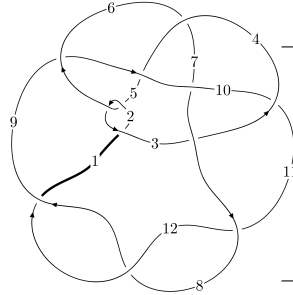
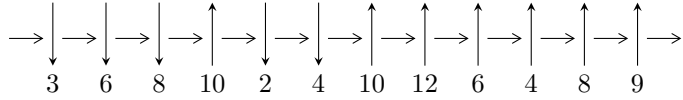


12n<sub>0318</sub> (K12n<sub>0318</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,10 \xrightarrow{c_4} 4 \xrightarrow{c_{10}} 8,11 \xrightarrow{c_{11}} 12 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_6} 6 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_9} 9 \rightsquigarrow c_5, c_8, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -46u^9 + 96u^8 - 471u^7 + 631u^6 - 1426u^5 + 1075u^4 - 1285u^3 + 249u^2 + 61b - 157u - 203, \\ -3u^9 + 5u^8 - 28u^7 + 29u^6 - 74u^5 + 37u^4 - 51u^3 + u^2 + a - 5u - 8, \\ u^{10} - 2u^9 + 10u^8 - 13u^7 + 29u^6 - 22u^5 + 24u^4 - 8u^3 + 3u^2 + 2u - 1 \rangle$$

$$I_2^u = \langle 4u^9 - 38u^8 + 23u^7 - 323u^6 + 100u^5 - 821u^4 + 395u^3 - 595u^2 + 185b + 617u - 243, \\ -439u^9 - 177u^8 - 3588u^7 - 117u^6 - 9310u^5 + 2461u^4 - 8895u^3 + 5315u^2 + 185a - 3937u + 1278, \\ u^{10} + 8u^8 - 3u^7 + 21u^6 - 14u^5 + 22u^4 - 20u^3 + 13u^2 - 6u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 20 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle -46u^9 + 96u^8 + \dots + 61b - 203, -3u^9 + 5u^8 + \dots + a - 8, u^{10} - 2u^9 + \dots + 2u - 1 \rangle$$

I.  $I_1^u =$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 3u^9 - 5u^8 + 28u^7 - 29u^6 + 74u^5 - 37u^4 + 51u^3 - u^2 + 5u + 8 \\ 0.754098u^9 - 1.57377u^8 + \dots + 2.57377u + 3.32787 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 7.27869u^9 - 12.0164u^8 + \dots + 22.0164u + 22.2951 \\ 3.27869u^9 - 5.01639u^8 + \dots + 9.01639u + 8.29508 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -7.70492u^9 + 12.6885u^8 + \dots - 21.6885u - 22.3934 \\ -3.40984u^9 + 5.37705u^8 + \dots - 8.37705u - 8.78689 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 3u^9 - 5u^8 + 28u^7 - 29u^6 + 74u^5 - 37u^4 + 51u^3 - u^2 + 5u + 8 \\ 0.754098u^9 - 1.57377u^8 + \dots + 3.57377u + 4.32787 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 3.75410u^9 - 6.57377u^8 + \dots + 7.57377u + 11.3279 \\ 0.803279u^9 - 1.45902u^8 + \dots + 4.45902u + 4.26230 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1.26230u^9 - 1.72131u^8 + \dots + 2.72131u + 3.98361 \\ 0.983607u^9 - 1.70492u^8 + \dots + 0.704918u + 1.68852 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 51.8033u^9 - 86.4590u^8 + \dots + 129.459u + 150.262 \\ 19.7377u^9 - 31.2787u^8 + \dots + 54.2787u + 58.0164 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -20.5410u^9 + 33.7377u^8 + \dots - 52.7377u - 58.2787 \\ -8.31148u^9 + 14.6066u^8 + \dots - 18.6066u - 23.9180 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{62}{61}u^9 + \frac{201}{61}u^8 - \frac{725}{61}u^7 + \frac{1487}{61}u^6 - \frac{2349}{61}u^5 + \frac{3080}{61}u^4 - \frac{2090}{61}u^3 + \frac{1667}{61}u^2 - \frac{445}{61}u + \frac{103}{61}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{10} + 22u^9 + \dots + 5917u + 49$
