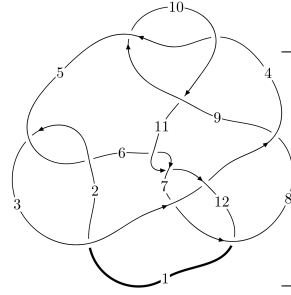
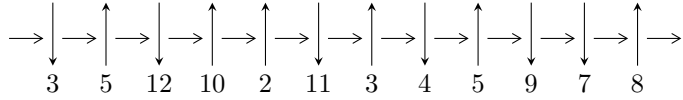


12n<sub>0352</sub> (K12n<sub>0352</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$4, 10 \xrightarrow{c_4} 5, 12 \xrightarrow{c_3} 3 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 11 \xrightarrow{c_6} 6 \twoheadrightarrow c_5, c_{10}, c_{12}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -3u^{18} - 24u^{17} + \dots + 2b - 14, -11u^{18} - 95u^{17} + \dots + 8a - 48, u^{19} + 9u^{18} + \dots + 44u + 8 \rangle$$

$$I_2^u = \langle 2u^{15} - 2u^{14} + 9u^{13} - 7u^{12} + 19u^{11} - 14u^{10} + 23u^9 - 16u^8 + 16u^7 - 12u^6 + 7u^5 - 4u^4 + 4u^3 + b + 2u + 1, \\ u^{15} + 2u^{14} + \dots + a + 4, \\ u^{16} - u^{15} + 5u^{14} - 4u^{13} + 12u^{12} - 9u^{11} + 17u^{10} - 12u^9 + 15u^8 - 11u^7 + 9u^6 - 6u^5 + 5u^4 - 2u^3 + 3u^2 + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 35 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -3u^{18} - 24u^{17} + \dots + 2b - 14, -11u^{18} - 95u^{17} + \dots + 8a - 48, u^{19} + 9u^{18} + \dots + 44u + 8 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} \frac{11}{2}u^{18} + \frac{95}{8}u^{17} + \dots + \frac{67}{2}u + 6 \\ \frac{33}{2}u^{18} + 12u^{17} + \dots + \frac{67}{2}u + 7 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{3}{8}u^{18} + \frac{21}{8}u^{17} + \dots - \frac{73}{4}u - \frac{9}{2} \\ \frac{1}{4}u^{18} + \frac{5}{4}u^{17} + \dots - 9u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{8}u^{18} + \frac{3}{8}u^{17} + \dots - \frac{157}{4}u - \frac{19}{2} \\ \frac{1}{4}u^{18} + \frac{5}{4}u^{17} + \dots - 11u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{3}{8}u^{18} + \frac{15}{8}u^{17} + \dots - \frac{85}{2}u - 10 \\ -u^{18} - \frac{19}{2}u^{17} + \dots - \frac{131}{2}u - 13 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{1}{8}u^{18} + \frac{11}{8}u^{17} + \dots + \frac{31}{4}u + 1 \\ -\frac{1}{4}u^{18} - \frac{7}{4}u^{17} + \dots - \frac{23}{2}u - 3 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{7}{8}u^{18} - \frac{61}{8}u^{17} + \dots - \frac{129}{2}u - 7 \\ \frac{1}{4}u^{18} + \frac{7}{4}u^{17} + \dots + \frac{57}{2}u + 7 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -8u^{18} - 66u^{17} - 305u^{16} - 975u^{15} - 2367u^{14} - 4600u^{13} - 7383u^{12} - 10049u^{11} - 11804u^{10} - 12134u^9 - 11000u^8 - 8792u^7 - 6229u^6 - 3932u^5 - 2281u^4 - 1230u^3 - 584u^2 - 212u - 42$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{19} + 50u^{18} + \dots + 9u - 1$
$c_2, c_5, c_7$	$u^{19} + 25u^{17} + \dots - u + 1$
$c_3$	$u^{19} - 4u^{18} + \dots + 5u - 1$
$c_4, c_9$	$u^{19} + 9u^{18} + \dots + 44u + 8$
$c_6, c_{11}$	$u^{19} + 3u^{18} + \dots + 28u^2 + 1$
$c_8$	$u^{19} - 9u^{18} + \dots - 4116u + 1960$
$c_{10}$	$u^{19} + 9u^{18} + \dots - 112u - 64$
$c_{12}$	$u^{19} - u^{18} + \dots - 104u + 193$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{19} - 202y^{18} + \dots + 101y - 1$
