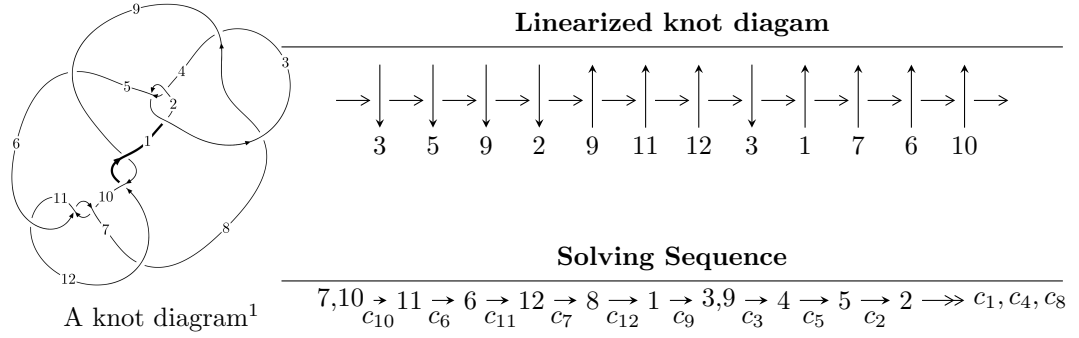


12n₀₁₇₀ (K12n₀₁₇₀)



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -2u^{46} + 4u^{45} + \dots + b + 2, 2u^{45} - 2u^{44} + \dots + a - 1, u^{47} - 2u^{46} + \dots - 12u^2 + 1 \rangle$$

$$I_2^u = \langle b - u, a - u - 1, u^3 + 2u - 1 \rangle$$

$$I_3^u = \langle u^3 + b + 2u + 1, a + 1, u^4 + u^3 + 2u^2 + 2u + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 54 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle -2u^{46} + 4u^{45} + \dots + b + 2, 2u^{45} - 2u^{44} + \dots + a - 1, u^{47} - 2u^{46} + \dots - 12u^2 + 1 \rangle$$

