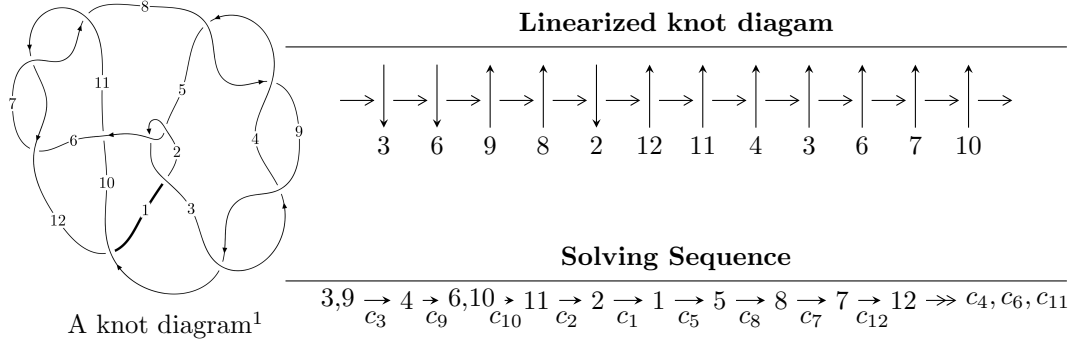


12n<sub>0523</sub> (K12n<sub>0523</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2237795u^{14} - 2035326u^{13} + \dots + 214299626b - 45089178, \\ -5439477u^{14} - 13822761u^{13} + \dots + 857198504a - 455155360, u^{15} + u^{14} + \dots - 24u^2 + 8 \rangle$$

$$I_2^u = \langle b + 1, 4a^3 - 2a^2u + 12a^2 - 4au + 12a - 3u + 4, u^2 + 2 \rangle$$

