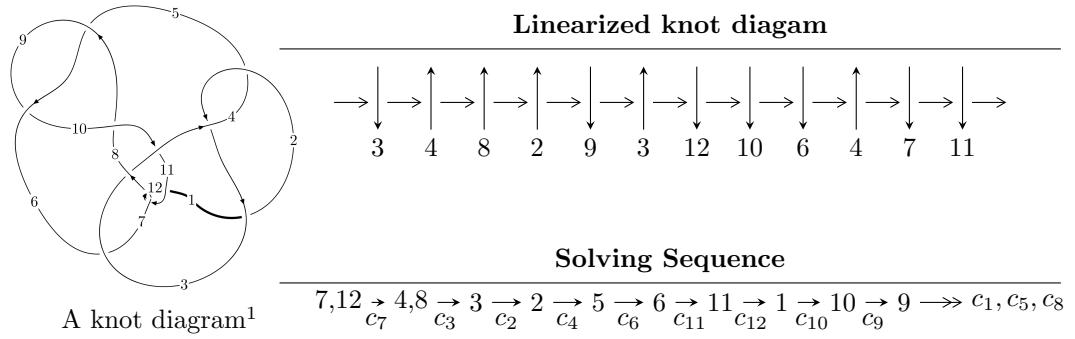


$12n_{0147}$ ($K12n_{0147}$)



Ideals for irreducible components² of X_{par}

$$\begin{aligned}
I_1^u &= \langle -3u^{15} - 5u^{14} + \dots + 4b - 5, -3u^{15} - 3u^{14} + \dots + 2a - 4, \\
&\quad u^{16} + u^{15} - 5u^{14} - 5u^{13} + 11u^{12} + 12u^{11} - 8u^{10} - 13u^9 - 8u^8 + 2u^7 + 18u^6 + 11u^5 - 7u^4 - 9u^3 - u^2 + 2u - 1 \rangle \\
I_2^u &= \langle 1404675088u^{27} + 680434033u^{26} + \dots + 5440114508b + 183536430, \\
&\quad 4259487893u^{27} + 5117778300u^{26} + \dots + 10880229016a - 10842072870, \\
&\quad u^{28} + 2u^{27} + \dots + 12u + 4 \rangle \\
I_3^u &= \langle u^3 + b + u + 1, -u^2 + a + 2u + 1, u^4 - u^2 + 1 \rangle \\
I_4^u &= \langle -u^3 + b - u + 1, -u^2 + a - u + 1, u^4 - u^2 + 1 \rangle \\
I_5^u &= \langle -u^3 + u^2 + b - u - 1, u^2 + a - u, u^4 - u^2 + 1 \rangle \\
I_6^u &= \langle u^3 - u^2 + b + u, a + 2u - 1, u^4 - u^2 + 1 \rangle \\
I_7^u &= \langle -u^3 + b - u, a - u, u^4 + u^3 + 1 \rangle \\
I_8^u &= \langle a^3 + 2a^2 + b + 3a + 1, a^4 + 3a^3 + 6a^2 + 4a + 1, u - 1 \rangle \\
I_9^u &= \langle b - 2, a - 1, u - 1 \rangle
\end{aligned}$$

