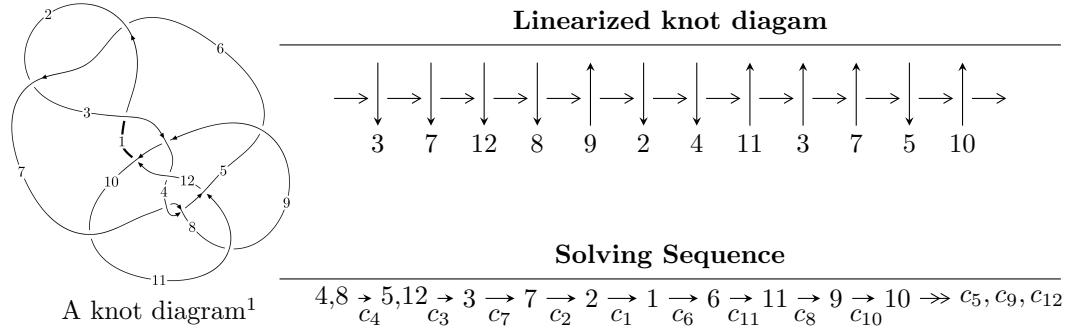


$12n_{0597}$  ( $K12n_{0597}$ )



### Ideals for irreducible components<sup>2</sup> of $X_{\text{par}}$

$$\begin{aligned}
 I_1^u &= \langle 6.48488 \times 10^{68} u^{54} + 2.22735 \times 10^{69} u^{53} + \dots + 3.01163 \times 10^{67} b - 4.54938 \times 10^{69}, \\
 &\quad 7.79191 \times 10^{69} u^{54} + 2.67697 \times 10^{70} u^{53} + \dots + 6.02326 \times 10^{67} a - 5.52191 \times 10^{70}, u^{55} + 4u^{54} + \dots - 32u - \dots \rangle \\
 I_2^u &= \langle 1742938u^{19} + 1162593u^{18} + \dots + 1826407b + 1460687, \\
 &\quad 147076u^{19} + 1158u^{18} + \dots + 166037a - 623712, u^{20} + u^{19} + \dots - 4u + 1 \rangle \\
 I_3^u &= \langle -a^3 + b + 2a + 1, a^4 - a^3 - 4a^2 + 2a + 5, u - 1 \rangle \\
 I_4^u &= \langle b - 1, a - 1, u - 1 \rangle \\
 I_5^u &= \langle b - u + 1, u^2 + a - 2u + 1, u^3 - u^2 + 1 \rangle
 \end{aligned}$$

\* 5 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 83 representations.

