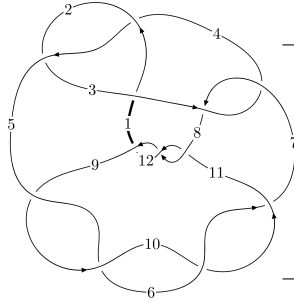
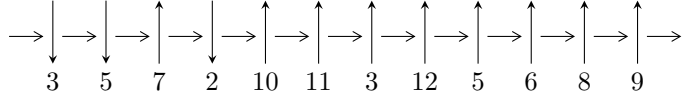


12n₀₁₉₀ (K12n₀₁₉₀)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$6, 11 \xrightarrow{c_6} 3, 7 \xrightarrow{c_7} 8 \xrightarrow{c_{11}} 12 \xrightarrow{c_{10}} 10 \xrightarrow{c_5} 5 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \rightsquigarrow c_3, c_8, c_{12}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 9.44661 \times 10^{16} u^{34} - 2.08351 \times 10^{16} u^{33} + \dots + 1.06489 \times 10^{17} b - 4.51309 \times 10^{16},$$

$$1.88308 \times 10^{16} u^{34} - 8.66830 \times 10^{16} u^{33} + \dots + 1.06489 \times 10^{17} a - 2.62684 \times 10^{17}, u^{35} - 2u^{34} + \dots - 3u^2 + \dots \rangle$$

$$I_2^u = \langle b + u + 1, u^2 + a - 3, u^3 + u^2 - 2u - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 38 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = (9.45 \times 10^{16} u^{34} - 2.08 \times 10^{16} u^{33} + \dots + 1.06 \times 10^{17} b - 4.51 \times 10^{16}, 1.88 \times 10^{16} u^{34} - 8.67 \times 10^{16} u^{33} + \dots + 1.06 \times 10^{17} a - 2.63 \times 10^{17}, u^{35} - 2u^{34} + \dots - 3u^2 + 1)$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.176834u^{34} + 0.814012u^{33} + \dots + 2.45226u + 2.46678 \\ -0.887101u^{34} + 0.195656u^{33} + \dots + 0.405852u + 0.423810 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0.833303u^{34} - 1.64324u^{33} + \dots - 2.63958u + 0.00424027 \\ 0.474997u^{34} - 0.230903u^{33} + \dots - 0.0819582u - 0.627396 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.772238u^{34} + 1.25159u^{33} + \dots + 1.49520u + 0.508098 \\ -0.536061u^{34} + 0.622559u^{33} + \dots + 1.22634u + 0.115057 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.120048u^{34} + 0.252095u^{33} + \dots + 2.07998u + 1.70401 \\ -0.898177u^{34} + 0.117584u^{33} + \dots + 0.120048u + 0.492190 \end{pmatrix} \\ a_1 &= \begin{pmatrix} 1.16760u^{34} - 1.53977u^{33} + \dots - 3.05490u - 0.519586 \\ 0.247602u^{34} - 0.512958u^{33} + \dots - 0.499946u - 0.126931 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.374572u^{34} + 1.04071u^{33} + \dots + 3.03494u + 2.43025 \\ -0.739813u^{34} + 0.0918438u^{33} + \dots + 0.208114u + 0.255027 \end{pmatrix} \\ a_9 &= \begin{pmatrix} u^3 - 2u \\ -u^3 + u \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

