# $12n_{0370}$ (K12n\_{0370})



#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle 1.28847 \times 10^{15} u^{11} - 4.74420 \times 10^{14} u^{10} + \dots + 8.72123 \times 10^{16} b + 2.22344 \times 10^{17}, \\ & 1.00938 \times 10^{15} u^{11} - 1.97502 \times 10^{14} u^{10} + \dots + 8.72123 \times 10^{16} a + 3.30952 \times 10^{17}, \\ & u^{12} - 34u^{10} - 10u^9 + 374u^8 + 256u^7 - 1158u^6 - 838u^5 + 1243u^4 + 1159u^3 + 685u^2 + 342u + 61 \rangle \\ I_2^u &= \langle -491u^9 - 169u^8 + 138u^7 + 2797u^6 - 952u^5 - 2978u^4 - 1762u^3 + 4940u^2 + 1423b + 1946u - 9974 + 120u^9 + 363u^8 - 709u^7 - 501u^6 - 1399u^5 + 5504u^4 - 1259u^3 - 2839u^2 + 1423a - 3481u + 4617, \\ & u^{10} - u^9 - 5u^7 + 9u^6 - 3u^4 - 9u^3 + 9u^2 - u - 1 \rangle \end{split}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 22 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^{2}</sup>$ All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

 $\begin{array}{c} \text{I. }I_{1}^{u}=\\ \langle 1.29 \times 10^{15} u^{11}-4.74 \times 10^{14} u^{10}+\cdots +8.72 \times 10^{16} b+2.22 \times 10^{17}, \ 1.01 \times 10^{15} u^{11}-\\ 1.98 \times 10^{14} u^{10}+\cdots +8.72 \times 10^{16} a+3.31 \times 10^{17}, \ u^{12}-34 u^{10}+\cdots +342 u+61 \rangle \end{array}$ 

(i) Arc colorings

$$\begin{aligned} a_{3} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{7} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{8} &= \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.0115739u^{11} + 0.00226461u^{10} + \dots - 3.98267u - 3.79478 \\ -0.0147739u^{11} + 0.00543983u^{10} + \dots - 6.01362u - 2.54946 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} 0.00320005u^{11} - 0.00317522u^{10} + \dots + 2.03095u - 1.24533 \\ -0.0147739u^{11} + 0.00543983u^{10} + \dots - 6.01362u - 2.54946 \end{pmatrix} \\ a_{6} &= \begin{pmatrix} -0.0414649u^{11} + 0.0165212u^{10} + \dots - 17.1890u - 6.03303 \\ -0.00596827u^{11} + 0.00228246u^{10} + \dots - 2.07003u - 1.25196 \end{pmatrix} \\ a_{2} &= \begin{pmatrix} 0.0163711u^{11} - 0.00810347u^{10} + \dots + 7.17353u + 1.18110 \\ -0.00876668u^{11} + 0.00418598u^{10} + \dots - 3.18088u - 1.53147 \end{pmatrix} \\ a_{1} &= \begin{pmatrix} 0.0163711u^{11} - 0.00810347u^{10} + \dots + 7.17353u + 1.18110 \\ -0.0125049u^{11} + 0.0052621u^{10} + \dots - 4.95363u - 2.02578 \end{pmatrix} \\ a_{9} &= \begin{pmatrix} 0.00757115u^{11} - 0.00279404u^{10} + \dots + 2.94107u + 2.37499 \\ 0.00556736u^{11} - 0.00252772u^{10} + \dots + 2.05708u + 0.942635 \end{pmatrix} \\ a_{5} &= \begin{pmatrix} -0.00964076u^{11} + 0.00285039u^{10} + \dots - 2.23827u - 1.62408 \\ -0.00279404u^{11} + 0.000870939u^{10} + \dots - 0.214346u - 0.461840 \end{pmatrix} \\ a_{4} &= \begin{pmatrix} -0.00416895u^{11} - 0.00269474u^{10} + \dots + 0.812978u + 1.59345 \\ 0.00358791u^{11} - 0.00224683u^{10} + \dots + 0.877740u + 0.524985 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = -1