* 9 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 69 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -3u^{15} - 5u^{14} + \dots + 4b - 5, -3u^{15} - 3u^{14} + \dots + 2a - 4, u^{16} + u^{15} + \dots + 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{3}{2}u^{15} + \frac{3}{2}u^{14} + \dots + \frac{5}{2}u + 2 \\ \frac{3}{4}u^{15} + \frac{5}{4}u^{14} + \dots + \frac{1}{2}u + \frac{5}{4} \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} \frac{1}{4}u^{15} + \frac{3}{4}u^{14} + \dots + \frac{1}{2}u + \frac{3}{4} \\ \frac{1}{2}u^{15} + \frac{3}{4}u^{14} + \dots + \frac{3}{4}u + \frac{3}{4} \end{pmatrix} \\ a_2 &= \begin{pmatrix} -\frac{11}{4}u^{15} - u^{14} + \dots - \frac{17}{4}u - \frac{7}{2} \\ -u^{15} - \frac{1}{2}u^{14} + \dots - \frac{1}{2}u - \frac{3}{2} \end{pmatrix} \\ a_5 &= \begin{pmatrix} \frac{5}{2}u^{15} + u^{14} + \dots + \frac{9}{2}u + 2 \\ u^{15} + \frac{1}{2}u^{14} + \dots + \frac{3}{2}u + \frac{3}{2} \end{pmatrix} \\ a_6 &= \begin{pmatrix} -2u^{15} - \frac{3}{4}u^{14} + \dots - \frac{13}{4}u - \frac{5}{4} \\ -\frac{3}{4}u^{15} - \frac{1}{4}u^{14} + \dots - \frac{3}{2}u - \frac{5}{4} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -2u^{15} - \frac{3}{4}u^{14} + \dots - \frac{13}{4}u - \frac{9}{4} \\ -\frac{3}{4}u^{15} - \frac{1}{4}u^{14} + \dots - \frac{1}{2}u - \frac{5}{4} \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{3}{4}u^{15} - \frac{1}{4}u^{14} + \dots - \frac{1}{2}u - \frac{1}{4} \\ -\frac{1}{4}u^{15} + \frac{3}{2}u^{13} + \dots - \frac{1}{4}u - \frac{1}{2} \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -6u^{15} - \frac{1}{2}u^{14} + 32u^{13} + u^{12} - \frac{151}{2}u^{11} - 4u^{10} + \frac{147}{2}u^9 + \frac{29}{2}u^8 + \frac{21}{2}u^7 - 30u^6 - \frac{159}{2}u^5 + \frac{41}{2}u^4 + \frac{103}{2}u^3 + \frac{5}{2}u^2 - \frac{35}{2}u - \frac{13}{2}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{16} + 16u^{15} + \cdots + 1760u + 256$
c_2, c_4	$u^{16} - 4u^{15} + \cdots - 56u + 16$
c_3	$u^{16} + 4u^{15} + \cdots + 12u + 4$
c_5, c_7, c_9 c_{11}	$u^{16} - u^{15} + \cdots - 2u + 1$
c_6, c_{10}	$u^{16} - u^{15} + \cdots + 64u + 16$
c_8, c_{12}	$u^{16} + 11u^{15} + \cdots + 6u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{16} - 24y^{15} + \cdots - 508416y + 65536$
c_2, c_4	$y^{16} + 16y^{15} + \cdots + 1760y + 256$
c_3	$y^{16} - 4y^{15} + \cdots - 56y + 16$
c_5, c_7, c_9 c_{11}	$y^{16} - 11y^{15} + \cdots - 6y + 1$
c_6, c_{10}	$y^{16} + 25y^{15} + \cdots + 256y + 256$
c_8, c_{12}	$y^{16} - 7y^{15} + \cdots + 10y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.053870 + 0.977866I$		
$a = 1.287840 - 0.220850I$	$-5.56822 - 3.25567I$	$-1.25924 + 2.26983I$
$b = -0.321900 - 0.803375I$		
$u = -0.053870 - 0.977866I$		
$a = 1.287840 + 0.220850I$	$-5.56822 + 3.25567I$	$-1.25924 - 2.26983I$
$b = -0.321900 + 0.803375I$		
$u = 1.201500 + 0.360870I$		
$a = -1.62412 - 1.03706I$	$-3.59239 - 7.60004I$	$-5.70207 + 6.90528I$
$b = -2.42883 - 2.34865I$		
$u = 1.201500 - 0.360870I$		
$a = -1.62412 + 1.03706I$	$-3.59239 + 7.60004I$	$-5.70207 - 6.90528I$
$b = -2.42883 + 2.34865I$		
$u = -0.670764 + 0.317932I$		
$a = 2.23583 - 1.40717I$	$-0.26009 + 4.34202I$	$-3.06611 - 5.18312I$
$b = 1.14025 - 0.90622I$		
$u = -0.670764 - 0.317932I$		
$a = 2.23583 + 1.40717I$	$-0.26009 - 4.34202I$	$-3.06611 + 5.18312I$
$b = 1.14025 + 0.90622I$		
$u = 0.703515 + 0.140913I$		
$a = 0.003040 + 0.299544I$	$-1.337230 - 0.185301I$	$-7.62381 + 0.24647I$
$b = 0.501025 + 0.546651I$		
$u = 0.703515 - 0.140913I$		
$a = 0.003040 - 0.299544I$	$-1.337230 + 0.185301I$	$-7.62381 - 0.24647I$
$b = 0.501025 - 0.546651I$		
$u = -1.280950 + 0.212067I$		
$a = 0.273114 - 0.087546I$	$-6.90379 + 2.57028I$	$-9.79223 - 1.93561I$
$b = 0.130376 + 0.667731I$		
$u = -1.280950 - 0.212067I$		
$a = 0.273114 + 0.087546I$	$-6.90379 - 2.57028I$	$-9.79223 + 1.93561I$
$b = 0.130376 - 0.667731I$		