$$\mathbf{(iii) Cusp Shapes} = -\frac{218803516467230358}{106488603430183673} u^{34} + \frac{323482212694991959}{106488603430183673} u^{33} + \dots + \frac{611689066048825845}{106488603430183673} u + \frac{1479659137766380195}{106488603430183673}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{35} + 34u^{34} + \dots + 115u + 1$
c_2, c_4	$u^{35} - 4u^{34} + \dots + 11u - 1$
c_3, c_7	$u^{35} - 3u^{34} + \dots - 68u + 8$
c_5, c_6, c_9 c_{10}	$u^{35} + 2u^{34} + \dots + 3u^2 - 1$
c_8, c_{11}, c_{12}	$u^{35} - 2u^{34} + \dots + 4u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{35} - 62y^{34} + \dots + 24691y - 1$
c_2, c_4	$y^{35} - 34y^{34} + \dots + 115y - 1$
c_3, c_7	$y^{35} + 21y^{34} + \dots + 3536y - 64$
c_5, c_6, c_9 c_{10}	$y^{35} - 36y^{34} + \dots + 6y - 1$
c_8, c_{11}, c_{12}	$y^{35} - 24y^{34} + \dots + 6y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.518512 + 0.839070I$ $a = -0.20090 - 1.52795I$ $b = 0.503396 + 0.528590I$	$-5.06245 - 8.93378I$	$5.61011 + 6.33790I$
$u = -0.518512 - 0.839070I$ $a = -0.20090 + 1.52795I$ $b = 0.503396 - 0.528590I$	$-5.06245 + 8.93378I$	$5.61011 - 6.33790I$
$u = 0.555627 + 0.849121I$ $a = -0.614318 + 1.234160I$ $b = 0.699304 - 0.374906I$	$-9.19263 + 2.79140I$	$2.44794 - 2.71252I$
$u = 0.555627 - 0.849121I$ $a = -0.614318 - 1.234160I$ $b = 0.699304 + 0.374906I$	$-9.19263 - 2.79140I$	$2.44794 + 2.71252I$
$u = -0.602141 + 0.838097I$ $a = -0.899952 - 0.776437I$ $b = 0.830081 + 0.123664I$	$-4.82699 + 3.41045I$	$4.79435 - 1.46350I$
$u = -0.602141 - 0.838097I$ $a = -0.899952 + 0.776437I$ $b = 0.830081 - 0.123664I$	$-4.82699 - 3.41045I$	$4.79435 + 1.46350I$
$u = 1.04102$ $a = -0.463489$ $b = 1.08686$	5.86840	16.9730
$u = 1.283960 + 0.039225I$ $a = 0.911676 + 0.081651I$ $b = -0.010028 - 0.690521I$	$1.087230 + 0.216328I$	$6.00000 + 1.40746I$
$u = 1.283960 - 0.039225I$ $a = 0.911676 - 0.081651I$ $b = -0.010028 + 0.690521I$	$1.087230 - 0.216328I$	$6.00000 - 1.40746I$
$u = -1.309800 + 0.120534I$ $a = 0.195097 - 0.058984I$ $b = 0.81817 + 1.70956I$	$2.00975 - 3.69263I$	$7.27638 + 5.74697I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.309800 - 0.120534I$ $a = 0.195097 + 0.058984I$ $b = 0.81817 - 1.70956I$	$2.00975 + 3.69263I$	$7.27638 - 5.74697I$
$u = -0.353161 + 0.521336I$ $a = -0.02390 + 1.82638I$ $b = -0.075939 - 1.075600I$	$1.00613 - 4.12242I$	$7.78031 + 7.98947I$
$u = -0.353161 - 0.521336I$ $a = -0.02390 - 1.82638I$ $b = -0.075939 + 1.075600I$	$1.00613 + 4.12242I$	$7.78031 - 7.98947I$
$u = -1.40049$ $a = 11.4155$ $b = -22.2377$	4.90865	190.120
$u = -1.41602 + 0.13402I$ $a = -0.533008 - 0.621383I$ $b = 0.89460 + 2.26294I$	$3.82362 - 2.94287I$	$6.00000 + 2.97348I$
$u = -1.41602 - 0.13402I$ $a = -0.533008 + 0.621383I$ $b = 0.89460 - 2.26294I$	$3.82362 + 2.94287I$	$6.00000 - 2.97348I$
$u = 1.43763 + 0.18351I$ $a = -0.659923 + 0.669202I$ $b = 0.47190 - 2.51680I$	$6.77944 + 6.69845I$	$11.84404 - 6.39087I$
$u = 1.43763 - 0.18351I$ $a = -0.659923 - 0.669202I$ $b = 0.47190 + 2.51680I$	$6.77944 - 6.69845I$	$11.84404 + 6.39087I$
$u = 1.45669 + 0.05704I$ $a = -0.812721 + 0.319156I$ $b = 1.47422 - 0.87678I$	$6.70581 + 0.15514I$	$13.76195 + 0.I$
$u = 1.45669 - 0.05704I$ $a = -0.812721 - 0.319156I$ $b = 1.47422 + 0.87678I$	$6.70581 - 0.15514I$	$13.76195 + 0.I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.343056 + 0.384524I$ $a = 2.29929 + 0.59274I$ $b = -0.303185 - 0.122127I$	$1.22163 + 1.17182I$	$8.86681 + 1.56652I$
$u = -0.343056 - 0.384524I$ $a = 2.29929 - 0.59274I$ $b = -0.303185 + 0.122127I$	$1.22163 - 1.17182I$	$8.86681 - 1.56652I$
$u = 0.082086 + 0.492790I$ $a = 0.390939 - 0.968584I$ $b = -1.184340 + 0.387269I$	$-2.24663 + 1.49649I$	$1.03964 - 4.19157I$
$u = 0.082086 - 0.492790I$ $a = 0.390939 + 0.968584I$ $b = -1.184340 - 0.387269I$	$-2.24663 - 1.49649I$	$1.03964 + 4.19157I$
$u = 0.247686 + 0.402332I$ $a = 0.48224 - 1.96211I$ $b = -0.468459 + 0.542393I$	$-1.55343 + 0.99744I$	$0.35469 - 3.95121I$
$u = 0.247686 - 0.402332I$ $a = 0.48224 + 1.96211I$ $b = -0.468459 - 0.542393I$	$-1.55343 - 0.99744I$	$0.35469 + 3.95121I$
$u = 1.53041 + 0.30636I$ $a = 0.801077 - 0.794153I$ $b = -1.46599 + 2.35320I$	$1.56823 + 13.12930I$	0
$u = 1.53041 - 0.30636I$ $a = 0.801077 + 0.794153I$ $b = -1.46599 - 2.35320I$	$1.56823 - 13.12930I$	0
$u = -1.54787 + 0.31879I$ $a = 0.749169 + 0.471916I$ $b = -1.55387 - 1.68510I$	$-2.37929 - 7.10760I$	0
$u = -1.54787 - 0.31879I$ $a = 0.749169 - 0.471916I$ $b = -1.55387 + 1.68510I$	$-2.37929 + 7.10760I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.410266$ $a = 0.502264$ $b = 0.198843$	0.605206	16.5510
$u = 1.58936 + 0.33145I$ $a = 0.519028 - 0.138883I$ $b = -1.30987 + 0.85550I$	$2.32499 + 0.97374I$	0
$u = 1.58936 - 0.33145I$ $a = 0.519028 + 0.138883I$ $b = -1.30987 - 0.85550I$	$2.32499 - 0.97374I$	0
$u = 0.363147$ $a = 6.36258$ $b = -0.317987$	-0.506810	28.7620
$u = -1.77917$ $a = -0.0244730$ $b = -0.370009$	16.2026	0

