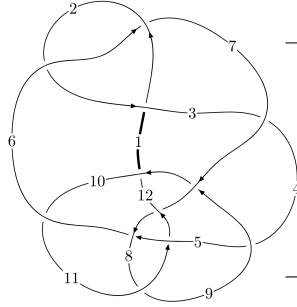
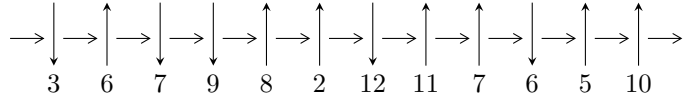


12n<sub>0314</sub> (K12n<sub>0314</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,7 \xrightarrow{c_6} 6 \xrightarrow{c_2} 3 \xrightarrow{c_3} 4,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_1} 1 \xrightarrow{c_9} 9 \xrightarrow{c_4} 5 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \twoheadrightarrow c_5, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 26419u^{19} + 221467u^{18} + \dots + 81793b + 229898,$$

$$655714u^{19} + 5585712u^{18} + \dots + 1717653a + 17248644, u^{20} + 9u^{19} + \dots + 105u + 21 \rangle$$

$$I_2^u = \langle u^{14} - 5u^{13} + \dots + 13b - 16, 3u^{14} - 2u^{13} + \dots + 13a + 56, u^{15} + 4u^{14} + \dots - 4u - 1 \rangle$$

$$I_3^u = \langle 179u^6a^3 + 84u^6a^2 + \dots + 240a - 68, 2u^6a^3 + 5u^6a^2 + \dots - a + 5, u^7 - 2u^6 + 2u^5 + u^2 - 2u + 1 \rangle$$

