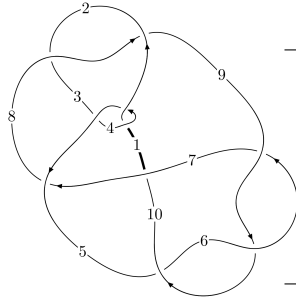
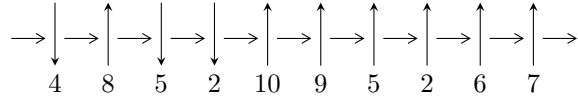


10₁₃₀ (K10n₂₀)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$5,10 \xrightarrow{c_5} 2,6 \xrightarrow{c_4} 4 \xrightarrow{c_1} 1 \xrightarrow{c_3} 3 \xrightarrow{c_9} 9 \xrightarrow{c_6} 7 \xrightarrow{c_8} 8 \longrightarrow c_2, c_7, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -u^7 + u^6 - 4u^5 + 3u^4 - 4u^3 + 2u^2 + b - 1, \\ -u^{10} + 2u^9 - 8u^8 + 11u^7 - 20u^6 + 19u^5 - 17u^4 + 8u^3 - u^2 + a - 5u + 1, \\ u^{11} - 2u^{10} + 8u^9 - 12u^8 + 22u^7 - 24u^6 + 24u^5 - 15u^4 + 7u^3 + 3u^2 - 2u + 1 \rangle$$

$$I_2^u = \langle b + 1, -u^2 + a - u - 1, u^3 + u^2 + 2u + 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 14 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -u^7 + u^6 - 4u^5 + 3u^4 - 4u^3 + 2u^2 + b - 1, -u^{10} + 2u^9 + \dots + a + 1, u^{11} - 2u^{10} + \dots - 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{10} - 2u^9 + 8u^8 - 11u^7 + 20u^6 - 19u^5 + 17u^4 - 8u^3 + u^2 + 5u - 1 \\ u^7 - u^6 + 4u^5 - 3u^4 + 4u^3 - 2u^2 + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{10} + 2u^9 - 7u^8 + 10u^7 - 16u^6 + 15u^5 - 13u^4 + 4u^3 - u^2 - 4u + 1 \\ u^8 - u^7 + 5u^6 - 4u^5 + 7u^4 - 4u^3 + 2u^2 + u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{10} + 2u^9 - 6u^8 + 9u^7 - 11u^6 + 11u^5 - 6u^4 + u^2 - 3u \\ u^8 - u^7 + 5u^6 - 4u^5 + 7u^4 - 4u^3 + 2u^2 + u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^4 - u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -u^{10} + 2u^9 - 7u^8 + 8u^7 - 12u^6 + 3u^5 + 3u^4 - 16u^3 + 15u^2 - 13u + 1$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4	$u^{11} - 4u^{10} - u^9 + 17u^8 + u^7 - 40u^6 + 3u^5 + 37u^4 - 3u^3 - 9u^2 + 7u - 1$
c_2, c_8	$u^{11} - u^{10} + \dots - 4u - 8$
c_3	$u^{11} + 18u^{10} + \dots + 31u + 1$
c_5, c_6, c_9	$u^{11} + 2u^{10} + \dots - 2u - 1$
c_7	$u^{11} + 12u^9 + 36u^7 - 2u^6 + 2u^5 - 13u^4 + 13u^3 - u^2 - 1$
c_{10}	$u^{11} - 2u^{10} + \dots - 6u - 9$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4	$y^{11} - 18y^{10} + \dots + 31y - 1$
c_2, c_8	$y^{11} + 21y^{10} + \dots + 336y - 64$
c_3	$y^{11} - 46y^{10} + \dots + 863y - 1$
c_5, c_6, c_9	$y^{11} + 12y^{10} + \dots - 2y - 1$
c_7	$y^{11} + 24y^{10} + \dots - 2y - 1$
c_{10}	$y^{11} + 12y^{10} + \dots - 594y - 81$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.816018 + 0.563764I$ $a = -0.368670 - 1.053910I$ $b = -1.86528 + 0.08844I$	$-12.35850 + 2.70718I$	$0.47291 - 2.44627I$
$u = 0.816018 - 0.563764I$ $a = -0.368670 + 1.053910I$ $b = -1.86528 - 0.08844I$	$-12.35850 - 2.70718I$	$0.47291 + 2.44627I$
$u = -0.157733 + 1.338590I$ $a = -0.577850 + 0.189675I$ $b = -0.283200 + 0.366521I$	$-3.43504 - 2.25109I$	$3.70368 + 2.34373I$
$u = -0.157733 - 1.338590I$ $a = -0.577850 - 0.189675I$ $b = -0.283200 - 0.366521I$	$-3.43504 + 2.25109I$	$3.70368 - 2.34373I$
$u = 0.05807 + 1.49843I$ $a = 1.69315 + 0.17490I$ $b = 1.26769 - 0.68760I$	$-8.01785 + 1.82060I$	$-2.54374 - 1.21714I$
$u = 0.05807 - 1.49843I$ $a = 1.69315 - 0.17490I$ $b = 1.26769 + 0.68760I$	$-8.01785 - 1.82060I$	$-2.54374 + 1.21714I$
$u = -0.480017$ $a = -0.562904$ $b = -0.182568$	0.824865	12.3320
$u = 0.238107 + 0.385438I$ $a = 0.41631 + 1.75871I$ $b = 0.911055 - 0.299346I$	$-1.69473 + 0.83621I$	$-2.12521 - 2.51411I$
$u = 0.238107 - 0.385438I$ $a = 0.41631 - 1.75871I$ $b = 0.911055 + 0.299346I$	$-1.69473 - 0.83621I$	$-2.12521 + 2.51411I$
$u = 0.28555 + 1.56335I$ $a = -1.88149 - 0.96849I$ $b = -1.93898 + 0.26128I$	$-19.3195 + 6.7782I$	$-2.17368 - 2.81310I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.28555 - 1.56335I$		
$a = -1.88149 + 0.96849I$	$-19.3195 - 6.7782I$	$-2.17368 + 2.81310I$
$b = -1.93898 - 0.26128I$		