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.29321 + 0.59629I$		
$a = 1.59347 + 1.06533I$	$-12.8610 - 14.5081I$	$-5.76542 + 7.91129I$
$b = 1.53873 + 2.99555I$		
$u = 1.29321 - 0.59629I$		
$a = 1.59347 - 1.06533I$	$-12.8610 + 14.5081I$	$-5.76542 - 7.91129I$
$b = 1.53873 - 2.99555I$		
$u = -0.358572 + 0.446053I$		
$a = -2.09650 + 0.59301I$	$1.55250 - 0.72268I$	$4.27343 + 0.90071I$
$b = -0.541243 + 0.861918I$		
$u = -0.358572 - 0.446053I$		
$a = -2.09650 - 0.59301I$	$1.55250 + 0.72268I$	$4.27343 - 0.90071I$
$b = -0.541243 - 0.861918I$		
$u = -1.33407 + 0.55318I$		
$a = -0.172674 - 0.381772I$	$-13.7981 + 7.5953I$	$-7.06455 - 3.46610I$
$b = -0.018408 - 1.337270I$		
$u = -1.33407 - 0.55318I$		
$a = -0.172674 + 0.381772I$	$-13.7981 - 7.5953I$	$-7.06455 + 3.46610I$
$b = -0.018408 + 1.337270I$		

$$\text{II. } I_2^u = \langle 1.40 \times 10^9 u^{27} + 6.80 \times 10^8 u^{26} + \dots + 5.44 \times 10^9 b + 1.84 \times 10^8, 4.26 \times 10^9 u^{27} + 5.12 \times 10^9 u^{26} + \dots + 1.09 \times 10^{10} a - 1.08 \times 10^{10}, u^{28} + 2u^{27} + \dots + 12u + 4 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.391489u^{27} - 0.470374u^{26} + \dots - 3.81459u + 0.996493 \\ -0.258207u^{27} - 0.125077u^{26} + \dots - 0.732283u - 0.0337376 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.413924u^{27} - 0.597145u^{26} + \dots - 5.26760u - 0.220183 \\ -0.0582121u^{27} - 0.0675302u^{26} + \dots + 0.340267u + 0.293866 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.477856u^{27} - 0.996708u^{26} + \dots - 13.3082u - 4.41263 \\ -0.112376u^{27} - 0.407794u^{26} + \dots - 2.58251u - 1.23931 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.954572u^{27} + 1.16393u^{26} + \dots + 13.8778u + 5.23994 \\ 0.578242u^{27} + 0.838640u^{26} + \dots + 6.12426u + 2.98085 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.553377u^{27} - 0.805395u^{26} + \dots - 4.19380u - 0.220141 \\ -0.289887u^{27} - 0.549598u^{26} + \dots - 2.44368u - 1.38590 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.344773u^{27} - 0.559849u^{26} + \dots - 12.5913u - 2.43833 \\ -0.107385u^{27} - 0.0325593u^{26} + \dots - 1.42978u - 0.191489 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.122884u^{27} + 0.0337522u^{26} + \dots - 7.99636u - 2.60537 \\ -0.0118276u^{27} + 0.0954702u^{26} + \dots - 1.56095u - 0.292717 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{3864981188}{1360028627}u^{27} - \frac{4406004267}{1360028627}u^{26} + \dots - \frac{49326955058}{1360028627}u - \frac{19445189018}{1360028627}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$(u^{14} + 21u^{13} + \cdots - 66u + 1)^2$
c_2, c_4	$(u^{14} - 3u^{13} + \cdots - 14u + 1)^2$
c_3	$(u^{14} - u^{13} + \cdots - 2u + 1)^2$
c_5, c_7, c_9 c_{11}	$u^{28} - 2u^{27} + \cdots - 12u + 4$
c_6, c_{10}	$u^{28} + 5u^{27} + \cdots + 251482u + 48331$
c_8, c_{12}	$u^{28} + 16u^{27} + \cdots - 104u + 16$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$(y^{14} - 59y^{13} + \cdots - 3858y + 1)^2$
c_2, c_4	$(y^{14} + 21y^{13} + \cdots - 66y + 1)^2$
c_3	$(y^{14} - 3y^{13} + \cdots - 14y + 1)^2$
c_5, c_7, c_9 c_{11}	$y^{28} - 16y^{27} + \cdots + 104y + 16$
c_6, c_{10}	$y^{28} + 29y^{27} + \cdots + 1236737368y + 2335885561$
c_8, c_{12}	$y^{28} - 8y^{27} + \cdots - 14112y + 256$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.944960 + 0.389379I$		
$a = 1.68750 - 1.23439I$	$-0.06814 + 4.27159I$	$-1.66019 - 6.67920I$
$b = 1.31224 - 1.71461I$		
$u = -0.944960 - 0.389379I$		
$a = 1.68750 + 1.23439I$	$-0.06814 - 4.27159I$	$-1.66019 + 6.67920I$
$b = 1.31224 + 1.71461I$		
$u = 0.167349 + 1.046550I$		
$a = -1.56673 - 0.27072I$	$-9.38462 + 8.62895I$	$-3.88181 - 4.95064I$
$b = 0.750716 - 1.143810I$		
$u = 0.167349 - 1.046550I$		
$a = -1.56673 + 0.27072I$	$-9.38462 - 8.62895I$	$-3.88181 + 4.95064I$
$b = 0.750716 + 1.143810I$		
$u = -0.071840 + 1.060620I$		
$a = -1.156110 - 0.491907I$	$-9.86399 - 1.83809I$	$-4.68358 + 0.51446I$
$b = 0.349038 - 0.236829I$		
$u = -0.071840 - 1.060620I$		
$a = -1.156110 + 0.491907I$	$-9.86399 + 1.83809I$	$-4.68358 - 0.51446I$
$b = 0.349038 + 0.236829I$		
$u = 0.930250 + 0.540185I$		
$a = -0.39656 - 1.39984I$	0.178509	$-1.66494 + 0.I$
$b = 0.82318 - 1.20145I$		
$u = 0.930250 - 0.540185I$		
$a = -0.39656 + 1.39984I$	0.178509	$-1.66494 + 0.I$
$b = 0.82318 + 1.20145I$		
$u = -0.967293 + 0.545264I$		
$a = 1.19253 - 1.46190I$	$0.97692 + 4.37418I$	$1.48632 - 5.65859I$
$b = -0.09011 - 2.03761I$		
$u = -0.967293 - 0.545264I$		
$a = 1.19253 + 1.46190I$	$0.97692 - 4.37418I$	$1.48632 + 5.65859I$
$b = -0.09011 + 2.03761I$		