I. $I_1^u =$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^5 + 2u^3 + u \\ -u^7 - 3u^5 - 2u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^4 - u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2u^{45} + 2u^{44} + \dots - 5u + 1 \\ 2u^{46} - 4u^{45} + \dots - 3u - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^8 + 3u^6 + u^4 - 2u^2 + 1 \\ u^8 + 4u^6 + 4u^4 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -4u^{45} + 4u^{44} + \dots + 16u^2 - 5u \\ 4u^{46} - 8u^{45} + \dots - 4u - 4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^{19} - 8u^{17} - 24u^{15} - 30u^{13} - 7u^{11} + 10u^9 - 4u^7 - 6u^5 + 3u^3 - 2u \\ -u^{19} - 9u^{17} - 32u^{15} - 55u^{13} - 43u^{11} - 9u^9 - 4u^5 + u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{45} + u^{44} + \dots - 4u + 2 \\ u^{46} - 2u^{45} + \dots - 2u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-4u^{46} + 8u^{45} + \dots + 38u + 5$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{47} + 14u^{46} + \dots - 5u + 1$
c_2, c_4	$u^{47} - 8u^{46} + \dots - 5u + 1$
c_3, c_8	$u^{47} + u^{46} + \dots + 192u + 128$
c_5	$u^{47} - 2u^{46} + \dots + 2u + 1$
c_6, c_{10}, c_{11}	$u^{47} - 2u^{46} + \dots - 12u^2 + 1$
c_7	$u^{47} + 2u^{46} + \dots + 96u + 72$
c_9, c_{12}	$u^{47} + 8u^{46} + \dots + 112u - 49$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{47} + 46y^{46} + \dots + 83y - 1$
c_2, c_4	$y^{47} - 14y^{46} + \dots - 5y - 1$
c_3, c_8	$y^{47} + 45y^{46} + \dots - 167936y - 16384$
c_5	$y^{47} - 52y^{46} + \dots + 24y - 1$
c_6, c_{10}, c_{11}	$y^{47} + 44y^{46} + \dots + 24y - 1$
c_7	$y^{47} + 12y^{46} + \dots + 50832y - 5184$
c_9, c_{12}	$y^{47} + 32y^{46} + \dots + 170128y - 2401$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.240850 + 1.172380I$ $a = 0.76218 + 1.23522I$ $b = 0.934577 + 0.402639I$	$4.61957 - 0.02295I$	0
$u = -0.240850 - 1.172380I$ $a = 0.76218 - 1.23522I$ $b = 0.934577 - 0.402639I$	$4.61957 + 0.02295I$	0
$u = 0.708507 + 0.363703I$ $a = -0.94806 + 1.22755I$ $b = 2.37910 + 1.16766I$	$3.42438 + 9.90306I$	$2.22004 - 7.67510I$
$u = 0.708507 - 0.363703I$ $a = -0.94806 - 1.22755I$ $b = 2.37910 - 1.16766I$	$3.42438 - 9.90306I$	$2.22004 + 7.67510I$
$u = -0.635055 + 0.455943I$ $a = 0.114980 + 0.251136I$ $b = 0.0894725 + 0.0904282I$	$-4.12081 - 2.09104I$	$4.57556 + 3.64684I$
$u = -0.635055 - 0.455943I$ $a = 0.114980 - 0.251136I$ $b = 0.0894725 - 0.0904282I$	$-4.12081 + 2.09104I$	$4.57556 - 3.64684I$
$u = 0.517341 + 0.581926I$ $a = -1.35583 - 1.46783I$ $b = -1.70532 + 1.15194I$	$2.58809 - 5.73384I$	$0.56569 + 2.04831I$
$u = 0.517341 - 0.581926I$ $a = -1.35583 + 1.46783I$ $b = -1.70532 - 1.15194I$	$2.58809 + 5.73384I$	$0.56569 - 2.04831I$
$u = 0.109843 + 1.219880I$ $a = 0.767710 + 0.740963I$ $b = 0.864402 + 0.041075I$	$-2.27528 + 2.11283I$	0
$u = 0.109843 - 1.219880I$ $a = 0.767710 - 0.740963I$ $b = 0.864402 - 0.041075I$	$-2.27528 - 2.11283I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.698777 + 0.324988I$ $a = 1.001160 - 0.887981I$ $b = -2.00444 - 1.18278I$	$4.64870 + 3.20376I$	$4.16524 - 3.31906I$
$u = 0.698777 - 0.324988I$ $a = 1.001160 + 0.887981I$ $b = -2.00444 + 1.18278I$	$4.64870 - 3.20376I$	$4.16524 + 3.31906I$
$u = -0.256980 + 1.225330I$ $a = -0.62010 - 1.29363I$ $b = -0.881559 - 0.519345I$	$4.25025 - 6.95397I$	0
$u = -0.256980 - 1.225330I$ $a = -0.62010 + 1.29363I$ $b = -0.881559 + 0.519345I$	$4.25025 + 6.95397I$	0
$u = 0.435156 + 0.599476I$ $a = 1.31533 + 1.27222I$ $b = 1.34439 - 0.94929I$	$3.57234 + 0.73807I$	$1.82651 - 2.67731I$
$u = 0.435156 - 0.599476I$ $a = 1.31533 - 1.27222I$ $b = 1.34439 + 0.94929I$	$3.57234 - 0.73807I$	$1.82651 + 2.67731I$
$u = -0.037205 + 1.270570I$ $a = -1.61889 - 0.61214I$ $b = -1.283830 + 0.388483I$	$-4.85814 - 0.97601I$	0
$u = -0.037205 - 1.270570I$ $a = -1.61889 + 0.61214I$ $b = -1.283830 - 0.388483I$	$-4.85814 + 0.97601I$	0
$u = -0.623399 + 0.342153I$ $a = -0.426734 + 0.510909I$ $b = -0.111541 + 0.262625I$	$-1.47489 - 3.82342I$	$0.98515 + 6.99857I$
$u = -0.623399 - 0.342153I$ $a = -0.426734 - 0.510909I$ $b = -0.111541 - 0.262625I$	$-1.47489 + 3.82342I$	$0.98515 - 6.99857I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.701377 + 0.026834I$ $a = -0.073148 + 1.342220I$ $b = -0.017726 + 0.554191I$	$8.08746 - 3.45650I$	$7.23123 + 2.83028I$
$u = -0.701377 - 0.026834I$ $a = -0.073148 - 1.342220I$ $b = -0.017726 - 0.554191I$	$8.08746 + 3.45650I$	$7.23123 - 2.83028I$
$u = 0.568091 + 0.371758I$ $a = -2.10914 - 0.10547I$ $b = 0.57523 + 2.44925I$	$-3.30787 + 1.75612I$	$1.06262 - 3.54613I$
$u = 0.568091 - 0.371758I$ $a = -2.10914 + 0.10547I$ $b = 0.57523 - 2.44925I$	$-3.30787 - 1.75612I$	$1.06262 + 3.54613I$
$u = 0.155614 + 1.341930I$ $a = -0.415404 + 0.937335I$ $b = 0.224512 + 0.844236I$	$-3.43598 + 2.59417I$	0
$u = 0.155614 - 1.341930I$ $a = -0.415404 - 0.937335I$ $b = 0.224512 - 0.844236I$	$-3.43598 - 2.59417I$	0
$u = -0.480171 + 0.404521I$ $a = 0.848787 - 0.023160I$ $b = 0.311223 - 0.154426I$	$-1.96248 + 0.31457I$	$-1.52612 + 0.64426I$
$u = -0.480171 - 0.404521I$ $a = 0.848787 + 0.023160I$ $b = 0.311223 + 0.154426I$	$-1.96248 - 0.31457I$	$-1.52612 - 0.64426I$
$u = -0.19689 + 1.43311I$ $a = -0.446867 + 0.559009I$ $b = -0.063667 + 0.550788I$	$-7.79399 - 2.25837I$	0
$u = -0.19689 - 1.43311I$ $a = -0.446867 - 0.559009I$ $b = -0.063667 - 0.550788I$	$-7.79399 + 2.25837I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.12786 + 1.44594I$ $a = -1.76062 + 0.79907I$ $b = -0.81689 + 1.44748I$	$-2.88567 + 2.62103I$	0
$u = 0.12786 - 1.44594I$ $a = -1.76062 - 0.79907I$ $b = -0.81689 - 1.44748I$	$-2.88567 - 2.62103I$	0
$u = -0.23877 + 1.43350I$ $a = 0.045007 - 0.588992I$ $b = -0.205747 - 0.403699I$	$-7.17228 - 6.98944I$	0
$u = -0.23877 - 1.43350I$ $a = 0.045007 + 0.588992I$ $b = -0.205747 + 0.403699I$	$-7.17228 + 6.98944I$	0
$u = 0.21933 + 1.43707I$ $a = 1.26805 - 3.51350I$ $b = -0.98988 - 3.16929I$	$-9.10435 + 4.67464I$	0
$u = 0.21933 - 1.43707I$ $a = 1.26805 + 3.51350I$ $b = -0.98988 + 3.16929I$	$-9.10435 - 4.67464I$	0
$u = 0.26857 + 1.43228I$ $a = 0.89236 + 2.94088I$ $b = 2.26858 + 1.61505I$	$-0.98075 + 6.72660I$	0
$u = 0.26857 - 1.43228I$ $a = 0.89236 - 2.94088I$ $b = 2.26858 - 1.61505I$	$-0.98075 - 6.72660I$	0
$u = 0.518516 + 0.082438I$ $a = 0.604605 + 0.167780I$ $b = -0.557380 - 0.379635I$	$1.061820 + 0.206928I$	$9.18626 - 0.93345I$
$u = 0.518516 - 0.082438I$ $a = 0.604605 - 0.167780I$ $b = -0.557380 + 0.379635I$	$1.061820 - 0.206928I$	$9.18626 + 0.93345I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.26958 + 1.45051I$ $a = -1.41479 - 3.13096I$ $b = -2.74488 - 1.48581I$	$-2.40424 + 13.46930I$	0
$u = 0.26958 - 1.45051I$ $a = -1.41479 + 3.13096I$ $b = -2.74488 + 1.48581I$	$-2.40424 - 13.46930I$	0
$u = 0.15911 + 1.47665I$ $a = 2.44634 - 0.79574I$ $b = 1.32702 - 1.81501I$	$-4.02537 - 3.37401I$	0
$u = 0.15911 - 1.47665I$ $a = 2.44634 + 0.79574I$ $b = 1.32702 + 1.81501I$	$-4.02537 + 3.37401I$	0
$u = -0.22773 + 1.47482I$ $a = -0.232276 - 0.098321I$ $b = -0.194212 + 0.027487I$	$-10.35500 - 5.24252I$	0
$u = -0.22773 - 1.47482I$ $a = -0.232276 + 0.098321I$ $b = -0.194212 - 0.027487I$	$-10.35500 + 5.24252I$	0
$u = -0.235762$ $a = 2.71069$ $b = 0.517152$	-1.27831	-10.8230

