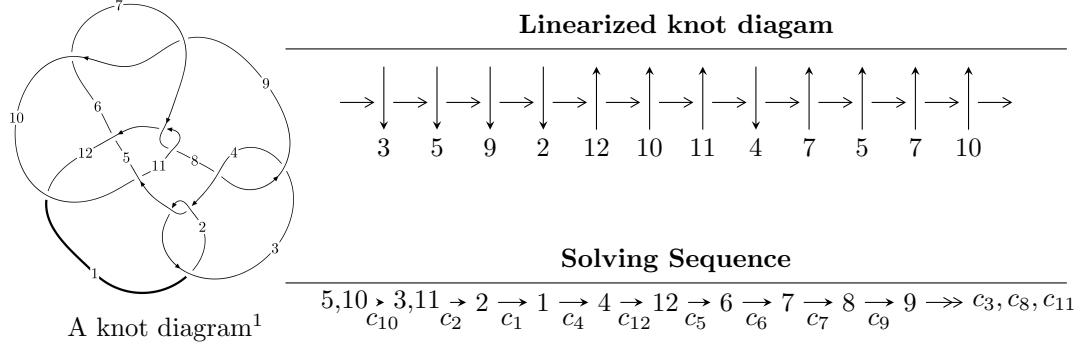


## $12n_{0257}$ ( $K12n_{0257}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 1.90485 \times 10^{17}u^{17} - 2.51658 \times 10^{17}u^{16} + \dots + 3.03349 \times 10^{16}b - 4.02818 \times 10^{17}, \\
 &\quad 2.08713 \times 10^{17}u^{17} - 2.72839 \times 10^{17}u^{16} + \dots + 7.58374 \times 10^{15}a - 3.96132 \times 10^{17}, u^{18} - u^{17} + \dots - 4u + 1 \rangle \\
 I_2^u &= \langle 3u^{11} - u^{10} + u^9 - 9u^8 - 6u^7 - 3u^6 + 4u^5 + 18u^4 + 12u^3 + 7u^2 + b - 3u - 3, \\
 &\quad - 4u^{11} + 3u^{10} - 2u^9 + 13u^8 + 2u^7 + 2u^6 - 9u^5 - 20u^4 - 8u^3 - u^2 + a + 8u + 4, \\
 &\quad u^{12} - 3u^9 - 3u^8 - u^7 + 2u^6 + 7u^5 + 6u^4 + 2u^3 - 2u^2 - 3u - 1 \rangle \\
 I_3^u &= \langle u^3 + 3u^2 + 18b - 17u + 46, -5u^3 + 3u^2 + 36a - 41u - 32, u^4 - u^3 + 7u^2 + 6u - 4 \rangle \\
 I_4^u &= \langle 2b + u - 1, a - u - 1, u^2 + u - 1 \rangle \\
 I_5^u &= \langle b - u - 1, -2u^3 + 3u^2 + 66a + 19u - 1, u^4 + 4u^3 + 7u^2 + 6u + 11 \rangle
 \end{aligned}$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 40 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.90 \times 10^{17} u^{17} - 2.52 \times 10^{17} u^{16} + \dots + 3.03 \times 10^{16} b - 4.03 \times 10^{17}, 2.09 \times 10^{17} u^{17} - 2.73 \times 10^{17} u^{16} + \dots + 7.58 \times 10^{15} a - 3.96 \times 10^{17}, u^{18} - u^{17} + \dots - 4u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -27.5212u^{17} + 35.9768u^{16} + \dots - 342.299u + 52.2344 \\ -6.27938u^{17} + 8.29598u^{16} + \dots - 84.9277u + 13.2790 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -27.5212u^{17} + 35.9768u^{16} + \dots - 342.299u + 52.2344 \\ -11.3536u^{17} + 14.8220u^{16} + \dots - 146.271u + 21.7346 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -7.55482u^{17} + 8.52485u^{16} + \dots - 73.2580u + 8.96058 \\ -1.14106u^{17} + 1.22922u^{16} + \dots - 9.94123u + 0.881867 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -12.4658u^{17} + 7.03725u^{16} + \dots + 23.8108u - 25.5769 \\ -1.03310u^{17} + 1.07235u^{16} + \dots - 13.6155u + 0.722053 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -6.41376u^{17} + 7.29563u^{16} + \dots - 63.3168u + 8.07871 \\ -1.14106u^{17} + 1.22922u^{16} + \dots - 9.94123u + 0.881867 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 6.19684u^{17} - 0.924141u^{16} + \dots - 69.5089u + 28.5882 \\ 0.881867u^{17} + 0.259189u^{16} + \dots - 17.5763u + 6.41376 