$c_2, c_5, c_7$	$y^{19} + 50y^{18} + \dots + 9y - 1$
$c_3$	$y^{19} - 2y^{18} + \dots + y - 1$
$c_4, c_9$	$y^{19} + 9y^{18} + \dots - 112y - 64$
$c_6, c_{11}$	$y^{19} - 49y^{18} + \dots - 56y - 1$
$c_8$	$y^{19} - 91y^{18} + \dots + 10638096y - 3841600$
$c_{10}$	$y^{19} + y^{18} + \dots - 35584y - 4096$
$c_{12}$	$y^{19} + 57y^{18} + \dots + 85314y - 37249$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.346161 + 0.956386I$		
$a = 1.46736 + 0.28036I$	$-0.63169 + 2.23536I$	$1.18472 - 3.58566I$
$b = 0.418807 - 0.392483I$		
$u = 0.346161 - 0.956386I$		
$a = 1.46736 - 0.28036I$	$-0.63169 - 2.23536I$	$1.18472 + 3.58566I$
$b = 0.418807 + 0.392483I$		
$u = -0.302273 + 1.061440I$		
$a = -1.21082 + 0.86313I$	$-3.68086 - 0.50062I$	$-7.63466 + 1.65999I$
$b = -1.020080 + 0.439454I$		
$u = -0.302273 - 1.061440I$		
$a = -1.21082 - 0.86313I$	$-3.68086 + 0.50062I$	$-7.63466 - 1.65999I$
$b = -1.020080 - 0.439454I$		
$u = -0.800161$		
$a = 1.21345$	$-3.42695$	$-3.98880$
$b = 0.717995$		
$u = -0.536472 + 1.088430I$		
$a = -1.78211 + 0.61588I$	$-2.09426 - 6.57381I$	$-0.65064 + 5.14701I$
$b = -0.874784 - 0.944864I$		
$u = -0.536472 - 1.088430I$		
$a = -1.78211 - 0.61588I$	$-2.09426 + 6.57381I$	$-0.65064 - 5.14701I$
$b = -0.874784 + 0.944864I$		
$u = -0.628002 + 0.338042I$		
$a = 0.039501 - 0.508734I$	$0.03067 + 1.98876I$	$2.15859 - 2.97799I$
$b = -0.649313 + 0.779497I$		
$u = -0.628002 - 0.338042I$		
$a = 0.039501 + 0.508734I$	$0.03067 - 1.98876I$	$2.15859 + 2.97799I$
$b = -0.649313 - 0.779497I$		
$u = -0.455443 + 1.212920I$		
$a = 1.89609 - 0.58745I$	$-6.99596 - 4.49122I$	$-9.18387 - 0.01438I$
$b = 0.758353 + 0.039269I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.455443 - 1.212920I$		
$a = 1.89609 + 0.58745I$	$-6.99596 + 4.49122I$	$-9.18387 + 0.01438I$
$b = 0.758353 - 0.039269I$		
$u = 0.413988 + 0.520782I$		
$a = 0.288663 - 0.426959I$	$0.657337 + 1.088170I$	$4.45180 - 5.21852I$
$b = -0.084685 + 0.588329I$		
$u = 0.413988 - 0.520782I$		
$a = 0.288663 + 0.426959I$	$0.657337 - 1.088170I$	$4.45180 + 5.21852I$
$b = -0.084685 - 0.588329I$		
$u = -1.41615 + 0.03594I$		
$a = 0.802995 - 0.190440I$	$18.3876 - 3.8412I$	$-1.79058 + 1.95309I$
$b = 1.04189 + 1.04688I$		
$u = -1.41615 - 0.03594I$		
$a = 0.802995 + 0.190440I$	$18.3876 + 3.8412I$	$-1.79058 - 1.95309I$
$b = 1.04189 - 1.04688I$		
$u = -0.78204 + 1.42833I$		
$a = 0.573067 - 0.779029I$	$14.2330 - 3.7497I$	$-3.12835 + 0.88970I$
$b = 0.97983 - 1.07686I$		
$u = -0.78204 - 1.42833I$		
$a = 0.573067 + 0.779029I$	$14.2330 + 3.7497I$	$-3.12835 - 0.88970I$
$b = 0.97983 + 1.07686I$		
$u = -0.73969 + 1.46029I$		
$a = 1.81853 - 0.33078I$	$13.8839 - 11.3207I$	$-3.41262 + 4.66030I$
$b = 1.07098 + 0.99229I$		
$u = -0.73969 - 1.46029I$		
$a = 1.81853 + 0.33078I$	$13.8839 + 11.3207I$	$-3.41262 - 4.66030I$
$b = 1.07098 - 0.99229I$		

