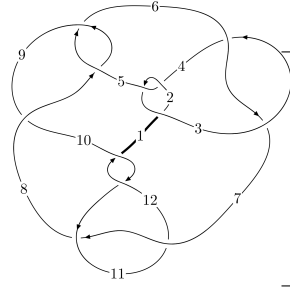
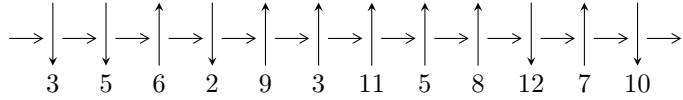


12n₀₀₉₇ (K12n₀₀₉₇)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$5,8 \xrightarrow{c_8} 9 \xrightarrow{c_5} 6 \xrightarrow{c_9} 3,10 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_{12}} 12 \xrightarrow{c_{10}} 11 \xrightarrow{c_7} 7 \twoheadrightarrow c_3, c_6, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -1.08330 \times 10^{15} u^{28} + 2.63231 \times 10^{15} u^{27} + \dots + 2.88806 \times 10^{15} b - 3.18100 \times 10^{15}, \\ -1.08330 \times 10^{15} u^{28} + 2.63231 \times 10^{15} u^{27} + \dots + 2.88806 \times 10^{15} a - 3.18100 \times 10^{15}, u^{29} - 2u^{28} + \dots + u - \\ I_2^u = \langle -u^8 - u^7 + 2u^6 + 3u^5 - u^4 - 3u^3 - 2u^2 + b + u + 1, -u^8 - u^7 + 2u^6 + 3u^5 - u^4 - 3u^3 - 2u^2 + a + 1, \\ u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 38 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -1.08 \times 10^{15} u^{28} + 2.63 \times 10^{15} u^{27} + \dots + 2.89 \times 10^{15} b - 3.18 \times 10^{15}, -1.08 \times 10^{15} u^{28} + 2.63 \times 10^{15} u^{27} + \dots + 2.89 \times 10^{15} a - 3.18 \times 10^{15}, u^{29} - 2u^{28} + \dots + u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.375096u^{28} - 0.911447u^{27} + \dots - 0.238354u + 1.10143 \\ 0.375096u^{28} - 0.911447u^{27} + \dots + 0.761646u + 1.10143 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.375096u^{28} - 0.911447u^{27} + \dots - 0.238354u + 1.10143 \\ 0.240332u^{28} - 0.538132u^{27} + \dots + 0.225295u + 1.26269 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.360721u^{28} - 0.778371u^{27} + \dots - 0.736984u + 0.338038 \\ 0.0965394u^{28} - 0.0157569u^{27} + \dots - 0.674515u + 0.641092 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.259382u^{28} - 0.660563u^{27} + \dots + 0.000197369u + 0.997644 \\ 0.264728u^{28} - 0.644578u^{27} + \dots + 1.13537u + 0.978187 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.0381007u^{28} + 0.244861u^{27} + \dots - 0.549804u + 0.530085 \\ -0.153814u^{28} + 0.495745u^{27} + \dots - 0.311253u + 0.426298 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.00860430u^{28} - 0.157377u^{27} + \dots + 0.318117u - 0.890976 \\ -0.00366395u^{28} - 0.0860215u^{27} + \dots + 0.240983u - 1.25230 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.264182u^{28} + 0.762614u^{27} + \dots + 0.0624682u + 0.303054 \\ -0.148468u^{28} + 0.511730u^{27} + \dots - 0.176083u + 0.406841 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{16119990594582668}{2888060083449331} u^{28} - \frac{28126461598340071}{2888060083449331} u^{27} + \dots + \frac{17982394285452960}{2888060083449331} u + \frac{11832001216098990}{2888060083449331}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{29} + 48u^{28} + \dots + 79u + 1$
c_2, c_4	$u^{29} - 10u^{28} + \dots + 19u - 1$