$c_2, c_5$	$u^{10} + 2u^9 + \dots - 59u + 7$
$c_3$	$u^{10} + 3u^9 + \dots + 12u - 13$
$c_4, c_{10}$	$u^{10} + 2u^9 + 10u^8 + 13u^7 + 29u^6 + 22u^5 + 24u^4 + 8u^3 + 3u^2 - 2u - 1$
$c_6$	$u^{10} - 3u^9 + \dots + 110u - 25$
$c_7$	$u^{10} + 3u^9 - 20u^7 - 41u^6 + 294u^5 - 405u^4 + 219u^3 + 58u^2 - 33u - 9$
$c_8, c_{11}, c_{12}$	$u^{10} - 3u^9 + \dots + 37u - 29$
$c_9$	$u^{10} + u^9 + \dots - 25u - 167$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{10} - 34y^9 + \dots - 33340185y + 2401$
$c_2, c_5$	$y^{10} - 22y^9 + \dots - 5917y + 49$
$c_3$	$y^{10} - 19y^9 + \dots - 2666y + 169$
$c_4, c_{10}$	$y^{10} + 16y^9 + \dots - 10y + 1$
$c_6$	$y^{10} - 27y^9 + \dots - 23900y + 625$
$c_7$	$y^{10} - 9y^9 + \dots - 2133y + 81$
$c_8, c_{11}, c_{12}$	$y^{10} - 21y^9 + \dots + 3097y + 841$
$c_9$	$y^{10} - 17y^9 + \dots - 55401y + 27889$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.058067 + 0.959343I$ $a = -1.02272 + 1.68359I$ $b = -0.56593 - 1.71994I$	$2.74627 + 1.52551I$	$1.61031 - 1.19705I$
$u = 0.058067 - 0.959343I$ $a = -1.02272 - 1.68359I$ $b = -0.56593 + 1.71994I$	$2.74627 - 1.52551I$	$1.61031 + 1.19705I$
$u = 0.369407 + 0.683035I$ $a = 0.045927 - 0.332128I$ $b = 0.679565 + 0.238520I$	$-1.42142 - 0.67316I$	$-3.66351 + 1.21479I$
$u = 0.369407 - 0.683035I$ $a = 0.045927 + 0.332128I$ $b = 0.679565 - 0.238520I$	$-1.42142 + 0.67316I$	$-3.66351 - 1.21479I$
$u = -0.387852$ $a = 1.30915$ $b = -0.163807$	$0.892115$	$12.2090$
$u = 0.346316$ $a = 11.5322$ $b = 4.45406$	$5.57991$	$1.58660$
$u = 0.45233 + 1.77782I$ $a = -0.557671 + 0.304853I$ $b = -0.225028 - 1.028840I$	$-9.90958 + 3.92064I$	$1.45511 - 3.03765I$
$u = 0.45233 - 1.77782I$ $a = -0.557671 - 0.304853I$ $b = -0.225028 + 1.028840I$	$-9.90958 - 3.92064I$	$1.45511 + 3.03765I$
$u = 0.14096 + 1.98796I$ $a = 1.61376 - 0.88253I$ $b = -3.53373 + 2.38309I$	$15.2183 + 8.0662I$	$1.70029 - 2.38226I$
$u = 0.14096 - 1.98796I$ $a = 1.61376 + 0.88253I$ $b = -3.53373 - 2.38309I$	$15.2183 - 8.0662I$	$1.70029 + 2.38226I$

$$\text{II. } I_2^u = \langle 4u^9 - 38u^8 + \dots + 185b - 243, -439u^9 - 177u^8 + \dots + 185a + 1278, u^{10} + 8u^8 + \dots - 6u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_5 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_4 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 2.37297u^9 + 0.956757u^8 + \dots + 21.2811u - 6.90811 \\ -0.0216216u^9 + 0.205405u^8 + \dots - 3.33514u + 1.31351 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 1.37297u^9 + 0.956757u^8 + \dots + 9.28108u - 0.908108 \\ 0.432432u^9 - 0.108108u^8 + \dots + 8.70270u - 2.27027 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.745946u^9 + 0.0864865u^8 + \dots - 7.56216u + 3.81622 \\ 0.745946u^9 - 0.0864865u^8 + \dots + 7.56216u - 1.81622 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 2.37297u^9 + 0.956757u^8 + \dots + 21.2811u - 6.90811 \\ 0.389189u^9 + 0.302703u^8 + \dots + 0.0324324u + 0.356757 \end{pmatrix} \\ a_6 &= \begin{pmatrix} 2.35135u^9 + 1.16216u^8 + \dots + 17.9459u - 5.59459 \\ 0.437838u^9 + 0.340541u^8 + \dots + 1.28649u + 0.151351 \end{pmatrix} \\ a_2 &= \begin{pmatrix} -3.11892u^9 - 0.870270u^8 + \dots - 28.8432u + 9.72432 \\ 0.313514u^9 + 0.0216216u^8 + \dots + 0.859459u - 0.545946 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -3.24324u^9 - 1.18919u^8 + \dots - 29.2703u + 9.02703 \\ -0.702703u^9 - 0.324324u^8 + \dots - 2.89189u + 0.189189 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -2.24324u^9 - 1.18919u^8 + \dots - 17.2703u + 4.02703 \\ -1.14054u^9 - 0.664865u^8 + \dots - 6.17838u + 2.03784 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= \frac{1244}{185}u^9 + \frac{577}{185}u^8 + \frac{10113}{185}u^7 + \frac{927}{185}u^6 + \frac{5147}{37}u^5 - \frac{5396}{185}u^4 + \frac{4552}{37}u^3 - \frac{2673}{37}u^2 + \frac{7997}{185}u - \frac{1943}{185}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{10} - 10u^9 + \dots - 13u + 1$
$c_2$	$u^{10} + 2u^9 - 3u^8 - 7u^7 + 4u^6 + 12u^5 - u^4 - 11u^3 - 2u^2 + 3u + 1$
$c_3$	$u^{10} + u^9 - u^8 - u^6 - 3u^5 + 3u^4 - u^3 + 5u^2 - 2u - 1$
$c_4$	$u^{10} + 8u^8 - 3u^7 + 21u^6 - 14u^5 + 22u^4 - 20u^3 + 13u^2 - 6u + 1$
$c_5$	$u^{10} - 2u^9 - 3u^8 + 7u^7 + 4u^6 - 12u^5 - u^4 + 11u^3 - 2u^2 - 3u + 1$
$c_6$	$u^{10} + 3u^9 + u^8 - 4u^7 - 8u^6 - 9u^5 + 11u^4 + 31u^3 + 24u^2 + 8u + 1$
$c_7$	$u^{10} + u^9 + 4u^8 + 4u^7 - 3u^6 - 8u^5 - 13u^4 - 21u^3 - 18u^2 - 7u - 1$
$c_8$	$u^{10} - 3u^9 + 9u^7 - 8u^6 - 7u^5 + 11u^4 - u^3 - 3u^2 + u - 1$
$c_9$	$u^{10} - u^9 + 2u^8 + u^7 - 11u^6 + 10u^5 - 7u^4 + 2u^3 + 4u^2 + u - 1$
$c_{10}$	$u^{10} + 8u^8 + 3u^7 + 21u^6 + 14u^5 + 22u^4 + 20u^3 + 13u^2 + 6u + 1$
$c_{11}, c_{12}$	$u^{10} + 3u^9 - 9u^7 - 8u^6 + 7u^5 + 11u^4 + u^3 - 3u^2 - u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{10} - 10y^9 + \dots - 33y + 1$
$c_2, c_5$	$y^{10} - 10y^9 + \dots - 13y + 1$
$c_3$	$y^{10} - 3y^9 - y^8 + 14y^7 + 7y^6 - 23y^5 - 5y^4 + 19y^3 + 15y^2 - 14y + 1$
$c_4, c_{10}$	$y^{10} + 16y^9 + \dots - 10y + 1$
$c_6$	$y^{10} - 7y^9 + \dots - 16y + 1$
$c_7$	$y^{10} + 7y^9 + \dots - 13y + 1$
$c_8, c_{11}, c_{12}$	$y^{10} - 9y^9 + \dots + 5y + 1$
$c_9$	$y^{10} + 3y^9 + \dots - 9y + 1$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.421587 + 1.150120I$		
$a = -0.068626 + 0.779782I$	$-0.46461 + 1.98898I$	$-0.06537 - 3.20823I$
$b = 0.442051 + 0.121008I$		
$u = -0.421587 - 1.150120I$		
$a = -0.068626 - 0.779782I$	$-0.46461 - 1.98898I$	$-0.06537 + 3.20823I$
$b = 0.442051 - 0.121008I$		
$u = 0.235261 + 0.587721I$		
$a = -0.300901 + 0.648896I$	$5.08555 + 2.55932I$	$4.45408 - 5.37582I$
$b = 0.14149 - 1.45935I$		
$u = 0.235261 - 0.587721I$		
$a = -0.300901 - 0.648896I$	$5.08555 - 2.55932I$	$4.45408 + 5.37582I$
$b = 0.14149 + 1.45935I$		
$u = 0.490498$		