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.120270 + 0.185451I$ $a = 0.336290 + 0.781567I$ $b = 0.0603554 + 0.0344181I$	$-2.83422 + 5.28701I$	$-7.29071 - 5.64998I$
$u = -1.120270 - 0.185451I$ $a = 0.336290 - 0.781567I$ $b = 0.0603554 - 0.0344181I$	$-2.83422 - 5.28701I$	$-7.29071 + 5.64998I$
$u = 0.661296 + 0.516335I$ $a = 1.39638 - 1.24212I$ $b = 1.77737 + 0.58800I$	$0.97692 - 4.37418I$	$1.48632 + 5.65859I$
$u = 0.661296 - 0.516335I$ $a = 1.39638 + 1.24212I$ $b = 1.77737 - 0.58800I$	$0.97692 + 4.37418I$	$1.48632 - 5.65859I$
$u = 0.986837 + 0.702176I$ $a = -1.43243 - 0.29298I$ $b = -0.95756 - 1.34618I$	$-2.83422 - 5.28701I$	$-7.29071 + 5.64998I$
$u = 0.986837 - 0.702176I$ $a = -1.43243 + 0.29298I$ $b = -0.95756 + 1.34618I$	$-2.83422 + 5.28701I$	$-7.29071 - 5.64998I$
$u = -0.576536 + 0.519983I$ $a = -1.80604 - 0.49276I$ $b = -1.20129 + 1.05231I$	2.08354	$4.91356 + 0.I$
$u = -0.576536 - 0.519983I$ $a = -1.80604 + 0.49276I$ $b = -1.20129 - 1.05231I$	2.08354	$4.91356 + 0.I$
$u = -1.296330 + 0.525251I$ $a = -1.29110 + 1.10158I$ $b = -1.32954 + 2.42151I$	$-9.38462 + 8.62895I$	$-3.88181 - 4.95064I$
$u = -1.296330 - 0.525251I$ $a = -1.29110 - 1.10158I$ $b = -1.32954 - 2.42151I$	$-9.38462 - 8.62895I$	$-3.88181 + 4.95064I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.323650 + 0.464051I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	$Cusp shape$
$a = 0.131487 - 0.110768I$	$-9.86399 - 1.83809I$	$-4.68358 + 0.51446I$
$b = -0.532418 - 0.972507I$		
$u = 1.323650 - 0.464051I$		
$a = 0.131487 + 0.110768I$	$-9.86399 + 1.83809I$	$-4.68358 - 0.51446I$
$b = -0.532418 + 0.972507I$		
$u = -1.39944 + 0.38754I$		
$a = 0.184103 - 0.013266I$	$-14.5006 - 3.5759I$	$-7.59435 + 2.22005I$
$b = 1.29482 - 1.20212I$		
$u = -1.39944 - 0.38754I$		
$a = 0.184103 + 0.013266I$	$-14.5006 + 3.5759I$	$-7.59435 - 2.22005I$
$b = 1.29482 + 1.20212I$		
$u = 1.38126 + 0.46460I$		
$a = 1.074130 + 0.763312I$	$-14.5006 - 3.5759I$	$-7.59435 + 2.22005I$
$b = 1.81408 + 1.69170I$		
$u = 1.38126 - 0.46460I$		
$a = 1.074130 - 0.763312I$	$-14.5006 + 3.5759I$	$-7.59435 - 2.22005I$
$b = 1.81408 - 1.69170I$		
$u = -0.073973 + 0.383908I$		
$a = 3.89655 + 0.21962I$	$-0.06814 + 4.27159I$	$-1.66019 - 6.67920I$
$b = 0.429118 + 0.189827I$		
$u = -0.073973 - 0.383908I$		
$a = 3.89655 - 0.21962I$	$-0.06814 - 4.27159I$	$-1.66019 + 6.67920I$
$b = 0.429118 - 0.189827I$		

