# $12n_{0514}$ (K12 $n_{0514}$ )



A knot diagram<sup>1</sup>

#### Ideals for irreducible components<sup>2</sup> of $X_{par}$

$$\begin{split} I_1^u &= \langle -8.97013 \times 10^{55} u^{29} - 1.58329 \times 10^{56} u^{28} + \dots + 4.35231 \times 10^{58} b + 6.55011 \times 10^{57}, \\ & 3.18509 \times 10^{57} u^{29} - 1.03463 \times 10^{58} u^{28} + \dots + 1.82362 \times 10^{61} a + 1.17215 \times 10^{61}, \\ & u^{30} + 2u^{29} + \dots + 100u - 419 \rangle \\ I_2^u &= \langle -5u^{12} + 21u^{10} - 7u^9 - 18u^8 + 33u^7 - 17u^6 - 26u^5 + 26u^4 + 7u^3 - 15u^2 + 2b + 3u + 5, \\ & 11u^{12} + 2u^{11} - 48u^{10} + 6u^9 + 49u^8 - 64u^7 + 21u^6 + 72u^5 - 53u^4 - 32u^3 + 37u^2 + 2a - u - 14, \\ & u^{13} + u^{12} - 4u^{11} - 3u^{10} + 4u^9 - 2u^8 - 2u^7 + 7u^6 + u^5 - 6u^4 + 2u^2 - u - 1 \rangle \end{split}$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 43 representations.

<sup>&</sup>lt;sup>1</sup>The image of knot diagram is generated by the software "**Draw programme**" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).

 $<sup>^{2}</sup>$ All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

1 0  $a_6 =$  $a_{11} =$  $\begin{array}{l} -0.000174658u^{29} + 0.000567352u^{28} + \dots + 1.47843u - 0.642763 \\ 0.00206100u^{29} + 0.00363781u^{28} + \dots - 0.596168u - 0.150497 \end{array} \right)$  $a_{3} =$  $u^2$  $a_7 =$  $\begin{array}{l} (0.00188635u^{29} + 0.00420517u^{28} + \dots + 0.882267u - 0.793260) \\ (0.00206100u^{29} + 0.00363781u^{28} + \dots - 0.596168u - 0.150497) \end{array}$  $a_2 =$  $(0.00358201u^{29} + 0.00533243u^{28} + \dots - 0.845448u + 0.146579)$  $-0.00430260u^{29} - 0.00434093u^{28} + \dots + 2.70318u - 1.08487$  $a_1 =$  $0.0000550185u^{29} + 0.00136950u^{28} + \dots + 0.855142u - 0.322525$  $-0.000908531u^{29} + 0.0000579815u^{28} + \dots + 0.0808855u - 1.03300$  $a_{5} =$  $0.000107308u^{29} + 0.000594620u^{28} + \dots + 0.877150u + 0.182757$  $0.0000965840u^{29} + 0.00130720u^{28} + \dots - 0.0289697u - 0.664503$  $a_4 =$  $\begin{array}{c} -0.0000748679u^{29} + 0.000914934u^{28} + \dots + 0.654950u + 0.759505 \\ -0.00255893u^{29} - 0.00377164u^{28} + \dots + 0.375116u - 0.944810 \end{array} \right)$  $a_8 =$  $a_{10} =$  $-0.0000732909u^{29} - 0.00133981u^{28} + \dots - 1.16207u - 0.158293$  $0.00125946u^{29} + 0.00337516u^{28} + \dots - 0.328027u + 0.0230528$  $a_9 =$  $\begin{array}{l} 0.00156530u^{29} + 0.00377669u^{28} + \dots - 0.300258u - 0.872709 \\ - 0.00228589u^{29} - 0.00278519u^{28} + \dots + 2.15799u - 0.0655795 \end{array}$  $a_{12} =$ 

I.  $I_1^u = \langle -8.97 \times 10^{55} u^{29} - 1.58 \times 10^{56} u^{28} + \dots + 4.35 \times 10^{58} b + 6.55 \times 10^{57}, \ 3.19 \times 10^{57} u^{29} - 1.03 \times 10^{58} u^{28} + \dots + 1.82 \times 10^{61} a + 1.17 \times 10^{61}, \ u^{30} + 2u^{29} + \dots + 100u - 419 \rangle$ 

(ii) Obstruction class = -1

(i) Arc colorings

(iii) Cusp Shapes =  $0.000964221u^{29} + 0.00738326u^{28} + \dots + 11.2158u + 0.582373$ 