$$I_1^v = \langle a, b - 1, v^3 + v^2 - 1 \rangle$$

\* 3 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 24 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle -2.24 \times 10^6 u^{14} - 2.04 \times 10^6 u^{13} + \dots + 2.14 \times 10^8 b - 4.51 \times 10^7, -5.44 \times 10^6 u^{14} - 1.38 \times 10^7 u^{13} + \dots + 8.57 \times 10^8 a - 4.55 \times 10^8, u^{15} + u^{14} + \dots - 24u^2 + 8 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.00634564u^{14} + 0.0161255u^{13} + \dots - 1.29993u + 0.530980 \\ 0.0104424u^{14} + 0.00949757u^{13} + \dots + 0.658438u + 0.210403 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.0534854u^{14} + 0.0891983u^{13} + \dots + 0.512158u - 1.09323 \\ -0.0306520u^{14} - 0.0138981u^{13} + \dots + 1.32388u + 0.760098 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0409458u^{14} + 0.0558447u^{13} + \dots - 0.692253u + 0.663144 \\ -0.0540665u^{14} - 0.0698196u^{13} + \dots - 0.280107u - 0.0129726 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0131207u^{14} - 0.0139749u^{13} + \dots - 0.972359u + 0.650171 \\ -0.0540665u^{14} - 0.0698196u^{13} + \dots - 0.280107u - 0.0129726 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^2 + 1 \\ -u^4 - 2u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.0757597u^{14} - 0.0957170u^{13} + \dots + 0.656898u + 1.36357 \\ 0.0170459u^{14} + 0.0203363u^{13} + \dots + 0.767262u + 0.281197 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.00634564u^{14} + 0.0161255u^{13} + \dots - 1.29993u + 0.530980 \\ -0.0346001u^{14} - 0.0397191u^{13} + \dots - 0.607673u - 0.132164 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = \frac{107735653}{428599252} u^{14} + \frac{61824743}{428599252} u^{13} + \dots - \frac{778177628}{107149813} u + \frac{655579008}{107149813}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{15} + 32u^{14} + \dots + 6478u + 289$
$c_2, c_5$	$u^{15} + 4u^{14} + \dots + 52u - 17$
$c_3, c_4, c_8$ $c_9$	$u^{15} - u^{14} + \dots + 24u^2 - 8$
$c_6, c_7, c_{11}$	$u^{15} - 2u^{14} + \dots + u - 3$
$c_{10}$	$u^{15} + 2u^{14} + \dots + 77u - 87$
$c_{12}$	$u^{15} - 2u^{14} + \dots - 127u - 171$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{15} - 88y^{14} + \dots + 29457142y - 83521$
$c_2, c_5$	$y^{15} - 32y^{14} + \dots + 6478y - 289$
$c_3, c_4, c_8$ $c_9$	$y^{15} + 29y^{14} + \dots + 384y - 64$
$c_6, c_7, c_{11}$	$y^{15} + 18y^{14} + \dots + 7y - 9$
$c_{10}$	$y^{15} + 26y^{14} + \dots - 75329y - 7569$
$c_{12}$	$y^{15} + 50y^{14} + \dots - 77237y - 29241$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.218267 + 1.045140I$ $a = -0.313995 + 0.477157I$ $b = 0.671441 - 0.644775I$	$-6.94499 + 3.31343I$	$-0.90808 - 3.10960I$
$u = -0.218267 - 1.045140I$ $a = -0.313995 - 0.477157I$ $b = 0.671441 + 0.644775I$	$-6.94499 - 3.31343I$	$-0.90808 + 3.10960I$
$u = 0.097863 + 0.602652I$ $a = 0.107862 - 0.284601I$ $b = 0.722048 + 0.340057I$	$-1.30578 - 1.09993I$	$-0.13148 + 4.47979I$
$u = 0.097863 - 0.602652I$ $a = 0.107862 + 0.284601I$ $b = 0.722048 - 0.340057I$	$-1.30578 + 1.09993I$	$-0.13148 - 4.47979I$
$u = 0.585051 + 0.119200I$ $a = 1.13543 + 1.12186I$ $b = -0.446783 - 0.537153I$	$-3.77822 + 2.04196I$	$4.64535 - 1.53079I$
$u = 0.585051 - 0.119200I$ $a = 1.13543 - 1.12186I$ $b = -0.446783 + 0.537153I$	$-3.77822 - 2.04196I$	$4.64535 + 1.53079I$
$u = 0.18120 + 1.44491I$ $a = -0.956860 - 0.227359I$ $b = -1.212370 - 0.335064I$	$-7.73448 + 0.54824I$	$-1.59243 - 0.48598I$
$u = 0.18120 - 1.44491I$ $a = -0.956860 + 0.227359I$ $b = -1.212370 + 0.335064I$	$-7.73448 - 0.54824I$	$-1.59243 + 0.48598I$
$u = -0.321204$ $a = 1.40589$ $b = -0.228997$	$0.692564$	$15.0030$
$u = -0.71797 + 1.87258I$ $a = -0.566365 + 0.445862I$ $b = -2.21916 + 0.81697I$	$-16.8214 - 1.5623I$	$-1.46630 + 0.66617I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.71797 - 1.87258I$		
$a = -0.566365 - 0.445862I$	$-16.8214 + 1.5623I$	$-1.46630 - 0.66617I$
$b = -2.21916 - 0.81697I$		
$u = -0.39582 + 2.04334I$		
$a = 1.144260 - 0.389222I$	$9.61396 - 8.62358I$	$-1.03984 + 3.00810I$
$b = 2.23977 + 0.72183I$		
$u = -0.39582 - 2.04334I$		
$a = 1.144260 + 0.389222I$	$9.61396 + 8.62358I$	$-1.03984 - 3.00810I$
$b = 2.23977 - 0.72183I$		
$u = 0.12855 + 2.10555I$		
$a = 1.246730 + 0.135922I$	$16.7551 + 3.3007I$	$0.99122 - 1.97685I$
$b = 2.35955 - 0.23642I$		
$u = 0.12855 - 2.10555I$		
$a = 1.246730 - 0.135922I$	$16.7551 - 3.3007I$	$0.99122 + 1.97685I$
$b = 2.35955 + 0.23642I$		

