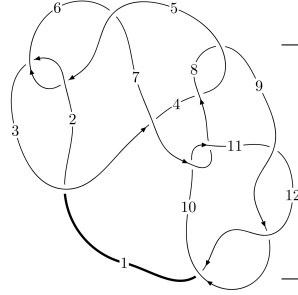
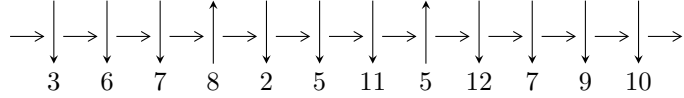


12n<sub>0290</sub> (K12n<sub>0290</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,8 \xrightarrow{c_8} 9,11 \xrightarrow{c_{11}} 12 \xrightarrow{c_4} 4 \xrightarrow{c_7} 7 \xrightarrow{c_3} 3 \xrightarrow{c_6} 6 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_{10}} 10 \rightsquigarrow c_5, c_9, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.68465 \times 10^{94} u^{40} - 9.84743 \times 10^{94} u^{39} + \dots + 1.38333 \times 10^{95} b - 5.11987 \times 10^{96}, \\ -4.36327 \times 10^{94} u^{40} - 1.61063 \times 10^{95} u^{39} + \dots + 2.76666 \times 10^{95} a - 8.27022 \times 10^{96}, \\ u^{41} + 4u^{40} + \dots + 544u + 64 \rangle$$

$$I_2^u = \langle b, a - 1, u + 1 \rangle$$

$$I_1^v = \langle a, 26v^5 + 33v^4 + 317v^3 + 123v^2 + 413b + 89v + 685, v^6 + 3v^5 + 15v^4 + 24v^3 + 11v^2 + 6v + 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 48 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -2.68 \times 10^{94} u^{40} - 9.85 \times 10^{94} u^{39} + \dots + 1.38 \times 10^{95} b - 5.12 \times 10^{96}, -4.36 \times 10^{94} u^{40} - 1.61 \times 10^{95} u^{39} + \dots + 2.77 \times 10^{95} a - 8.27 \times 10^{96}, u^{41} + 4u^{40} + \dots + 544u + 64 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.157709u^{40} + 0.582157u^{39} + \dots + 171.531u + 29.8924 \\ 0.194072u^{40} + 0.711864u^{39} + \dots + 205.306u + 37.0112 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.0560706u^{40} - 0.198690u^{39} + \dots - 50.1633u - 10.2342 \\ 0.220015u^{40} + 0.806259u^{39} + \dots + 232.028u + 41.7645 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0860026u^{40} - 0.314486u^{39} + \dots - 88.7056u - 16.8751 \\ 0.244795u^{40} + 0.889941u^{39} + \dots + 248.405u + 43.2805 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.0998198u^{40} - 0.360991u^{39} + \dots - 89.6766u - 14.8006 \\ 0.137856u^{40} + 0.501525u^{39} + \dots + 141.893u + 24.7433 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0860026u^{40} - 0.314486u^{39} + \dots - 88.7056u - 16.8751 \\ 0.253986u^{40} + 0.923580u^{39} + \dots + 258.962u + 45.1700 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.214458u^{40} - 0.770687u^{39} + \dots - 201.880u - 34.5510 \\ 0.344343u^{40} + 1.25111u^{39} + \dots + 349.391u + 60.8829 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.158792u^{40} - 0.575454u^{39} + \dots - 159.700u - 26.4054 \\ 0.269010u^{40} + 0.976627u^{39} + \dots + 270.728u + 47.1022 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.357088u^{40} + 1.31046u^{39} + \dots + 376.594u + 66.5801 \\ -0.262269u^{40} - 0.954859u^{39} + \dots - 266.063u - 46.3657 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-2.16290u^{40} - 7.86224u^{39} + \dots - 2195.29u - 401.897$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_6$	$u^{41} + 10u^{40} + \dots + 124u + 1$
