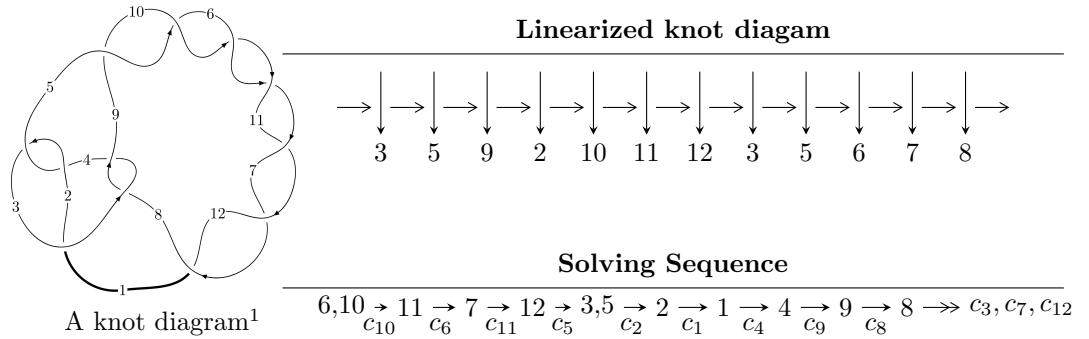


$12n_{0242}$  ( $K12n_{0242}$ )



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$\begin{aligned} I_1^u &= \langle b - u, u^2 + a - 2u, u^3 - 3u^2 + 2u + 1 \rangle \\ I_2^u &= \langle b + u, -u^2 + a + 2, u^3 + u^2 - 2u - 1 \rangle \end{aligned}$$

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\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 6 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle b - u, u^2 + a - 2u, u^3 - 3u^2 + 2u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ -3u^2 + 3u + 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^2 + 1 \\ -5u^2 + 7u + 3 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -u^2 + 2u \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 3u^2 - 3u - 2 \\ 4u^2 - 4u - 2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -4u^2 + 7u + 2 \\ 7u + 2 \end{pmatrix} \\ a_4 &= \begin{pmatrix} -5u^2 + 12u + 4 \\ -8u^2 + 17u + 6 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 3u^2 - 4u - 1 \\ 5u^2 - 10u - 4 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $u^2 - u - 19$

**(iv) u-Polynomials at the component**

| Crossings  | u-Polynomials at each crossing |
|--|--------------------------------|
| $c_1$  | $u^3 - 13u^2 + 51u + 1$        |
| $c_2, c_4$   | $u^3 - u^2 + 7u + 1$           |
| $c_3, c_8$   | $u^3 - 4u^2 + 20u + 8$         |
| $c_5, c_6, c_7$<br>$c_9, c_{10}, c_{11}$<br>$c_{12}$ | $u^3 - 3u^2 + 2u + 1$          |

**(v) Riley Polynomials at the component**

| Crossings  | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1$  | $y^3 - 67y^2 + 2627y - 1$          |
| $c_2, c_4$   | $y^3 + 13y^2 + 51y - 1$            |
| $c_3, c_8$   | $y^3 + 24y^2 + 464y - 64$          |
| $c_5, c_6, c_7$<br>$c_9, c_{10}, c_{11}$<br>$c_{12}$ | $y^3 - 5y^2 + 10y - 1$             |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_1^u$       | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|----------------------------|---------------------------------------|----------------------|
| $u = -0.324718$            |                                       |                      |
| $a = -0.754878$            | -0.531480                             | -18.5700             |
| $b = -0.324718$            |                                       |                      |
| $u = 1.66236 + 0.56228I$   |                                       |                      |
| $a = 0.877439 - 0.744862I$ | $-4.66906 - 2.82812I$                 | $-18.2151 + 1.3071I$ |
| $b = 1.66236 + 0.56228I$   |                                       |                      |
| $u = 1.66236 - 0.56228I$   |                                       |                      |
| $a = 0.877439 + 0.744862I$ | $-4.66906 + 2.82812I$                 | $-18.2151 - 1.3071I$ |
| $b = 1.66236 - 0.56228I$   |                                       |                      |

$$\text{II. } I_2^u = \langle b + u, -u^2 + a + 2, u^3 + u^2 - 2u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_6 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -u \\ u^2 - u - 1 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^2 + 1 \\ -u^2 + u + 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u^2 - 2 \\ -u \end{pmatrix} \\ a_5 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} u^2 - u - 2 \\ -2u \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u \\ -u \end{pmatrix} \\ a_4 &= \begin{pmatrix} u^2 - 2 \\ -u \end{pmatrix} \\ a_9 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-u^2 - u - 17$

**(iv) u-Polynomials at the component**

| Crossings                         | u-Polynomials at each crossing |
|-----------------------------------|--------------------------------|
| $c_1, c_2$                        | $(u - 1)^3$                    |
| $c_3, c_8$                        | $u^3$                          |
| $c_4$                             | $(u + 1)^3$                    |
| $c_5, c_6, c_7$                   | $u^3 - u^2 - 2u + 1$           |
| $c_9, c_{10}, c_{11}$<br>$c_{12}$ | $u^3 + u^2 - 2u - 1$           |

**(v) Riley Polynomials at the component**

| Crossings  | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_4$                                      | $(y - 1)^3$                        |
| $c_3, c_8$   | $y^3$                              |
| $c_5, c_6, c_7$<br>$c_9, c_{10}, c_{11}$<br>$c_{12}$ | $y^3 - 5y^2 + 6y - 1$              |

**(vi) Complex Volumes and Cusp Shapes**

| Solutions to $I_2^u$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = 1.24698$        |                                       |            |
| $a = -0.445042$      | -7.98968                              | -19.8020   |
| $b = -1.24698$       |                                       |            |
| $u = -0.445042$      |                                       |            |
| $a = -1.80194$       | -2.34991                              | -16.7530   |
| $b = 0.445042$       |                                       |            |
| $u = -1.80194$       |                                       |            |
| $a = 1.24698$        | -19.2692                              | -18.4450   |
| $b = 1.80194$        |                                       |            |

### III. u-Polynomials

| Crossings                         | u-Polynomials at each crossing              |
|-----------------------------------|---|
| $c_1$                             | $(u - 1)^3(u^3 - 13u^2 + 51u + 1)$          |
| $c_2$                             | $(u - 1)^3(u^3 - u^2 + 7u + 1)$             |
| $c_3, c_8$                        | $u^3(u^3 - 4u^2 + 20u + 8)$                 |
| $c_4$                             | $(u + 1)^3(u^3 - u^2 + 7u + 1)$             |
| $c_5, c_6, c_7$                   | $(u^3 - 3u^2 + 2u + 1)(u^3 - u^2 - 2u + 1)$ |
| $c_9, c_{10}, c_{11}$<br>$c_{12}$ | $(u^3 - 3u^2 + 2u + 1)(u^3 + u^2 - 2u - 1)$ |

#### IV. Riley Polynomials

| Crossings  | Riley Polynomials at each crossing            |
|--|---|
| $c_1$  | $(y - 1)^3(y^3 - 67y^2 + 2627y - 1)$          |
| $c_2, c_4$   | $(y - 1)^3(y^3 + 13y^2 + 51y - 1)$            |
| $c_3, c_8$   | $y^3(y^3 + 24y^2 + 464y - 64)$                |
| $c_5, c_6, c_7$<br>$c_9, c_{10}, c_{11}$<br>$c_{12}$ | $(y^3 - 5y^2 + 6y - 1)(y^3 - 5y^2 + 10y - 1)$ |