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 7.07871u^{17} - 0.664952u^{16} + \dots - 87.0852u + 35.0020 \\ 0.881867u^{17} + 0.259189u^{16} + \dots - 17.5763u + 6.41376 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 7.07871u^{17} - 0.664952u^{16} + \dots - 86.0852u + 35.0020 \\ 0.881867u^{17} + 0.259189u^{16} + \dots - 17.5763u + 6.41376 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 22.1744u^{17} - 27.4894u^{16} + \dots + 263.201u - 35.7652 \\ 5.27270u^{17} - 6.06640u^{16} + \dots + 53.3756u - 6.19684 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{2063530662655740221}{39519432929474093823}u^{17} + \frac{4790167344610047657}{60669891560994640}u^{16} + \dots -$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{18} + 9u^{17} + \cdots - 656u + 256$
$c_2, c_4$	$u^{18} - 3u^{17} + \cdots + 52u - 16$
$c_3, c_8$	$u^{18} - 5u^{17} + \cdots + 80u + 64$
$c_5, c_6, c_9$	$u^{18} + 5u^{16} + \cdots - 5u - 1$
$c_7, c_{10}, c_{11}$	$u^{18} + u^{17} + \cdots + 4u + 1$
$c_{12}$	$u^{18} + 12u^{17} + \cdots + 6u - 4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{18} + 3y^{17} + \cdots + 495872y + 65536$
$c_2, c_4$	$y^{18} - 9y^{17} + \cdots + 656y + 256$
$c_3, c_8$	$y^{18} + 9y^{17} + \cdots - 29440y + 4096$
$c_5, c_6, c_9$	$y^{18} + 10y^{17} + \cdots - 45y + 1$
$c_7, c_{10}, c_{11}$	$y^{18} + 31y^{17} + \cdots + 6y + 1$
$c_{12}$	$y^{18} - 50y^{17} + \cdots - 2700y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.584558 + 0.366182I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.031695 + 0.764128I$	$1.158820 - 0.715487I$	$6.82546 + 3.87567I$
$b = -0.238877 + 0.648680I$		
$u = -0.584558 - 0.366182I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.031695 - 0.764128I$	$1.158820 + 0.715487I$	$6.82546 - 3.87567I$
$b = -0.238877 - 0.648680I$		
$u = 1.51394 + 0.18364I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.619867 + 0.808006I$	$10.72160 + 4.05902I$	$-5.48776 - 6.30227I$
$b = -0.40901 + 1.77160I$		
$u = 1.51394 - 0.18364I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.619867 - 0.808006I$	$10.72160 - 4.05902I$	$-5.48776 + 6.30227I$
$b = -0.40901 - 1.77160I$		
$u = -0.022331 + 0.452997I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.61941 + 0.40552I$	$0.21869 - 2.12649I$	$2.57122 + 5.28808I$
$b = 0.156583 + 0.047051I$		
$u = -0.022331 - 0.452997I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.61941 - 0.40552I$	$0.21869 + 2.12649I$	$2.57122 - 5.28808I$