Crossings	u-Polynomials at each crossing
$c_1$	$u^{30} + 54u^{29} + \dots + 35644u + 961$
$c_2, c_5$	$u^{30} + 2u^{29} + \dots + 274u + 31$
$c_{3}, c_{9}$	$u^{30} - u^{29} + \dots - 18u - 9$
$c_4, c_7$	$u^{30} + 7u^{29} + \dots - 58u + 7$
$c_6, c_{10}$	$u^{30} + 2u^{29} + \dots + 100u - 419$
$c_8, c_{11}$	$u^{30} - u^{29} + \dots - u - 1$
c <sub>12</sub>	$u^{30} + 3u^{29} + \dots + 276288u - 31624$

#### (iv) u-Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{30} - 166y^{29} + \dots + 2665988060y + 923521$
$c_2, c_5$	$y^{30} - 54y^{29} + \dots - 35644y + 961$
$c_3, c_9$	$y^{30} + 47y^{29} + \dots + 972y + 81$
$c_4, c_7$	$y^{30} + 23y^{29} + \dots - 1614y + 49$
$c_{6}, c_{10}$	$y^{30} + 10y^{29} + \dots + 590846y + 175561$
$c_8, c_{11}$	$y^{30} - 21y^{29} + \dots - 19y + 1$
c <sub>12</sub>	$y^{30} + 121y^{29} + \dots + 1307553376y + 1000077376$

## $(\mathbf{v})$ Riley Polynomials at the component

(vi)	Complex	Volumes	and	Cusp	Shapes	

Solutions to $I_1^u$	$\sqrt{-1}(\operatorname{vol}+\sqrt{-1}CS)$	Cusp shape
u = 0.642590 + 0.700606I		
a = 0.106716 - 1.072760I	0.82927 + 4.60566I	7.38656 - 8.01596I
b = -0.347246 + 1.044670I		
u = 0.642590 - 0.700606I		
a = 0.106716 + 1.072760I	0.82927 - 4.60566I	7.38656 + 8.01596I
b = -0.347246 - 1.044670I		
u = -0.814116 + 0.677327I		
a = 0.504066 + 1.067370I	-0.77900 - 2.06540I	3.22171 + 2.38317I
b = -0.549219 - 0.145896I		
u = -0.814116 - 0.677327I		
a = 0.504066 - 1.067370I	-0.77900 + 2.06540I	3.22171 - 2.38317I
b = -0.549219 + 0.145896I		
u = 0.560922 + 0.747663I		
a = 0.472626 - 0.864157I	0.327633 - 0.843648I	6.72873 + 1.86017I
b = -0.104866 + 0.109501I		
u = 0.560922 - 0.747663I		
a = 0.472626 + 0.864157I	0.327633 + 0.843648I	6.72873 - 1.86017I
b = -0.104866 - 0.109501I		
u = -0.055990 + 1.128490I		
a = -0.924318 + 0.178825I	-10.40080 + 1.46441I	-1.99581 - 5.01569I
b = 2.41962 - 0.23089I		
u = -0.055990 - 1.128490I		
a = -0.924318 - 0.178825I	-10.40080 - 1.46441I	-1.99581 + 5.01569I
b = 2.41962 + 0.23089I		
u = -0.586638 + 0.553835I		
a = 0.155793 + 1.119640I	-1.29989 - 1.54235I	1.52237 + 4.53495I
b = -0.651578 - 0.537140I		
u = -0.586638 - 0.553835I		
a = 0.155793 - 1.119640I	-1.29989 + 1.54235I	1.52237 - 4.53495I
b = -0.651578 + 0.537140I		

Solutions to $I_1^u$	$\sqrt{-1}(\operatorname{vol}+\sqrt{-1}CS)$	Cusp shape	
u = 1.307100 + 0.036349I			
a = 0.71975 + 1.63357I	3.26183 - 2.73720I	10.18982 + 2.92398I	
b = -0.798397 - 0.708430I			
u = 1.307100 - 0.036349I			
a = 0.71975 - 1.63357I	3.26183 + 2.73720I	10.18982 - 2.92398I	
b = -0.798397 + 0.708430I			
u = -0.049314 + 1.329620I			
a = -0.356304 + 0.123824I	-11.24640 - 1.91319I	0.75047 + 3.50106I	
b = 1.85890 - 0.07524I			
u = -0.049314 - 1.329620I			
a = -0.356304 - 0.123824I	-11.24640 + 1.91319I	0.75047 - 3.50106I	
b = 1.85890 + 0.07524I			
u = 0.403283 + 1.277970I			
a = -0.507314 - 0.949307I	-3.40270 - 3.64668I	2.86245 + 2.46962I	
b = 1.40638 + 0.97678I			
u = 0.403283 - 1.277970I			
a = -0.507314 + 0.949307I	-3.40270 + 3.64668I	2.86245 - 2.46962I	
b = 1.40638 - 0.97678I			
u = -0.276632 + 1.333170I			
a = -0.334409 + 0.791751I	-7.55076 - 1.32763I	-0.010757 + 0.862501I	
b = 1.39749 - 0.61314I			
u = -0.276632 - 1.333170I			
a = -0.334409 - 0.791751I	-7.55076 + 1.32763I	-0.010757 - 0.862501I	
b = 1.39749 + 0.61314I			
u = -0.309884 + 0.543530I			
a = -0.220039 + 0.852834I	-1.56864 - 1.53975I	1.10369 + 4.69285I	
b = -0.933653 - 0.345827I			
u = -0.309884 - 0.543530I			
a = -0.220039 - 0.852834I	-1.56864 + 1.53975I	1.10369 - 4.69285I	
b = -0.933653 + 0.345827I			

