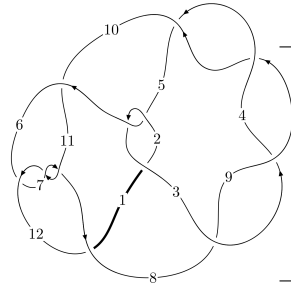
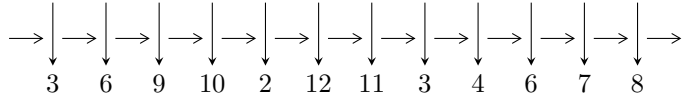


12n₀₄₇₃ (K12n₀₄₇₃)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$3,8 \xrightarrow{c_8} 9 \xrightarrow{c_3} 4 \xrightarrow{c_9} 6,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_5} 5 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 12 \Rightarrow c_4, c_6, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 5447u^8 - 4753u^7 + \dots + 46532b + 23300, -461u^8 - 3128u^7 + \dots + 93064a - 27096, \\ u^9 - 18u^7 - 36u^6 + 12u^5 + 68u^4 + 36u^3 + 8u^2 + 24u + 8 \rangle$$

$$I_2^u = \langle b^3 - b^2 + 1, 2a - u, u^2 - 2 \rangle$$

$$I_1^v = \langle a, v^2 + b - 1, v^3 - v + 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 18 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 5447u^8 - 4753u^7 + \cdots + 46532b + 23300, -461u^8 - 3128u^7 + \cdots + 93064a - 27096, u^9 - 18u^7 + \cdots + 24u + 8 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.00495358u^8 + 0.0336113u^7 + \cdots - 1.27001u + 0.291154 \\ -0.117059u^8 + 0.102145u^7 + \cdots - 0.727843u - 0.500731 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0289801u^8 - 0.0392633u^7 + \cdots - 0.182670u + 0.813977 \\ 0.0609903u^8 - 0.0503739u^7 + \cdots + 1.76017u + 0.788705 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0267235u^8 - 0.0442706u^7 + \cdots + 0.191954u - 0.199347 \\ 0.0998238u^8 - 0.159439u^7 + \cdots + 1.80830u + 0.494198 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.0267235u^8 - 0.0442706u^7 + \cdots + 0.191954u - 0.199347 \\ 0.00758618u^8 - 0.00221353u^7 + \cdots + 0.959598u + 0.140033 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 - 2u \\ u^5 - 3u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0326442u^8 - 0.0442276u^7 + \cdots - 0.952893u + 0.526090 \\ -0.0316341u^8 - 0.0297215u^7 + \cdots - 0.338606u - 0.139173 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0343097u^8 - 0.0464841u^7 + \cdots + 1.15155u - 0.0593140 \\ 0.00758618u^8 - 0.00221353u^7 + \cdots + 0.959598u + 0.140033 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -\frac{20957}{46532}u^8 + \frac{5941}{23266}u^7 + \frac{185067}{23266}u^6 + \frac{274717}{23266}u^5 - \frac{139019}{11633}u^4 - \frac{299261}{11633}u^3 - \frac{57101}{11633}u^2 + \frac{28694}{11633}u - \frac{223158}{11633}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^9 + 73u^8 + \cdots + 729u + 49$
c_2, c_5	$u^9 + 13u^8 + 48u^7 + 72u^6 + 18u^5 - 14u^4 - 40u^3 - 27u - 7$
c_3, c_4, c_8 c_9	$u^9 - 18u^7 - 36u^6 + 12u^5 + 68u^4 + 36u^3 + 8u^2 + 24u + 8$
c_6, c_7, c_{11}	$u^9 + 3u^8 + 7u^7 + 14u^6 + 14u^5 + 25u^4 + 11u^3 + 15u^2 - 1$
c_{10}, c_{12}	$u^9 + 9u^8 - 73u^7 + 56u^6 + 430u^5 - 75u^4 - 417u^3 + 173u^2 + 36u - 13$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^9 - 4393y^8 + \dots + 723913y - 2401$
c_2, c_5	$y^9 - 73y^8 + \dots + 729y - 49$
c_3, c_4, c_8 c_9	$y^9 - 36y^8 + \dots + 448y - 64$
c_6, c_7, c_{11}	$y^9 + 5y^8 - 7y^7 - 128y^6 - 440y^5 - 731y^4 - 601y^3 - 175y^2 + 30y - 1$
c_{10}, c_{12}	$y^9 - 227y^8 + \dots + 5794y - 169$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.186450 + 0.424170I$ $a = 0.251161 + 0.846300I$ $b = 1.76218 + 0.93575I$	$-1.02910 - 2.89378I$	$-13.46616 + 2.37667I$
$u = -1.186450 - 0.424170I$ $a = 0.251161 - 0.846300I$ $b = 1.76218 - 0.93575I$	$-1.02910 + 2.89378I$	$-13.46616 - 2.37667I$
$u = 0.273011 + 0.580428I$ $a = -0.750166 - 0.744053I$ $b = 1.201410 + 0.238186I$	$2.44926 - 1.76826I$	$-8.73509 + 3.07632I$
$u = 0.273011 - 0.580428I$ $a = -0.750166 + 0.744053I$ $b = 1.201410 - 0.238186I$	$2.44926 + 1.76826I$	$-8.73509 - 3.07632I$
$u = 1.44806$ $a = 0.605279$ $b = -0.107770$	-6.65928	-13.3420
$u = -0.347212$ $a = 0.692622$ $b = -0.151972$	-0.501693	-19.7740
$u = -2.09595 + 0.74847I$ $a = 1.180400 - 0.226493I$ $b = 1.57561 - 4.87250I$	$13.5998 + 8.3082I$	$-13.79311 - 2.86755I$
$u = -2.09595 - 0.74847I$ $a = 1.180400 + 0.226493I$ $b = 1.57561 + 4.87250I$	$13.5998 - 8.3082I$	$-13.79311 + 2.86755I$
$u = 4.91794$ $a = -1.66068$ $b = -37.8186$	6.72995	-14.8960