**II.**

$$I_2^u = \langle 2u^{15} - 2u^{14} + \dots + b + 1, u^{15} + 2u^{14} + \dots + a + 4, u^{16} - u^{15} + \dots + 3u^2 + 1 \rangle$$

**(i) Arc colorings**

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^{15} - 2u^{14} + \dots + u - 4 \\ -2u^{15} + 2u^{14} + \dots - 2u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{15} - 2u^{13} + \dots + u - 3 \\ -2u^{15} + 3u^{14} + \dots - 2u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{15} - u^{13} + \dots + 2u - 3 \\ -3u^{15} + 4u^{14} + \dots - 2u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^{15} - u^{14} + \dots + 2u - 3 \\ -3u^{15} + 3u^{14} + \dots - 2u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^{14} - 2u^{13} + \dots - 3u + 1 \\ u^{15} - u^{14} + \dots + u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2u^{14} - 3u^{13} + \dots - 3u + 2 \\ u^{15} + 3u^{13} + \dots + 2u^2 + 2 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes** =  $8u^{15} - 8u^{14} + 36u^{13} - 27u^{12} + 74u^{11} - 55u^{10} + 90u^9 - 67u^8 + 63u^7 - 54u^6 + 32u^5 - 18u^4 + 16u^3 + 3u^2 + 10u - 3$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{16} - 11u^{15} + \dots - 9u + 1$
$c_2, c_7$	$u^{16} - u^{15} + \dots - u + 1$
$c_3$	$u^{16} + 7u^{15} + \dots + 5u + 1$
$c_4$	$u^{16} - u^{15} + \dots + 3u^2 + 1$
$c_5$	$u^{16} + u^{15} + \dots + u + 1$
$c_6$	$u^{16} + 2u^{15} + \dots + 2u + 1$
$c_8$	$u^{16} - u^{15} + \dots + 4u^2 + 1$
$c_9$	$u^{16} + u^{15} + \dots + 3u^2 + 1$
$c_{10}$	$u^{16} + 9u^{15} + \dots + 6u + 1$
$c_{11}$	$u^{16} - 2u^{15} + \dots - 2u + 1$
$c_{12}$	$u^{16} + 7u^{14} + \dots + 4u^2 + 1$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{16} - 5y^{15} + \dots + 5y + 1$
$c_2, c_5, c_7$	$y^{16} + 11y^{15} + \dots + 9y + 1$
$c_3$	$y^{16} - y^{15} + \dots + y + 1$
$c_4, c_9$	$y^{16} + 9y^{15} + \dots + 6y + 1$
$c_6, c_{11}$	$y^{16} - 12y^{15} + \dots - 6y + 1$
$c_8$	$y^{16} - 7y^{15} + \dots + 8y + 1$
$c_{10}$	$y^{16} + y^{15} + \dots + 2y + 1$
$c_{12}$	$y^{16} + 14y^{15} + \dots + 8y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.335104 + 0.911069I$		
$a = 2.45662 - 0.85727I$	$-7.02394 + 1.39379I$	$-9.47279 + 0.73629I$
$b = 0.921522 + 0.158810I$		
$u = 0.335104 - 0.911069I$		
$a = 2.45662 + 0.85727I$	$-7.02394 - 1.39379I$	$-9.47279 - 0.73629I$
$b = 0.921522 - 0.158810I$		
$u = -0.379248 + 1.028620I$		
$a = -0.646901 + 1.136830I$	$-3.77746 + 0.63307I$	$-8.74418 - 3.43739I$
$b = -1.14774 + 0.83032I$		
$u = -0.379248 - 1.028620I$		
$a = -0.646901 - 1.136830I$	$-3.77746 - 0.63307I$	$-8.74418 + 3.43739I$
$b = -1.14774 - 0.83032I$		
$u = 0.814712 + 0.313052I$		
$a = -0.637439 + 0.085695I$	$-2.04483 + 1.12270I$	$0.01080 - 2.10787I$
$b = -0.219047 + 0.658555I$		
$u = 0.814712 - 0.313052I$		
$a = -0.637439 - 0.085695I$	$-2.04483 - 1.12270I$	$0.01080 + 2.10787I$
$b = -0.219047 - 0.658555I$		
$u = -0.532348 + 1.055360I$		
$a = -1.92201 + 0.51905I$	$-2.65168 - 7.12816I$	$-8.0544 + 12.2171I$
$b = -0.99317 - 1.17536I$		