Solutions to $I_1^u$	$\sqrt{-1}(\operatorname{vol}+\sqrt{-1}CS)$	Cusp shape
u = 0.242225 + 1.368910I		
a = -0.111633 - 0.819227I	-4.09460 + 6.61711I	2.97271 - 4.66549I
b = 1.153510 + 0.418732I		
u = 0.242225 - 1.368910I		
a = -0.111633 + 0.819227I	-4.09460 - 6.61711I	2.97271 + 4.66549I
b = 1.153510 - 0.418732I		
u = 0.531314		
a = 0.442861	0.719441	14.3760
b = 0.183744		
u = -1.55692		
a = -0.621196	7.16181	20.2020
b = 0.986893		
u = -1.34575 + 1.55021I		
a = 1.43706 + 0.93333I	-15.4447 - 11.8067I	3.77024 + 5.11220I
b = -2.22516 - 0.41486I		
u = -1.34575 - 1.55021I		
a = 1.43706 - 0.93333I	-15.4447 + 11.8067I	3.77024 - 5.11220I
b = -2.22516 + 0.41486I		
u = 1.48358 + 1.48152I		
a = 1.42930 - 1.02156I	-19.4159 + 5.5271I	1.12565 - 2.12056I
b = -2.15106 + 0.44424I		
u = 1.48358 - 1.48152I		
a = 1.42930 + 1.02156I	-19.4159 - 5.5271I	1.12565 + 2.12056I
b = -2.15106 - 0.44424I		
u = -1.68857 + 1.42229I		
a = 1.44579 + 1.14500I	-14.5803 + 0.6531I	6.00000 + 0.I
b = -2.06005 - 0.54414I		
u = -1.68857 - 1.42229I		
a = 1.44579 - 1.14500I	-14.5803 - 0.6531I	6.00000 + 0.I
b = -2.06005 + 0.54414I		