$$I_4^u = \langle b + u, a^2 - au + 2a + 1, u^2 - u + 1 \rangle$$

$$I_5^u = \langle b - u + 1, a^2 - au - a + u - 1, u^2 - u + 1 \rangle$$

$$I_1^v = \langle a, b^2 + b + 1, v + 1 \rangle$$

\* 6 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 73 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 26419u^{19} + 221467u^{18} + \cdots + 81793b + 229898, 6.56 \times 10^5 u^{19} + 5.59 \times 10^6 u^{18} + \cdots + 1.72 \times 10^6 a + 1.72 \times 10^7, u^{20} + 9u^{19} + \cdots + 105u + 21 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.381750u^{19} - 3.25194u^{18} + \cdots - 46.7992u - 10.0420 \\ -0.322998u^{19} - 2.70765u^{18} + \cdots - 17.1281u - 2.81073 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0499612u^{19} - 0.781440u^{18} + \cdots - 40.9540u - 11.0912 \\ 0.183805u^{19} + 1.66304u^{18} + \cdots + 30.0418u + 8.01675 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0587517u^{19} - 0.544292u^{18} + \cdots - 29.6712u - 7.23125 \\ -0.322998u^{19} - 2.70765u^{18} + \cdots - 17.1281u - 2.81073 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.0265624u^{19} - 0.108474u^{18} + \cdots - 14.3377u - 5.90838 \\ 0.320040u^{19} + 2.54825u^{18} + \cdots + 6.84217u + 0.951341 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.737673u^{19} + 5.54575u^{18} + \cdots + 12.8313u + 2.55517 \\ -0.998753u^{19} - 6.14769u^{18} + \cdots + 5.47587u + 3.09776 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.274738u^{19} + 2.46057u^{18} + \cdots + 14.2381u + 2.03681 \\ -0.436358u^{19} - 2.67451u^{18} + \cdots + 2.33972u + 1.20475 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\mathbf{(iii) } \text{Cusp Shapes} = \frac{34565}{81793}u^{19} + \frac{528526}{81793}u^{18} + \cdots + \frac{18069450}{81793}u + \frac{4396806}{81793}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{20} + 5u^{19} + \dots + 2751u + 441$
$c_2, c_6$	$u^{20} - 9u^{19} + \dots - 105u + 21$
$c_3$	$u^{20} + 9u^{19} + \dots - 123711u + 33789$
$c_4, c_{10}$	$u^{20} + u^{19} + \dots + 3u + 1$
$c_5, c_{11}$	$u^{20} + 2u^{19} + \dots + u + 1$
$c_7$	$u^{20} + 16u^{19} + \dots + 160u + 32$
$c_8$	$u^{20} + 22u^{19} + \dots + 273u + 21$
$c_9, c_{12}$	$u^{20} - u^{19} + \dots - 21u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{20} + 53y^{19} + \dots + 2156931y + 194481$
$c_2, c_6$	$y^{20} + 5y^{19} + \dots + 2751y + 441$
$c_3$	$y^{20} + 107y^{19} + \dots + 4904181177y + 1141696521$
$c_4, c_{10}$	$y^{20} + 31y^{19} + \dots - 9y + 1$
$c_5, c_{11}$	$y^{20} - 6y^{19} + \dots + y + 1$
$c_7$	$y^{20} + 42y^{18} + \dots + 15872y + 1024$
$c_8$	$y^{20} - 16y^{19} + \dots - 3423y + 441$
$c_9, c_{12}$	$y^{20} - 49y^{19} + \dots - 81y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.211126 + 0.952456I$ $a = 0.747076 - 0.491514I$ $b = 0.116391 + 0.783403I$	$-3.11229 - 1.03633I$	$-6.44153 + 1.75193I$
$u = 0.211126 - 0.952456I$ $a = 0.747076 + 0.491514I$ $b = 0.116391 - 0.783403I$	$-3.11229 + 1.03633I$	$-6.44153 - 1.75193I$
$u = 0.519530 + 0.750364I$ $a = 0.898033 + 0.618882I$ $b = -0.484563 + 1.044830I$	$0.63548 - 1.96108I$	$4.25150 + 5.47708I$
$u = 0.519530 - 0.750364I$ $a = 0.898033 - 0.618882I$ $b = -0.484563 - 1.044830I$	$0.63548 + 1.96108I$	$4.25150 - 5.47708I$
$u = -0.523090 + 0.979837I$ $a = 0.414457 - 0.445713I$ $b = -0.1256290 - 0.0436326I$	$0.13882 - 2.55024I$	$1.45356 - 0.37856I$
$u = -0.523090 - 0.979837I$ $a = 0.414457 + 0.445713I$ $b = -0.1256290 + 0.0436326I$	$0.13882 + 2.55024I$	$1.45356 + 0.37856I$
$u = -0.577826 + 0.618275I$ $a = 0.017905 + 0.660573I$ $b = -0.253132 + 0.138016I$	$1.22469 - 1.87328I$	$5.09006 + 3.79292I$
$u = -0.577826 - 0.618275I$ $a = 0.017905 - 0.660573I$ $b = -0.253132 - 0.138016I$	$1.22469 + 1.87328I$	$5.09006 - 3.79292I$
$u = 0.713575 + 1.077000I$ $a = -0.756489 - 0.141468I$ $b = 0.306890 - 1.351890I$	$-0.16430 + 7.31617I$	$2.67024 - 6.35722I$
$u = 0.713575 - 1.077000I$ $a = -0.756489 + 0.141468I$ $b = 0.306890 + 1.351890I$	$-0.16430 - 7.31617I$	$2.67024 + 6.35722I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.351235 + 0.606197I$ $a = 0.973122 - 0.073477I$ $b = -0.040017 + 0.338792I$	$0.08352 - 1.47554I$	$0.46232 + 5.22837I$
$u = -0.351235 - 0.606197I$ $a = 0.973122 + 0.073477I$ $b = -0.040017 - 0.338792I$	$0.08352 + 1.47554I$	$0.46232 - 5.22837I$
$u = -1.06324 + 1.11292I$ $a = 1.23198 + 0.99332I$ $b = 2.62262 - 0.87571I$	$15.6693 - 14.8627I$	$4.85498 + 6.94268I$
$u = -1.06324 - 1.11292I$ $a = 1.23198 - 0.99332I$ $b = 2.62262 + 0.87571I$	$15.6693 + 14.8627I$	$4.85498 - 6.94268I$
$u = -1.14401 + 1.05029I$ $a = 0.913221 + 1.067070I$ $b = 2.78508 + 0.08218I$	$15.9439 + 6.7947I$	$5.34960 - 3.11489I$
$u = -1.14401 - 1.05029I$ $a = 0.913221 - 1.067070I$ $b = 2.78508 - 0.08218I$	$15.9439 - 6.7947I$	$5.34960 + 3.11489I$
$u = -1.22782 + 0.99971I$ $a = -0.933207 - 0.875787I$ $b = -2.92684 - 0.10703I$	$14.3487 - 2.4918I$	$8.82559 - 1.44733I$
$u = -1.22782 - 0.99971I$ $a = -0.933207 + 0.875787I$ $b = -2.92684 + 0.10703I$	$14.3487 + 2.4918I$	$8.82559 + 1.44733I$
$u = -1.05700 + 1.19896I$ $a = -1.00610 - 1.04385I$ $b = -2.50080 + 0.96199I$	$13.6274 - 5.8207I$	$6.48369 + 6.53505I$
$u = -1.05700 - 1.19896I$ $a = -1.00610 + 1.04385I$ $b = -2.50080 - 0.96199I$	$13.6274 + 5.8207I$	$6.48369 - 6.53505I$

