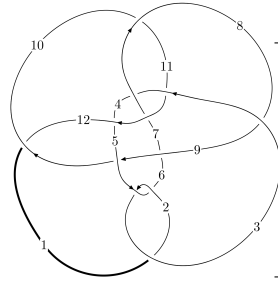
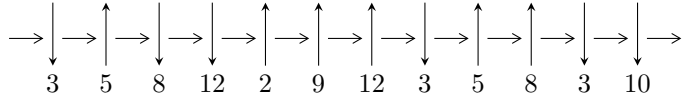


12n₀₄₆₂ (K12n₀₄₆₂)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$3,5 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1,10 \xrightarrow{c_9} 9 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \xrightarrow{c_4} 4 \xrightarrow{c_7} 7 \xrightarrow{c_6} 6 \xrightarrow{c_{11}} 11 \rightsquigarrow c_3, c_5, c_{10}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle -149788246u^{19} + 735301154u^{18} + \dots + 16882806339b - 24202510048, \\ -38489542585u^{19} + 46865050127u^{18} + \dots + 16882806339a - 207132124495, \\ u^{20} - u^{19} + \dots + 11u + 1 \rangle$$

$$I_2^u = \langle u^2 + b + 1, u^5 - 2u^4 + 5u^3 - 6u^2 + 3a + 6u - 1, u^6 - u^5 + 5u^4 - 4u^3 + 7u^2 - 2u + 3 \rangle$$