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<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/math/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 6.48 \times 10^{68} u^{54} + 2.23 \times 10^{69} u^{53} + \dots + 3.01 \times 10^{67} b - 4.55 \times 10^{69}, 7.79 \times 10^{69} u^{54} + 2.68 \times 10^{70} u^{53} + \dots + 6.02 \times 10^{67} a - 5.52 \times 10^{70}, u^{55} + 4u^{54} + \dots - 32u - 4 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -129.364u^{54} - 444.439u^{53} + \dots + 5697.58u + 916.764 \\ -21.5328u^{54} - 73.9584u^{53} + \dots + 941.610u + 151.061 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 3.94666u^{54} + 13.1180u^{53} + \dots - 136.672u - 18.8314 \\ -20.4560u^{54} - 70.0814u^{53} + \dots + 894.192u + 143.944 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -4.54849u^{54} - 15.8254u^{53} + \dots + 226.873u + 38.8130 \\ -28.9511u^{54} - 99.0248u^{53} + \dots + 1257.74u + 201.588 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -172.432u^{54} - 590.262u^{53} + \dots + 7505.58u + 1199.19 \\ 40.4434u^{54} + 139.041u^{53} + \dots - 1788.25u - 286.747 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -20.9960u^{54} - 71.3826u^{53} + \dots + 880.148u + 137.913 \\ 66.7999u^{54} + 229.120u^{53} + \dots - 2923.17u - 468.173 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -109.774u^{54} - 377.006u^{53} + \dots + 4820.14u + 775.762 \\ -15.4249u^{54} - 52.9241u^{53} + \dots + 670.322u + 107.355 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 190.838u^{54} + 654.783u^{53} + \dots - 8370.59u - 1338.55 \\ -44.5724u^{54} - 152.962u^{53} + \dots + 1958.63u + 314.711 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -139.838u^{54} - 480.350u^{53} + \dots + 6148.79u + 989.017 \\ -45.4892u^{54} - 156.268u^{53} + \dots + 1998.97u + 320.610 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-41.4839u^{54} - 141.696u^{53} + \dots + 1753.72u + 276.705$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{55} + 84u^{54} + \cdots - 72u + 1$
$c_2, c_6$	$u^{55} - 2u^{54} + \cdots + 22u - 1$
$c_3$	$u^{55} - 8u^{54} + \cdots - 120u + 25$
$c_4, c_7$	$u^{55} - 4u^{54} + \cdots - 32u + 4$
$c_5$	$u^{55} - 3u^{54} + \cdots + 75901u - 173113$
$c_8$	$u^{55} + 10u^{54} + \cdots - 1715u - 229$
$c_9$	$u^{55} - u^{54} + \cdots - 216467u + 35417$
$c_{10}$	$u^{55} - 4u^{54} + \cdots - 936251u - 118509$
$c_{11}$	$u^{55} + 2u^{54} + \cdots + 4u - 24$
$c_{12}$	$u^{55} - u^{54} + \cdots + 3199358u - 321516$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{55} - 212y^{54} + \cdots + 10440y - 1$
$c_2, c_6$	$y^{55} - 84y^{54} + \cdots - 72y - 1$
$c_3$	$y^{55} + 20y^{54} + \cdots - 800y - 625$
$c_4, c_7$	$y^{55} - 36y^{54} + \cdots - 200y - 16$
$c_5$	$y^{55} + 35y^{54} + \cdots + 119306470953y - 29968110769$
$c_8$	$y^{55} + 20y^{54} + \cdots - 2180589y - 52441$
$c_9$	$y^{55} + 91y^{54} + \cdots + 50901662647y - 1254363889$
$c_{10}$	$y^{55} + 58y^{54} + \cdots - 129372587591y - 14044383081$
$c_{11}$	$y^{55} - 6y^{54} + \cdots - 12656y - 576$
$c_{12}$	$y^{55} + 85y^{54} + \cdots + 3623181372652y - 103372538256$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.228394 + 0.930097I$ $a = -0.355410 + 0.174211I$ $b = -0.216207 - 0.780987I$	$2.63763 - 2.19314I$	$0.766014 + 1.147808I$
$u = -0.228394 - 0.930097I$ $a = -0.355410 - 0.174211I$ $b = -0.216207 + 0.780987I$	$2.63763 + 2.19314I$	$0.766014 - 1.147808I$