$$\langle u^{14} - 5u^{13} + \dots + 13b - 16, 3u^{14} - 2u^{13} + \dots + 13a + 56, u^{15} + 4u^{14} + \dots - 4u - 1 \rangle$$

II.  $I_2^u =$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.230769u^{14} + 0.153846u^{13} + \dots - 10.3077u - 4.30769 \\ -0.0769231u^{14} + 0.384615u^{13} + \dots + 0.230769u + 1.23077 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.153846u^{14} + 0.230769u^{13} + \dots - 6.46154u - 4.46154 \\ 1.07692u^{14} + 4.61538u^{13} + \dots - 5.23077u - 0.230769 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.153846u^{14} - 0.230769u^{13} + \dots - 10.5385u - 5.53846 \\ -0.0769231u^{14} + 0.384615u^{13} + \dots + 0.230769u + 1.23077 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2.23077u^{14} + 7.84615u^{13} + \dots - 8.69231u + 0.307692 \\ -0.384615u^{14} - 2.07692u^{13} + \dots + 6.15385u + 1.15385 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -3.15385u^{14} - 11.2308u^{13} + \dots + 13.4615u + 3.46154 \\ -0.0769231u^{14} + 0.384615u^{13} + \dots - 1.76923u - 0.769231 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.769231u^{14} + 2.15385u^{13} + \dots + 0.692308u + 1.69231 \\ -0.0769231u^{14} - 0.615385u^{13} + \dots + 3.23077u + 0.230769 \end{pmatrix}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -\frac{4}{13}u^{14} + \frac{20}{13}u^{13} + \frac{49}{13}u^{12} + \frac{207}{13}u^{11} + \frac{331}{13}u^{10} + \frac{590}{13}u^9 + \frac{503}{13}u^8 + \frac{567}{13}u^7 + \frac{150}{13}u^6 + \frac{2}{13}u^5 - 24u^4 - \frac{489}{13}u^3 - \frac{307}{13}u^2 - \frac{274}{13}u - \frac{1}{13}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{15} - 6u^{14} + \dots - 6u + 1$
$c_2$	$u^{15} - 4u^{14} + \dots - 4u + 1$
$c_3$	$u^{15} + 4u^{14} + \dots - 6u + 1$
$c_4, c_{10}$	$u^{15} + 8u^{13} + \dots + 4u - 1$
$c_5, c_{11}$	$u^{15} + u^{14} + \dots + 2u + 1$
$c_6$	$u^{15} + 4u^{14} + \dots - 4u - 1$
$c_7$	$u^{15} + 6u^{14} + \dots + 5u + 1$
$c_8$	$u^{15} + 11u^{14} + \dots + 1118u + 169$
$c_9, c_{12}$	$u^{15} - 8u^{14} + \dots + 2u - 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{15} + 6y^{14} + \dots + 2y - 1$
$c_2, c_6$	$y^{15} + 6y^{14} + \dots - 6y - 1$
$c_3$	$y^{15} + 12y^{14} + \dots - 224y^2 - 1$
$c_4, c_{10}$	$y^{15} + 16y^{14} + \dots - 6y - 1$
$c_5, c_{11}$	$y^{15} - 5y^{14} + \dots + 8y - 1$
$c_7$	$y^{15} - 2y^{13} + \dots + 7y - 1$
$c_8$	$y^{15} - 11y^{14} + \dots + 118300y - 28561$
$c_9, c_{12}$	$y^{15} - 16y^{14} + \dots - 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.119628 + 0.929628I$ $a = 1.085450 + 0.734281I$ $b = -0.896569 + 0.439913I$	$1.32926 - 1.15840I$	$10.02147 + 1.35486I$
$u = 0.119628 - 0.929628I$ $a = 1.085450 - 0.734281I$ $b = -0.896569 - 0.439913I$	$1.32926 + 1.15840I$	$10.02147 - 1.35486I$
$u = 0.927045$ $a = -1.23357$ $b = -1.65358$	$4.01270$	$10.3920$
$u = 0.396806 + 1.009340I$ $a = -0.100376 + 0.697396I$ $b = -0.762363 - 0.345807I$	$0.57283 + 3.31790I$	$5.20563 - 6.98486I$
$u = 0.396806 - 1.009340I$ $a = -0.100376 - 0.697396I$ $b = -0.762363 + 0.345807I$	$0.57283 - 3.31790I$	$5.20563 + 6.98486I$
$u = -0.838508 + 0.071078I$ $a = 0.057971 - 0.286484I$ $b = 0.417658 + 1.125080I$	$2.88845 - 5.01567I$	$6.54273 + 3.81231I$
$u = -0.838508 - 0.071078I$ $a = 0.057971 + 0.286484I$ $b = 0.417658 - 1.125080I$	$2.88845 + 5.01567I$	$6.54273 - 3.81231I$
$u = -0.323439 + 1.178010I$ $a = 0.640201 + 0.826390I$ $b = -0.313721 - 0.616088I$	$-1.15408 + 0.99595I$	$2.36087 - 3.16141I$
$u = -0.323439 - 1.178010I$ $a = 0.640201 - 0.826390I$ $b = -0.313721 + 0.616088I$	$-1.15408 - 0.99595I$	$2.36087 + 3.16141I$
$u = -0.493362 + 1.123440I$ $a = -0.974071 - 0.249094I$ $b = 0.251285 + 0.447031I$	$-0.15694 - 9.16119I$	$0.57307 + 9.40240I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.493362 - 1.123440I$ $a = -0.974071 + 0.249094I$ $b = 0.251285 - 0.447031I$	$-0.15694 + 9.16119I$	$0.57307 - 9.40240I$
$u = -0.228765 + 0.477425I$ $a = -1.52624 - 1.56710I$ $b = 0.739527 - 0.375189I$	$2.35397 + 5.43215I$	$3.98759 - 5.23601I$
$u = -0.228765 - 0.477425I$ $a = -1.52624 + 1.56710I$ $b = 0.739527 + 0.375189I$	$2.35397 - 5.43215I$	$3.98759 + 5.23601I$
$u = -1.09588 + 1.06775I$ $a = -1.06614 - 0.98430I$ $b = -2.60903 + 0.37822I$	$13.54430 - 3.99769I$	$5.11287 + 2.07343I$
$u = -1.09588 - 1.06775I$ $a = -1.06614 + 0.98430I$ $b = -2.60903 - 0.37822I$	$13.54430 + 3.99769I$	$5.11287 - 2.07343I$