$$I_3^u = \langle b - u, a - u, u^2 + u + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 28 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -1.50 \times 10^8 u^{19} + 7.35 \times 10^8 u^{18} + \dots + 1.69 \times 10^{10} b - 2.42 \times 10^{10}, -3.85 \times 10^{10} u^{19} + 4.69 \times 10^{10} u^{18} + \dots + 1.69 \times 10^{10} a - 2.07 \times 10^{11}, u^{20} - u^{19} + \dots + 11u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 2.27981u^{19} - 2.77590u^{18} + \dots + 74.2433u + 12.2688 \\ 0.00887224u^{19} - 0.0435533u^{18} + \dots + 9.24808u + 1.43356 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 2.27981u^{19} - 2.77590u^{18} + \dots + 74.2433u + 12.2688 \\ 0.0852452u^{19} - 0.0369754u^{18} + \dots + 12.4253u + 1.92966 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 2.36505u^{19} - 2.81288u^{18} + \dots + 86.6686u + 14.1985 \\ 0.0852452u^{19} - 0.0369754u^{18} + \dots + 12.4253u + 1.92966 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.00359098u^{19} + 0.391699u^{18} + \dots + 9.11164u + 4.91265 \\ 0.327637u^{19} - 0.499312u^{18} + \dots + 0.549227u + 0.495867 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.627286u^{19} - 0.803555u^{18} + \dots + 31.8391u + 2.03483 \\ 0.253178u^{19} - 0.0827151u^{18} + \dots + 12.4507u + 0.748328 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1.92966u^{19} - 2.01490u^{18} + \dots + 73.2986u + 8.80089 \\ 0.509356u^{19} - 0.765818u^{18} + \dots + 2.50917u + 0.308552 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.324046u^{19} - 0.107613u^{18} + \dots + 9.66087u + 5.40852 \\ 0.327637u^{19} - 0.499312u^{18} + \dots + 0.549227u + 0.495867 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{12674828861}{16882806339}u^{19} + \frac{1750449202}{2411829477}u^{18} + \dots - \frac{510127682849}{16882806339}u + \frac{10680247402}{16882806339}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{20} + 27u^{19} + \dots - 27u + 1$
c_2, c_5	$u^{20} + u^{19} + \dots - 11u + 1$
c_3, c_8	$u^{20} - u^{19} + \dots + 11u + 1$
c_4	$u^{20} + 2u^{19} + \dots - 27u + 51$
c_6	$u^{20} + 16u^{18} + \dots - 16u + 52$
c_7	$u^{20} - 3u^{19} + \dots + 109u^2 + 21$
c_9	$u^{20} - 2u^{19} + \dots + 27u + 51$
c_{10}	$u^{20} + 5u^{19} + \dots + 57u + 7$
c_{11}	$u^{20} + 16u^{18} + \dots + 16u + 52$
c_{12}	$u^{20} - 5u^{19} + \dots - 57u + 7$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{20} - 61y^{19} + \dots + 169y + 1$
c_2, c_3, c_5 c_8	$y^{20} + 27y^{19} + \dots - 27y + 1$
c_4, c_9	$y^{20} + 18y^{19} + \dots + 17835y + 2601$
c_6, c_{11}	$y^{20} + 32y^{19} + \dots + 7024y + 2704$
c_7	$y^{20} - 33y^{19} + \dots + 4578y + 441$
c_{10}, c_{12}	$y^{20} - 15y^{19} + \dots - 1835y + 49$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.160143 + 0.768509I$ $a = -0.394995 - 1.004840I$ $b = -0.636041 - 0.396936I$	$-1.10947 - 1.48655I$	$-5.12329 + 2.41841I$
$u = 0.160143 - 0.768509I$ $a = -0.394995 + 1.004840I$ $b = -0.636041 + 0.396936I$	$-1.10947 + 1.48655I$	$-5.12329 - 2.41841I$
$u = -0.484926 + 0.607075I$ $a = 0.577525 - 0.647733I$ $b = -0.026523 - 0.353444I$	$-1.43025I$	$0. + 5.92138I$
$u = -0.484926 - 0.607075I$ $a = 0.577525 + 0.647733I$ $b = -0.026523 + 0.353444I$	$1.43025I$	$0. - 5.92138I$
$u = -0.08307 + 1.42113I$ $a = -0.271547 + 1.012220I$ $b = -1.110600 + 0.490957I$	$3.72589 - 1.03786I$	$1.73919 + 0.58908I$
$u = -0.08307 - 1.42113I$ $a = -0.271547 - 1.012220I$ $b = -1.110600 - 0.490957I$	$3.72589 + 1.03786I$	$1.73919 - 0.58908I$
$u = 1.18575 + 0.83320I$ $a = 0.626136 + 0.573895I$ $b = 0.569199 + 0.092819I$	$8.81653 + 3.95168I$	$0.25331 - 3.24699I$
$u = 1.18575 - 0.83320I$ $a = 0.626136 - 0.573895I$ $b = 0.569199 - 0.092819I$	$8.81653 - 3.95168I$	$0.25331 + 3.24699I$
$u = -0.104414 + 0.507262I$ $a = 1.44705 - 1.63599I$ $b = 0.64554 + 1.51309I$	$10.23410 - 0.33723I$	$1.46943 - 0.53181I$
$u = -0.104414 - 0.507262I$ $a = 1.44705 + 1.63599I$ $b = 0.64554 - 1.51309I$	$10.23410 + 0.33723I$	$1.46943 + 0.53181I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.32507 + 1.48224I$		
$a = 0.843038 - 0.018166I$	$-3.72589 - 1.03786I$	$-1.73919 + 0.58908I$
$b = 1.69755 - 0.64672I$		
$u = -0.32507 - 1.48224I$		
$a = 0.843038 + 0.018166I$	$-3.72589 + 1.03786I$	$-1.73919 - 0.58908I$
$b = 1.69755 + 0.64672I$		
$u = -0.11912 + 1.73852I$		
$a = -1.211980 - 0.171698I$	$-8.81653 - 3.95168I$	$-0.25331 + 3.24699I$
$b = -2.38905 - 0.18528I$		
$u = -0.11912 - 1.73852I$		
$a = -1.211980 + 0.171698I$	$-8.81653 + 3.95168I$	$-0.25331 - 3.24699I$
$b = -2.38905 + 0.18528I$		
$u = 0.11567 + 1.76293I$		
$a = 0.697284 + 0.000472I$	$-10.23410 + 0.33723I$	$-1.46943 + 0.53181I$
$b = 2.05356 + 0.22436I$		
$u = 0.11567 - 1.76293I$		
$a = 0.697284 - 0.000472I$	$-10.23410 - 0.33723I$	$-1.46943 - 0.53181I$
$b = 2.05356 - 0.22436I$		
$u = 0.32058 + 1.78463I$		
$a = -0.974674 + 0.336167I$	$9.75717I$	$0. - 4.10936I$
$b = -2.29883 + 0.36675I$		
$u = 0.32058 - 1.78463I$		
$a = -0.974674 - 0.336167I$	$- 9.75717I$	$0. + 4.10936I$
$b = -2.29883 - 0.36675I$		
$u = -0.165551 + 0.073534I$		
$a = 2.16216 + 4.82053I$	$1.10947 + 1.48655I$	$5.12329 - 2.41841I$
$b = -0.004791 + 0.715102I$		
$u = -0.165551 - 0.073534I$		
$a = 2.16216 - 4.82053I$	$1.10947 - 1.48655I$	$5.12329 + 2.41841I$
$b = -0.004791 - 0.715102I$		