$b = 0.156583 - 0.047051I$		
$u = 0.025010 + 0.431550I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.34703 + 2.60646I$	$-2.52651 - 6.83690I$	$1.00389 + 11.16505I$
$b = 0.250192 + 0.749320I$		
$u = 0.025010 - 0.431550I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.34703 - 2.60646I$	$-2.52651 + 6.83690I$	$1.00389 - 11.16505I$
$b = 0.250192 - 0.749320I$		
$u = 0.007817 + 0.411255I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.85304 - 2.78085I$	$-3.55439 + 1.25550I$	$-1.98701 - 1.61045I$
$b = 0.325456 - 0.844226I$		
$u = 0.007817 - 0.411255I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.85304 + 2.78085I$	$-3.55439 - 1.25550I$	$-1.98701 + 1.61045I$
$b = 0.325456 + 0.844226I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.75357$		
$a = -0.620403$	7.06782	-18.1410
$b = 1.40026$		
$u = 0.204909$		
$a = 4.38528$	-1.30691	-9.62130
$b = 0.536453$		
$u = -1.10465 + 2.31020I$		
$a = 0.029942 + 0.642788I$	$-13.4615 - 12.9156I$	0
$b = 0.31930 + 2.83217I$		
$u = -1.10465 - 2.31020I$		
$a = 0.029942 - 0.642788I$	$-13.4615 + 12.9156I$	0
$b = 0.31930 - 2.83217I$		
$u = -0.50858 + 2.58223I$		
$a = 0.535381 - 0.129487I$	$-8.47225 - 5.66445I$	0
$b = -0.444741 - 0.317296I$		
$u = -0.50858 - 2.58223I$		
$a = 0.535381 + 0.129487I$	$-8.47225 + 5.66445I$	0
$b = -0.444741 + 0.317296I$		
$u = 0.19411 + 2.91147I$		
$a = -0.215532 - 0.577704I$	$-13.28390 + 2.28868I$	0
$b = 0.82274 - 2.38447I$		
$u = 0.19411 - 2.91147I$		
$a = -0.215532 + 0.577704I$	$-13.28390 - 2.28868I$	0
$b = 0.82274 + 2.38447I$		

$$I_2^u = \langle 3u^{11} - u^{10} + \dots + b - 3, \ -4u^{11} + 3u^{10} + \dots + a + 4, \ u^{12} - 3u^9 + \dots - 3u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 4u^{11} - 3u^{10} + \dots - 8u - 4 \\ -3u^{11} + u^{10} + \dots + 3u + 3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 4u^{11} - 3u^{10} + \dots - 8u - 4 \\ -5u^{11} + 2u^{10} + \dots + 8u + 6 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -3u^{11} + u^{10} + 9u^8 + 6u^7 - 7u^5 - 19u^4 - 11u^3 - u^2 + 8u + 6 \\ -u^2 - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -6u^{11} + 4u^{10} + \dots + 14u + 8 \\ 7u^{11} - 5u^{10} + \dots - 21u - 13 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -3u^{11} + u^{10} + 9u^8 + 6u^7 - 7u^5 - 19u^4 - 11u^3 + 8u + 7 \\ -u^2 - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 7u^{11} - 3u^{10} + \dots - 14u - 13 \\ -u^{11} + 3u^8 + 3u^7 + u^6 - 2u^5 - 7u^4 - 6u^3 - 