$u = -0.532348 - 1.055360I$		
$a = -1.92201 - 0.51905I$	$-2.65168 + 7.12816I$	$-8.0544 - 12.2171I$
$b = -0.99317 + 1.17536I$		
$u = -0.569437 + 0.482937I$		
$a = 0.475047 + 0.043194I$	$-0.93348 + 2.66812I$	$-2.81990 - 6.15304I$
$b = -0.782251 + 1.053490I$		
$u = -0.569437 - 0.482937I$		
$a = 0.475047 - 0.043194I$	$-0.93348 - 2.66812I$	$-2.81990 + 6.15304I$
$b = -0.782251 - 1.053490I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.182107 + 0.721236I$		
$a = -2.18930 + 1.30740I$	$-2.38549 - 3.31503I$	$-6.02251 + 3.66103I$
$b = -0.958246 - 0.624440I$		
$u = -0.182107 - 0.721236I$		
$a = -2.18930 - 1.30740I$	$-2.38549 + 3.31503I$	$-6.02251 - 3.66103I$
$b = -0.958246 + 0.624440I$		
$u = 0.614974 + 1.102350I$		
$a = 0.301915 + 0.157095I$	$-4.28291 + 4.20394I$	$-2.40515 - 3.76480I$
$b = 0.241401 - 0.693802I$		
$u = 0.614974 - 1.102350I$		
$a = 0.301915 - 0.157095I$	$-4.28291 - 4.20394I$	$-2.40515 + 3.76480I$
$b = 0.241401 + 0.693802I$		
$u = 0.398350 + 1.236570I$		
$a = -1.83794 + 0.04383I$	$-6.50903 + 5.01414I$	$-1.49188 - 7.53690I$
$b = -0.562464 + 0.307777I$		
$u = 0.398350 - 1.236570I$		
$a = -1.83794 - 0.04383I$	$-6.50903 - 5.01414I$	$-1.49188 + 7.53690I$
$b = -0.562464 - 0.307777I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{16} - 11u^{15} + \dots - 9u + 1)(u^{19} + 50u^{18} + \dots + 9u - 1)$
$c_2, c_7$	$(u^{16} - u^{15} + \dots - u + 1)(u^{19} + 25u^{17} + \dots - u + 1)$
$c_3$	$(u^{16} + 7u^{15} + \dots + 5u + 1)(u^{19} - 4u^{18} + \dots + 5u - 1)$
$c_4$	$(u^{16} - u^{15} + \dots + 3u^2 + 1)(u^{19} + 9u^{18} + \dots + 44u + 8)$
$c_5$	$(u^{16} + u^{15} + \dots + u + 1)(u^{19} + 25u^{17} + \dots - u + 1)$
$c_6$	$(u^{16} + 2u^{15} + \dots + 2u + 1)(u^{19} + 3u^{18} + \dots + 28u^2 + 1)$
$c_8$	$(u^{16} - u^{15} + \dots + 4u^2 + 1)(u^{19} - 9u^{18} + \dots - 4116u + 1960)$
$c_9$	$(u^{16} + u^{15} + \dots + 3u^2 + 1)(u^{19} + 9u^{18} + \dots + 44u + 8)$
$c_{10}$	$(u^{16} + 9u^{15} + \dots + 6u + 1)(u^{19} + 9u^{18} + \dots - 112u - 64)$
$c_{11}$	$(u^{16} - 2u^{15} + \dots - 2u + 1)(u^{19} + 3u^{18} + \dots + 28u^2 + 1)$
$c_{12}$	$(u^{16} + 7u^{14} + \dots + 4u^2 + 1)(u^{19} - u^{18} + \dots - 104u + 193)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{16} - 5y^{15} + \dots + 5y + 1)(y^{19} - 202y^{18} + \dots + 101y - 1)$
$c_2, c_5, c_7$	$(y^{16} + 11y^{15} + \dots + 9y + 1)(y^{19} + 50y^{18} + \dots + 9y - 1)$
$c_3$	$(y^{16} - y^{15} + \dots + y + 1)(y^{19} - 2y^{18} + \dots + y - 1)$
$c_4, c_9$	$(y^{16} + 9y^{15} + \dots + 6y + 1)(y^{19} + 9y^{18} + \dots - 112y - 64)$
$c_6, c_{11}$	$(y^{16} - 12y^{15} + \dots - 6y + 1)(y^{19} - 49y^{18} + \dots - 56y - 1)$
$c_8$	$(y^{16} - 7y^{15} + \dots + 8y + 1)$ $\cdot (y^{19} - 91y^{18} + \dots + 10638096y - 3841600)$
$c_{10}$	$(y^{16} + y^{15} + \dots + 2y + 1)(y^{19} + y^{18} + \dots - 35584y - 4096)$
$c_{12}$	$(y^{16} + 14y^{15} + \dots + 8y + 1)(y^{19} + 57y^{18} + \dots + 85314y - 37249)$