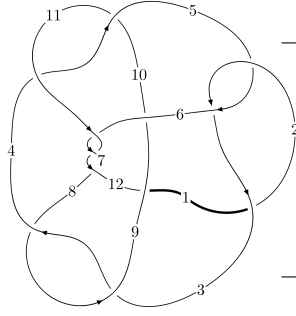
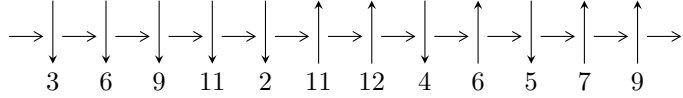


12n<sub>0488</sub> (K12n<sub>0488</sub>)

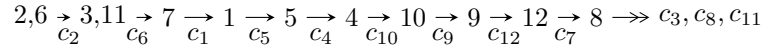


A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^8 - 2u^7 + 3u^6 - 3u^5 + 4u^4 - 3u^3 + 2u^2 + b - u, u^6 - 2u^5 + 2u^4 - u^3 + 2u^2 + a - 2u, \\ u^9 - 3u^8 + 5u^7 - 5u^6 + 6u^5 - 7u^4 + 6u^3 - 2u^2 + u - 1 \rangle$$

$$I_2^u = \langle u^6 + 2u^5 + u^4 - 2u^3 - 2u^2 + b, u^6 + 2u^5 + 2u^4 - u^3 - 2u^2 + a - 2u, u^7 + 2u^6 + 2u^5 - u^4 - u^3 - u^2 - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 16 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle u^8 - 2u^7 + \dots + b - u, u^6 - 2u^5 + 2u^4 - u^3 + 2u^2 + a - 2u, u^9 - 3u^8 + \dots + u - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^6 + 2u^5 - 2u^4 + u^3 - 2u^2 + 2u \\ -u^8 + 2u^7 - 3u^6 + 3u^5 - 4u^4 + 3u^3 - 2u^2 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^7 + u^6 - u^5 + u^4 - 3u^3 + 2u^2 - u + 1 \\ -u^8 + u^7 - u^6 + u^5 - 2u^4 + u^2 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^8 - 2u^7 + 2u^6 - 2u^5 + 3u^4 - 3u^3 + u^2 + 1 \\ u^8 - 3u^7 + 3u^6 - 3u^5 + 4u^4 - 5u^3 + 2u^2 + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^7 - 2u^6 + 3u^5 - 3u^4 + 4u^3 - 3u^2 + 2u - 1 \\ -u^8 + 3u^7 - 4u^6 + 4u^5 - 5u^4 + 6u^3 - 3u^2 + u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^7 - 2u^6 + 3u^5 - 3u^4 + 4u^3 - 3u^2 + 2u - 1 \\ u^7 - 2u^6 + 2u^5 - u^4 + 2u^3 - 2u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^7 - u^6 + u^5 - u^4 + 2u^3 - 2u^2 + u \\ u^8 - u^7 + u^6 - u^5 + u^4 - u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -2u^7 + 4u^6 - 5u^5 + 4u^4 - 8u^3 + 5u^2 - 2u + 2 \\ -u^8 + u^7 - u^5 - 3u^4 + 2u^2 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-5u^8 + 12u^7 - 17u^6 + 12u^5 - 20u^4 + 20u^3 - 13u^2 - 6u - 3$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^9 - u^8 + 7u^7 - 5u^6 + 16u^5 - 7u^4 + 10u^3 + 6u^2 - 3u + 1$
$c_2, c_5$	$u^9 + 3u^8 + 5u^7 + 5u^6 + 6u^5 + 7u^4 + 6u^3 + 2u^2 + u + 1$
$c_3, c_4, c_8$ $c_{10}$	$u^9 - 2u^7 + 4u^6 + 17u^5 + 9u^4 + 9u^3 + 2u^2 + 2u + 1$
$c_6, c_7, c_{11}$	$u^9 + 8u^8 + 27u^7 + 46u^6 + 33u^5 - 10u^4 - 27u^3 - u^2 + 14u + 4$
$c_9, c_{12}$	$u^9 - 4u^8 + 8u^7 - 3u^6 - 2u^4 + 24u^3 - 23u^2 + 9u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^9 + 13y^8 + 71y^7 + 205y^6 + 332y^5 + 291y^4 + 98y^3 - 82y^2 - 3y - 1$
$c_2, c_5$	$y^9 + y^8 + 7y^7 + 5y^6 + 16y^5 + 7y^4 + 10y^3 - 6y^2 - 3y - 1$
$c_3, c_4, c_8$ $c_{10}$	$y^9 - 4y^8 + 38y^7 - 66y^6 + 185y^5 + 201y^4 + 105y^3 + 14y^2 - 1$
$c_6, c_7, c_{11}$	$y^9 - 10y^8 + \dots + 204y - 16$
$c_9, c_{12}$	$y^9 + 40y^7 + 23y^6 + 206y^5 + 10y^4 + 490y^3 - 93y^2 + 127y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.543663 + 0.958634I$ $a = -0.62928 - 1.29649I$ $b = -1.044710 - 0.790946I$	$8.80377 + 2.34106I$	$3.55048 - 3.71378I$
$u = -0.543663 - 0.958634I$ $a = -0.62928 + 1.29649I$ $b = -1.044710 + 0.790946I$	$8.80377 - 2.34106I$	$3.55048 + 3.71378I$
$u = 0.780042$ $a = 0.429639$ $b = -0.0889832$	$-1.02700$	$-12.4430$
$u = 1.022250 + 0.813773I$ $a = 1.249250 - 0.023619I$ $b = 0.74446 + 1.23201I$	$-2.68542 + 1.09922I$	$0.831621 - 0.481760I$
$u = 1.022250 - 0.813773I$ $a = 1.249250 + 0.023619I$ $b = 0.74446 - 1.23201I$	$-2.68542 - 1.09922I$	$0.831621 + 0.481760I$
$u = 0.877200 + 1.062120I$ $a = 0.148693 - 1.372070I$ $b = 1.77486 - 1.66508I$	$-1.87595 - 8.01095I$	$1.68345 + 4.08979I$
$u = 0.877200 - 1.062120I$ $a = 0.148693 + 1.372070I$ $b = 1.77486 + 1.66508I$	$-1.87595 + 8.01095I$	$1.68345 - 4.08979I$
$u = -0.245807 + 0.515171I$ $a = 0.016526 + 1.227710I$ $b = 0.569881 + 0.456696I$	$1.20590 + 0.78253I$	$4.15601 - 2.65874I$
$u = -0.245807 - 0.515171I$ $a = 0.016526 - 1.227710I$ $b = 0.569881 - 0.456696I$	$1.20590 - 0.78253I$	$4.15601 + 2.65874I$