$$\text{II. } I_2^u = \langle b - u, a - u - 1, u^3 + 2u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 + 1 \\ -u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^2 + u \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - u + 1 \\ -u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u + 1 \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + u \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u + 1 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^2 + u - 1 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^2 + 2 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $7u^2 + 5u + 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^3$
c_3, c_8	u^3
c_4	$(u + 1)^3$
c_5, c_6, c_9	$u^3 + 2u + 1$
c_7	$u^3 + 3u^2 + 5u + 2$
c_{10}, c_{11}, c_{12}	$u^3 + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^3$
c_3, c_8	y^3
c_5, c_6, c_9 c_{10}, c_{11}, c_{12}	$y^3 + 4y^2 + 4y - 1$
c_7	$y^3 + y^2 + 13y - 4$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.22670 + 1.46771I$	$-11.08570 - 5.13794I$	$-9.85299 + 2.68036I$
$a = 0.77330 + 1.46771I$		
$b = -0.22670 + 1.46771I$		
$u = -0.22670 - 1.46771I$	$-11.08570 + 5.13794I$	$-9.85299 - 2.68036I$
$a = 0.77330 - 1.46771I$		
$b = -0.22670 - 1.46771I$		
$u = 0.453398$	-0.857735	9.70600
$a = 1.45340$		
$b = 0.453398$		