$$\begin{aligned} \text{II. } I_2^u &= \\ \langle -5u^{12} + 21u^{10} + \dots + 2b + 5, \ 11u^{12} + 2u^{11} + \dots + 2a - 14, \ u^{13} + u^{12} + \dots - u - 1 \rangle \end{aligned}$$
(i) Arc colorings
$$a_6 &= \begin{pmatrix} 1 \\ 0 \\ u \\ a_{11} &= \begin{pmatrix} 0 \\ u \\ \end{pmatrix} \\a_{31} &= \begin{pmatrix} -\frac{11}{2}u^{12} - u^{11} + \dots + \frac{1}{2}u + 7 \\ \frac{5}{2}u^{12} - \frac{21}{2}u^{10} + \dots - \frac{3}{2}u - \frac{5}{2} \end{pmatrix} \\a_7 &= \begin{pmatrix} 1 \\ -u^2 \\ \frac{5}{2}u^{12} - \frac{21}{2}u^{10} + \dots - \frac{3}{2}u - \frac{5}{2} \end{pmatrix} \\a_1 &= \begin{pmatrix} -\frac{3}{2}u^{12} - u^{11} + \dots - u + \frac{9}{2} \\ \frac{3}{2}u^{12} + \frac{1}{2}u^{11} + \dots - 2u - \frac{3}{2} \end{pmatrix} \\a_5 &= \begin{pmatrix} 2u^{12} + u^{11} + \dots + u^2 - \frac{3}{2} \\ \frac{5}{2}u^{12} + \frac{1}{2}u^{11} + \dots + \frac{17}{2}u^2 - \frac{7}{2} \end{pmatrix} \\a_4 &= \begin{pmatrix} -u^{12} + 5u^{10} - u^9 - 7u^8 + 6u^7 - 9u^5 + 6u^4 + 7u^3 - 6u^2 - 2u + 3 \\ -3u^{12} - u^{11} + \dots + \frac{3}{2}u + \frac{9}{2} \end{pmatrix} \\a_{10} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\a_{10} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\a_{10} &= \begin{pmatrix} -u \\ u \end{pmatrix} \\a_{12} &= \begin{pmatrix} -\frac{12}{2}u^{12} + \frac{3}{2}u^{11} + \dots + 4u - 2 \\ -u^{12} - \frac{12}{2}u^{11} + \dots + \frac{1}{2}u + 2 \end{pmatrix} \\a_{12} &= \begin{pmatrix} -4u^{12} - 2u^{11} + \dots + 4u^2 + \frac{13}{2} \\ 4u^{12} + \frac{1}{2}u^{11} + \dots - \frac{7}{2}u - 3 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $3u^{12} - 4u^{11} - \frac{21}{2}u^{10} + \frac{39}{2}u^9 - \frac{7}{2}u^8 - \frac{51}{2}u^7 + 42u^6 - 15u^5 - \frac{41}{2}u^4 + \frac{41}{2}u^3 - 3u^2 - 12u + \frac{21}{2}u^6 - \frac{15}{2}u^7 + \frac{12}{2}u^6 - \frac{15}{2}u^7 + \frac{12}{2}u^7 +$  (iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{13} - 13u^{12} + \dots + 7u - 1$
<i>C</i> <sub>2</sub>	$u^{13} + 3u^{12} + \dots - 3u - 1$
$c_3$	$u^{13} + 8u^{11} + \dots + 3u + 1$
<i>C</i> 4	$u^{13} + 2u^{11} + \dots + 3u + 1$
C5	$u^{13} - 3u^{12} + \dots - 3u + 1$
<i>c</i> <sub>6</sub>	$u^{13} + u^{12} + \dots - u - 1$
<i>C</i> <sub>7</sub>	$u^{13} + 2u^{11} + \dots + 3u - 1$
<i>c</i> <sub>8</sub>	$u^{13} - 6u^{11} + \dots - 2u - 3$
<i>C</i> 9	$u^{13} + 8u^{11} + \dots + 3u - 1$
$c_{10}$	$u^{13} - u^{12} + \dots - u + 1$
$c_{11}$	$u^{13} - 6u^{11} + \dots - 2u + 3$
$c_{12}$	$u^{13} - 2u^{12} + \dots - 13u + 1$

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{13} - 37y^{12} + \dots + 11y - 1$
$c_2, c_5$	$y^{13} - 13y^{12} + \dots + 7y - 1$
$c_{3}, c_{9}$	$y^{13} + 16y^{12} + \dots - 5y - 1$
$c_4, c_7$	$y^{13} + 4y^{12} + \dots + y - 1$
$c_6, c_{10}$	$y^{13} - 9y^{12} + \dots + 5y - 1$
$c_8, c_{11}$	$y^{13} - 12y^{12} + \dots + 46y - 9$
c <sub>12</sub>	$y^{13} + 30y^{12} + \dots + 25y - 1$

## $(\mathbf{v})$ Riley Polynomials at the component

## (vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\operatorname{vol} + \sqrt{-1}CS)$	Cusp shape
u = 0.954573 + 0.260088I		
a = -0.92363 - 1.20575I	-3.98060 + 1.00568I	1.162112 - 0.615451I
$b=\ \ 0.582097 - 0.018888 I$		
u = 0.954573 - 0.260088I		
a = -0.92363 + 1.20575I	-3.98060 - 1.00568I	1.162112 + 0.615451I
b = 0.582097 + 0.018888I		
u = 0.266976 + 1.054200I		
a = -0.532456 + 0.412592I	-9.61091 - 1.01135I	7.06702 - 0.15470I
b = 2.10432 - 0.01987I		
u = 0.266976 - 1.054200I		
a = -0.532456 - 0.412592I	-9.61091 + 1.01135I	7.06702 + 0.15470I
b = 2.10432 + 0.01987I		
u = -0.752928 + 0.297393I		
a = 1.030040 + 0.709707I	-0.796848 - 0.470467I	2.94539 - 1.34493I
b = -0.921610 - 0.177058I		
u = -0.752928 - 0.297393I		
a = 1.030040 - 0.709707I	-0.796848 + 0.470467I	2.94539 + 1.34493I
b = -0.921610 + 0.177058I		
u = -0.684151 + 0.344382I		
a = -1.27505 + 0.67741I	-1.36517 - 5.98644I	4.94299 + 5.64527I
b = 0.314319 + 0.549467I		
u = -0.684151 - 0.344382I		
a = -1.27505 - 0.67741I	-1.36517 + 5.98644I	4.94299 - 5.64527I
b = 0.314319 - 0.549467I		
u = 0.460968 + 0.533555I		
a = 0.56985 - 1.90658I	0.43653 + 3.26322I	5.30243 - 3.80898I
b = -0.813036 + 0.713273I		
u = 0.460968 - 0.533555I		
a = 0.56985 + 1.90658I	0.43653 - 3.26322I	5.30243 + 3.80898I
b = -0.813036 - 0.713273I		