2u^2 + 2u + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 6u^{11} - 3u^{10} + u^9 - 18u^8 - 9u^7 + 12u^5 + 35u^4 + 17u^3 + u^2 - 12u - 10 \\ -u^{11} + 3u^8 + 3u^7 + u^6 - 2u^5 - 7u^4 - 6u^3 - 2u^2 + 2u + 3 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 6u^{11} - 3u^{10} + u^9 - 18u^8 - 9u^7 + 12u^5 + 35u^4 + 17u^3 + u^2 - 13u - 10 \\ -u^{11} + 3u^8 + 3u^7 + u^6 - 2u^5 - 7u^4 - 5u^3 - 2u^2 + 2u + 3 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 10u^{11} - 6u^{10} + \dots - 21u - 17 \\ -3u^{11} + u^{10} + 9u^8 + 6u^7 - 7u^5 - 19u^4 - 11u^3 + 8u + 7 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= 12u^{11} - 12u^{10} + 3u^9 - 41u^8 + 15u^6 + 38u^5 + 73u^4 - u^3 - 22u^2 - 57u - 30$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{12} - 4u^{11} + \dots - 13u + 1$
$c_2$	$u^{12} + 4u^{11} + \dots - u + 1$
$c_3$	$u^{12} + 6u^{10} + 3u^9 + 13u^8 + 7u^7 + 15u^6 + 6u^5 + 2u^3 - 2u^2 - 3u + 1$
$c_4$	$u^{12} - 4u^{11} + \dots + u + 1$
$c_5, c_9$	$u^{12} - 3u^{11} + 2u^{10} + 2u^9 - 6u^8 + 7u^7 - 2u^6 - u^5 + 3u^4 - 3u^3 - 1$
$c_6$	$u^{12} + 3u^{11} + 2u^{10} - 2u^9 - 6u^8 - 7u^7 - 2u^6 + u^5 + 3u^4 + 3u^3 - 1$
$c_7, c_{10}$	$u^{12} - 3u^9 - 3u^8 - u^7 + 2u^6 + 7u^5 + 6u^4 + 2u^3 - 2u^2 - 3u - 1$
$c_8$	$u^{12} + 6u^{10} - 3u^9 + 13u^8 - 7u^7 + 15u^6 - 6u^5 - 2u^3 - 2u^2 + 3u + 1$
$c_{11}$	$u^{12} + 3u^9 - 3u^8 + u^7 + 2u^6 - 7u^5 + 6u^4 - 2u^3 - 2u^2 + 3u - 1$
$c_{12}$	$u^{12} - 12u^{11} + \dots - 12u + 9$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{12} + 12y^{11} + \cdots - 81y + 1$
$c_2, c_4$	$y^{12} - 4y^{11} + \cdots - 13y + 1$
$c_3, c_8$	$y^{12} + 12y^{11} + \cdots - 13y + 1$
$c_5, c_6, c_9$	$y^{12} - 5y^{11} + 4y^{10} + 10y^9 - 27y^7 - 8y^6 + 25y^5 + 15y^4 - 5y^3 - 6y^2 + 1$
$c_7, c_{10}, c_{11}$	$y^{12} - 6y^{10} - 5y^9 + 15y^8 + 25y^7 - 8y^6 - 27y^5 + 10y^3 + 4y^2 - 5y + 1$
$c_{12}$	$y^{12} - 24y^{11} + \cdots - 234y + 81$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.366604 + 0.825368I$		
$a = 1.11814 + 0.91713I$	$-2.86185 + 6.14960I$	$-3.55511 - 1.94828I$
$b = -0.413716 + 0.377477I$		
$u = -0.366604 - 0.825368I$		
$a = 1.11814 - 0.91713I$	$-2.86185 - 6.14960I$	$-3.55511 + 1.94828I$
$b = -0.413716 - 0.377477I$		
$u = -0.851892$		
$a = -0.391239$	3.56755	13.7860
$b = -2.26079$		
$u = 0.111536 + 1.194340I$		
$a = 0.317924 - 0.704003I$	$-5.28057 - 0.69048I$	$-8.92309 + 4.67234I$
$b = -0.993719 + 0.895794I$		
$u = 0.111536 - 1.194340I$		