$$\text{III. } I_3^u = \langle u^3 + b + u + 1, -u^2 + a + 2u + 1, u^4 - u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^2 - 2u - 1 \\ -u^3 - u - 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^3 + u^2 - u - 1 \\ -u^3 - 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -3u^3 + u - 1 \\ -2u^3 - u^2 + 2u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^3 \\ u^3 - u \end{pmatrix} \\ a_6 &= \begin{pmatrix} u^3 + 2u \\ 2u^3 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 3u^2 - 3 \\ u^2 - 3 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -2 \\ -u^2 - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $12u^2 - 8$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4, c_8	$(u^2 - u + 1)^2$
c_2, c_{12}	$(u^2 + u + 1)^2$
c_3, c_5, c_7 c_9, c_{11}	$u^4 - u^2 + 1$
c_6	$(u^2 + 2u + 2)^2$
c_{10}	$(u^2 - 2u + 2)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_8, c_{12}	$(y^2 + y + 1)^2$
c_3, c_5, c_7 c_9, c_{11}	$(y^2 - y + 1)^2$
c_6, c_{10}	$(y^2 + 4)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.866025 + 0.500000I$		
$a = -2.23205 - 0.13397I$	$- 6.08965I$	$-2.00000 + 10.39230I$
$b = -1.86603 - 1.50000I$		
$u = 0.866025 - 0.500000I$		
$a = -2.23205 + 0.13397I$	$6.08965I$	$-2.00000 - 10.39230I$
$b = -1.86603 + 1.50000I$		
$u = -0.866025 + 0.500000I$		
$a = 1.23205 - 1.86603I$	$6.08965I$	$-2.00000 - 10.39230I$
$b = -0.13397 - 1.50000I$		
$u = -0.866025 - 0.500000I$		
$a = 1.23205 + 1.86603I$	$- 6.08965I$	$-2.00000 + 10.39230I$
$b = -0.13397 + 1.50000I$		

$$\text{IV. } I_4^u = \langle -u^3 + b - u + 1, -u^2 + a - u + 1, u^4 - u^2 + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^2 + u - 1 \\ u^3 + u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^2 - 1 \\ u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 + u^2 \\ -2u^3 + u^2 + 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 \\ u^3 - u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^3 - u^2 - u + 2 \\ u^2 - 2u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 - 2u^2 + u + 1 \\ 2u^3 - 2u^2 - u + 3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^3 - u^2 + 2u \\ u^3 - 2u^2 + u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-4u^2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4, c_8	$(u^2 - u + 1)^2$
c_2, c_{12}	$(u^2 + u + 1)^2$
c_3, c_5, c_7 c_9, c_{11}	$u^4 - u^2 + 1$
c_6	$u^4 + 4u^3 + 5u^2 + 2u + 1$
c_{10}	$u^4 + 2u^3 + 5u^2 + 4u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_8, c_{12}	$(y^2 + y + 1)^2$
c_3, c_5, c_7 c_9, c_{11}	$(y^2 - y + 1)^2$
c_6	$y^4 - 6y^3 + 11y^2 + 6y + 1$
c_{10}	$y^4 + 6y^3 + 11y^2 - 6y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.866025 + 0.500000I$ $a = 0.36603 + 1.36603I$ $b = -0.13397 + 1.50000I$	$2.02988I$	$-2.00000 - 3.46410I$
$u = 0.866025 - 0.500000I$ $a = 0.36603 - 1.36603I$ $b = -0.13397 - 1.50000I$	$-2.02988I$	$-2.00000 + 3.46410I$
$u = -0.866025 + 0.500000I$ $a = -1.36603 - 0.36603I$ $b = -1.86603 + 1.50000I$	$-2.02988I$	$-2.00000 + 3.46410I$
$u = -0.866025 - 0.500000I$ $a = -1.36603 + 0.36603I$ $b = -1.86603 - 1.50000I$	$2.02988I$	$-2.00000 - 3.46410I$

