$12n_{0218}$  (K12n\_{0218})



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle -u^{22} - 2u^{21} + \dots + b - 1, \ -u^{22} - u^{21} + \dots + a - 1, \ u^{23} + 2u^{22} + \dots + 2u + 1 \rangle \\ I_2^u &= \langle u^8 - 2u^6 + u^5 + 2u^4 - u^3 + b + u, \ u^7 - 2u^5 + u^4 + 2u^3 - u^2 + a + u, \\ u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1 \rangle \end{split}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 32 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^{2}</sup>$ All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\begin{split} & \prod_{i=1}^{L} (-u^{22} - 2u^{21} + \dots + b - 1, \ -u^{22} - u^{21} + \dots + a - 1, \ u^{23} + 2u^{22} + \dots + 2u + 1) \\ \text{(i) Arc colorings} \\ & a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ & a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix} \\ & a_3 = \begin{pmatrix} u^{22} + u^{21} + \dots + 2u + 1 \\ u^{22} + 2u^{21} + \dots + 2u + 1 \end{pmatrix} \\ & a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ & a_2 = \begin{pmatrix} 2u^{22} + 2u^{21} + \dots + 3u + 1 \\ 2u^{22} + 3u^{21} + \dots + 3u + 2 \end{pmatrix} \\ & a_1 = \begin{pmatrix} -u^{21} + 5u^{19} - 13u^{17} + 20u^{15} + 8u^{13} - 5u^{11} + 2u^9 - 2u^7 - u^3 \\ -u^{21} + 5u^{19} - 13u^{17} + 20u^{15} - 20u^{13} + 11u^{11} - u^9 - 4u^7 + u^5 + u^3 - u \end{pmatrix} \\ & a_4 = \begin{pmatrix} 3u^{22} + 3u^{21} + \dots + 5u + 2 \\ 3u^{22} + 4u^{21} + \dots + 5u + 2 \\ 3u^{22} + 4u^{21} + \dots + 5u + 3 \end{pmatrix} \\ & a_{10} = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix} \\ & a_{12} = \begin{pmatrix} u^6 - u^4 + 1 \\ u^6 - 2u^4 + u^2 \end{pmatrix} \\ & a_8 = \begin{pmatrix} -u^{11} + 2u^9 - 2u^7 - u^3 \\ -u^{13} + 3u^{11} - 5u^9 + 4u^7 - 2u^5 - u^3 + u \end{pmatrix} \end{split}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $10u^{22} + 11u^{21} - 52u^{20} - 76u^{19} + 117u^{18} + 231u^{17} - 102u^{16} - 390u^{15} - 69u^{14} + 358u^{13} + 268u^{12} - 113u^{11} - 261u^{10} - 92u^9 + 98u^8 + 84u^7 + 19u^6 + 10u^5 - 11u^4 - 33u^3 - u^2 + 12u + 11$ 

(iv	) u-Polynomials	at the	component
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Crossings	u-Polynomials at each crossing
$c_1$	$u^{23} + 44u^{22} + \dots + 46u + 1$
$c_2, c_4$	$u^{23} - 10u^{22} + \dots + 10u - 1$
$c_{3}, c_{7}$	$u^{23} - u^{22} + \dots + 512u - 512$
$c_5, c_{10}$	$u^{23} - 2u^{22} + \dots + 2u - 1$
$c_{6}, c_{9}$	$u^{23} - 6u^{22} + \dots + 30u - 7$
$c_8, c_{12}$	$u^{23} + 24u^{21} + \dots + 2u - 1$
c <sub>11</sub>	$u^{23} - 12u^{22} + \dots + 2u - 1$

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{23} - 168y^{22} + \dots + 3538y - 1$
$c_2, c_4$	$y^{23} - 44y^{22} + \dots + 46y - 1$
$c_3, c_7$	$y^{23} + 57y^{22} + \dots + 2621440y - 262144$
$c_5, c_{10}$	$y^{23} - 12y^{22} + \dots + 2y - 1$
$c_{6}, c_{9}$	$y^{23} + 12y^{22} + \dots + 410y - 49$
$c_8, c_{12}$	$y^{23} + 48y^{22} + \dots + 2y - 1$
$c_{11}$	$y^{23} + 24y^{21} + \dots - 2y - 1$