$$\text{III. } I_3^u = \langle 179u^6a^3 + 84u^6a^2 + \dots + 240a - 68, 2u^6a^3 + 5u^6a^2 + \dots - a + 5, u^7 - 2u^6 + 2u^5 + u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -0.650909a^3u^6 - 0.305455a^2u^6 + \dots - 0.872727a + 0.247273 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.650909a^3u^6 + 0.305455a^2u^6 + \dots + 1.87273a - 0.247273 \\ -0.738182a^3u^6 - 0.229091a^2u^6 + \dots - 0.654545a + 0.185455 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.650909a^3u^6 + 0.305455a^2u^6 + \dots + 1.87273a - 0.247273 \\ -0.650909a^3u^6 - 0.305455a^2u^6 + \dots - 0.872727a + 0.247273 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^5 - u^4 - a^2u + u^2 + u + 1 \\ 0.0581818a^3u^6 - 1.05091a^2u^6 + \dots + 1.85455a - 0.625455 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.0581818a^3u^6 + 0.949091a^2u^6 + \dots - 0.145455a + 1.37455 \\ 0.0436364a^3u^6 - 0.538182a^2u^6 + \dots + 1.89091a - 0.469091 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0145455a^3u^6 - 0.512727a^2u^6 + \dots - 0.0363636a - 1.15636 \\ -0.0436364a^3u^6 + 0.538182a^2u^6 + \dots - 1.89091a - 0.530909 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{48}{275}u^6a^3 - \frac{592}{275}u^6a^2 + \dots + \frac{416}{55}a + \frac{4709}{275}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u^7 + 4u^5 - 4u^3 - u^2 + 2u - 1)^4$
$c_2, c_6$	$(u^7 + 2u^6 + 2u^5 - u^2 - 2u - 1)^4$
$c_3$	$(u^7 - 2u^6 + 10u^5 + 8u^4 - 18u^3 - 39u^2 - 22u - 5)^4$
$c_4, c_{10}$	$u^{28} + 23u^{26} + \dots + 1459u + 4993$
$c_5, c_{11}$	$u^{28} - 3u^{26} + \dots - 21u + 13$
$c_7$	$(u^2 - u + 1)^{14}$
$c_8$	$(u^7 - 3u^6 + 2u^5 + 5u^4 - 9u^3 + u^2 + 6u - 4)^4$
$c_9, c_{12}$	$u^{28} - 5u^{27} + \dots + 21416u + 10543$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^7 + 8y^6 + 8y^5 - 28y^4 + 32y^3 - 17y^2 + 2y - 1)^4$
$c_2, c_6$	$(y^7 + 4y^5 - 4y^3 - y^2 + 2y - 1)^4$
$c_3$	$(y^7 + 16y^6 + 96y^5 - 624y^4 + 488y^3 - 649y^2 + 94y - 25)^4$
$c_4, c_{10}$	$y^{28} + 46y^{27} + \cdots + 280734755y + 24930049$
$c_5, c_{11}$	$y^{28} - 6y^{27} + \cdots - 3561y + 169$
$c_7$	$(y^2 + y + 1)^{14}$
$c_8$	$(y^7 - 5y^6 + 16y^5 - 43y^4 + 71y^3 - 69y^2 + 44y - 16)^4$
$c_9, c_{12}$	$y^{28} - 53y^{27} + \cdots + 543656868y + 111154849$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.234558 + 0.938347I$ $a = 0.557581 + 0.629769I$ $b = -0.005594 + 0.375241I$	$0.141984 - 1.068600I$	$1.62838 + 2.98348I$
$u = -0.234558 + 0.938347I$ $a = 1.48963 + 0.01254I$ $b = -0.834015 - 0.189579I$	$0.141984 - 1.068600I$	$1.62838 + 2.98348I$
$u = -0.234558 + 0.938347I$ $a = 0.289555 + 0.078561I$ $b = 1.047710 - 0.498808I$	$0.14198 - 5.12837I$	$1.62838 + 9.91169I$
$u = -0.234558 + 0.938347I$ $a = -0.75691 - 2.17265I$ $b = -0.467113 + 1.133100I$	$0.14198 - 5.12837I$	$1.62838 + 9.91169I$
$u = -0.234558 - 0.938347I$ $a = 0.557581 - 0.629769I$ $b = -0.005594 - 0.375241I$	$0.141984 + 1.068600I$	$1.62838 - 2.98348I$
$u = -0.234558 - 0.938347I$ $a = 1.48963 - 0.01254I$ $b = -0.834015 + 0.189579I$	$0.141984 + 1.068600I$	$1.62838 - 2.98348I$
$u = -0.234558 - 0.938347I$ $a = 0.289555 - 0.078561I$ $b = 1.047710 + 0.498808I$	$0.14198 + 5.12837I$	$1.62838 - 9.91169I$
$u = -0.234558 - 0.938347I$ $a = -0.75691 + 2.17265I$ $b = -0.467113 - 1.133100I$	$0.14198 + 5.12837I$	$1.62838 - 9.91169I$
$u = -0.954563$ $a = -0.978481 + 0.427663I$ $b = -1.94430 + 1.59422I$	$4.10408 - 2.02988I$	$10.25058 + 3.46410I$
$u = -0.954563$ $a = -0.978481 - 0.427663I$ $b = -1.94430 - 1.59422I$	$4.10408 + 2.02988I$	$10.25058 - 3.46410I$