$u = -0.061115 + 1.061790I$ $a = 0.121223 - 0.494313I$ $b = 0.396675 + 1.163810I$	$1.55867 - 3.48219I$	$0. + 3.47906I$
$u = -0.061115 - 1.061790I$ $a = 0.121223 + 0.494313I$ $b = 0.396675 - 1.163810I$	$1.55867 + 3.48219I$	$0. - 3.47906I$
$u = 1.013150 + 0.429080I$ $a = -2.09376 - 0.07084I$ $b = -1.30226 - 1.21278I$	$-8.91481 - 6.34317I$	0
$u = 1.013150 - 0.429080I$ $a = -2.09376 + 0.07084I$ $b = -1.30226 + 1.21278I$	$-8.91481 + 6.34317I$	0
$u = -1.079130 + 0.236177I$ $a = 1.53166 - 0.57910I$ $b = 0.77564 - 1.31217I$	$-1.46530 + 4.21934I$	0
$u = -1.079130 - 0.236177I$ $a = 1.53166 + 0.57910I$ $b = 0.77564 + 1.31217I$	$-1.46530 - 4.21934I$	0
$u = -1.113000 + 0.147678I$ $a = -1.55961 - 0.95086I$ $b = -0.546370 + 1.079590I$	$-12.12370 + 4.63839I$	0
$u = -1.113000 - 0.147678I$ $a = -1.55961 + 0.95086I$ $b = -0.546370 - 1.079590I$	$-12.12370 - 4.63839I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.398648 + 0.764365I$		
$a = 0.490007 + 1.105910I$	$-10.69800 + 3.28061I$	$-4.43813 - 2.05243I$
$b = -0.751133 - 0.461027I$		
$u = -0.398648 - 0.764365I$		
$a = 0.490007 - 1.105910I$	$-10.69800 - 3.28061I$	$-4.43813 + 2.05243I$
$b = -0.751133 + 0.461027I$		
$u = -0.818436 + 0.220706I$		
$a = -0.462335 - 0.757558I$	$1.02370 + 2.96901I$	$6.22160 - 5.57360I$
$b = -0.258171 - 1.314110I$		
$u = -0.818436 - 0.220706I$		
$a = -0.462335 + 0.757558I$	$1.02370 - 2.96901I$	$6.22160 + 5.57360I$
$b = -0.258171 + 1.314110I$		
$u = 0.823693$		
$a = 2.96416$	$-0.453310$	$-12.4430$
$b = 1.33894$		
$u = 0.629407 + 1.015120I$		
$a = -0.124519 + 0.360519I$	$-0.865641 - 0.009239I$	$0$
$b = 0.354817 - 0.497624I$		
$u = 0.629407 - 1.015120I$		
$a = -0.124519 - 0.360519I$	$-0.865641 + 0.009239I$	$0$
$b = 0.354817 + 0.497624I$		
$u = 0.056692 + 1.212890I$		
$a = -0.103950 - 0.233463I$	$-8.74789 + 8.87696I$	$0$
$b = -0.682228 + 1.128040I$		
$u = 0.056692 - 1.212890I$		
$a = -0.103950 + 0.233463I$	$-8.74789 - 8.87696I$	$0$
$b = -0.682228 - 1.128040I$		
$u = 0.354907 + 0.697158I$		
$a = -0.098793 - 0.883310I$	$2.01009 - 2.16153I$	$2.20037 + 5.52786I$
$b = 0.155774 + 1.110550I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.354907 - 0.697158I$		
$a = -0.098793 + 0.883310I$	$2.01009 + 2.16153I$	$2.20037 - 5.52786I$
$b = 0.155774 - 1.110550I$		
$u = 0.388472 + 0.676966I$		
$a = 0.392074 + 0.586948I$	$-7.10371 + 2.13418I$	$-1.61598 - 0.45444I$
$b = -0.77671 + 1.19630I$		
$u = 0.388472 - 0.676966I$		
$a = 0.392074 - 0.586948I$	$-7.10371 - 2.13418I$	$-1.61598 + 0.45444I$
$b = -0.77671 - 1.19630I$		
$u = 1.169370 + 0.406827I$		
$a = 0.160942 - 0.680261I$	$-2.81126 - 1.20544I$	0
$b = 0.558665 - 1.106950I$		
$u = 1.169370 - 0.406827I$		
$a = 0.160942 + 0.680261I$	$-2.81126 + 1.20544I$	0
$b = 0.558665 + 1.106950I$		
$u = -1.256970 + 0.280156I$		
$a = 1.366380 + 0.304132I$	$-6.24743 + 2.95707I$	0
$b = 1.164040 + 0.121414I$		
$u = -1.256970 - 0.280156I$		
$a = 1.366380 - 0.304132I$	$-6.24743 - 2.95707I$	0
$b = 1.164040 - 0.121414I$		
$u = 1.247720 + 0.445260I$		
$a = -1.217490 - 0.284802I$	$-1.00747 - 2.30946I$	0
$b = -0.241125 - 0.911262I$		
$u = 1.247720 - 0.445260I$		
$a = -1.217490 + 0.284802I$	$-1.00747 + 2.30946I$	0
$b = -0.241125 + 0.911262I$		
$u = 1.283620 + 0.343428I$		
$a = -1.33294 + 0.59936I$	$-15.4853 - 6.9210I$	0
$b = -1.55960 + 0.59836I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.283620 - 0.343428I$		