$$\text{II. } I_2^u = \langle u^6 + 2u^5 + u^4 - 2u^3 - 2u^2 + b, u^6 + 2u^5 + 2u^4 - u^3 - 2u^2 + a - 2u, u^7 + 2u^6 + 2u^5 - u^4 - u^3 - u^2 - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^6 - 2u^5 - 2u^4 + u^3 + 2u^2 + 2u \\ -u^6 - 2u^5 - u^4 + 2u^3 + 2u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^6 + 3u^5 + 4u^4 - 3u^2 - 3u \\ u^6 + 2u^5 + 2u^4 - 2u^3 - 2u^2 + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ -u^4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^5 + 2u^4 + 2u^3 - u^2 - u - 1 \\ u^6 + 2u^5 + 2u^4 - u^3 - u^2 - u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^5 - 2u^4 - u^3 + 2u^2 + 2u \\ -u^5 - u^4 + 2u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^5 - 2u^4 - u^3 + 2u^2 + 2u \\ u^3 + u^2 - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u^6 + 3u^5 + 4u^4 + u^3 - 3u^2 - 3u - 1 \\ u^6 + 2u^5 + u^4 - 2u^3 - 2u^2 - u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^5 - 2u^4 - 2u^3 + u^2 + 2u + 2 \\ -u^4 + u^2 + 2u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $3u^6 + 5u^5 + 3u^4 - 5u^3 - u^2 - u + 3$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^7 + 6u^5 - u^4 + 3u^3 - 3u^2 - 2u - 1$
$c_2$	$u^7 + 2u^6 + 2u^5 - u^4 - u^3 - u^2 - 1$
$c_3, c_{10}$	$u^7 + u^6 + 4u^5 + 3u^4 + 6u^3 + 2u^2 + 3u - 1$
$c_4, c_8$	$u^7 - u^6 + 4u^5 - 3u^4 + 6u^3 - 2u^2 + 3u + 1$
$c_5$	$u^7 - 2u^6 + 2u^5 + u^4 - u^3 + u^2 + 1$
$c_6, c_7$	$u^7 - 5u^5 + 7u^3 - u + 1$
$c_9, c_{12}$	$u^7 + 3u^6 - 8u^4 - 4u^3 + 8u^2 + 4u - 3$
$c_{11}$	$u^7 - 5u^5 + 7u^3 - u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^7 + 12y^6 + 42y^5 + 31y^4 - 21y^3 - 23y^2 - 2y - 1$
$c_2, c_5$	$y^7 + 6y^5 - y^4 + 3y^3 - 3y^2 - 2y - 1$
$c_3, c_4, c_8$ $c_{10}$	$y^7 + 7y^6 + 22y^5 + 41y^4 + 50y^3 + 38y^2 + 13y - 1$
$c_6, c_7, c_{11}$	$y^7 - 10y^6 + 39y^5 - 72y^4 + 59y^3 - 14y^2 + y - 1$
$c_9, c_{12}$	$y^7 - 9y^6 + 40y^5 - 104y^4 + 162y^3 - 144y^2 + 64y - 9$