$$\mathbf{V. } I_5^u = \langle -u^3 + u^2 + b - u - 1, \ u^2 + a - u, \ u^4 - u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_7 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} -u^2 + u \\ u^3 - u^2 + u + 1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^2 \\ -u^2 + u + 1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -u^3 - 1 \\ -2u^3 - u^2 + 2u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u^3 \\ u^3 - u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -u^3 \\ -2u^3 + 2u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} u^2 + 1 \\ 3u^2 - 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 2u^2 \\ 3u^2 - 3 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4u^2 - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4, c_8	$(u^2 - u + 1)^2$
c_2, c_{12}	$(u^2 + u + 1)^2$
c_3, c_5, c_7 c_9, c_{11}	$u^4 - u^2 + 1$
c_6	$u^4 - 2u^3 + 2u^2 - 4u + 4$
c_{10}	$u^4 + 2u^3 + 2u^2 + 4u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_8, c_{12}	$(y^2 + y + 1)^2$
c_3, c_5, c_7 c_9, c_{11}	$(y^2 - y + 1)^2$
c_6, c_{10}	$y^4 - 4y^2 + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_5^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.866025 + 0.500000I$		
$a = 0.366025 - 0.366025I$	$- 2.02988I$	$-2.00000 + 3.46410I$
$b = 1.36603 + 0.63397I$		
$u = 0.866025 - 0.500000I$		
$a = 0.366025 + 0.366025I$	$2.02988I$	$-2.00000 - 3.46410I$
$b = 1.36603 - 0.63397I$		
$u = -0.866025 + 0.500000I$		
$a = -1.36603 + 1.36603I$	$2.02988I$	$-2.00000 - 3.46410I$
$b = -0.36603 + 2.36603I$		
$u = -0.866025 - 0.500000I$		
$a = -1.36603 - 1.36603I$	$- 2.02988I$	$-2.00000 + 3.46410I$
$b = -0.36603 - 2.36603I$		

$$\text{VI. } I_6^u = \langle u^3 - u^2 + b + u, \ a + 2u - 1, \ u^4 - u^2 + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -2u + 1 \\ -u^3 + u^2 - u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^3 - u + 1 \\ -u^3 + u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -3u^3 + u^2 + u \\ -2u^3 + u^2 + 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 \\ u^3 - u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -3u^3 + 2u^2 + u - 1 \\ -2u^3 + u^2 + 2u - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 - 2u + 3 \\ -u^3 + 2u^2 - u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2u^3 - 3u^2 - u + 4 \\ u^3 - 2u + 3 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4u^2 - 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4, c_8	$(u^2 - u + 1)^2$
c_2, c_{12}	$(u^2 + u + 1)^2$
c_3, c_5, c_7 c_9, c_{11}	$u^4 - u^2 + 1$
c_6	$u^4 - 2u^3 + 5u^2 - 4u + 1$
c_{10}	$u^4 - 4u^3 + 5u^2 - 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_8, c_{12}	$(y^2 + y + 1)^2$
c_3, c_5, c_7 c_9, c_{11}	$(y^2 - y + 1)^2$
c_6	$y^4 + 6y^3 + 11y^2 - 6y + 1$
c_{10}	$y^4 - 6y^3 + 11y^2 + 6y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_6^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.866025 + 0.500000I$		
$a = -0.732051 - 1.000000I$	$- 2.02988I$	$-2.00000 + 3.46410I$
$b = -0.366025 - 0.633975I$		
$u = 0.866025 - 0.500000I$		
$a = -0.732051 + 1.000000I$	$2.02988I$	$-2.00000 - 3.46410I$
$b = -0.366025 + 0.633975I$		
$u = -0.866025 + 0.500000I$		
$a = 2.73205 - 1.000000I$	$2.02988I$	$-2.00000 - 3.46410I$
$b = 1.36603 - 2.36603I$		
$u = -0.866025 - 0.500000I$		
$a = 2.73205 + 1.000000I$	$- 2.02988I$	$-2.00000 + 3.46410I$
$b = 1.36603 + 2.36603I$		