# $(\mathbf{v})$ Riley Polynomials at the component

(vi)	Complex	Volumes	and	Cusp	Shapes	

Solutions to $I_1^u$	$\sqrt{-1}(\operatorname{vol}+\sqrt{-1}CS)$	Cusp shape
u = -0.793555 + 0.695238I		
a = 0.27094 - 1.56138I	19.5669 - 2.6314I	-2.85971 + 2.82212I
b = 0.563681 - 0.478675I		
u = -0.793555 - 0.695238I		
a = 0.27094 + 1.56138I	19.5669 + 2.6314I	-2.85971 - 2.82212I
b = 0.563681 + 0.478675I		
u = 1.022100 + 0.407841I		
a = 1.44074 + 0.54244I	0.05293 + 1.76634I	1.02070 - 2.91905I
b = -0.140040 + 1.113520I		
u = 1.022100 - 0.407841I		
a = 1.44074 - 0.54244I	0.05293 - 1.76634I	1.02070 + 2.91905I
b = -0.140040 - 1.113520I		
u = -0.260502 + 0.851460I		
a = -0.101202 + 0.883554I	-16.8734 + 5.0391I	-2.11769 - 1.80422I
b = 2.59298 - 0.76044I		
u = -0.260502 - 0.851460I		
a = -0.101202 - 0.883554I	-16.8734 - 5.0391I	-2.11769 + 1.80422I
b = 2.59298 + 0.76044I		
u = -1.072240 + 0.511021I		
a = 0.05623 + 2.46640I	-0.80606 - 4.86361I	0.58399 + 4.58744I
b = 1.31169 + 1.69266I		
u = -1.072240 - 0.511021I		
a = 0.05623 - 2.46640I	-0.80606 + 4.86361I	0.58399 - 4.58744I
b = 1.31169 - 1.69266I		
u = -1.151200 + 0.397103I		
a = 0.378436 - 0.814303I	4.03412 - 1.87941I	8.76933 + 1.17253I
b = -0.061499 - 0.968355I		
u = -1.151200 - 0.397103I		
a = 0.378436 + 0.814303I	4.03412 + 1.87941I	8.76933 - 1.17253I
b = -0.061499 + 0.968355I		

Solutions to $I_1^u$	$\sqrt{-1}(\operatorname{vol}+\sqrt{-1}CS)$	Cusp shape
u = 0.669270 + 0.402839I		
a = 0.378364 - 0.834298I	-1.04289 + 1.55239I	-1.64388 - 5.32889I
b = 0.169751 + 0.377973I		
u = 0.669270 - 0.402839I		
a = 0.378364 + 0.834298I	-1.04289 - 1.55239I	-1.64388 + 5.32889I
b = 0.169751 - 0.377973I		
u = -0.769798		
a = 0.600191	1.02417	10.8970
b = 0.484933		
u = 1.151500 + 0.497191I		
a = -0.371757 - 0.631221I	3.31594 + 6.22870I	6.08610 - 5.76635I
b = 0.523099 - 0.584172I		
u = 1.151500 - 0.497191I		
a = -0.371757 + 0.631221I	3.31594 - 6.22870I	6.08610 + 5.76635I
b = 0.523099 + 0.584172I		
u = 1.233100 + 0.274609I		
a = -2.75962 + 0.02500I	-12.07890 - 1.46711I	2.75909 - 0.30473I
b = -1.94681 - 1.66946I		
u = 1.233100 - 0.274609I		
a = -2.75962 - 0.02500I	-12.07890 + 1.46711I	2.75909 + 0.30473I
b = -1.94681 + 1.66946I		
u = 0.152344 + 0.678389I		
a = 0.370495 + 0.387642I	0.49322 - 1.74871I	2.97942 + 3.32574I
b = -0.142963 - 0.519552I		
u = 0.152344 - 0.678389I		
a = 0.370495 - 0.387642I	0.49322 + 1.74871I	2.97942 - 3.32574I
b = -0.142963 + 0.519552I		
u = -1.179040 + 0.569666I		
a = -1.36258 - 2.90160I	-14.1285 - 10.2729I	0.79116 + 5.29982I
b = -3.23838 - 0.97939I		