$a = -1.33294 - 0.59936I$	$-15.4853 + 6.9210I$	0
$b = -1.55960 - 0.59836I$		
$u = 1.318640 + 0.262440I$		
$a = 1.39643 + 0.81108I$	$-3.05878 - 4.93696I$	0
$b = 0.598048 + 0.736018I$		
$u = 1.318640 - 0.262440I$		
$a = 1.39643 - 0.81108I$	$-3.05878 + 4.93696I$	0
$b = 0.598048 - 0.736018I$		
$u = -1.254450 + 0.537906I$		
$a = -1.361600 + 0.016121I$	$-0.61529 + 7.55097I$	0
$b = -0.644516 + 0.771416I$		
$u = -1.254450 - 0.537906I$		
$a = -1.361600 - 0.016121I$	$-0.61529 - 7.55097I$	0
$b = -0.644516 - 0.771416I$		
$u = 0.543362 + 0.279828I$		
$a = -0.184351 + 0.678862I$	$-1.238630 - 0.333157I$	$-8.21440 + 1.77959I$
$b = 0.386325 + 0.158096I$		
$u = 0.543362 - 0.279828I$		
$a = -0.184351 - 0.678862I$	$-1.238630 + 0.333157I$	$-8.21440 - 1.77959I$
$b = 0.386325 - 0.158096I$		
$u = -0.532879 + 0.265595I$		
$a = -1.87909 - 0.15769I$	$1.53458 - 0.08260I$	$8.02360 - 0.70539I$
$b = -0.496585 + 0.280323I$		
$u = -0.532879 - 0.265595I$		
$a = -1.87909 + 0.15769I$	$1.53458 + 0.08260I$	$8.02360 + 0.70539I$
$b = -0.496585 - 0.280323I$		
$u = -1.211180 + 0.728080I$		
$a = -0.875893 - 0.683728I$	$-12.79060 + 2.58251I$	0
$b = -0.631732 + 1.072700I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.211180 - 0.728080I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.875893 + 0.683728I$	$-12.79060 - 2.58251I$	0
$b = -0.631732 - 1.072700I$		
$u = 1.25664 + 0.67520I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.073550 - 0.367845I$	$-3.21944 - 6.43186I$	0
$b = 0.700106 + 0.896451I$		
$u = 1.25664 - 0.67520I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.073550 + 0.367845I$	$-3.21944 + 6.43186I$	0
$b = 0.700106 - 0.896451I$		
$u = -0.568585 + 0.002353I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 2.93796 + 2.07601I$	$-10.21720 + 3.48231I$	$-4.98199 + 0.62812I$
$b = -0.463493 + 0.346007I$		
$u = -0.568585 - 0.002353I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 2.93796 - 2.07601I$	$-10.21720 - 3.48231I$	$-4.98199 - 0.62812I$
$b = -0.463493 - 0.346007I$		
$u = -1.34385 + 0.51761I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.43449 - 0.18164I$	$-2.54819 + 9.08466I$	0
$b = 0.60052 - 1.30971I$		
$u = -1.34385 - 0.51761I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 1.43449 + 0.18164I$	$-2.54819 - 9.08466I$	0
$b = 0.60052 + 1.30971I$		
$u = 1.37774 + 0.58999I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.49234 - 0.04356I$	$-12.9172 - 15.1751I$	0
$b = -0.87943 - 1.33400I$		
$u = 1.37774 - 0.58999I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -1.49234 + 0.04356I$	$-12.9172 + 15.1751I$	0
$b = -0.87943 + 1.33400I$		
$u = -1.50431 + 0.07352I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -0.364764 - 1.062760I$	$-13.50180 + 0.32367I$	0
$b = -0.507231 - 0.684175I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.50431 - 0.07352I$		
$a = -0.364764 + 1.062760I$	$-13.50180 - 0.32367I$	0
$b = -0.507231 + 0.684175I$		
$u = -1.60007 + 0.48099I$		
$a = -0.249894 - 0.427368I$	$-14.0455 - 2.4232I$	0
$b = -0.631921 - 0.689866I$		
$u = -1.60007 - 0.48099I$		
$a = -0.249894 + 0.427368I$	$-14.0455 + 2.4232I$	0
$b = -0.631921 + 0.689866I$		
$u = -0.080542 + 0.193890I$		
$a = 2.61995 - 1.69033I$	$1.26586 + 2.57084I$	$-0.85088 - 2.32793I$
$b = 0.228619 - 1.091470I$		
$u = -0.080542 - 0.193890I$		
$a = 2.61995 + 1.69033I$	$1.26586 - 2.57084I$	$-0.85088 + 2.32793I$
$b = 0.228619 + 1.091470I$		