(iii	) Cusp Shapes			
_	8580809856421526 ,11	3421020397474812 ,10	4710390701175382035	26157625863371374
	$-\frac{1}{87212327051456087}u$	$r_{\overline{87212327051456087}}u + \cdots$	$-\frac{87212327051456087}{1}u^{-1}$	1429710279532067

(iv)	) u-Polynomials	at the	component
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Crossings	u-Polynomials at each crossing
$c_1$	$u^{12} + 10u^{10} + \dots + 3u + 1$
$c_2, c_5$	$u^{12} + 4u^{11} + \dots - u - 1$
$c_3, c_4, c_9$	$u^{12} + u^{11} + \dots + 4u + 1$
$c_{6}, c_{11}$	$u^{12} - 8u^{11} + \dots + 10u - 4$
	$u^{12} - 34u^{10} + \dots + 342u + 61$
$c_8, c_{12}$	$u^{12} - u^{11} + \dots + 13u - 1$
$c_{10}$	$u^{12} + 4u^{11} + \dots + 44u + 16$

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{12} + 20y^{11} + \dots - 3y + 1$
$c_2, c_5$	$y^{12} + 10y^{10} + \dots - 3y + 1$
$c_3, c_4, c_9$	$y^{12} - 29y^{11} + \dots - 12y + 1$
$c_6, c_{11}$	$y^{12} - 4y^{11} + \dots - 44y + 16$
C <sub>7</sub>	$y^{12} - 68y^{11} + \dots - 33394y + 3721$
$c_8, c_{12}$	$y^{12} + 33y^{11} + \dots - 269y + 1$
$c_{10}$	$y^{12} + 48y^{11} + \dots + 3216y + 256$

## $(\mathbf{v})$ Riley Polynomials at the component

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\operatorname{vol}+\sqrt{-1}CS)$	Cusp shape
u = -0.015982 + 0.502004I		
a = -1.33976 + 0.88379I	-0.313401 + 1.169960I	-3.81973 - 5.53143I
b = -0.373800 + 0.452174I		
u = -0.015982 - 0.502004I		
a = -1.33976 - 0.88379I	-0.313401 - 1.169960I	-3.81973 + 5.53143I
b = -0.373800 - 0.452174I		
u = -0.487209		
a = -1.96376	-2.57792	8.93780
b = 0.690624		
u = 1.53808 + 0.50690I		
a = 0.700750 + 0.138104I	3.43038 + 0.92181I	0.166703 - 0.576827I
b = 0.742800 - 0.761818I		
u = 1.53808 - 0.50690I		
a = 0.700750 - 0.138104I	3.43038 - 0.92181I	0.166703 + 0.576827I
b = 0.742800 + 0.761818I		
u = -1.64293 + 0.28456I		
a = 1.107820 - 0.267147I	2.73449 - 4.65154I	-0.40649 + 6.35112I
b = 0.969113 + 0.706030I		
u = -1.64293 - 0.28456I		
a = 1.107820 + 0.267147I	2.73449 + 4.65154I	-0.40649 - 6.35112I
b = 0.969113 - 0.706030I		
u = -0.299850		
a = -2.90979	-1.69975	-3.47970
b = -0.917503		
u = -3.60163 + 0.13896I		
a = 0.400586 + 0.118619I	-12.68910 + 1.00394I	-1.189954 + 0.108309I
b = 1.42147 - 1.15303I		
u = -3.60163 - 0.13896I		
a = 0.400586 - 0.118619I	-12.68910 - 1.00394I	-1.189954 - 0.108309I
b = 1.42147 + 1.15303I		