(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.679131 + 0.739231I$ $a = -0.090421 + 0.468757I$ $b = 1.067080 - 0.219644I$	$4.71019 + 2.40933I$	$0.29860 - 3.62563I$
$u = -0.679131 - 0.739231I$ $a = -0.090421 - 0.468757I$ $b = 1.067080 + 0.219644I$	$4.71019 - 2.40933I$	$0.29860 + 3.62563I$
$u = 0.939920$ $a = 0.759448$ $b = 0.490461$	$-0.502424$	$5.10270$
$u = 0.273857 + 0.616814I$ $a = -0.63288 + 2.30893I$ $b = -1.49346 + 0.77301I$	$9.14166 - 1.05666I$	$5.26558 - 1.27318I$
$u = 0.273857 - 0.616814I$ $a = -0.63288 - 2.30893I$ $b = -1.49346 - 0.77301I$	$9.14166 + 1.05666I$	$5.26558 + 1.27318I$
$u = -1.06469 + 1.08838I$ $a = -0.656418 - 0.759679I$ $b = -1.318850 - 0.288008I$	$11.07340 + 3.97449I$	$4.88445 - 3.30547I$
$u = -1.06469 - 1.08838I$ $a = -0.656418 + 0.759679I$ $b = -1.318850 + 0.288008I$	$11.07340 - 3.97449I$	$4.88445 + 3.30547I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^7 + 6u^5 - u^4 + 3u^3 - 3u^2 - 2u - 1)$ $\cdot (u^9 - u^8 + 7u^7 - 5u^6 + 16u^5 - 7u^4 + 10u^3 + 6u^2 - 3u + 1)$
$c_2$	$(u^7 + 2u^6 + 2u^5 - u^4 - u^3 - u^2 - 1)$ $\cdot (u^9 + 3u^8 + 5u^7 + 5u^6 + 6u^5 + 7u^4 + 6u^3 + 2u^2 + u + 1)$
$c_3, c_{10}$	$(u^7 + u^6 + 4u^5 + 3u^4 + 6u^3 + 2u^2 + 3u - 1)$ $\cdot (u^9 - 2u^7 + 4u^6 + 17u^5 + 9u^4 + 9u^3 + 2u^2 + 2u + 1)$
$c_4, c_8$	$(u^7 - u^6 + 4u^5 - 3u^4 + 6u^3 - 2u^2 + 3u + 1)$ $\cdot (u^9 - 2u^7 + 4u^6 + 17u^5 + 9u^4 + 9u^3 + 2u^2 + 2u + 1)$
$c_5$	$(u^7 - 2u^6 + 2u^5 + u^4 - u^3 + u^2 + 1)$ $\cdot (u^9 + 3u^8 + 5u^7 + 5u^6 + 6u^5 + 7u^4 + 6u^3 + 2u^2 + u + 1)$
$c_6, c_7$	$(u^7 - 5u^5 + 7u^3 - u + 1)$ $\cdot (u^9 + 8u^8 + 27u^7 + 46u^6 + 33u^5 - 10u^4 - 27u^3 - u^2 + 14u + 4)$
$c_9, c_{12}$	$(u^7 + 3u^6 - 8u^4 - 4u^3 + 8u^2 + 4u - 3)$ $\cdot (u^9 - 4u^8 + 8u^7 - 3u^6 - 2u^4 + 24u^3 - 23u^2 + 9u + 1)$
$c_{11}$	$(u^7 - 5u^5 + 7u^3 - u - 1)$ $\cdot (u^9 + 8u^8 + 27u^7 + 46u^6 + 33u^5 - 10u^4 - 27u^3 - u^2 + 14u + 4)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^7 + 12y^6 + 42y^5 + 31y^4 - 21y^3 - 23y^2 - 2y - 1)$ $\cdot (y^9 + 13y^8 + 71y^7 + 205y^6 + 332y^5 + 291y^4 + 98y^3 - 82y^2 - 3y - 1)$
$c_2, c_5$	$(y^7 + 6y^5 - y^4 + 3y^3 - 3y^2 - 2y - 1)$ $\cdot (y^9 + y^8 + 7y^7 + 5y^6 + 16y^5 + 7y^4 + 10y^3 - 6y^2 - 3y - 1)$
$c_3, c_4, c_8$ $c_{10}$	$(y^7 + 7y^6 + 22y^5 + 41y^4 + 50y^3 + 38y^2 + 13y - 1)$ $\cdot (y^9 - 4y^8 + 38y^7 - 66y^6 + 185y^5 + 201y^4 + 105y^3 + 14y^2 - 1)$
$c_6, c_7, c_{11}$	$(y^7 - 10y^6 + 39y^5 - 72y^4 + 59y^3 - 14y^2 + y - 1)$ $\cdot (y^9 - 10y^8 + \dots + 204y - 16)$
$c_9, c_{12}$	$(y^7 - 9y^6 + 40y^5 - 104y^4 + 162y^3 - 144y^2 + 64y - 9)$ $\cdot (y^9 + 40y^7 + 23y^6 + 206y^5 + 10y^4 + 490y^3 - 93y^2 + 127y - 1)$