c_3, c_6	$u^{29} + 5u^{28} + \dots + 1536u - 512$
c_5, c_8	$u^{29} - 2u^{28} + \dots + u - 1$
c_7, c_{11}	$u^{29} + 2u^{28} + \dots - u - 1$
c_9	$u^{29} + 30u^{27} + \dots - u - 1$
c_{10}, c_{12}	$u^{29} + 12u^{28} + \dots - u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{29} - 124y^{28} + \dots - 7313y - 1$
c_2, c_4	$y^{29} - 48y^{28} + \dots + 79y - 1$
c_3, c_6	$y^{29} + 57y^{28} + \dots + 3932160y - 262144$
c_5, c_8	$y^{29} + 30y^{27} + \dots - y - 1$
c_7, c_{11}	$y^{29} + 12y^{28} + \dots - y - 1$
c_9	$y^{29} + 60y^{28} + \dots - 5y - 1$
c_{10}, c_{12}	$y^{29} + 12y^{28} + \dots + 19y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.365827 + 0.867755I$		
$a = -0.58586 - 1.71900I$	$-3.76536 + 5.51790I$	$-3.77377 - 7.24287I$
$b = -0.220028 - 0.851246I$		
$u = 0.365827 - 0.867755I$		
$a = -0.58586 + 1.71900I$	$-3.76536 - 5.51790I$	$-3.77377 + 7.24287I$
$b = -0.220028 + 0.851246I$		
$u = 1.038780 + 0.399171I$		
$a = -0.532542 - 0.137121I$	$3.61222 + 0.74335I$	$9.35759 + 0.47912I$
$b = 0.506240 + 0.262051I$		
$u = 1.038780 - 0.399171I$		
$a = -0.532542 + 0.137121I$	$3.61222 - 0.74335I$	$9.35759 - 0.47912I$
$b = 0.506240 - 0.262051I$		
$u = 0.149316 + 0.856366I$		
$a = -0.21482 - 2.05855I$	$-4.88663 - 0.95031I$	$-6.59475 + 1.19001I$
$b = -0.065503 - 1.202180I$		
$u = 0.149316 - 0.856366I$		
$a = -0.21482 + 2.05855I$	$-4.88663 + 0.95031I$	$-6.59475 - 1.19001I$
$b = -0.065503 + 1.202180I$		
$u = -1.024520 + 0.534163I$		
$a = 0.624645 - 0.175606I$	$2.77162 - 6.24281I$	$6.28797 + 4.80418I$
$b = -0.399874 + 0.358557I$		
$u = -1.024520 - 0.534163I$		
$a = 0.624645 + 0.175606I$	$2.77162 + 6.24281I$	$6.28797 - 4.80418I$
$b = -0.399874 - 0.358557I$		
$u = -0.350587 + 0.709669I$		
$a = 0.21366 - 1.51930I$	$-1.85641 - 1.40408I$	$-0.21276 + 2.68754I$
$b = -0.136928 - 0.809633I$		
$u = -0.350587 - 0.709669I$		
$a = 0.21366 + 1.51930I$	$-1.85641 + 1.40408I$	$-0.21276 - 2.68754I$
$b = -0.136928 + 0.809633I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.563294 + 0.524681I$ $a = 0.170413 - 0.678152I$ $b = -0.392881 - 0.153472I$	$-1.43698 - 1.52178I$	$-1.26786 + 4.70761I$
$u = -0.563294 - 0.524681I$ $a = 0.170413 + 0.678152I$ $b = -0.392881 + 0.153472I$	$-1.43698 + 1.52178I$	$-1.26786 - 4.70761I$
$u = 0.702050$ $a = -0.244600$ $b = 0.457450$	0.941539	11.3890
$u = -0.121762 + 0.604163I$ $a = -0.084430 + 0.174292I$ $b = -0.206192 + 0.778455I$	$0.47173 + 2.34023I$	$2.64159 - 2.77169I$
$u = -0.121762 - 0.604163I$ $a = -0.084430 - 0.174292I$ $b = -0.206192 - 0.778455I$	$0.47173 - 2.34023I$	$2.64159 + 2.77169I$
$u = -0.444471 + 0.402241I$ $a = -0.957420 - 0.680211I$ $b = -1.40189 - 0.27797I$	$-1.17268 - 1.39986I$	$-2.59264 + 6.14012I$
$u = -0.444471 - 0.402241I$ $a = -0.957420 + 0.680211I$ $b = -1.40189 + 0.27797I$	$-1.17268 + 1.39986I$	$-2.59264 - 6.14012I$