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	Solutions to $I_1^u$	$\sqrt{-1}(\operatorname{vol}+\sqrt{-1}CS)$	Cusp shape
u =	4.11599 + 0.72988I		
a =	0.591968 + 0.319795I	-12.4077 + 8.7999I	-0.97957 - 3.65752I
b =	1.35386 - 1.23724I		
u =	4.11599 - 0.72988I		
a =	0.591968 - 0.319795I	-12.4077 - 8.7999I	-0.97957 + 3.65752I
b =	1.35386 + 1.23724I		

II. 
$$I_2^u = \langle -491u^9 - 169u^8 + \dots + 1423b - 997, \ 120u^9 + 363u^8 + \dots + 1423a + 4617, \ u^{10} - u^9 - 5u^7 + 9u^6 - 3u^4 - 9u^3 + 9u^2 - u - 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_{3} &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_{7} &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_{8} &= \begin{pmatrix} 1 \\ -u^{2} \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.0843289u^{9} - 0.255095u^{8} + \dots + 2.44624u - 3.24455 \\ 0.345046u^{9} + 0.118763u^{8} + \dots - 1.36753u + 0.700632 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.429375u^{9} - 0.373858u^{8} + \dots + 3.81377u - 3.94519 \\ 0.345046u^{9} + 0.118763u^{8} + \dots - 1.36753u + 0.700632 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.454673u^{9} + 0.849613u^{8} + \dots - 7.55235u + 1.78145 \\ 1.04287u^{9} - 0.545327u^{8} + \dots + 3.31483u + 0.824315 \end{pmatrix} \\ a_{2} &= \begin{pmatrix} 0.613493u^{9} - 0.919185u^{8} + \dots + 7.12860u - 2.12087 \\ -0.781448u^{9} + 0.236121u^{8} + \dots - 2.19817u - 0.666198 \end{pmatrix} \\ a_{1} &= \begin{pmatrix} 0.613493u^{9} - 0.919185u^{8} + \dots + 7.12860u - 2.12087 \\ -0.676037u^{9} + 0.304989u^{8} + \dots - 2.50597u - 0.360506 \end{pmatrix} \\ a_{9} &= \begin{pmatrix} -0.345046u^{9} - 0.118763u^{8} + \dots + 1.36753u - 0.700632 \\ -0.436402u^{9} + 0.354884u^{8} + \dots - 3.56571u - 0.965566 \end{pmatrix} \\ a_{5} &= \begin{pmatrix} -0.0337316u^{9} + 0.297962u^{8} + \dots + 1.04568u + 0.345046 \\ 0.463809u^{9} - 0.0969782u^{8} + \dots + 1.04568u + 0.345046 \end{pmatrix} \\ a_{4} &= \begin{pmatrix} -0.497540u^{9} + 0.394940u^{8} + \dots - 1.86718u - 1.04287 \\ 0.463809u^{9} - 0.0969782u^{8} + \dots + 1.04568u + 0.345046 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.376669u^{9} - 0.339424u^{8} + \dots + 2.65987u - 0.292340 \\ -0.539002u^{9} + 0.594519u^{8} + \dots - 5.10611u - 1.46311 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $\frac{2033}{1423}u^9 - \frac{3491}{1423}u^8 + \frac{1495}{1423}u^7 - \frac{10729}{1423}u^6 + \frac{25736}{1423}u^5 - \frac{14237}{1423}u^4 - \frac{2961}{1423}u^3 - \frac{18582}{1423}u^2 + \frac{34363}{1423}u - \frac{16730}{1423}u^3 - \frac{10729}{1423}u^4 - \frac{10729}{1$ 