$$\text{II. } I_2^u = \langle u^2 + b + 1, u^5 - 2u^4 + 5u^3 - 6u^2 + 3a + 6u - 1, u^6 - u^5 + 5u^4 - 4u^3 + 7u^2 - 2u + 3 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_3 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_1 &= \begin{pmatrix} u^2 + 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -\frac{1}{3}u^5 + \frac{2}{3}u^4 + \dots - 2u + \frac{1}{3} \\ -u^2 - 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -\frac{1}{3}u^5 + \frac{2}{3}u^4 + \dots - 2u + \frac{1}{3} \\ \frac{1}{3}u^5 - u^4 + \dots + \frac{5}{3}u - 2 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -\frac{1}{3}u^4 - \frac{5}{3}u^2 - \frac{1}{3}u - \frac{5}{3} \\ \frac{1}{3}u^5 - u^4 + \dots + \frac{5}{3}u - 2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -\frac{1}{3}u^5 + \frac{2}{3}u^4 + \dots - 2u + \frac{7}{3} \\ -\frac{2}{3}u^5 + u^4 + \dots - \frac{4}{3}u + 1 \end{pmatrix} \\ a_4 &= \begin{pmatrix} \frac{2}{3}u^5 + \frac{1}{3}u^4 + \dots + \frac{2}{3}u + \frac{5}{3} \\ \frac{2}{3}u^5 + \frac{7}{3}u^3 - \frac{1}{3}u^2 + \frac{4}{3}u - 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} -\frac{2}{3}u^5 + \frac{1}{3}u^4 + \dots - u - \frac{1}{3} \\ u^3 + u^2 + 2u + 1 \end{pmatrix} \\ a_6 &= \begin{pmatrix} u \\ u^3 + u \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^5 + \frac{5}{3}u^4 + \dots - \frac{10}{3}u + \frac{10}{3} \\ -\frac{2}{3}u^5 + u^4 + \dots - \frac{4}{3}u + 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = u^5 - 3u^4 + 5u^3 - 11u^2 + 8u - 6$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^6 - 9u^5 + 31u^4 - 56u^3 + 63u^2 - 38u + 9$
c_2, c_8	$u^6 - u^5 + 5u^4 - 4u^3 + 7u^2 - 2u + 3$
c_3, c_5	$u^6 + u^5 + 5u^4 + 4u^3 + 7u^2 + 2u + 3$
c_4	$u^6 + 2u^4 + 3u^3 + 2u^2 + 1$
c_6	$u^6 - u^5 + 4u^4 - 2u^3 - 8u^2 + 6u + 9$
c_7	$u^6 - 3u^5 + u^4 - 2u^3 + 6u^2 + 5u + 1$
c_9	$u^6 + 2u^4 - 3u^3 + 2u^2 + 1$
c_{10}	$u^6 - 3u^5 + 5u^3 - u^2 - 2u + 3$
c_{11}	$u^6 + u^5 + 4u^4 + 2u^3 - 8u^2 - 6u + 9$
c_{12}	$u^6 + 3u^5 - 5u^3 - u^2 + 2u + 3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^6 - 19y^5 + 79y^4 + 104y^3 + 271y^2 - 310y + 81$
c_2, c_3, c_5 c_8	$y^6 + 9y^5 + 31y^4 + 56y^3 + 63y^2 + 38y + 9$
c_4, c_9	$y^6 + 4y^5 + 8y^4 + y^3 + 8y^2 + 4y + 1$
c_6, c_{11}	$y^6 + 7y^5 - 4y^4 - 38y^3 + 160y^2 - 180y + 81$
c_7	$y^6 - 7y^5 + y^4 + 40y^3 + 58y^2 - 13y + 1$
c_{10}, c_{12}	$y^6 - 9y^5 + 28y^4 - 31y^3 + 21y^2 - 10y + 9$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.615293 + 1.007340I$ $a = -0.488052 - 0.086507I$ $b = -0.363854 - 1.239620I$	$10.45590 + 2.33911I$	$2.00744 - 2.34673I$
$u = 0.615293 - 1.007340I$ $a = -0.488052 + 0.086507I$ $b = -0.363854 + 1.239620I$	$10.45590 - 2.33911I$	$2.00744 + 2.34673I$
$u = -0.061440 + 0.817267I$ $a = -0.744380 - 0.966777I$ $b = -0.335850 + 0.100426I$	$-2.22275I$	$0. + 4.90360I$
$u = -0.061440 - 0.817267I$ $a = -0.744380 + 0.966777I$ $b = -0.335850 - 0.100426I$	$2.22275I$	$0. - 4.90360I$
$u = -0.05385 + 1.78958I$ $a = 0.899099 + 0.320901I$ $b = 2.19970 + 0.19275I$	$-10.45590 - 2.33911I$	$-2.00744 + 2.34673I$
$u = -0.05385 - 1.78958I$ $a = 0.899099 - 0.320901I$ $b = 2.19970 - 0.19275I$	$-10.45590 + 2.33911I$	$-2.00744 - 2.34673I$

$$\text{III. } \Gamma_3^u = \langle b - u, a - u, u^2 + u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ -u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u \\ u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 2u + 1 \\ u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u**-Polynomials at the component