$$\text{II. } I_2^u = \langle 1.74 \times 10^6 u^{19} + 1.16 \times 10^6 u^{18} + \cdots + 1.83 \times 10^6 b + 1.46 \times 10^6, 147076u^{19} + 1158u^{18} + \cdots + 166037a - 623712, u^{20} + u^{19} + \cdots - 4u + 1 \rangle$$

(i) **Arc colorings**

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.885803u^{19} - 0.00697435u^{18} + \cdots - 0.332149u + 3.75646 \\ -0.954299u^{19} - 0.636547u^{18} + \cdots + 2.12930u - 0.799760 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -0.167149u^{19} - 0.371082u^{18} + \cdots - 4.30841u + 3.40433 \\ -0.378146u^{19} - 0.145836u^{18} + \cdots - 2.54026u + 0.496680 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -0.946799u^{19} - 0.655425u^{18} + \cdots - 2.35244u + 2.96809 \\ -1.15780u^{19} - 0.430180u^{18} + \cdots - 0.584292u + 0.0604367 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -2.36020u^{19} - 0.734061u^{18} + \cdots + 6.88680u - 0.210030 \\ -1.50970u^{19} - 0.927327u^{18} + \cdots + 5.68923u - 1.07153 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -0.0662196u^{19} - 0.397076u^{18} + \cdots + 1.44845u + 1.51392 \\ 0.193160u^{19} + 0.171997u^{18} + \cdots + 1.73103u - 0.520690 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -1.22425u^{19} - 0.993563u^{18} + \cdots - 2.60396u + 3.83553 \\ -1.23184u^{19} - 1.39082u^{18} + \cdots - 0.124812u - 0.151619 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -0.119859u^{19} + 0.185423u^{18} + \cdots - 1.51911u + 2.97387 \\ 0.588138u^{19} + 0.846974u^{18} + \cdots - 1.40998u - 0.239062 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -0.807363u^{19} - 0.0873266u^{18} + \cdots - 1.05289u + 3.44587 \\ -0.814955u^{19} - 0.484584u^{18} + \cdots + 1.42626u - 0.541284 \end{pmatrix} \end{aligned}$$

(ii) **Obstruction class = 1**

$$(iii) \text{ Cusp Shapes} = \frac{3759113}{1826407}u^{19} + \frac{9918792}{1826407}u^{18} + \cdots + \frac{33892975}{1826407}u - \frac{13352398}{1826407}$$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1$	$u^{20} - 22u^{19} + \cdots - 3u + 1$
$c_2$	$u^{20} + 2u^{19} + \cdots - u + 1$
$c_3$	$u^{20} + 5u^{19} + \cdots + 5u + 1$
$c_4$	$u^{20} + u^{19} + \cdots - 4u + 1$
$c_5$	$u^{20} - u^{19} + \cdots + 5u + 1$
$c_6$	$u^{20} - 2u^{19} + \cdots + u + 1$
$c_7$	$u^{20} - u^{19} + \cdots + 4u + 1$
$c_8$	$u^{20} + 6u^{19} + \cdots + u + 1$
$c_9$	$u^{20} - u^{19} + \cdots + 9u + 1$
$c_{10}$	$u^{20} + 6u^{19} + \cdots + 62u + 25$
$c_{11}$	$u^{20} + u^{19} + \cdots - 24u + 23$
$c_{12}$	$u^{20} - u^{19} + \cdots + 3u + 1$