Crossings u-Polynomials at each crossing	
$c_1$	$u^{10} - u^9 + 6u^8 - 6u^7 + 9u^6 - 12u^5 - 3u^4 + 2u^3 + 6u^2 - 4u + 1$
<i>C</i> <sub>2</sub>	$u^{10} + 3u^9 + 4u^8 - 5u^6 - 6u^5 - u^4 + 2u^3 + 2u^2 - 1$
C3	$u^{10} - 5u^8 + 9u^6 + 2u^5 - 6u^4 - 6u^3 + 5u + 1$
$c_4, c_9$	$u^{10} - 5u^8 + 9u^6 - 2u^5 - 6u^4 + 6u^3 - 5u + 1$
$c_5$	$u^{10} - 3u^9 + 4u^8 - 5u^6 + 6u^5 - u^4 - 2u^3 + 2u^2 - 1$
<i>c</i> <sub>6</sub>	$u^{10} - 2u^8 + 4u^6 - 4u^4 + u^3 + 2u^2 - 1$
<i>C</i> <sub>7</sub>	$u^{10} - u^9 - 5u^7 + 9u^6 - 3u^4 - 9u^3 + 9u^2 - u - 1$
<i>c</i> <sub>8</sub>	$u^{10} + 6u^8 - u^7 + 15u^6 - 5u^5 + 18u^4 - 9u^3 + 9u^2 - 6u + 1$
$c_{10}$	$u^{10} - 4u^9 + \dots - 4u + 1$
$c_{11}$	$u^{10} - 2u^8 + 4u^6 - 4u^4 - u^3 + 2u^2 - 1$
c <sub>12</sub>	$u^{10} + 6u^8 + u^7 + 15u^6 + 5u^5 + 18u^4 + 9u^3 + 9u^2 + 6u + 1$

### (iv) u-Polynomials at the component

Crossings	Riley Polynomials at each crossing	
$c_1$	$y^{10} + 11y^9 + \dots - 4y + 1$	
$c_2, c_5$	$y^{10} - y^9 + 6y^8 - 6y^7 + 9y^6 - 12y^5 - 3y^4 + 2y^3 + 6y^2 - 4y + 1$	
$c_3, c_4, c_9$	$y^{10} - 10y^9 + \dots - 25y + 1$	
$c_{6}, c_{11}$	$y^{10} - 4y^9 + \dots - 4y + 1$	
	$y^{10} - y^9 + \dots - 19y + 1$	
$c_8, c_{12}$	$y^{10} + 12y^9 + \dots - 18y + 1$	
$c_{10}$	$y^{10} + 8y^9 + \dots + 8y + 1$	

## $(\mathbf{v})$ Riley Polynomials at the component

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\operatorname{vol}+\sqrt{-1}CS)$	Cusp shape
u = -0.811923 + 0.722020I		
a = 1.45325 + 0.35022I	5.24934 - 6.06210I	-0.58831 + 6.06500I
b = 0.975490 + 0.644063I		
u = -0.811923 - 0.722020I		
a = 1.45325 - 0.35022I	5.24934 + 6.06210I	-0.58831 - 6.06500I
b = 0.975490 - 0.644063I		
u = 1.115350 + 0.663499I		
a = 0.272302 - 0.257296I	6.04451 - 1.01363I	0.978414 + 0.079961I
b = 0.724375 - 0.642107I		
u = 1.115350 - 0.663499I		
a = 0.272302 + 0.257296I	6.04451 + 1.01363I	0.978414 - 0.079961I
b = 0.724375 + 0.642107I		
u = 1.31175		
a = -0.322011	1.74489	-3.09540
b = -1.13039		
u = 0.602612 + 0.281923I		
a = -1.12138 + 1.00067I	2.28696 - 3.31057I	-1.50855 + 1.46154I
b = -0.995438 - 0.830468I		
u = 0.602612 - 0.281923I		
a = -1.12138 - 1.00067I	2.28696 + 3.31057I	-1.50855 - 1.46154I
b = -0.995438 + 0.830468I		
u = -0.257810		
a = -3.77592	-2.87740	-18.8820
b = 0.809153		
u = -0.93301 + 1.57780I		
a = -1.055210 + 0.217921I	5.07972 - 2.66860I	3.60710 + 4.02718I
b = -0.543811 - 0.460848I		
u = -0.93301 - 1.57780I		
a = -1.055210 - 0.217921I	5.07972 + 2.66860I	3.60710 - 4.02718I
b = -0.543811 + 0.460848I		