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.954563$ $a = 1.031960 + 0.520296I$ $b = 0.869450 - 0.267482I$	$4.10408 + 2.02988I$	$10.25058 - 3.46410I$
$u = -0.954563$ $a = 1.031960 - 0.520296I$ $b = 0.869450 + 0.267482I$	$4.10408 - 2.02988I$	$10.25058 + 3.46410I$
$u = 0.656474 + 0.273636I$ $a = -0.931267 + 0.317916I$ $b = -0.97436 - 1.34239I$	$3.33504 + 2.23752I$	$9.53857 - 3.70520I$
$u = 0.656474 + 0.273636I$ $a = 1.244040 - 0.363481I$ $b = 1.83972 - 1.54468I$	$3.33504 + 6.29728I$	$9.5386 - 10.6334I$
$u = 0.656474 + 0.273636I$ $a = -1.95049 - 0.33453I$ $b = -1.232480 + 0.014553I$	$3.33504 + 2.23752I$	$9.53857 - 3.70520I$
$u = 0.656474 + 0.273636I$ $a = 0.21122 - 2.12389I$ $b = 0.413640 + 0.297426I$	$3.33504 + 6.29728I$	$9.5386 - 10.6334I$
$u = 0.656474 - 0.273636I$ $a = -0.931267 - 0.317916I$ $b = -0.97436 + 1.34239I$	$3.33504 - 2.23752I$	$9.53857 + 3.70520I$
$u = 0.656474 - 0.273636I$ $a = 1.244040 + 0.363481I$ $b = 1.83972 + 1.54468I$	$3.33504 - 6.29728I$	$9.5386 + 10.6334I$
$u = 0.656474 - 0.273636I$ $a = -1.95049 + 0.33453I$ $b = -1.232480 - 0.014553I$	$3.33504 - 2.23752I$	$9.53857 + 3.70520I$
$u = 0.656474 - 0.273636I$ $a = 0.21122 + 2.12389I$ $b = 0.413640 - 0.297426I$	$3.33504 - 6.29728I$	$9.5386 + 10.6334I$



Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.05537 + 1.04881I$ $a = 0.973714 - 0.891961I$ $b = 2.24383 - 0.01181I$	$14.2101 + 5.9023I$	$7.20776 - 5.84206I$
$u = 1.05537 + 1.04881I$ $a = 1.13442 - 0.89114I$ $b = 2.03850 + 0.56037I$	$14.2101 + 1.8425I$	$7.20776 + 1.08615I$
$u = 1.05537 + 1.04881I$ $a = -0.84886 + 1.29485I$ $b = -2.83247 + 0.38149I$	$14.2101 + 1.8425I$	$7.20776 + 1.08615I$
$u = 1.05537 + 1.04881I$ $a = -1.46612 + 0.93741I$ $b = -2.66251 - 1.14672I$	$14.2101 + 5.9023I$	$7.20776 - 5.84206I$
$u = 1.05537 - 1.04881I$ $a = 0.973714 + 0.891961I$ $b = 2.24383 + 0.01181I$	$14.2101 - 5.9023I$	$7.20776 + 5.84206I$
$u = 1.05537 - 1.04881I$ $a = 1.13442 + 0.89114I$ $b = 2.03850 - 0.56037I$	$14.2101 - 1.8425I$	$7.20776 - 1.08615I$
$u = 1.05537 - 1.04881I$ $a = -0.84886 - 1.29485I$ $b = -2.83247 - 0.38149I$	$14.2101 - 1.8425I$	$7.20776 - 1.08615I$
$u = 1.05537 - 1.04881I$ $a = -1.46612 - 0.93741I$ $b = -2.66251 + 1.14672I$	$14.2101 - 5.9023I$	$7.20776 + 5.84206I$

$$\text{IV. } I_4^u = \langle b + u, a^2 - au + 2a + 1, u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ -u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} au + u \\ -au - u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a + u \\ -u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} au + a + u + 1 \\ -a + u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a + u \\ -u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} au - 1 \\ -u + 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-5u + 5$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$ $c_7, c_9, c_{12}$	$(u^2 - u + 1)^2$
$c_2$	$(u^2 + u + 1)^2$
$c_4, c_5, c_{10}$ $c_{11}$	$u^4 - 2u^3 + 2u^2 - u + 1$
$c_8$	$u^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7, c_9$ $c_{12}$	$(y^2 + y + 1)^2$
$c_4, c_5, c_{10}$ $c_{11}$	$y^4 + 2y^2 + 3y + 1$
$c_8$	$y^4$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$ $a = -0.378256 - 0.440597I$ $b = -0.500000 - 0.866025I$	4.05977I	2.50000 - 4.33013I
$u = 0.500000 + 0.866025I$ $a = -1.12174 + 1.30662I$ $b = -0.500000 - 0.866025I$	4.05977I	2.50000 - 4.33013I
$u = 0.500000 - 0.866025I$ $a = -0.378256 + 0.440597I$ $b = -0.500000 + 0.866025I$	- 4.05977I	2.50000 + 4.33013I
$u = 0.500000 - 0.866025I$ $a = -1.12174 - 1.30662I$ $b = -0.500000 + 0.866025I$	- 4.05977I	2.50000 + 4.33013I