$a = 0.317924 + 0.704003I$	$-5.28057 + 0.69048I$	$-8.92309 - 4.67234I$
$b = -0.993719 - 0.895794I$		
$u = 0.765921$		
$a = 1.24205$	2.40622	-53.6250
$b = -9.03089$		
$u = -0.496770 + 1.152800I$		
$a = -0.554307 + 0.648652I$	$-0.483582 + 0.496104I$	$-0.592681 - 0.118839I$
$b = 0.388509 + 0.841432I$		
$u = -0.496770 - 1.152800I$		
$a = -0.554307 - 0.648652I$	$-0.483582 - 0.496104I$	$-0.592681 + 0.118839I$
$b = 0.388509 - 0.841432I$		
$u = -0.629825 + 0.069225I$		
$a = 1.33711 - 0.51168I$	$4.44304 + 1.79476I$	$4.83493 - 4.62713I$
$b = -0.874744 + 0.682079I$		
$u = -0.629825 - 0.069225I$		
$a = 1.33711 + 0.51168I$	$4.44304 - 1.79476I$	$4.83493 + 4.62713I$
$b = -0.874744 - 0.682079I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.42465 + 0.18625I$		
$a = -0.644266 + 0.830701I$	$11.06570 + 3.92660I$	$15.1553 + 1.2084I$
$b = -0.46049 + 1.87154I$		
$u = 1.42465 - 0.18625I$		
$a = -0.644266 - 0.830701I$	$11.06570 - 3.92660I$	$15.1553 - 1.2084I$
$b = -0.46049 - 1.87154I$		

$$\text{III. } I_3^u = \langle u^3 + 3u^2 + 18b - 17u + 46, -5u^3 + 3u^2 + 36a - 41u - 32, u^4 - u^3 + 7u^2 + 6u - 4 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \left( \frac{5}{36}u^3 - \frac{1}{12}u^2 + \frac{41}{36}u + \frac{8}{9} \right) \\ a_{11} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_2 &= \left( \frac{5}{36}u^3 - \frac{1}{12}u^2 + \frac{41}{36}u + \frac{8}{9} \right) \\ a_1 &= \left( \frac{1}{9}u^3 - \frac{1}{6}u^2 + \frac{11}{18}u + \frac{11}{18} \right) \\ a_4 &= \left( \frac{1}{9}u^3 - \frac{1}{6}u^2 + \frac{11}{18}u + \frac{11}{18} \right) \\ a_{12} &= \left( -\frac{1}{18}u^3 - \frac{1}{6}u^2 - \frac{1}{18}u - \frac{14}{9} \right) \\ a_6 &= \left( \frac{5}{12}u^3 - \frac{1}{4}u^2 + \frac{29}{12}u + \frac{5}{3} \right) \\ a_7 &= \left( \frac{5}{36}u^3 - \frac{1}{12}u^2 + \frac{41}{36}u + \frac{8}{9} \right) \\ a_8 &= \left( \frac{11}{12}u^3 - \frac{7}{6}u^2 - \frac{43}{18}u + \frac{1}{9} \right) \\ a_9 &= \left( -\frac{1}{9}u^3 + \frac{1}{6}u^2 - \frac{11}{18}u - \frac{11}{18} \right) \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -2

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 + 3u + 1)^2$
$c_2, c_4, c_{12}$	$(u^2 - u - 1)^2$
$c_3, c_8$	$(u^2 + u - 1)^2$
$c_5, c_6, c_9$	$u^4 + 4u^3 + 5u^2 - 8u - 11$
$c_7, c_{10}, c_{11}$	$u^4 + u^3 + 7u^2 - 6u - 4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 - 7y + 1)^2$
$c_2, c_3, c_4$ $c_8, c_{12}$	$(y^2 - 3y + 1)^2$
$c_5, c_6, c_9$	$y^4 - 6y^3 + 67y^2 - 174y + 121$