$c_2, c_5$	$u^{41} + 4u^{40} + \dots - 8u + 1$
$c_3$	$u^{41} - 2u^{40} + \dots - 56802u + 4129$
$c_4, c_8$	$u^{41} + 4u^{40} + \dots + 544u + 64$
$c_7, c_{10}$	$u^{41} + 4u^{40} + \dots - 2u + 2$
$c_9, c_{11}, c_{12}$	$u^{41} - 5u^{40} + \dots - 11u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$y^{41} + 46y^{40} + \dots + 12420y - 1$
$c_2, c_5$	$y^{41} - 10y^{40} + \dots + 124y - 1$
$c_3$	$y^{41} + 106y^{40} + \dots + 3427830276y - 17048641$
$c_4, c_8$	$y^{41} - 36y^{40} + \dots + 46080y - 4096$
$c_7, c_{10}$	$y^{41} + 42y^{39} + \dots + 24y - 4$
$c_9, c_{11}, c_{12}$	$y^{41} - 29y^{40} + \dots + 141y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.900371 + 0.275130I$		
$a = -0.07966 - 1.47335I$	$-1.03538 + 3.10516I$	$-9.19728 - 4.58914I$
$b = 0.570501 + 0.849499I$		
$u = 0.900371 - 0.275130I$		
$a = -0.07966 + 1.47335I$	$-1.03538 - 3.10516I$	$-9.19728 + 4.58914I$
$b = 0.570501 - 0.849499I$		
$u = -0.863117 + 0.163519I$		
$a = 0.530392 - 1.038990I$	$-0.434343 - 0.606208I$	$-8.36824 + 3.20718I$
$b = 0.906841 + 0.441301I$		
$u = -0.863117 - 0.163519I$		
$a = 0.530392 + 1.038990I$	$-0.434343 + 0.606208I$	$-8.36824 - 3.20718I$
$b = 0.906841 - 0.441301I$		
$u = -1.118190 + 0.134810I$		
$a = 0.285482 + 1.154880I$	$2.14754 - 4.46827I$	$-5.46325 + 6.31020I$
$b = -0.692354 - 0.679657I$		
$u = -1.118190 - 0.134810I$		
$a = 0.285482 - 1.154880I$	$2.14754 + 4.46827I$	$-5.46325 - 6.31020I$
$b = -0.692354 + 0.679657I$		
$u = -0.208887 + 0.817072I$		
$a = 0.191298 - 0.000456I$	$-6.67711 + 2.45351I$	$-15.2931 - 1.4222I$
$b = -1.390780 + 0.124154I$		
$u = -0.208887 - 0.817072I$		
$a = 0.191298 + 0.000456I$	$-6.67711 - 2.45351I$	$-15.2931 + 1.4222I$
$b = -1.390780 - 0.124154I$		
$u = -0.142298 + 0.686085I$		
$a = 0.754137 - 0.156560I$	$-0.95163 + 1.08981I$	$-8.28855 - 6.14268I$
$b = 0.609820 - 0.257002I$		
$u = -0.142298 - 0.686085I$		
$a = 0.754137 + 0.156560I$	$-0.95163 - 1.08981I$	$-8.28855 + 6.14268I$
$b = 0.609820 + 0.257002I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.320790 + 0.205247I$ $a = 0.272392 + 0.830191I$ $b = -0.359803 - 0.924561I$	$3.58935 + 0.36497I$	0
$u = 1.320790 - 0.205247I$ $a = 0.272392 - 0.830191I$ $b = -0.359803 + 0.924561I$	$3.58935 - 0.36497I$	0
$u = -1.47758 + 0.08314I$ $a = -0.028558 + 0.821385I$ $b = 1.27898 - 1.15594I$	$7.32002 + 1.31400I$	0
$u = -1.47758 - 0.08314I$ $a = -0.028558 - 0.821385I$ $b = 1.27898 + 1.15594I$	$7.32002 - 1.31400I$	0
$u = 1.47211 + 0.17758I$ $a = -0.081855 - 0.839711I$ $b = 1.19530 + 1.24551I$	$7.22140 + 5.18811I$	0
$u = 1.47211 - 0.17758I$ $a = -0.081855 + 0.839711I$ $b = 1.19530 - 1.24551I$	$7.22140 - 5.18811I$	0
$u = -0.493631$ $a = 1.54896$ $b = -0.291712$	-1.40989	-5.76550
$u = 0.55563 + 1.40865I$ $a = 0.332513 + 0.052129I$ $b = -0.033282 - 0.910556I$	$4.81513 + 1.29204I$	0