Solutions to $I_1^u$	$\sqrt{-1}(\operatorname{vol}+\sqrt{-1}CS)$	Cusp shape
u = -1.179040 - 0.569666I		
a = -1.36258 + 2.90160I	-14.1285 + 10.2729I	0.79116 - 5.29982I
b = -3.23838 + 0.97939I		
u = -0.386868 + 0.554823I		
a = -1.100140 - 0.404039I	-2.78460 + 0.52794I	-2.81721 + 0.26390I
b = -1.37398 + 0.73498I		
u = -0.386868 - 0.554823I		
a = -1.100140 + 0.404039I	-2.78460 - 0.52794I	-2.81721 - 0.26390I
b = -1.37398 - 0.73498I		

$$\text{II. } I_2^u = \langle u^8 - 2u^6 + u^5 + 2u^4 - u^3 + b + u, \ u^7 - 2u^5 + u^4 + 2u^3 - u^2 + a + u, \ u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1 \rangle$$

(i) Arc colorings

$$a_{6} = \begin{pmatrix} 1\\0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0\\u \end{pmatrix}$$

$$a_{3} = \begin{pmatrix} -u^{7} + 2u^{5} - u^{4} - 2u^{3} + u^{2} - u\\-u^{8} + 2u^{6} - u^{5} - 2u^{4} + u^{3} - u \end{pmatrix}$$

$$a_{5} = \begin{pmatrix} 1\\u^{2} \end{pmatrix}$$

$$a_{2} = \begin{pmatrix} -u^{7} + 2u^{5} - u^{4} - 2u^{3} + u^{2} - u - 1\\-u^{8} + 2u^{6} - u^{5} - 2u^{4} + u^{3} - u^{2} - u \end{pmatrix}$$

$$a_{1} = \begin{pmatrix} -1\\-u^{2} \end{pmatrix}$$

$$a_{4} = \begin{pmatrix} -u^{7} + 2u^{5} - u^{4} - 2u^{3} + u^{2} - u\\-u^{8} + 2u^{6} - u^{5} - 2u^{4} + u^{3} - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u\\-u^{3} + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^{3}\\u^{5} - u^{3} + u \end{pmatrix}$$

$$a_{9} = \begin{pmatrix} -u^{3}\\-u^{3} + u \end{pmatrix}$$

$$a_{7} = \begin{pmatrix} u^{6} - u^{4} + 1\\u^{6} - 2u^{4} + u^{2} \end{pmatrix}$$

$$a_{8} = \begin{pmatrix} u^{6} - u^{4} + 1\\u^{6} - 2u^{4} + u^{2} \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-u^8 - 2u^7 + u^6 + 4u^5 - 3u^4 - 6u^3 + u^2 - u - 2$ 

(iv	) u-Polynomials	at the	component
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Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u-1)^9$
$c_{3}, c_{7}$	$u^9$
$c_4$	$(u+1)^9$
C5	$u^9 - u^8 - 2u^7 + 3u^6 + u^5 - 3u^4 + 2u^3 - u + 1$
<i>c</i> <sub>6</sub>	$u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1$
<i>c</i> <sub>8</sub>	$u^9 - u^8 + 2u^7 - u^6 + 3u^5 - u^4 + 2u^3 + u + 1$
<i>C</i> 9	$u^{9} + 3u^{8} + 8u^{7} + 13u^{6} + 17u^{5} + 17u^{4} + 12u^{3} + 6u^{2} + u - 1$
$c_{10}$	$u^9 + u^8 - 2u^7 - 3u^6 + u^5 + 3u^4 + 2u^3 - u - 1$
c <sub>11</sub>	$u^{9} - 5u^{8} + 12u^{7} - 15u^{6} + 9u^{5} + u^{4} - 4u^{3} + 2u^{2} + u - 1$
$c_{12}$	$u^9 + u^8 + 2u^7 + u^6 + 3u^5 + u^4 + 2u^3 + u - 1$

# $(\mathbf{v})$ Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y-1)^9$
$c_3, c_7$	$y^9$
$c_5, c_{10}$	$y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1$
$c_{6}, c_{9}$	$y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1$
$c_8, c_{12}$	$y^{9} + 3y^{8} + 8y^{7} + 13y^{6} + 17y^{5} + 17y^{4} + 12y^{3} + 6y^{2} + y - 1$
c <sub>11</sub>	$y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1$