$u = 0.508912 + 0.193701I$ $a = 1.88309 - 0.38641I$ $b = 2.39201 - 0.19271I$	$-1.87493 - 2.49067I$	$4.89703 - 8.29090I$
$u = 0.508912 - 0.193701I$ $a = 1.88309 + 0.38641I$ $b = 2.39201 + 0.19271I$	$-1.87493 + 2.49067I$	$4.89703 + 8.29090I$
$u = 1.07631 + 1.11196I$ $a = -0.679049 + 1.085630I$ $b = 0.39726 + 2.19758I$	$-14.1601 + 12.3738I$	$-0.83426 - 6.38685I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.07631 - 1.11196I$ $a = -0.679049 - 1.085630I$ $b = 0.39726 - 2.19758I$	$-14.1601 - 12.3738I$	$-0.83426 + 6.38685I$
$u = -1.08388 + 1.11855I$ $a = 0.705879 + 1.020200I$ $b = -0.37800 + 2.13875I$	$-12.19450 - 6.48359I$	$1.17949 + 2.27770I$
$u = -1.08388 - 1.11855I$ $a = 0.705879 - 1.020200I$ $b = -0.37800 - 2.13875I$	$-12.19450 + 6.48359I$	$1.17949 - 2.27770I$
$u = 1.09561 + 1.10785I$ $a = -0.847927 + 1.022520I$ $b = 0.24768 + 2.13037I$	$-18.7416 + 4.0694I$	$-3.78877 - 1.98533I$
$u = 1.09561 - 1.10785I$ $a = -0.847927 - 1.022520I$ $b = 0.24768 - 2.13037I$	$-18.7416 - 4.0694I$	$-3.78877 + 1.98533I$
$u = 1.11251 + 1.10380I$ $a = -0.923170 + 0.842832I$ $b = 0.18934 + 1.94663I$	$-14.0670 - 4.2413I$	$-1.00950 + 2.34740I$
$u = 1.11251 - 1.10380I$ $a = -0.923170 - 0.842832I$ $b = 0.18934 - 1.94663I$	$-14.0670 + 4.2413I$	$-1.00950 - 2.34740I$
$u = -1.10978 + 1.11274I$ $a = 0.849824 + 0.873104I$ $b = -0.25996 + 1.98584I$	$-12.12700 - 1.69249I$	$1.01629 + 1.84111I$
$u = -1.10978 - 1.11274I$ $a = 0.849824 - 0.873104I$ $b = -0.25996 - 1.98584I$	$-12.12700 + 1.69249I$	$1.01629 - 1.84111I$

$$\text{II. } I_2^u = \langle -u^8 - u^7 + \cdots + b + 1, -u^8 - u^7 + \cdots + a + 1, u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^8 + u^7 - 2u^6 - 3u^5 + u^4 + 3u^3 + 2u^2 - 1 \\ u^8 + u^7 - 2u^6 - 3u^5 + u^4 + 3u^3 + 2u^2 - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^8 + u^7 - 2u^6 - 3u^5 + u^4 + 3u^3 + 2u^2 - 1 \\ u^8 + u^7 - 2u^6 - 3u^5 + u^4 + 3u^3 + 2u^2 - 2u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^8 + u^7 - 2u^6 - 3u^5 + u^4 + 3u^3 + 2u^2 - 1 \\ u^8 + u^7 - 2u^6 - 3u^5 + u^4 + 3u^3 + 2u^2 - u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^5 + 2u^3 - u \\ -u^5 + u^3 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^8 + 3u^6 - 3u^4 + 1 \\ -u^8 + 2u^6 - 2u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-u^8 + 2u^7 + 2u^6 - 3u^5 - 6u^4 + 3u^3 + 3u^2 + 4u - 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^9$
c_3, c_6	u^9
c_4	$(u + 1)^9$
c_5	$u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$
c_7	$u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$
c_8	$u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$
c_9	$u^9 - 5u^8 + 12u^7 - 15u^6 + 9u^5 + u^4 - 4u^3 + 2u^2 + u - 1$
c_{10}	$u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$
c_{11}	$u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$
c_{12}	$u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^9$
c_3, c_6	y^9