$$\mathbf{V. } I_5^u = \langle b - u + 1, a^2 - au - a + u - 1, u^2 - u + 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u \\ u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ u - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} au - u + 1 \\ -au + 2u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a - u + 1 \\ u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -2au + a \\ au \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a - u + 1 \\ u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -au + a - 1 \\ u \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =  $3u + 1$**

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_6$ $c_7, c_9, c_{12}$	$(u^2 - u + 1)^2$
$c_2$	$(u^2 + u + 1)^2$
$c_4, c_5, c_{10}$ $c_{11}$	$u^4 + u^3 + 2u^2 + 2u + 1$
$c_8$	$u^4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_7, c_9$ $c_{12}$	$(y^2 + y + 1)^2$
$c_4, c_5, c_{10}$ $c_{11}$	$y^4 + 3y^3 + 2y^2 + 1$
$c_8$	$y^4$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.500000 + 0.866025I$ $a = -0.192440 + 0.547877I$ $b = -0.500000 + 0.866025I$	0	$2.50000 + 2.59808I$
$u = 0.500000 + 0.866025I$ $a = 1.69244 + 0.31815I$ $b = -0.500000 + 0.866025I$	0	$2.50000 + 2.59808I$
$u = 0.500000 - 0.866025I$ $a = -0.192440 - 0.547877I$ $b = -0.500000 - 0.866025I$	0	$2.50000 - 2.59808I$
$u = 0.500000 - 0.866025I$ $a = 1.69244 - 0.31815I$ $b = -0.500000 - 0.866025I$	0	$2.50000 - 2.59808I$

$$\text{VI. } I_1^v = \langle a, b^2 + b + 1, v + 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ b \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -b \\ b \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -b \\ b \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -b - 2 \\ b + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -b \\ b \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -1 \\ b + 1 \end{pmatrix}$$

(ii) Obstruction class =  $-1$

(iii) Cusp Shapes =  $4b + 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_8$	$u^2$
$c_4, c_5, c_9$ $c_{10}, c_{11}, c_{12}$	$u^2 - u + 1$
$c_7$	$u^2 + u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_6, c_8$	$y^2$
$c_4, c_5, c_7$ $c_9, c_{10}, c_{11}$ $c_{12}$	$y^2 + y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$ $a = 0$ $b = -0.500000 + 0.866025I$	$-2.02988I$	$0. + 3.46410I$
$v = -1.00000$ $a = 0$ $b = -0.500000 - 0.866025I$	$2.02988I$	$0. - 3.46410I$