**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{20} - 38y^{19} + \cdots + 97y + 1$
$c_2, c_6$	$y^{20} - 22y^{19} + \cdots - 3y + 1$
$c_3$	$y^{20} + 13y^{19} + \cdots + 3y + 1$
$c_4, c_7$	$y^{20} - 15y^{19} + \cdots - 14y + 1$
$c_5$	$y^{20} + 3y^{19} + \cdots - 17y + 1$
$c_8$	$y^{20} + 8y^{19} + \cdots + y + 1$
$c_9$	$y^{20} + 15y^{19} + \cdots - 15y + 1$
$c_{10}$	$y^{20} + 20y^{19} + \cdots - 794y + 625$
$c_{11}$	$y^{20} + y^{19} + \cdots - 1220y + 529$
$c_{12}$	$y^{20} + 13y^{19} + \cdots - 5y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.533776 + 0.839429I$		
$a = 0.082187 + 0.976957I$	$1.33087 - 1.27262I$	$-3.32667 - 0.25948I$
$b = -0.161143 - 1.107230I$		
$u = 0.533776 - 0.839429I$		
$a = 0.082187 - 0.976957I$	$1.33087 + 1.27262I$	$-3.32667 + 0.25948I$
$b = -0.161143 + 1.107230I$		
$u = -1.000530 + 0.259540I$		
$a = -1.06090 - 1.21552I$	$-1.40774 + 1.89082I$	$-2.02415 - 6.71944I$
$b = -1.23287 - 1.38392I$		
$u = -1.000530 - 0.259540I$		
$a = -1.06090 + 1.21552I$	$-1.40774 - 1.89082I$	$-2.02415 + 6.71944I$
$b = -1.23287 + 1.38392I$		
$u = -0.191181 + 0.929591I$		
$a = -0.108015 + 0.312018I$	$2.87685 - 3.71581I$	$2.69381 + 5.50994I$
$b = -0.397250 - 1.097980I$		
$u = -0.191181 - 0.929591I$		
$a = -0.108015 - 0.312018I$	$2.87685 + 3.71581I$	$2.69381 - 5.50994I$
$b = -0.397250 + 1.097980I$		
$u = 0.873633 + 0.175179I$		
$a = -0.0423713 - 0.1227380I$	$0.38476 - 3.13050I$	$-6.71544 + 6.46581I$
$b = -0.053990 - 1.361470I$		
$u = 0.873633 - 0.175179I$		
$a = -0.0423713 + 0.1227380I$	$0.38476 + 3.13050I$	$-6.71544 - 6.46581I$
$b = -0.053990 + 1.361470I$		
$u = -0.795716 + 0.349204I$		
$a = 1.94782 + 1.71456I$	$-10.29940 + 4.53068I$	$-4.78345 - 5.80170I$
$b = 0.680999 - 0.825877I$		
$u = -0.795716 - 0.349204I$		
$a = 1.94782 - 1.71456I$	$-10.29940 - 4.53068I$	$-4.78345 + 5.80170I$
$b = 0.680999 + 0.825877I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.250290 + 0.249862I$	$-2.91355 - 2.89211I$	$-7.67752 + 2.98084I$
$a = -1.43958 - 0.31269I$		
$b = -0.718556 - 0.811927I$		
$u = 1.250290 - 0.249862I$	$-2.91355 + 2.89211I$	$-7.67752 - 2.98084I$
$a = -1.43958 + 0.31269I$		
$b = -0.718556 + 0.811927I$		
$u = -1.284370 + 0.538335I$	$-0.60784 + 9.10431I$	$-1.89591 - 7.92757I$
$a = -1.45575 + 0.12107I$		
$b = -0.703474 + 1.149430I$		
$u = -1.284370 - 0.538335I$	$-0.60784 - 9.10431I$	$-1.89591 + 7.92757I$
$a = -1.45575 - 0.12107I$		
$b = -0.703474 - 1.149430I$		
$u = 1.306690 + 0.489189I$	$-1.49698 - 3.77692I$	$-3.66921 + 4.30140I$
$a = 1.147690 + 0.402592I$		
$b = 0.078049 + 0.861799I$		
$u = 1.306690 - 0.489189I$	$-1.49698 + 3.77692I$	$-3.66921 - 4.30140I$
$a = 1.147690 - 0.402592I$		
$b = 0.078049 - 0.861799I$		
$u = -1.49584 + 0.23640I$	$-13.12220 - 1.74178I$	$-3.87046 + 2.15304I$
$a = -0.348081 + 0.618798I$		
$b = 0.327314 + 0.504059I$		
$u = -1.49584 - 0.23640I$	$-13.12220 + 1.74178I$	$-3.87046 - 2.15304I$
$a = -0.348081 - 0.618798I$		
$b = 0.327314 - 0.504059I$		
$u = 0.303243 + 0.180235I$	$0.581123 + 0.014308I$	$-1.73100 + 0.68149I$
$a = 2.77701 - 1.28061I$		
$b = -0.319083 + 0.192447I$		
$u = 0.303243 - 0.180235I$	$0.581123 - 0.014308I$	$-1.73100 - 0.68149I$
$a = 2.77701 + 1.28061I$		
$b = -0.319083 - 0.192447I$		

$$\text{III. } I_3^u = \langle -a^3 + b + 2a + 1, a^4 - a^3 - 4a^2 + 2a + 5, u - 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} a \\ a^3 - 2a - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -a^3 - 2a^2 + 3a + 6 \\ -a^3 - a^2 + 3a + 4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -a^3 - a^2 + 3a + 4 \\ -a^3 + 3a + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -a \\ -a^3 + 2a + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} a^3 - 3a - 1 \\ -a \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a^3 - 2a - 1 \\ 2a^3 - 5a - 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a^3 + a^2 - 3a - 4 \\ a^3 - 3a - 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} a \\ a^3 - 2a - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_9$	$u^4 + u^3 + 2u^2 + 1$
$c_2, c_5, c_6$	$u^4 - u^3 + 1$
$c_4, c_7$	$(u + 1)^4$
$c_8$	$u^4 - u^3 + 2u^2 + 1$
$c_{10}, c_{11}$	$u^4 - u^2 + 2u + 3$
$c_{12}$	$u^4$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_8$ $c_9$	$y^4 + 3y^3 + 6y^2 + 4y + 1$
$c_2, c_5, c_6$	$y^4 - y^3 + 2y^2 + 1$
$c_4, c_7$	$(y - 1)^4$
$c_{10}, c_{11}$	$y^4 - 2y^3 + 7y^2 - 10y + 9$
$c_{12}$	$y^4$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = -1.246050 + 0.267489I$	-1.64493	-6.00000
$b = -0.175098 + 0.691825I$		
$u = 1.00000$		
$a = -1.246050 - 0.267489I$	-1.64493	-6.00000
$b = -0.175098 - 0.691825I$		
$u = 1.00000$		
$a = 1.74605 + 0.17255I$	-1.64493	-6.00000
$b = 0.675098 + 1.227920I$		
$u = 1.00000$		
$a = 1.74605 - 0.17255I$	-1.64493	-6.00000
$b = 0.675098 - 1.227920I$		

