7u^2 + 2u + 1)(u^6 - 3u^5 + 5u^4 - 4u^3 + 2u^2 - u + 1)^2$ $\cdot (u^{77} + 4u^{76} + \dots - 3u - 1)$

## V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y^2 + y + 1)^6)(y^4 + 5y^3 + \dots + 2y + 1)(y^{77} - 6y^{76} + \dots + 13671y - 1)$
$c_2, c_5$	$((y^2 + y + 1)^6)(y^4 + y^3 + 3y^2 + 2y + 1)(y^{77} + 42y^{76} + \dots - 173y - 1)$
$c_3$	$(y^2 + y + 1)^6(y^4 + 9y^3 + 31y^2 + 19y + 4)$ $\cdot (y^{77} - 54y^{76} + \dots - 552548680y - 2999824)$
$c_4, c_8$	$y^{12}(y^4 + 5y^3 + 7y^2 + 2y + 1)$ $\cdot (y^{77} - 60y^{76} + \dots + 234881024y - 16777216)$
$c_6$	$(y^4 + 10y^3 + 31y^2 - 11y + 1)(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$ $\cdot (y^{77} - 9y^{76} + \dots - 135685107448604y - 5528738660929)$
$c_7$	$(y^4 + 10y^3 + 31y^2 - 11y + 1)(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$ $\cdot (y^{77} - 77y^{76} + \dots + 2964755496y - 63664441)$
$c_9, c_{11}$	$(y - 1)^4(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$ $\cdot (y^{77} - 63y^{76} + \dots - 2399y - 1)$
$c_{10}$	$y^4(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$ $\cdot (y^{77} + 21y^{76} + \dots + 15168y - 256)$
$c_{12}$	$(y^4 - 11y^3 + 31y^2 + 10y + 1)(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$ $\cdot (y^{77} + 2y^{76} + \dots - 29y - 1)$