$$\text{II. } I_2^u = \langle b^3 - b^2 + 1, 2a - u, u^2 - 2 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} \frac{1}{2}u \\ b \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{1}{2}bu - 1 \\ -b^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{1}{2}u \\ b + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} \frac{1}{2}u \\ b \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -\frac{1}{2}b^2u - b^2 + \frac{1}{2}u + 1 \\ -b^2 + b + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} b + \frac{1}{2}u \\ b \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4b - 20$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_5	$(u - 1)^6$
c_2	$(u + 1)^6$
c_3, c_4, c_8 c_9	$(u^2 - 2)^3$
c_6, c_7	$(u^3 + u^2 + 2u + 1)^2$
c_{10}, c_{12}	$(u^3 + u^2 - 1)^2$
c_{11}	$(u^3 - u^2 + 2u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y - 1)^6$
c_3, c_4, c_8 c_9	$(y - 2)^6$
c_6, c_7, c_{11}	$(y^3 + 3y^2 + 2y - 1)^2$
c_{10}, c_{12}	$(y^3 - y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.41421$ $a = 0.707107$ $b = 0.877439 + 0.744862I$	$-3.55561 - 2.82812I$	$-16.4902 + 2.9794I$
$u = 1.41421$ $a = 0.707107$ $b = 0.877439 - 0.744862I$	$-3.55561 + 2.82812I$	$-16.4902 - 2.9794I$
$u = 1.41421$ $a = 0.707107$ $b = -0.754878$	-7.69319	-23.0200
$u = -1.41421$ $a = -0.707107$ $b = 0.877439 + 0.744862I$	$-3.55561 - 2.82812I$	$-16.4902 + 2.9794I$
$u = -1.41421$ $a = -0.707107$ $b = 0.877439 - 0.744862I$	$-3.55561 + 2.82812I$	$-16.4902 - 2.9794I$
$u = -1.41421$ $a = -0.707107$ $b = -0.754878$	-7.69319	-23.0200

$$\text{III. } I_1^v = \langle a, v^2 + b - 1, v^3 - v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -v^2 + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -v^2 - v + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} v \\ v^2 - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ v^2 - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v^2 + v \\ v + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v^2 - 1 \\ v^2 - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $-4v^2 - 2v - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)^3$
c_3, c_4, c_8 c_9	u^3
c_5	$(u + 1)^3$
c_6, c_7	$u^3 - u^2 + 2u - 1$
c_{10}, c_{12}	$u^3 - u^2 + 1$
c_{11}	$u^3 + u^2 + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_5	$(y - 1)^3$
c_3, c_4, c_8 c_9	y^3
c_6, c_7, c_{11}	$y^3 + 3y^2 + 2y - 1$
c_{10}, c_{12}	$y^3 - y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^v	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = 0.662359 + 0.562280I$ $a = 0$ $b = 0.877439 - 0.744862I$	$1.37919 + 2.82812I$	$-11.81496 - 4.10401I$
$v = 0.662359 - 0.562280I$ $a = 0$ $b = 0.877439 + 0.744862I$	$1.37919 - 2.82812I$	$-11.81496 + 4.10401I$
$v = -1.32472$ $a = 0$ $b = -0.754878$	-2.75839	-14.3700

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$((u - 1)^9)(u^9 + 73u^8 + \dots + 729u + 49)$
c_2	$(u - 1)^3(u + 1)^6$ $\cdot (u^9 + 13u^8 + 48u^7 + 72u^6 + 18u^5 - 14u^4 - 40u^3 - 27u - 7)$
c_3, c_4, c_8 c_9	$u^3(u^2 - 2)^3(u^9 - 18u^7 + \dots + 24u + 8)$
c_5	$(u - 1)^6(u + 1)^3$ $\cdot (u^9 + 13u^8 + 48u^7 + 72u^6 + 18u^5 - 14u^4 - 40u^3 - 27u - 7)$
c_6, c_7	$(u^3 - u^2 + 2u - 1)(u^3 + u^2 + 2u + 1)^2$ $\cdot (u^9 + 3u^8 + 7u^7 + 14u^6 + 14u^5 + 25u^4 + 11u^3 + 15u^2 - 1)$
c_{10}, c_{12}	$(u^3 - u^2 + 1)(u^3 + u^2 - 1)^2$ $\cdot (u^9 + 9u^8 - 73u^7 + 56u^6 + 430u^5 - 75u^4 - 417u^3 + 173u^2 + 36u - 13)$
c_{11}	$(u^3 - u^2 + 2u - 1)^2(u^3 + u^2 + 2u + 1)$ $\cdot (u^9 + 3u^8 + 7u^7 + 14u^6 + 14u^5 + 25u^4 + 11u^3 + 15u^2 - 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$((y - 1)^9)(y^9 - 4393y^8 + \dots + 723913y - 2401)$
c_2, c_5	$((y - 1)^9)(y^9 - 73y^8 + \dots + 729y - 49)$
c_3, c_4, c_8 c_9	$y^3(y - 2)^6(y^9 - 36y^8 + \dots + 448y - 64)$
c_6, c_7, c_{11}	$(y^3 + 3y^2 + 2y - 1)^3$ $\cdot (y^9 + 5y^8 - 7y^7 - 128y^6 - 440y^5 - 731y^4 - 601y^3 - 175y^2 + 30y - 1)$
c_{10}, c_{12}	$((y^3 - y^2 + 2y - 1)^3)(y^9 - 227y^8 + \dots + 5794y - 169)$