Crossings	u -Polynomials at each crossing
c_1, c_3, c_4 c_5, c_{10}	$u^2 - u + 1$
c_2, c_7, c_8 c_9, c_{12}	$u^2 + u + 1$
c_6, c_{11}	u^2

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3 c_4, c_5, c_7 c_8, c_9, c_{10} c_{12}	$y^2 + y + 1$
c_6, c_{11}	y^2

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.500000 + 0.866025I$	0	0
$a = -0.500000 + 0.866025I$		
$b = -0.500000 + 0.866025I$		
$u = -0.500000 - 0.866025I$	0	0
$a = -0.500000 - 0.866025I$		
$b = -0.500000 - 0.866025I$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u^2 - u + 1)(u^6 - 9u^5 + 31u^4 - 56u^3 + 63u^2 - 38u + 9)$ $\cdot (u^{20} + 27u^{19} + \dots - 27u + 1)$
c_2	$(u^2 + u + 1)(u^6 - u^5 + 5u^4 - 4u^3 + 7u^2 - 2u + 3)$ $\cdot (u^{20} + u^{19} + \dots - 11u + 1)$
c_3	$(u^2 - u + 1)(u^6 + u^5 + 5u^4 + 4u^3 + 7u^2 + 2u + 3)$ $\cdot (u^{20} - u^{19} + \dots + 11u + 1)$
c_4	$(u^2 - u + 1)(u^6 + 2u^4 + \dots + 2u^2 + 1)(u^{20} + 2u^{19} + \dots - 27u + 51)$
c_5	$(u^2 - u + 1)(u^6 + u^5 + 5u^4 + 4u^3 + 7u^2 + 2u + 3)$ $\cdot (u^{20} + u^{19} + \dots - 11u + 1)$
c_6	$u^2(u^6 - u^5 + \dots + 6u + 9)(u^{20} + 16u^{18} + \dots - 16u + 52)$
c_7	$(u^2 + u + 1)(u^6 - 3u^5 + u^4 - 2u^3 + 6u^2 + 5u + 1)$ $\cdot (u^{20} - 3u^{19} + \dots + 109u^2 + 21)$
c_8	$(u^2 + u + 1)(u^6 - u^5 + 5u^4 - 4u^3 + 7u^2 - 2u + 3)$ $\cdot (u^{20} - u^{19} + \dots + 11u + 1)$
c_9	$(u^2 + u + 1)(u^6 + 2u^4 + \dots + 2u^2 + 1)(u^{20} - 2u^{19} + \dots + 27u + 51)$
c_{10}	$(u^2 - u + 1)(u^6 - 3u^5 + \dots - 2u + 3)(u^{20} + 5u^{19} + \dots + 57u + 7)$
c_{11}	$u^2(u^6 + u^5 + \dots - 6u + 9)(u^{20} + 16u^{18} + \dots + 16u + 52)$
c_{12}	$(u^2 + u + 1)(u^6 + 3u^5 + \dots + 2u + 3)(u^{20} - 5u^{19} + \dots - 57u + 7)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$(y^2 + y + 1)(y^6 - 19y^5 + 79y^4 + 104y^3 + 271y^2 - 310y + 81)$ $\cdot (y^{20} - 61y^{19} + \dots + 169y + 1)$
c_2, c_3, c_5 c_8	$(y^2 + y + 1)(y^6 + 9y^5 + 31y^4 + 56y^3 + 63y^2 + 38y + 9)$ $\cdot (y^{20} + 27y^{19} + \dots - 27y + 1)$
c_4, c_9	$(y^2 + y + 1)(y^6 + 4y^5 + 8y^4 + y^3 + 8y^2 + 4y + 1)$ $\cdot (y^{20} + 18y^{19} + \dots + 17835y + 2601)$
c_6, c_{11}	$y^2(y^6 + 7y^5 - 4y^4 - 38y^3 + 160y^2 - 180y + 81)$ $\cdot (y^{20} + 32y^{19} + \dots + 7024y + 2704)$
c_7	$(y^2 + y + 1)(y^6 - 7y^5 + y^4 + 40y^3 + 58y^2 - 13y + 1)$ $\cdot (y^{20} - 33y^{19} + \dots + 4578y + 441)$
c_{10}, c_{12}	$(y^2 + y + 1)(y^6 - 9y^5 + 28y^4 - 31y^3 + 21y^2 - 10y + 9)$ $\cdot (y^{20} - 15y^{19} + \dots - 1835y + 49)$