$$\text{II. } I_2^u = \langle b + 1, -u^2 + a - u - 1, u^3 + u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + u + 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + u + 2 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 + u + 1 \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^2 + 1 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u^2 - u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $3u^2 + 4u + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_3	$(u - 1)^3$
c_2, c_8	u^3
c_4	$(u + 1)^3$
c_5, c_6	$u^3 + u^2 + 2u + 1$
c_7, c_{10}	$u^3 + u^2 - 1$
c_9	$u^3 - u^2 + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_3, c_4	$(y - 1)^3$
c_2, c_8	y^3
c_5, c_6, c_9	$y^3 + 3y^2 + 2y - 1$
c_7, c_{10}	$y^3 - y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.215080 + 1.307140I$ $a = -0.877439 + 0.744862I$ $b = -1.00000$	$-4.66906 - 2.82812I$	$-1.84740 + 3.54173I$
$u = -0.215080 - 1.307140I$ $a = -0.877439 - 0.744862I$ $b = -1.00000$	$-4.66906 + 2.82812I$	$-1.84740 - 3.54173I$
$u = -0.569840$ $a = 0.754878$ $b = -1.00000$	-0.531480	2.69480

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u-1)^3 \cdot (u^{11} - 4u^{10} - u^9 + 17u^8 + u^7 - 40u^6 + 3u^5 + 37u^4 - 3u^3 - 9u^2 + 7u - 1)$
c_2, c_8	$u^3(u^{11} - u^{10} + \dots - 4u - 8)$
c_3	$((u-1)^3)(u^{11} + 18u^{10} + \dots + 31u + 1)$
c_4	$(u+1)^3 \cdot (u^{11} - 4u^{10} - u^9 + 17u^8 + u^7 - 40u^6 + 3u^5 + 37u^4 - 3u^3 - 9u^2 + 7u - 1)$
c_5, c_6	$(u^3 + u^2 + 2u + 1)(u^{11} + 2u^{10} + \dots - 2u - 1)$
c_7	$(u^3 + u^2 - 1)(u^{11} + 12u^9 + 36u^7 - 2u^6 + 2u^5 - 13u^4 + 13u^3 - u^2 - 1)$
c_9	$(u^3 - u^2 + 2u - 1)(u^{11} + 2u^{10} + \dots - 2u - 1)$
c_{10}	$(u^3 + u^2 - 1)(u^{11} - 2u^{10} + \dots - 6u - 9)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_4	$((y - 1)^3)(y^{11} - 18y^{10} + \dots + 31y - 1)$
c_2, c_8	$y^3(y^{11} + 21y^{10} + \dots + 336y - 64)$
c_3	$((y - 1)^3)(y^{11} - 46y^{10} + \dots + 863y - 1)$
c_5, c_6, c_9	$(y^3 + 3y^2 + 2y - 1)(y^{11} + 12y^{10} + \dots - 2y - 1)$
c_7	$(y^3 - y^2 + 2y - 1)(y^{11} + 24y^{10} + \dots - 2y - 1)$
c_{10}	$(y^3 - y^2 + 2y - 1)(y^{11} + 12y^{10} + \dots - 594y - 81)$