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{10} - u^9 + 6u^8 - 6u^7 + 9u^6 - 12u^5 - 3u^4 + 2u^3 + 6u^2 - 4u + 1)$ $\cdot (u^{12} + 10u^{10} + \dots + 3u + 1)$
<i>c</i> <sub>2</sub>	$(u^{10} + 3u^9 + 4u^8 - 5u^6 - 6u^5 - u^4 + 2u^3 + 2u^2 - 1)$ $\cdot (u^{12} + 4u^{11} + \dots - u - 1)$
<i>c</i> <sub>3</sub>	$(u^{10} - 5u^8 + \dots + 5u + 1)(u^{12} + u^{11} + \dots + 4u + 1)$
$c_4, c_9$	$(u^{10} - 5u^8 + \dots - 5u + 1)(u^{12} + u^{11} + \dots + 4u + 1)$
<i>C</i> <sub>5</sub>	$(u^{10} - 3u^9 + 4u^8 - 5u^6 + 6u^5 - u^4 - 2u^3 + 2u^2 - 1)$ $\cdot (u^{12} + 4u^{11} + \dots - u - 1)$
<i>c</i> <sub>6</sub>	$(u^{10} - 2u^8 + \dots + 2u^2 - 1)(u^{12} - 8u^{11} + \dots + 10u - 4)$
C7	$(u^{10} - u^9 - 5u^7 + 9u^6 - 3u^4 - 9u^3 + 9u^2 - u - 1)$ $\cdot (u^{12} - 34u^{10} + \dots + 342u + 61)$
<i>c</i> <sub>8</sub>	$(u^{10} + 6u^8 - u^7 + 15u^6 - 5u^5 + 18u^4 - 9u^3 + 9u^2 - 6u + 1)$ $\cdot (u^{12} - u^{11} + \dots + 13u - 1)$
$c_{10}$	$(u^{10} - 4u^9 + \dots - 4u + 1)(u^{12} + 4u^{11} + \dots + 44u + 16)$
c <sub>11</sub>	$(u^{10} - 2u^8 + \dots + 2u^2 - 1)(u^{12} - 8u^{11} + \dots + 10u - 4)$
$c_{12}$	$(u^{10} + 6u^8 + u^7 + 15u^6 + 5u^5 + 18u^4 + 9u^3 + 9u^2 + 6u + 1)$ $\cdot (u^{12} - u^{11} + \dots + 13u - 1)$

III. u-Polynomials

Crossings	Riley Polynomials at each crossing	
<i>c</i> <sub>1</sub>	$(y^{10} + 11y^9 + \dots - 4y + 1)(y^{12} + 20y^{11} + \dots - 3y + 1)$	
$c_2, c_5$	$(y^{10} - y^9 + 6y^8 - 6y^7 + 9y^6 - 12y^5 - 3y^4 + 2y^3 + 6y^2 - 4y + 1)$ $\cdot (y^{12} + 10y^{10} + \dots - 3y + 1)$	
$c_3, c_4, c_9$	$(y^{10} - 10y^9 + \dots - 25y + 1)(y^{12} - 29y^{11} + \dots - 12y + 1)$	
$c_6, c_{11}$	$(y^{10} - 4y^9 + \dots - 4y + 1)(y^{12} - 4y^{11} + \dots - 44y + 16)$	
C <sub>7</sub>	$(y^{10} - y^9 + \dots - 19y + 1)(y^{12} - 68y^{11} + \dots - 33394y + 3721)$	
$c_8, c_{12}$	$(y^{10} + 12y^9 + \dots - 18y + 1)(y^{12} + 33y^{11} + \dots - 269y + 1)$	
$c_{10}$	$(y^{10} + 8y^9 + \dots + 8y + 1)(y^{12} + 48y^{11} + \dots + 3216y + 256)$	

### IV. Riley Polynomials