$$\text{IV. } I_4^u = \langle b - 1, a - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_3$	
$c_4, c_5, c_6$	$u + 1$
$c_7, c_9$	
$c_8$	$u - 1$
$c_{10}, c_{11}, c_{12}$	$u$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_4, c_5, c_6$ $c_7, c_8, c_9$	$y - 1$
$c_{10}, c_{11}, c_{12}$	$y$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 1.00000$	-1.64493	-6.00000
$b = 1.00000$		

$$\mathbf{V} \cdot I_5^u = \langle b - u + 1, u^2 + a - 2u + 1, u^3 - u^2 + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_4 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_8 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -u^2 + 2u - 1 \\ u - 1 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -2u^2 + 3u - 1 \\ -u^2 + 2u - 1 \end{pmatrix} \\ a_7 &= \begin{pmatrix} u \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} -2u^2 + 2u - 1 \\ -u^2 + u - 1 \end{pmatrix} \\ a_1 &= \begin{pmatrix} -u \\ -u \end{pmatrix} \\ a_6 &= \begin{pmatrix} -2u^2 + 3u - 1 \\ -u^2 + 2u - 1 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -u^2 + 2u - 1 \\ u - 1 \end{pmatrix} \\ a_9 &= \begin{pmatrix} -2u^2 + 4u - 3 \\ -u^2 + 3u - 2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} -u^2 + 3u - 1 \\ 2u - 1 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $u^2 - 4u + 4$

**(iv) u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_2, c_{10}$ $c_{12}$	$(u - 1)^3$
$c_3$	$u^3 + 2u^2 + u + 1$
$c_4, c_5$	$u^3 - u^2 + 1$
$c_6$	$(u + 1)^3$
$c_7, c_9$	$u^3 + u^2 - 1$
$c_8$	$u^3 + 3u^2 + 2u + 1$
$c_{11}$	$u^3$

**(v) Riley Polynomials at the component**

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_6$ $c_{10}, c_{12}$	$(y - 1)^3$
$c_3$	$y^3 - 2y^2 - 3y - 1$
$c_4, c_5, c_7$ $c_9$	$y^3 - y^2 + 2y - 1$
$c_8$	$y^3 - 5y^2 - 2y - 1$
$c_{11}$	$y^3$

**(vi) Complex Volumes and Cusp Shapes**

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.877439 + 0.744862I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.539798 + 0.182582I$	0	$0.70532 - 1.67231I$
$b = -0.122561 + 0.744862I$		
$u = 0.877439 - 0.744862I$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = 0.539798 - 0.182582I$	0	$0.70532 + 1.67231I$
$b = -0.122561 - 0.744862I$		
$u = -0.754878$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	
$a = -3.07960$	0	7.58940
$b = -1.75488$		