$$\text{VII. } I_7^u = \langle -u^3 + b - u, \ a - u, \ u^4 + u^3 + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 \\ -2u^3 + 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 + 1 \\ u^3 + u^2 - u + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^3 \\ -u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^3 + 1 \\ u^3 + u^2 - u + 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 + 2 \\ u^3 + 2u^2 - u + 2 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^4 + 3u^3 + 6u^2 + 4u + 1$
c_2, c_4	$u^4 - u^3 + 2u^2 + 1$
c_3, c_6, c_7 c_{11}	$u^4 - u^3 + 1$
c_5, c_8, c_9	$(u + 1)^4$
c_{10}	$u^4 - 3u^3 + 6u^2 - 4u + 1$
c_{12}	$u^4 + u^3 + 2u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_{10}	$y^4 + 3y^3 + 14y^2 - 4y + 1$
c_2, c_4, c_{12}	$y^4 + 3y^3 + 6y^2 + 4y + 1$
c_3, c_6, c_7 c_{11}	$y^4 - y^3 + 2y^2 + 1$
c_5, c_8, c_9	$(y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_7^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.518913 + 0.666610I$		
$a = 0.518913 + 0.666610I$	-1.64493	-6.00000
$b = -0.033125 + 0.908884I$		
$u = 0.518913 - 0.666610I$		
$a = 0.518913 - 0.666610I$	-1.64493	-6.00000
$b = -0.033125 - 0.908884I$		
$u = -1.018910 + 0.602565I$		
$a = -1.018910 + 0.602565I$	-1.64493	-6.00000
$b = -0.96687 + 2.26050I$		
$u = -1.018910 - 0.602565I$		
$a = -1.018910 - 0.602565I$	-1.64493	-6.00000
$b = -0.96687 - 2.26050I$		

$$\text{VIII. } I_8^u = \langle a^3 + 2a^2 + b + 3a + 1, a^4 + 3a^3 + 6a^2 + 4a + 1, u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ -a^3 - 2a^2 - 3a - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a^3 + 2a^2 + 5a + 1 \\ a \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a^3 + a^2 + 3a \\ -a^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2a - 2 \\ -2a - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -a^3 - a^2 - 3a \\ a^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a^3 + 2a^2 + 3a + 2 \\ -a^2 - 2a \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -a^3 - 4a^2 - 6a - 1 \\ -a^3 - 4a^2 - 5a - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^4 + 3u^3 + 6u^2 + 4u + 1$
c_2, c_4	$u^4 - u^3 + 2u^2 + 1$
c_3, c_5, c_9 c_{10}	$u^4 - u^3 + 1$
c_6	$u^4 - 3u^3 + 6u^2 - 4u + 1$
c_7, c_{11}, c_{12}	$(u + 1)^4$
c_8	$u^4 + u^3 + 2u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_6	$y^4 + 3y^3 + 14y^2 - 4y + 1$
c_2, c_4, c_8	$y^4 + 3y^3 + 6y^2 + 4y + 1$
c_3, c_5, c_9 c_{10}	$y^4 - y^3 + 2y^2 + 1$
c_7, c_{11}, c_{12}	$(y - 1)^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_8^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = -0.447962 + 0.242275I$	-1.64493	-6.00000
$b = 0.070951 - 0.424335I$		
$u = 1.00000$		
$a = -0.447962 - 0.242275I$	-1.64493	-6.00000
$b = 0.070951 + 0.424335I$		
$u = 1.00000$		
$a = -1.05204 + 1.65794I$	-1.64493	-6.00000
$b = -2.07095 + 1.05537I$		
$u = 1.00000$		
$a = -1.05204 - 1.65794I$	-1.64493	-6.00000
$b = -2.07095 - 1.05537I$		

$$\text{IX. } I_9^u = \langle b - 2, a - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2 \\ 3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 3 \\ 4 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_4	$u - 1$
c_3, c_5, c_6 c_7, c_8, c_9 c_{10}, c_{11}, c_{12}	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3	
c_4, c_5, c_6	
c_7, c_8, c_9	$y - 1$
c_{10}, c_{11}, c_{12}	

(vi) Complex Volumes and Cusp Shapes

Solutions to I_9^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 1.00000$	-1.64493	-6.00000
$b = 2.00000$		

X. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u - 1)(u^2 - u + 1)^8(u^4 + 3u^3 + 6u^2 + 4u + 1)^2 \\ \cdot ((u^{14} + 21u^{13} + \dots - 66u + 1)^2)(u^{16} + 16u^{15} + \dots + 1760u + 256)$
c_2	$(u - 1)(u^2 + u + 1)^8(u^4 - u^3 + 2u^2 + 1)^2(u^{14} - 3u^{13} + \dots - 14u + 1)^2 \\ \cdot (u^{16} - 4u^{15} + \dots - 56u + 16)$
c_3	$(u + 1)(u^4 - u^2 + 1)^4(u^4 - u^3 + 1)^2(u^{14} - u^{13} + \dots - 2u + 1)^2 \\ \cdot (u^{16} + 4u^{15} + \dots + 12u + 4)$
c_4	$(u - 1)(u^2 - u + 1)^8(u^4 - u^3 + 2u^2 + 1)^2(u^{14} - 3u^{13} + \dots - 14u + 1)^2 \\ \cdot (u^{16} - 4u^{15} + \dots - 56u + 16)$
c_5, c_7, c_9 c_{11}	$((u + 1)^5)(u^4 - u^2 + 1)^4(u^4 - u^3 + 1)(u^{16} - u^{15} + \dots - 2u + 1) \\ \cdot (u^{28} - 2u^{27} + \dots - 12u + 4)$
c_6	$(u + 1)(u^2 + 2u + 2)^2(u^4 - 3u^3 + \dots - 4u + 1)(u^4 - 2u^3 + \dots - 4u + 4) \\ \cdot (u^4 - 2u^3 + 5u^2 - 4u + 1)(u^4 - u^3 + 1)(u^4 + 4u^3 + 5u^2 + 2u + 1) \\ \cdot (u^{16} - u^{15} + \dots + 64u + 16)(u^{28} + 5u^{27} + \dots + 251482u + 48331)$
c_8	$((u + 1)^5)(u^2 - u + 1)^8(u^4 + u^3 + 2u^2 + 1)(u^{16} + 11u^{15} + \dots + 6u + 1) \\ \cdot (u^{28} + 16u^{27} + \dots - 104u + 16)$
c_{10}	$(u + 1)(u^2 - 2u + 2)^2(u^4 - 4u^3 + \dots - 2u + 1)(u^4 - 3u^3 + \dots - 4u + 1) \\ \cdot (u^4 - u^3 + 1)(u^4 + 2u^3 + 2u^2 + 4u + 4)(u^4 + 2u^3 + 5u^2 + 4u + 1) \\ \cdot (u^{16} - u^{15} + \dots + 64u + 16)(u^{28} + 5u^{27} + \dots + 251482u + 48331)$
c_{12}	$((u + 1)^5)(u^2 + u + 1)^8(u^4 + u^3 + 2u^2 + 1)(u^{16} + 11u^{15} + \dots + 6u + 1) \\ \cdot (u^{28} + 16u^{27} + \dots - 104u + 16)$

XI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$(y - 1)(y^2 + y + 1)^8(y^4 + 3y^3 + 14y^2 - 4y + 1)^2 \\ \cdot (y^{14} - 59y^{13} + \dots - 3858y + 1)^2 \\ \cdot (y^{16} - 24y^{15} + \dots - 508416y + 65536)$
c_2, c_4	$(y - 1)(y^2 + y + 1)^8(y^4 + 3y^3 + 6y^2 + 4y + 1)^2 \\ \cdot ((y^{14} + 21y^{13} + \dots - 66y + 1)^2)(y^{16} + 16y^{15} + \dots + 1760y + 256)$
c_3	$(y - 1)(y^2 - y + 1)^8(y^4 - y^3 + 2y^2 + 1)^2(y^{14} - 3y^{13} + \dots - 14y + 1)^2 \\ \cdot (y^{16} - 4y^{15} + \dots - 56y + 16)$
c_5, c_7, c_9 c_{11}	$((y - 1)^5)(y^2 - y + 1)^8(y^4 - y^3 + 2y^2 + 1)(y^{16} - 11y^{15} + \dots - 6y + 1) \\ \cdot (y^{28} - 16y^{27} + \dots + 104y + 16)$
c_6, c_{10}	$(y - 1)(y^2 + 4)^2(y^4 - 4y^2 + 16)(y^4 - 6y^3 + 11y^2 + 6y + 1) \\ \cdot (y^4 - y^3 + 2y^2 + 1)(y^4 + 3y^3 + \dots - 4y + 1)(y^4 + 6y^3 + \dots - 6y + 1) \\ \cdot (y^{16} + 25y^{15} + \dots + 256y + 256) \\ \cdot (y^{28} + 29y^{27} + \dots + 1236737368y + 2335885561)$
c_8, c_{12}	$(y - 1)^5(y^2 + y + 1)^8(y^4 + 3y^3 + 6y^2 + 4y + 1) \\ \cdot (y^{16} - 7y^{15} + \dots + 10y + 1)(y^{28} - 8y^{27} + \dots - 14112y + 256)$