$u = 0.55563 - 1.40865I$ $a = 0.332513 - 0.052129I$ $b = -0.033282 + 0.910556I$	$4.81513 - 1.29204I$	0
$u = 0.279316 + 0.386457I$ $a = -3.05813 - 4.36695I$ $b = -0.098053 + 0.379909I$	$-2.86863 - 0.30349I$	$1.29089 - 11.45256I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.279316 - 0.386457I$ $a = -3.05813 + 4.36695I$ $b = -0.098053 - 0.379909I$	$-2.86863 + 0.30349I$	$1.29089 + 11.45256I$
$u = -0.012640 + 0.387805I$ $a = -8.88584 + 0.60443I$ $b = -0.500213 + 0.034819I$	$1.80837 - 2.87388I$	$-39.8656 + 3.3819I$
$u = -0.012640 - 0.387805I$ $a = -8.88584 - 0.60443I$ $b = -0.500213 - 0.034819I$	$1.80837 + 2.87388I$	$-39.8656 - 3.3819I$
$u = -0.64609 + 1.49909I$ $a = 0.280505 - 0.050822I$ $b = -0.227266 + 0.902339I$	$4.34862 + 5.20839I$	0
$u = -0.64609 - 1.49909I$ $a = 0.280505 + 0.050822I$ $b = -0.227266 - 0.902339I$	$4.34862 - 5.20839I$	0
$u = -0.353952$ $a = 0.190811$ $b = -1.66327$	$-9.84381$	$14.6310$
$u = -1.50019 + 0.69974I$ $a = -0.107163 - 0.866028I$ $b = 0.797327 + 0.867883I$	$-1.34409 - 8.57415I$	0
$u = -1.50019 - 0.69974I$ $a = -0.107163 + 0.866028I$ $b = 0.797327 - 0.867883I$	$-1.34409 + 8.57415I$	0
$u = -0.305001$ $a = 1.67143$ $b = 0.580690$	$-1.10346$	$-8.70760$
$u = -1.63935 + 0.45660I$ $a = -0.069974 + 0.912206I$ $b = -1.19023 - 1.18604I$	$11.66750 - 7.74036I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.63935 - 0.45660I$ $a = -0.069974 - 0.912206I$ $b = -1.19023 + 1.18604I$	$11.66750 + 7.74036I$	0
$u = 1.56194 + 0.67841I$ $a = 0.009027 + 0.726408I$ $b = 0.492906 - 0.964772I$	$1.69219 + 4.01190I$	0
$u = 1.56194 - 0.67841I$ $a = 0.009027 - 0.726408I$ $b = 0.492906 + 0.964772I$	$1.69219 - 4.01190I$	0
$u = 1.67787 + 0.37565I$ $a = -0.035629 - 0.893097I$ $b = -1.10249 + 1.25882I$	$11.97710 + 1.09300I$	0
$u = 1.67787 - 0.37565I$ $a = -0.035629 + 0.893097I$ $b = -1.10249 - 1.25882I$	$11.97710 - 1.09300I$	0
$u = -1.49517 + 0.90641I$ $a = 0.139383 - 0.997291I$ $b = 1.11424 + 1.19188I$	$7.3447 - 13.9917I$	0
$u = -1.49517 - 0.90641I$ $a = 0.139383 + 0.997291I$ $b = 1.11424 - 1.19188I$	$7.3447 + 13.9917I$	0
$u = 1.54232 + 0.88599I$ $a = 0.131039 + 0.948244I$ $b = 1.03138 - 1.24212I$	$8.03425 + 7.41571I$	0
$u = 1.54232 - 0.88599I$ $a = 0.131039 - 0.948244I$ $b = 1.03138 + 1.24212I$	$8.03425 - 7.41571I$	0
$u = -1.63054 + 0.83010I$ $a = -0.034959 - 0.425949I$ $b = 0.284331 + 0.549059I$	$-3.12842 - 0.82148I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.63054 - 0.83010I$		
$a = -0.034959 + 0.425949I$	$-3.12842 + 0.82148I$	0
$b = 0.284331 - 0.549059I$		

$$\text{II. } I_2^u = \langle b, a - 1, u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_9$	$u - 1$
$c_5, c_6, c_8$ $c_{11}, c_{12}$	$u + 1$
$c_7, c_{10}$	$u$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_6$ $c_8, c_9, c_{11}$ $c_{12}$	$y - 1$
$c_7, c_{10}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 1.00000$	-3.28987	-12.0000
$b = 0$		