$a = 3.09930$	$6.94382$	$10.5630$
$b = 0.465102$		
$u = 0.12366 + 1.64371I$		
$a = -1.257140 - 0.128400I$	$-6.58180 + 1.84846I$	$1.62067 - 1.24709I$
$b = 1.83592 + 0.29637I$		
$u = 0.12366 - 1.64371I$		
$a = -1.257140 + 0.128400I$	$-6.58180 - 1.84846I$	$1.62067 + 1.24709I$
$b = 1.83592 - 0.29637I$		
$u = 0.293026$		
$a = -1.91458$	$0.102739$	$-0.844670$
$b = 0.591313$		
$u = -0.32909 + 2.03714I$		
$a = 0.534307 - 0.226160I$	$-11.43200 - 3.15494I$	$-2.86863 + 1.76027I$
$b = -1.44767 + 0.48227I$		
$u = -0.32909 - 2.03714I$		
$a = 0.534307 + 0.226160I$	$-11.43200 + 3.15494I$	$-2.86863 - 1.76027I$
$b = -1.44767 - 0.48227I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{10} - 10u^9 + \dots - 13u + 1)(u^{10} + 22u^9 + \dots + 5917u + 49)$
$c_2$	$(u^{10} + 2u^9 + \dots - 59u + 7)$ $\cdot (u^{10} + 2u^9 - 3u^8 - 7u^7 + 4u^6 + 12u^5 - u^4 - 11u^3 - 2u^2 + 3u + 1)$
$c_3$	$(u^{10} + u^9 - u^8 - u^6 - 3u^5 + 3u^4 - u^3 + 5u^2 - 2u - 1)$ $\cdot (u^{10} + 3u^9 + \dots + 12u - 13)$
$c_4$	$(u^{10} + 8u^8 - 3u^7 + 21u^6 - 14u^5 + 22u^4 - 20u^3 + 13u^2 - 6u + 1)$ $\cdot (u^{10} + 2u^9 + 10u^8 + 13u^7 + 29u^6 + 22u^5 + 24u^4 + 8u^3 + 3u^2 - 2u - 1)$
$c_5$	$(u^{10} - 2u^9 - 3u^8 + 7u^7 + 4u^6 - 12u^5 - u^4 + 11u^3 - 2u^2 - 3u + 1)$ $\cdot (u^{10} + 2u^9 + \dots - 59u + 7)$
$c_6$	$(u^{10} - 3u^9 + \dots + 110u - 25)$ $\cdot (u^{10} + 3u^9 + u^8 - 4u^7 - 8u^6 - 9u^5 + 11u^4 + 31u^3 + 24u^2 + 8u + 1)$
$c_7$	$(u^{10} + u^9 + 4u^8 + 4u^7 - 3u^6 - 8u^5 - 13u^4 - 21u^3 - 18u^2 - 7u - 1)$ $\cdot (u^{10} + 3u^9 - 20u^7 - 41u^6 + 294u^5 - 405u^4 + 219u^3 + 58u^2 - 33u - 9)$
$c_8$	$(u^{10} - 3u^9 + 9u^7 - 8u^6 - 7u^5 + 11u^4 - u^3 - 3u^2 + u - 1)$ $\cdot (u^{10} - 3u^9 + \dots + 37u - 29)$
$c_9$	$(u^{10} - u^9 + 2u^8 + u^7 - 11u^6 + 10u^5 - 7u^4 + 2u^3 + 4u^2 + u - 1)$ $\cdot (u^{10} + u^9 + \dots - 25u - 167)$
$c_{10}$	$(u^{10} + 8u^8 + 3u^7 + 21u^6 + 14u^5 + 22u^4 + 20u^3 + 13u^2 + 6u + 1)$ $\cdot (u^{10} + 2u^9 + 10u^8 + 13u^7 + 29u^6 + 22u^5 + 24u^4 + 8u^3 + 3u^2 - 2u - 1)$
$c_{11}, c_{12}$	$(u^{10} - 3u^9 + \dots + 37u - 29)$ $\cdot (u^{10} + 3u^9 - 9u^7 - 8u^6 + 7u^5 + 11u^4 + u^3 - 3u^2 - u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{10} - 34y^9 + \dots - 33340185y + 2401)(y^{10} - 10y^9 + \dots - 33y + 1)$
$c_2, c_5$	$(y^{10} - 22y^9 + \dots - 5917y + 49)(y^{10} - 10y^9 + \dots - 13y + 1)$
$c_3$	$(y^{10} - 19y^9 + \dots - 2666y + 169)$ $\cdot (y^{10} - 3y^9 - y^8 + 14y^7 + 7y^6 - 23y^5 - 5y^4 + 19y^3 + 15y^2 - 14y + 1)$
$c_4, c_{10}$	$(y^{10} + 16y^9 + \dots - 10y + 1)(y^{10} + 16y^9 + \dots - 10y + 1)$
$c_6$	$(y^{10} - 27y^9 + \dots - 23900y + 625)(y^{10} - 7y^9 + \dots - 16y + 1)$
$c_7$	$(y^{10} - 9y^9 + \dots - 2133y + 81)(y^{10} + 7y^9 + \dots - 13y + 1)$
$c_8, c_{11}, c_{12}$	$(y^{10} - 21y^9 + \dots + 3097y + 841)(y^{10} - 9y^9 + \dots + 5y + 1)$
$c_9$	$(y^{10} - 17y^9 + \dots - 55401y + 27889)(y^{10} + 3y^9 + \dots - 9y + 1)$