c_5, c_8	$y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$
c_7, c_{11}	$y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1$
c_9	$y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$
c_{10}, c_{12}	$y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.772920 + 0.510351I$ $a = -0.900982 - 0.594909I$ $b = -0.128062 - 1.105260I$	$-3.42837 - 2.09337I$	$-3.06656 + 3.71284I$
$u = -0.772920 - 0.510351I$ $a = -0.900982 + 0.594909I$ $b = -0.128062 + 1.105260I$	$-3.42837 + 2.09337I$	$-3.06656 - 3.71284I$
$u = 0.825933$ $a = 1.21075$ $b = 0.384820$	-0.446489	2.03810
$u = 1.173910 + 0.391555I$ $a = 0.766570 - 0.255687I$ $b = -0.407341 - 0.647242I$	$2.72642 + 1.33617I$	$2.51011 - 2.54413I$
$u = 1.173910 - 0.391555I$ $a = 0.766570 + 0.255687I$ $b = -0.407341 + 0.647242I$	$2.72642 - 1.33617I$	$2.51011 + 2.54413I$
$u = -0.141484 + 0.739668I$ $a = -0.249476 - 1.304240I$ $b = -0.10799 - 2.04391I$	$-1.02799 + 2.45442I$	$-4.16828 - 1.00072I$
$u = -0.141484 - 0.739668I$ $a = -0.249476 + 1.304240I$ $b = -0.10799 + 2.04391I$	$-1.02799 - 2.45442I$	$-4.16828 + 1.00072I$
$u = -1.172470 + 0.500383I$ $a = -0.721488 - 0.307914I$ $b = 0.450985 - 0.808297I$	$1.95319 - 7.08493I$	$1.70570 + 8.17350I$
$u = -1.172470 - 0.500383I$ $a = -0.721488 + 0.307914I$ $b = 0.450985 + 0.808297I$	$1.95319 + 7.08493I$	$1.70570 - 8.17350I$

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u - 1)^9)(u^{29} + 48u^{28} + \dots + 79u + 1)$
c_2	$((u - 1)^9)(u^{29} - 10u^{28} + \dots + 19u - 1)$
c_3, c_6	$u^9(u^{29} + 5u^{28} + \dots + 1536u - 512)$
c_4	$((u + 1)^9)(u^{29} - 10u^{28} + \dots + 19u - 1)$
c_5	$(u^9 - u^8 + \dots - u + 1)(u^{29} - 2u^{28} + \dots + u - 1)$
c_7	$(u^9 - u^8 + \dots + u + 1)(u^{29} + 2u^{28} + \dots - u - 1)$
c_8	$(u^9 + u^8 + \dots - u - 1)(u^{29} - 2u^{28} + \dots + u - 1)$
c_9	$(u^9 - 5u^8 + 12u^7 - 15u^6 + 9u^5 + u^4 - 4u^3 + 2u^2 + u - 1)$ $\cdot (u^{29} + 30u^{27} + \dots - u - 1)$
c_{10}	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)$ $\cdot (u^{29} + 12u^{28} + \dots - u - 1)$
c_{11}	$(u^9 + u^8 + \dots + u - 1)(u^{29} + 2u^{28} + \dots - u - 1)$
c_{12}	$(u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)$ $\cdot (u^{29} + 12u^{28} + \dots - u - 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^9)(y^{29} - 124y^{28} + \dots - 7313y - 1)$
c_2, c_4	$((y - 1)^9)(y^{29} - 48y^{28} + \dots + 79y - 1)$
c_3, c_6	$y^9(y^{29} + 57y^{28} + \dots + 3932160y - 262144)$
c_5, c_8	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot (y^{29} + 30y^{27} + \dots - y - 1)$
c_7, c_{11}	$(y^9 + 3y^8 + 8y^7 + 13y^6 + 17y^5 + 17y^4 + 12y^3 + 6y^2 + y - 1)$ $\cdot (y^{29} + 12y^{28} + \dots - y - 1)$
c_9	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)$ $\cdot (y^{29} + 60y^{28} + \dots - 5y - 1)$
c_{10}, c_{12}	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)$ $\cdot (y^{29} + 12y^{28} + \dots + 19y - 1)$