### III.

$$I_1^v = \langle a, 26v^5 + 33v^4 + \dots + 413b + 685, v^6 + 3v^5 + 15v^4 + 24v^3 + 11v^2 + 6v + 1 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -0.0629540v^5 - 0.0799031v^4 + \dots - 0.215496v - 1.65860 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0629540v^5 + 0.0799031v^4 + \dots + 0.215496v + 1.65860 \\ -0.0629540v^5 - 0.0799031v^4 + \dots - 0.215496v - 1.65860 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ -0.0629540v^5 - 0.0799031v^4 + \dots - 0.215496v - 2.65860 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.108959v^5 - 0.176755v^4 + \dots + 3.28087v - 0.0629540 \\ 0.326877v^5 + 0.530266v^4 + \dots - 5.84262v + 0.188862 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.150121v^5 - 0.421308v^4 + \dots - 0.590799v + 0.891041 \\ -0.0629540v^5 - 0.0799031v^4 + \dots - 0.215496v - 2.65860 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.600484v^5 - 1.68523v^4 + \dots - 2.36320v - 1.43584 \\ 1.26392v^5 + 3.45036v^4 + \dots + 4.94189v + 3.53027 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0.0629540v^5 + 0.0799031v^4 + \dots + 0.215496v + 2.65860 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.0629540v^5 - 0.0799031v^4 + \dots - 0.215496v - 1.65860 \\ 0.0629540v^5 + 0.0799031v^4 + \dots + 0.215496v + 2.65860 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes** =  $-\frac{3042}{413}v^5 - \frac{8817}{413}v^4 - \frac{44523}{413}v^3 - \frac{68494}{413}v^2 - \frac{24042}{413}v - \frac{18195}{413}$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u^3 - u^2 + 2u - 1)^2$
$c_2$	$(u^3 + u^2 - 1)^2$
$c_4, c_8$	$u^6$
$c_5$	$(u^3 - u^2 + 1)^2$
$c_6$	$(u^3 + u^2 + 2u + 1)^2$
$c_7, c_9$	$(u^2 + u - 1)^3$
$c_{10}, c_{11}, c_{12}$	$(u^2 - u - 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_6$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_2, c_5$	$(y^3 - y^2 + 2y - 1)^2$
$c_4, c_8$	$y^6$
$c_7, c_9, c_{10}$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^3$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.49186$ $a = 0$ $b = 0.618034$	$-2.10041$	$-19.6940$
$v = -0.082153 + 0.499284I$ $a = 0$ $b = -1.61803$	$-5.85852 + 2.82812I$	$-6.54788 - 4.14885I$
$v = -0.082153 - 0.499284I$ $a = 0$ $b = -1.61803$	$-5.85852 - 2.82812I$	$-6.54788 + 4.14885I$
$v = -0.217660$ $a = 0$ $b = -1.61803$	$-9.99610$	$-38.1750$
$v = -0.56309 + 3.42214I$ $a = 0$ $b = 0.618034$	$2.03717 + 2.82812I$	$0.982489 + 0.847836I$
$v = -0.56309 - 3.42214I$ $a = 0$ $b = 0.618034$	$2.03717 - 2.82812I$	$0.982489 - 0.847836I$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u-1)(u^3-u^2+2u-1)^2(u^{41}+10u^{40}+\dots+124u+1)$
$c_2$	$(u-1)(u^3+u^2-1)^2(u^{41}+4u^{40}+\dots-8u+1)$
$c_3$	$(u-1)(u^3-u^2+2u-1)^2(u^{41}-2u^{40}+\dots-56802u+4129)$
$c_4$	$u^6(u-1)(u^{41}+4u^{40}+\dots+544u+64)$
$c_5$	$(u+1)(u^3-u^2+1)^2(u^{41}+4u^{40}+\dots-8u+1)$
$c_6$	$(u+1)(u^3+u^2+2u+1)^2(u^{41}+10u^{40}+\dots+124u+1)$
$c_7$	$u(u^2+u-1)^3(u^{41}+4u^{40}+\dots-2u+2)$
$c_8$	$u^6(u+1)(u^{41}+4u^{40}+\dots+544u+64)$
$c_9$	$(u-1)(u^2+u-1)^3(u^{41}-5u^{40}+\dots-11u-1)$
$c_{10}$	$u(u^2-u-1)^3(u^{41}+4u^{40}+\dots-2u+2)$
$c_{11}, c_{12}$	$(u+1)(u^2-u-1)^3(u^{41}-5u^{40}+\dots-11u-1)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_6$	$(y - 1)(y^3 + 3y^2 + 2y - 1)^2(y^{41} + 46y^{40} + \dots + 12420y - 1)$
$c_2, c_5$	$(y - 1)(y^3 - y^2 + 2y - 1)^2(y^{41} - 10y^{40} + \dots + 124y - 1)$
$c_3$	$(y - 1)(y^3 + 3y^2 + 2y - 1)^2$ $\cdot (y^{41} + 106y^{40} + \dots + 3427830276y - 17048641)$
$c_4, c_8$	$y^6(y - 1)(y^{41} - 36y^{40} + \dots + 46080y - 4096)$
$c_7, c_{10}$	$y(y^2 - 3y + 1)^3(y^{41} + 42y^{39} + \dots + 24y - 4)$
$c_9, c_{11}, c_{12}$	$(y - 1)(y^2 - 3y + 1)^3(y^{41} - 29y^{40} + \dots + 141y - 1)$