## VII. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$u^2(u^2 - u + 1)^4(u^7 + 4u^5 - 4u^3 - u^2 + 2u - 1)^4$ $\cdot (u^{15} - 6u^{14} + \dots - 6u + 1)(u^{20} + 5u^{19} + \dots + 2751u + 441)$
$c_2$	$u^2(u^2 + u + 1)^4(u^7 + 2u^6 + 2u^5 - u^2 - 2u - 1)^4$ $\cdot (u^{15} - 4u^{14} + \dots - 4u + 1)(u^{20} - 9u^{19} + \dots - 105u + 21)$
$c_3$	$u^2(u^2 - u + 1)^4(u^7 - 2u^6 + 10u^5 + 8u^4 - 18u^3 - 39u^2 - 22u - 5)^4$ $\cdot (u^{15} + 4u^{14} + \dots - 6u + 1)(u^{20} + 9u^{19} + \dots - 123711u + 33789)$
$c_4, c_{10}$	$(u^2 - u + 1)(u^4 - 2u^3 + 2u^2 - u + 1)(u^4 + u^3 + 2u^2 + 2u + 1)$ $\cdot (u^{15} + 8u^{13} + \dots + 4u - 1)(u^{20} + u^{19} + \dots + 3u + 1)$ $\cdot (u^{28} + 23u^{26} + \dots + 1459u + 4993)$
$c_5, c_{11}$	$(u^2 - u + 1)(u^4 - 2u^3 + 2u^2 - u + 1)(u^4 + u^3 + 2u^2 + 2u + 1)$ $\cdot (u^{15} + u^{14} + \dots + 2u + 1)(u^{20} + 2u^{19} + \dots + u + 1)$ $\cdot (u^{28} - 3u^{26} + \dots - 21u + 13)$
$c_6$	$u^2(u^2 - u + 1)^4(u^7 + 2u^6 + 2u^5 - u^2 - 2u - 1)^4$ $\cdot (u^{15} + 4u^{14} + \dots - 4u - 1)(u^{20} - 9u^{19} + \dots - 105u + 21)$
$c_7$	$((u^2 - u + 1)^{18})(u^2 + u + 1)(u^{15} + 6u^{14} + \dots + 5u + 1)$ $\cdot (u^{20} + 16u^{19} + \dots + 160u + 32)$
$c_8$	$u^{10}(u^7 - 3u^6 + 2u^5 + 5u^4 - 9u^3 + u^2 + 6u - 4)^4$ $\cdot (u^{15} + 11u^{14} + \dots + 1118u + 169)(u^{20} + 22u^{19} + \dots + 273u + 21)$
$c_9, c_{12}$	$((u^2 - u + 1)^5)(u^{15} - 8u^{14} + \dots + 2u - 1)(u^{20} - u^{19} + \dots - 21u + 1)$ $\cdot (u^{28} - 5u^{27} + \dots + 21416u + 10543)$

### VIII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$y^2(y^2 + y + 1)^4(y^7 + 8y^6 + 8y^5 - 28y^4 + 32y^3 - 17y^2 + 2y - 1)^4$ $\cdot (y^{15} + 6y^{14} + \dots + 2y - 1)(y^{20} + 53y^{19} + \dots + 2156931y + 194481)$
$c_2, c_6$	$y^2(y^2 + y + 1)^4(y^7 + 4y^5 - 4y^3 - y^2 + 2y - 1)^4$ $\cdot (y^{15} + 6y^{14} + \dots - 6y - 1)(y^{20} + 5y^{19} + \dots + 2751y + 441)$
$c_3$	$y^2(y^2 + y + 1)^4$ $\cdot (y^7 + 16y^6 + 96y^5 - 624y^4 + 488y^3 - 649y^2 + 94y - 25)^4$ $\cdot (y^{15} + 12y^{14} + \dots - 224y^2 - 1)$ $\cdot (y^{20} + 107y^{19} + \dots + 4904181177y + 1141696521)$
$c_4, c_{10}$	$(y^2 + y + 1)(y^4 + 2y^2 + 3y + 1)(y^4 + 3y^3 + 2y^2 + 1)$ $\cdot (y^{15} + 16y^{14} + \dots - 6y - 1)(y^{20} + 31y^{19} + \dots - 9y + 1)$ $\cdot (y^{28} + 46y^{27} + \dots + 280734755y + 24930049)$
$c_5, c_{11}$	$(y^2 + y + 1)(y^4 + 2y^2 + 3y + 1)(y^4 + 3y^3 + 2y^2 + 1)$ $\cdot (y^{15} - 5y^{14} + \dots + 8y - 1)(y^{20} - 6y^{19} + \dots + y + 1)$ $\cdot (y^{28} - 6y^{27} + \dots - 3561y + 169)$
$c_7$	$((y^2 + y + 1)^{19})(y^{15} - 2y^{13} + \dots + 7y - 1)$ $\cdot (y^{20} + 42y^{18} + \dots + 15872y + 1024)$
$c_8$	$y^{10}(y^7 - 5y^6 + 16y^5 - 43y^4 + 71y^3 - 69y^2 + 44y - 16)^4$ $\cdot (y^{15} - 11y^{14} + \dots + 118300y - 28561)$ $\cdot (y^{20} - 16y^{19} + \dots - 3423y + 441)$
$c_9, c_{12}$	$((y^2 + y + 1)^5)(y^{15} - 16y^{14} + \dots - 2y - 1)(y^{20} - 49y^{19} + \dots - 81y + 1)$ $\cdot (y^{28} - 53y^{27} + \dots + 543656868y + 111154849)$