(vi)	Complex	Volumes	and	Cusp	Shapes	

$\sqrt{-1}(\operatorname{vol}+\sqrt{-1}CS)$	Cusp shape
-3.42837 + 2.09337I	-2.59545 - 4.13635I
-3.42837 - 2.09337I	-2.59545 + 4.13635I
-0.446489	0.580470
2.72642 - 1.33617I	3.11790 + 0.38556I
2.72642 + 1.33617I	3.11790 - 0.38556I
-1.02799 - 2.45442I	-1.02595 + 3.19656I
-1.02799 + 2.45442I	-1.02595 - 3.19656I
1.95319 + 7.08493I	2.21327 - 6.71575I
1.95319 - 7.08493I	2.21327 + 6.71575I
	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ $-3.42837 + 2.09337I$ $-3.42837 - 2.09337I$ $-0.446489$ $2.72642 - 1.33617I$ $2.72642 + 1.33617I$ $-1.02799 - 2.45442I$ $-1.02799 - 2.45442I$ $1.95319 + 7.08493I$ $1.95319 - 7.08493I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^9)(u^{23} + 44u^{22} + \dots + 46u + 1)$
<i>c</i> <sub>2</sub>	$((u-1)^9)(u^{23} - 10u^{22} + \dots + 10u - 1)$
$c_{3}, c_{7}$	$u^9(u^{23} - u^{22} + \dots + 512u - 512)$
$C_4$	$((u+1)^9)(u^{23} - 10u^{22} + \dots + 10u - 1)$
C5	$(u^9 - u^8 + \dots - u + 1)(u^{23} - 2u^{22} + \dots + 2u - 1)$
<i>c</i> <sub>6</sub>	$(u^9 - 3u^8 + 8u^7 - 13u^6 + 17u^5 - 17u^4 + 12u^3 - 6u^2 + u + 1)$ $\cdot (u^{23} - 6u^{22} + \dots + 30u - 7)$
$c_8$	$(u^9 - u^8 + \dots + u + 1)(u^{23} + 24u^{21} + \dots + 2u - 1)$
<i>C</i> 9	$(u^9 + 3u^8 + 8u^7 + 13u^6 + 17u^5 + 17u^4 + 12u^3 + 6u^2 + u - 1)$ $\cdot (u^{23} - 6u^{22} + \dots + 30u - 7)$
<i>c</i> <sub>10</sub>	$(u^9 + u^8 + \dots - u - 1)(u^{23} - 2u^{22} + \dots + 2u - 1)$
c <sub>11</sub>	$(u^9 - 5u^8 + 12u^7 - 15u^6 + 9u^5 + u^4 - 4u^3 + 2u^2 + u - 1)$ $\cdot (u^{23} - 12u^{22} + \dots + 2u - 1)$
<i>c</i> <sub>12</sub>	$(u^9 + u^8 + \dots + u - 1)(u^{23} + 24u^{21} + \dots + 2u - 1)$

IV.	Riley	Polynomials

Crossings	Riley Polynomials at each crossing	
$c_1$	$((y-1)^9)(y^{23} - 168y^{22} + \dots + 3538y - 1)$	
$c_2, c_4$	$((y-1)^9)(y^{23} - 44y^{22} + \dots + 46y - 1)$	
$c_{3}, c_{7}$	$y^9(y^{23} + 57y^{22} + \dots + 2621440y - 262144)$	
$c_5, c_{10}$	$(y^9 - 5y^8 + 12y^7 - 15y^6 + 9y^5 + y^4 - 4y^3 + 2y^2 + y - 1)$ $\cdot (y^{23} - 12y^{22} + \dots + 2y - 1)$	
$c_6, c_9$	$(y^9 + 7y^8 + 20y^7 + 25y^6 + 5y^5 - 15y^4 + 22y^2 + 13y - 1)$ $\cdot (y^{23} + 12y^{22} + \dots + 410y - 49)$	
$c_8, c_{12}$	$(y^{9} + 3y^{8} + 8y^{7} + 13y^{6} + 17y^{5} + 17y^{4} + 12y^{3} + 6y^{2} + y - 1)$ $\cdot (y^{23} + 48y^{22} + \dots + 2y - 1)$	
$c_{11}$	$(y^9 - y^8 + 12y^7 - 7y^6 + 37y^5 + y^4 - 10y^2 + 5y - 1)$ $\cdot (y^{23} + 24y^{21} + \dots - 2y - 1)$	