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Solutions to $I_2^u$	$\sqrt{-1}(\mathrm{vol} + \sqrt{-1}CS)$	Cusp shape
u = -1.60034 + 0.28645I		
a = -0.84754 + 1.61343I	2.06490 + 2.83942I	2.96766 - 2.65257I
b = 0.858896 - 0.743211I		
u = -1.60034 - 0.28645I		
a = -0.84754 - 1.61343I	2.06490 - 2.83942I	2.96766 + 2.65257I
b = 0.858896 + 0.743211I		
u = 1.70981		
a = 0.957563	6.76499	-0.775210
b = -1.24998		

III. u-Polynomials		
Crossings	u-Polynomials at each crossing	
$c_1$	$(u^{13} - 13u^{12} + \dots + 7u - 1)(u^{30} + 54u^{29} + \dots + 35644u + 961)$	
<i>C</i> <sub>2</sub>	$(u^{13} + 3u^{12} + \dots - 3u - 1)(u^{30} + 2u^{29} + \dots + 274u + 31)$	
<i>C</i> 3	$(u^{13} + 8u^{11} + \dots + 3u + 1)(u^{30} - u^{29} + \dots - 18u - 9)$	
<i>C</i> <sub>4</sub>	$(u^{13} + 2u^{11} + \dots + 3u + 1)(u^{30} + 7u^{29} + \dots - 58u + 7)$	
<i>C</i> <sub>5</sub>	$(u^{13} - 3u^{12} + \dots - 3u + 1)(u^{30} + 2u^{29} + \dots + 274u + 31)$	
<i>c</i> <sub>6</sub>	$(u^{13} + u^{12} + \dots - u - 1)(u^{30} + 2u^{29} + \dots + 100u - 419)$	
<i>C</i> <sub>7</sub>	$(u^{13} + 2u^{11} + \dots + 3u - 1)(u^{30} + 7u^{29} + \dots - 58u + 7)$	
<i>c</i> <sub>8</sub>	$(u^{13} - 6u^{11} + \dots - 2u - 3)(u^{30} - u^{29} + \dots - u - 1)$	
<i>C</i> 9	$(u^{13} + 8u^{11} + \dots + 3u - 1)(u^{30} - u^{29} + \dots - 18u - 9)$	
$c_{10}$	$(u^{13} - u^{12} + \dots - u + 1)(u^{30} + 2u^{29} + \dots + 100u - 419)$	
$c_{11}$	$(u^{13} - 6u^{11} + \dots - 2u + 3)(u^{30} - u^{29} + \dots - u - 1)$	
c <sub>12</sub>	$(u^{13} - 2u^{12} + \dots - 13u + 1)(u^{30} + 3u^{29} + \dots + 276288u - 31624)$ 15	

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{13} - 37y^{12} + \dots + 11y - 1)$ $\cdot (y^{30} - 166y^{29} + \dots + 2665988060y + 923521)$
$c_2, c_5$	$(y^{13} - 13y^{12} + \dots + 7y - 1)(y^{30} - 54y^{29} + \dots - 35644y + 961)$
$c_3, c_9$	$(y^{13} + 16y^{12} + \dots - 5y - 1)(y^{30} + 47y^{29} + \dots + 972y + 81)$
$c_4, c_7$	$(y^{13} + 4y^{12} + \dots + y - 1)(y^{30} + 23y^{29} + \dots - 1614y + 49)$
$c_6, c_{10}$	$(y^{13} - 9y^{12} + \dots + 5y - 1)(y^{30} + 10y^{29} + \dots + 590846y + 175561)$
$c_8, c_{11}$	$(y^{13} - 12y^{12} + \dots + 46y - 9)(y^{30} - 21y^{29} + \dots - 19y + 1)$
$c_{12}$	$(y^{13} + 30y^{12} + \dots + 25y - 1)$ $\cdot (y^{30} + 121y^{29} + \dots + 1307553376y + 1000077376)$

IV. Riley Polynomials