$c_7, c_{10}, c_{11}$	$y^4 + 13y^3 + 53y^2 - 92y + 16$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.06243$		
$a = -0.581719$	2.96088	-2.00000
$b = -3.68046$		
$u = 0.444394$		
$a = 1.39074$	2.96088	-2.00000
$b = -2.17364$		
$u = 0.80902 + 2.79600I$		
$a = -0.154508 + 0.533989I$	-12.8305	-2.00000
$b = 0.42705 + 2.79600I$		
$u = 0.80902 - 2.79600I$		
$a = -0.154508 - 0.533989I$	-12.8305	-2.00000
$b = 0.42705 - 2.79600I$		

$$\text{IV. } I_4^u = \langle 2b + u - 1, a - u - 1, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} u+1 \\ -\frac{1}{2}u + \frac{1}{2} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ u-1 \end{pmatrix} \\ a_2 &= \begin{pmatrix} u+1 \\ -\frac{3}{2}u + \frac{1}{2} \end{pmatrix} \\ a_1 &= \begin{pmatrix} 0 \\ -u \end{pmatrix} \\ a_4 &= \begin{pmatrix} u+1 \\ -\frac{1}{2}u + \frac{1}{2} \end{pmatrix} \\ a_{12} &= \begin{pmatrix} u \\ -u \end{pmatrix} \\ a_6 &= \begin{pmatrix} 2u-1 \\ -u+1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u \\ -u+1 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 2u \\ -3u+2 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 2u \\ -3u+2 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-\frac{45}{4}u + \frac{45}{4}$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^2$
$c_3, c_8$	$u^2$
$c_4$	$(u + 1)^2$
$c_5, c_6$	$u^2 + 3u + 1$
$c_7$	$u^2 - u - 1$
$c_9$	$u^2 - 3u + 1$
$c_{10}, c_{11}, c_{12}$	$u^2 + u - 1$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^2$
$c_3, c_8$	$y^2$
$c_5, c_6, c_9$	$y^2 - 7y + 1$
$c_7, c_{10}, c_{11}$ $c_{12}$	$y^2 - 3y + 1$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$		
$a = 1.61803$	-0.657974	4.29710
$b = 0.190983$		
$u = -1.61803$		
$a = -0.618034$	7.23771	29.4530
$b = 1.30902$		

$$\mathbf{V. } I_5^u = \langle b - u - 1, -2u^3 + 3u^2 + 66a + 19u - 1, u^4 + 4u^3 + 7u^2 + 6u + 11 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_3 &= \begin{pmatrix} 0.0303030u^3 - 0.0454545u^2 - 0.287879u + 0.0151515 \\ u + 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} 1 \\ -u^2 \end{pmatrix} \\ a_2 &= \begin{pmatrix} 0.0303030u^3 - 0.0454545u^2 - 0.287879u + 0.0151515 \\ -\frac{1}{6}u^3 - u^2 + \frac{1}{3}u - \frac{5}{6} \end{pmatrix} \\ a_1 &= \begin{pmatrix} -0.121212u^3 - 0.318182u^2 - 0.348485u - 0.560606 \\ -\frac{1}{6}u^3 - \frac{1}{2}u^2 - \frac{1}{6}u - \frac{1}{3} \end{pmatrix} \\ a_4 &= \begin{pmatrix} -0.121212u^3 - 0.318182u^2 - 0.348485u - 0.560606 \\ \frac{1}{6}u^3 + \frac{3}{2}u^2 + \frac{7}{6}u + \frac{10}{3} \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.0454545u^3 + 0.181818u^2 - 0.181818u - 0.227273 \\ -\frac{1}{6}u^3 - \frac{1}{2}u^2 - \frac{1}{6}u - \frac{1}{3} \end{pmatrix} \\ a_6 &= \begin{pmatrix} 0.227273u^3 + 0.409091u^2 + 0.590909u + 0.363636 \\ -\frac{1}{6}u^3 + \frac{1}{3}u + \frac{1}{6} \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.0606061u^3 + 0.409091u^2 + 0.924242u + 0.530303 \\ -\frac{1}{6}u^3 + \frac{1}{3}u + \frac{1}{6} \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.272727u^3 - 0.590909u^2 - 0.409091u - 1.13636 \\ \frac{1}{6}u^3 + 2u^2 - \frac{4}{3}u + \frac{23}{6} \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.121212u^3 + 0.318182u^2 + 0.348485u + 0.560606 \\ -\frac{1}{2}u^2 + \frac{1}{2}u - \frac{3}{2} \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -2

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$(u^2 + 3u + 1)^2$
$c_2, c_4, c_{12}$	$(u^2 - u - 1)^2$
$c_3, c_8$	$(u^2 + u - 1)^2$
$c_5, c_6, c_9$	$u^4 - u^3 + 5u^2 + 2u + 4$
$c_7, c_{10}, c_{11}$	$u^4 - 4u^3 + 7u^2 - 6u + 11$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^2 - 7y + 1)^2$
$c_2, c_3, c_4$ $c_8, c_{12}$	$(y^2 - 3y + 1)^2$
$c_5, c_6, c_9$	$y^4 + 9y^3 + 37y^2 + 36y + 16$
$c_7, c_{10}, c_{11}$	$y^4 - 2y^3 + 23y^2 + 118y + 121$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.118034 + 1.322880I$		
$a = 0.041356 - 0.463500I$	-4.93480	-2.00000
$b = 1.11803 + 1.32288I$		
$u = 0.118034 - 1.322880I$		
$a = 0.041356 + 0.463500I$	-4.93480	-2.00000
$b = 1.11803 - 1.32288I$		
$u = -2.11803 + 1.32288I$		
$a = 0.549553 + 0.343238I$	-4.93480	-2.00000
$b = -1.11803 + 1.32288I$		
$u = -2.11803 - 1.32288I$		
$a = 0.549553 - 0.343238I$	-4.93480	-2.00000
$b = -1.11803 - 1.32288I$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^2)(u^2 + 3u + 1)^4(u^{12} - 4u^{11} + \dots - 13u + 1)$ $\cdot (u^{18} + 9u^{17} + \dots - 656u + 256)$
$c_2$	$((u - 1)^2)(u^2 - u - 1)^4(u^{12} + 4u^{11} + \dots - u + 1)$ $\cdot (u^{18} - 3u^{17} + \dots + 52u - 16)$
$c_3$	$u^2(u^2 + u - 1)^4$ $\cdot (u^{12} + 6u^{10} + 3u^9 + 13u^8 + 7u^7 + 15u^6 + 6u^5 + 2u^3 - 2u^2 - 3u + 1)$ $\cdot (u^{18} - 5u^{17} + \dots + 80u + 64)$
$c_4$	$((u + 1)^2)(u^2 - u - 1)^4(u^{12} - 4u^{11} + \dots + u + 1)$ $\cdot (u^{18} - 3u^{17} + \dots + 52u - 16)$
$c_5$	$(u^2 + 3u + 1)(u^4 - u^3 + 5u^2 + 2u + 4)(u^4 + 4u^3 + 5u^2 - 8u - 11)$ $\cdot (u^{12} - 3u^{11} + 2u^{10} + 2u^9 - 6u^8 + 7u^7 - 2u^6 - u^5 + 3u^4 - 3u^3 - 1)$ $\cdot (u^{18} + 5u^{16} + \dots - 5u - 1)$