$$\text{II. } I_2^u = \langle b + 1, 4a^3 - 2a^2u + 12a^2 - 4au + 12a - 3u + 4, u^2 + 2 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^2u + au + u \\ -au \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u \\ -u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -a^2u - 2a^2 - 2au - 3a - \frac{3}{2}u - 2 \\ -2a^2u - 2a^2 - 4au - 4a - 3u - 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -a - 2 \\ -2a - 3 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $4au + 4u$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$(u - 1)^6$
$c_2$	$(u + 1)^6$
$c_3, c_4, c_8$ $c_9$	$(u^2 + 2)^3$
$c_6, c_7$	$(u^3 - u^2 + 2u - 1)^2$
$c_{10}$	$(u^3 - u^2 + 1)^2$
$c_{11}$	$(u^3 + u^2 + 2u + 1)^2$
$c_{12}$	$(u^3 + u^2 - 1)^2$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^6$
$c_3, c_4, c_8$ $c_9$	$(y + 2)^6$
$c_6, c_7, c_{11}$	$(y^3 + 3y^2 + 2y - 1)^2$
$c_{10}, c_{12}$	$(y^3 - y^2 + 2y - 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.414210I$ $a = -1.000000 - 0.533779I$ $b = -1.000000$	-5.46628	$3.01951 + 0.I$
$u = 1.414210I$ $a = -0.473303 + 0.620443I$ $b = -1.000000$	$-9.60386 - 2.82812I$	$-3.50976 + 2.97945I$
$u = 1.414210I$ $a = -1.52670 + 0.62044I$ $b = -1.000000$	$-9.60386 + 2.82812I$	$-3.50976 - 2.97945I$
$u = -1.414210I$ $a = -1.000000 + 0.533779I$ $b = -1.000000$	-5.46628	$3.01951 + 0.I$
$u = -1.414210I$ $a = -0.473303 - 0.620443I$ $b = -1.000000$	$-9.60386 + 2.82812I$	$-3.50976 - 2.97945I$
$u = -1.414210I$ $a = -1.52670 - 0.62044I$ $b = -1.000000$	$-9.60386 - 2.82812I$	$-3.50976 + 2.97945I$

$$\text{III. } I_1^v = \langle a, b - 1, v^3 + v^2 - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} v \\ -v \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} v^2 + v - 1 \\ -v^2 + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} v^2 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-2v^2 + 2v + 2$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$(u - 1)^3$
$c_3, c_4, c_8$ $c_9$	$u^3$
$c_5$	$(u + 1)^3$
$c_6, c_7$	$u^3 + u^2 + 2u + 1$
$c_{10}, c_{12}$	$u^3 + u^2 - 1$
$c_{11}$	$u^3 - u^2 + 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_5$	$(y - 1)^3$
$c_3, c_4, c_8$ $c_9$	$y^3$
$c_6, c_7, c_{11}$	$y^3 + 3y^2 + 2y - 1$
$c_{10}, c_{12}$	$y^3 - y^2 + 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -0.877439 + 0.744862I$ $a = 0$ $b = 1.00000$	$-4.66906 - 2.82812I$	$-0.18504 + 4.10401I$
$v = -0.877439 - 0.744862I$ $a = 0$ $b = 1.00000$	$-4.66906 + 2.82812I$	$-0.18504 - 4.10401I$
$v = 0.754878$ $a = 0$ $b = 1.00000$	$-0.531480$	$2.37010$

#### IV. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^9)(u^{15} + 32u^{14} + \dots + 6478u + 289)$
$c_2$	$((u - 1)^3)(u + 1)^6(u^{15} + 4u^{14} + \dots + 52u - 17)$
$c_3, c_4, c_8$ $c_9$	$u^3(u^2 + 2)^3(u^{15} - u^{14} + \dots + 24u^2 - 8)$
$c_5$	$((u - 1)^6)(u + 1)^3(u^{15} + 4u^{14} + \dots + 52u - 17)$
$c_6, c_7$	$((u^3 - u^2 + 2u - 1)^2)(u^3 + u^2 + 2u + 1)(u^{15} - 2u^{14} + \dots + u - 3)$
$c_{10}$	$((u^3 - u^2 + 1)^2)(u^3 + u^2 - 1)(u^{15} + 2u^{14} + \dots + 77u - 87)$
$c_{11}$	$(u^3 - u^2 + 2u - 1)(u^3 + u^2 + 2u + 1)^2(u^{15} - 2u^{14} + \dots + u - 3)$
$c_{12}$	$((u^3 + u^2 - 1)^3)(u^{15} - 2u^{14} + \dots - 127u - 171)$

### V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^9)(y^{15} - 88y^{14} + \dots + 2.94571 \times 10^7 y - 83521)$
$c_2, c_5$	$((y - 1)^9)(y^{15} - 32y^{14} + \dots + 6478y - 289)$
$c_3, c_4, c_8$ $c_9$	$y^3(y + 2)^6(y^{15} + 29y^{14} + \dots + 384y - 64)$
$c_6, c_7, c_{11}$	$((y^3 + 3y^2 + 2y - 1)^3)(y^{15} + 18y^{14} + \dots + 7y - 9)$
$c_{10}$	$((y^3 - y^2 + 2y - 1)^3)(y^{15} + 26y^{14} + \dots - 75329y - 7569)$
$c_{12}$	$((y^3 - y^2 + 2y - 1)^3)(y^{15} + 50y^{14} + \dots - 77237y - 29241)$