$$\text{III. } I_3^u = \langle u^3 + b + 2u + 1, a + 1, u^4 + u^3 + 2u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^2 + 1 \\ u^3 + 2u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 + 2u + 1 \\ -u^3 - u^2 - u - 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 + u^2 + 2u + 2 \\ u^3 + 2u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ -u^3 - 2u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^3 + 2u + 1 \\ -u^3 - u^2 - u - 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ -u^3 - 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^3 - u^2 - 2u - 2 \\ -u^3 - 2u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 + u^2 + 2u + 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $3u^3 - 2u^2 + 2u - 5$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^4$
c_3, c_8	u^4
c_4	$(u + 1)^4$
c_5, c_6, c_9	$u^4 - u^3 + 2u^2 - 2u + 1$
c_7	$(u^2 - u + 1)^2$
c_{10}, c_{11}, c_{12}	$u^4 + u^3 + 2u^2 + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^4$
c_3, c_8	y^4
c_5, c_6, c_9 c_{10}, c_{11}, c_{12}	$y^4 + 3y^3 + 2y^2 + 1$
c_7	$(y^2 + y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.621744 + 0.440597I$ $a = -1.00000$ $b = 0.121744 - 1.306620I$	$-4.93480 - 2.02988I$	$-6.26314 + 3.25323I$
$u = -0.621744 - 0.440597I$ $a = -1.00000$ $b = 0.121744 + 1.306620I$	$-4.93480 + 2.02988I$	$-6.26314 - 3.25323I$
$u = 0.121744 + 1.306620I$ $a = -1.00000$ $b = -0.621744 - 0.440597I$	$-4.93480 + 2.02988I$	$-3.23686 - 4.54099I$
$u = 0.121744 - 1.306620I$ $a = -1.00000$ $b = -0.621744 + 0.440597I$	$-4.93480 - 2.02988I$	$-3.23686 + 4.54099I$

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u - 1)^7)(u^{47} + 14u^{46} + \dots - 5u + 1)$
c_2	$((u - 1)^7)(u^{47} - 8u^{46} + \dots - 5u + 1)$
c_3, c_8	$u^7(u^{47} + u^{46} + \dots + 192u + 128)$
c_4	$((u + 1)^7)(u^{47} - 8u^{46} + \dots - 5u + 1)$
c_5	$(u^3 + 2u + 1)(u^4 - u^3 + 2u^2 - 2u + 1)(u^{47} - 2u^{46} + \dots + 2u + 1)$
c_6	$(u^3 + 2u + 1)(u^4 - u^3 + 2u^2 - 2u + 1)(u^{47} - 2u^{46} + \dots - 12u^2 + 1)$
c_7	$((u^2 - u + 1)^2)(u^3 + 3u^2 + 5u + 2)(u^{47} + 2u^{46} + \dots + 96u + 72)$
c_9	$(u^3 + 2u + 1)(u^4 - u^3 + 2u^2 - 2u + 1)(u^{47} + 8u^{46} + \dots + 112u - 49)$
c_{10}, c_{11}	$(u^3 + 2u - 1)(u^4 + u^3 + 2u^2 + 2u + 1)(u^{47} - 2u^{46} + \dots - 12u^2 + 1)$
c_{12}	$(u^3 + 2u - 1)(u^4 + u^3 + 2u^2 + 2u + 1)(u^{47} + 8u^{46} + \dots + 112u - 49)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^7)(y^{47} + 46y^{46} + \dots + 83y - 1)$
c_2, c_4	$((y - 1)^7)(y^{47} - 14y^{46} + \dots - 5y - 1)$
c_3, c_8	$y^7(y^{47} + 45y^{46} + \dots - 167936y - 16384)$
c_5	$(y^3 + 4y^2 + 4y - 1)(y^4 + 3y^3 + 2y^2 + 1)(y^{47} - 52y^{46} + \dots + 24y - 1)$
c_6, c_{10}, c_{11}	$(y^3 + 4y^2 + 4y - 1)(y^4 + 3y^3 + 2y^2 + 1)(y^{47} + 44y^{46} + \dots + 24y - 1)$
c_7	$((y^2 + y + 1)^2)(y^3 + y^2 + 13y - 4)(y^{47} + 12y^{46} + \dots + 50832y - 5184)$
c_9, c_{12}	$(y^3 + 4y^2 + 4y - 1)(y^4 + 3y^3 + 2y^2 + 1)$ $\cdot (y^{47} + 32y^{46} + \dots + 170128y - 2401)$