$c_6$	$(u^2 + 3u + 1)(u^4 - u^3 + 5u^2 + 2u + 4)(u^4 + 4u^3 + 5u^2 - 8u - 11)$ $\cdot (u^{12} + 3u^{11} + 2u^{10} - 2u^9 - 6u^8 - 7u^7 - 2u^6 + u^5 + 3u^4 + 3u^3 - 1)$ $\cdot (u^{18} + 5u^{16} + \dots - 5u - 1)$
$c_7$	$(u^2 - u - 1)(u^4 - 4u^3 + 7u^2 - 6u + 11)(u^4 + u^3 + 7u^2 - 6u - 4)$ $\cdot (u^{12} - 3u^9 - 3u^8 - u^7 + 2u^6 + 7u^5 + 6u^4 + 2u^3 - 2u^2 - 3u - 1)$ $\cdot (u^{18} + u^{17} + \dots + 4u + 1)$
$c_8$	$u^2(u^2 + u - 1)^4$ $\cdot (u^{12} + 6u^{10} - 3u^9 + 13u^8 - 7u^7 + 15u^6 - 6u^5 - 2u^3 - 2u^2 + 3u + 1)$ $\cdot (u^{18} - 5u^{17} + \dots + 80u + 64)$
$c_9$	$(u^2 - 3u + 1)(u^4 - u^3 + 5u^2 + 2u + 4)(u^4 + 4u^3 + 5u^2 - 8u - 11)$ $\cdot (u^{12} - 3u^{11} + 2u^{10} + 2u^9 - 6u^8 + 7u^7 - 2u^6 - u^5 + 3u^4 - 3u^3 - 1)$ $\cdot (u^{18} + 5u^{16} + \dots - 5u - 1)$
$c_{10}$	$(u^2 + u - 1)(u^4 - 4u^3 + 7u^2 - 6u + 11)(u^4 + u^3 + 7u^2 - 6u - 4)$ $\cdot (u^{12} - 3u^9 - 3u^8 - u^7 + 2u^6 + 7u^5 + 6u^4 + 2u^3 - 2u^2 - 3u - 1)$ $\cdot (u^{18} + u^{17} + \dots + 4u + 1)$
$c_{11}$	$(u^2 + u - 1)(u^4 - 4u^3 + 7u^2 - 6u + 11)(u^4 + u^3 + 7u^2 - 6u - 4)$ $\cdot (u^{12} + 3u^9 - 3u^8 + u^7 + 2u^6 - 7u^5 + 6u^4 - 2u^3 - 2u^2 + 3u - 1)$ $\cdot (u^{18} + u^{17} + \dots + 4u + 1)$
$c_{12}$	$((u^2 - u - 1)^4)(u^2 + u - 1)(u^{12} - 12u^{11} + \dots - 12u + 9)$ $\cdot (u^{18} + 12u^{17} + \dots + 6u - 4)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^2)(y^2 - 7y + 1)^4(y^{12} + 12y^{11} + \dots - 81y + 1)$ $\cdot (y^{18} + 3y^{17} + \dots + 495872y + 65536)$
$c_2, c_4$	$((y - 1)^2)(y^2 - 3y + 1)^4(y^{12} - 4y^{11} + \dots - 13y + 1)$ $\cdot (y^{18} - 9y^{17} + \dots + 656y + 256)$
$c_3, c_8$	$y^2(y^2 - 3y + 1)^4(y^{12} + 12y^{11} + \dots - 13y + 1)$ $\cdot (y^{18} + 9y^{17} + \dots - 29440y + 4096)$
$c_5, c_6, c_9$	$(y^2 - 7y + 1)(y^4 - 6y^3 + 67y^2 - 174y + 121)$ $\cdot (y^4 + 9y^3 + 37y^2 + 36y + 16)$ $\cdot (y^{12} - 5y^{11} + 4y^{10} + 10y^9 - 27y^7 - 8y^6 + 25y^5 + 15y^4 - 5y^3 - 6y^2 + 1)$ $\cdot (y^{18} + 10y^{17} + \dots - 45y + 1)$
$c_7, c_{10}, c_{11}$	$(y^2 - 3y + 1)(y^4 - 2y^3 + 23y^2 + 118y + 121)$ $\cdot (y^4 + 13y^3 + 53y^2 - 92y + 16)$ $\cdot (y^{12} - 6y^{10} - 5y^9 + 15y^8 + 25y^7 - 8y^6 - 27y^5 + 10y^3 + 4y^2 - 5y + 1)$ $\cdot (y^{18} + 31y^{17} + \dots + 6y + 1)$
$c_{12}$	$((y^2 - 3y + 1)^5)(y^{12} - 24y^{11} + \dots - 234y + 81)$ $\cdot (y^{18} - 50y^{17} + \dots - 2700y + 16)$