$$\text{II. } I_2^u = \langle b + u + 1, u^2 + a - 3, u^3 + u^2 - 2u - 1 \rangle$$

(i) Arc colorings

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^2 + 3 \\ -u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ u^2 - u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2 \\ -u^2 - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^2 + 3 \\ -u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + 1 \\ u^2 - u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-u^2 + 4u + 4$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^3$
c_3, c_7	u^3
c_4	$(u + 1)^3$
c_5, c_6, c_8	$u^3 + u^2 - 2u - 1$
c_9, c_{10}, c_{11} c_{12}	$u^3 - u^2 - 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)^3$
c_3, c_7	y^3
c_5, c_6, c_8 c_9, c_{10}, c_{11} c_{12}	$y^3 - 5y^2 + 6y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.24698$ $a = 1.44504$ $b = -2.24698$	4.69981	7.43300
$u = -0.445042$ $a = 2.80194$ $b = -0.554958$	-0.939962	2.02180
$u = -1.80194$ $a = -0.246980$ $b = 0.801938$	15.9794	-6.45470

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u-1)^3)(u^{35} + 34u^{34} + \dots + 115u + 1)$
c_2	$((u-1)^3)(u^{35} - 4u^{34} + \dots + 11u - 1)$
c_3, c_7	$u^3(u^{35} - 3u^{34} + \dots - 68u + 8)$
c_4	$((u+1)^3)(u^{35} - 4u^{34} + \dots + 11u - 1)$
c_5, c_6	$(u^3 + u^2 - 2u - 1)(u^{35} + 2u^{34} + \dots + 3u^2 - 1)$
c_8	$(u^3 + u^2 - 2u - 1)(u^{35} - 2u^{34} + \dots + 4u - 1)$
c_9, c_{10}	$(u^3 - u^2 - 2u + 1)(u^{35} + 2u^{34} + \dots + 3u^2 - 1)$
c_{11}, c_{12}	$(u^3 - u^2 - 2u + 1)(u^{35} - 2u^{34} + \dots + 4u - 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^3)(y^{35} - 62y^{34} + \dots + 24691y - 1)$
c_2, c_4	$((y - 1)^3)(y^{35} - 34y^{34} + \dots + 115y - 1)$
c_3, c_7	$y^3(y^{35} + 21y^{34} + \dots + 3536y - 64)$
c_5, c_6, c_9 c_{10}	$(y^3 - 5y^2 + 6y - 1)(y^{35} - 36y^{34} + \dots + 6y - 1)$
c_8, c_{11}, c_{12}	$(y^3 - 5y^2 + 6y - 1)(y^{35} - 24y^{34} + \dots + 6y - 1)$