## VI. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u - 1)^3)(u + 1)(u^4 + u^3 + 2u^2 + 1)(u^{20} - 22u^{19} + \dots - 3u + 1)$ $\cdot (u^{55} + 84u^{54} + \dots - 72u + 1)$
$c_2$	$((u - 1)^3)(u + 1)(u^4 - u^3 + 1)(u^{20} + 2u^{19} + \dots - u + 1)$ $\cdot (u^{55} - 2u^{54} + \dots + 22u - 1)$
$c_3$	$(u + 1)(u^3 + 2u^2 + u + 1)(u^4 + u^3 + 2u^2 + 1)(u^{20} + 5u^{19} + \dots + 5u + 1)$ $\cdot (u^{55} - 8u^{54} + \dots - 120u + 25)$
$c_4$	$((u + 1)^5)(u^3 - u^2 + 1)(u^{20} + u^{19} + \dots - 4u + 1)$ $\cdot (u^{55} - 4u^{54} + \dots - 32u + 4)$
$c_5$	$(u + 1)(u^3 - u^2 + 1)(u^4 - u^3 + 1)(u^{20} - u^{19} + \dots + 5u + 1)$ $\cdot (u^{55} - 3u^{54} + \dots + 75901u - 173113)$
$c_6$	$((u + 1)^4)(u^4 - u^3 + 1)(u^{20} - 2u^{19} + \dots + u + 1)$ $\cdot (u^{55} - 2u^{54} + \dots + 22u - 1)$
$c_7$	$((u + 1)^5)(u^3 + u^2 - 1)(u^{20} - u^{19} + \dots + 4u + 1)$ $\cdot (u^{55} - 4u^{54} + \dots - 32u + 4)$
$c_8$	$(u - 1)(u^3 + 3u^2 + 2u + 1)(u^4 - u^3 + 2u^2 + 1)(u^{20} + 6u^{19} + \dots + u + 1)$ $\cdot (u^{55} + 10u^{54} + \dots - 1715u - 229)$
$c_9$	$(u + 1)(u^3 + u^2 - 1)(u^4 + u^3 + 2u^2 + 1)(u^{20} - u^{19} + \dots + 9u + 1)$ $\cdot (u^{55} - u^{54} + \dots - 216467u + 35417)$
$c_{10}$	$u(u - 1)^3(u^4 - u^2 + 2u + 3)(u^{20} + 6u^{19} + \dots + 62u + 25)$ $\cdot (u^{55} - 4u^{54} + \dots - 936251u - 118509)$
$c_{11}$	$u^4(u^4 - u^2 + 2u + 3)(u^{20} + u^{19} + \dots - 24u + 23)$ $\cdot (u^{55} + 2u^{54} + \dots + 4u - 24)$
$c_{12}$	$u^5(u - 1)^3(u^{20} - u^{19} + \dots + 3u + 1)$ $\cdot (u^{55} - u^{54} + \dots + 3199358u - 321516)$

## VII. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$((y - 1)^4)(y^4 + 3y^3 + \dots + 4y + 1)(y^{20} - 38y^{19} + \dots + 97y + 1)$ $\cdot (y^{55} - 212y^{54} + \dots + 10440y - 1)$
$c_2, c_6$	$((y - 1)^4)(y^4 - y^3 + 2y^2 + 1)(y^{20} - 22y^{19} + \dots - 3y + 1)$ $\cdot (y^{55} - 84y^{54} + \dots - 72y - 1)$
$c_3$	$(y - 1)(y^3 - 2y^2 - 3y - 1)(y^4 + 3y^3 + 6y^2 + 4y + 1)$ $\cdot (y^{20} + 13y^{19} + \dots + 3y + 1)(y^{55} + 20y^{54} + \dots - 800y - 625)$
$c_4, c_7$	$((y - 1)^5)(y^3 - y^2 + 2y - 1)(y^{20} - 15y^{19} + \dots - 14y + 1)$ $\cdot (y^{55} - 36y^{54} + \dots - 200y - 16)$
$c_5$	$(y - 1)(y^3 - y^2 + 2y - 1)(y^4 - y^3 + 2y^2 + 1)(y^{20} + 3y^{19} + \dots - 17y + 1)$ $\cdot (y^{55} + 35y^{54} + \dots + 119306470953y - 29968110769)$
$c_8$	$(y - 1)(y^3 - 5y^2 - 2y - 1)(y^4 + 3y^3 + 6y^2 + 4y + 1)$ $\cdot (y^{20} + 8y^{19} + \dots + y + 1)(y^{55} + 20y^{54} + \dots - 2180589y - 52441)$
$c_9$	$(y - 1)(y^3 - y^2 + 2y - 1)(y^4 + 3y^3 + 6y^2 + 4y + 1)$ $\cdot (y^{20} + 15y^{19} + \dots - 15y + 1)$ $\cdot (y^{55} + 91y^{54} + \dots + 50901662647y - 1254363889)$
$c_{10}$	$y(y - 1)^3(y^4 - 2y^3 + \dots - 10y + 9)(y^{20} + 20y^{19} + \dots - 794y + 625)$ $\cdot (y^{55} + 58y^{54} + \dots - 129372587591y - 14044383081)$
$c_{11}$	$y^4(y^4 - 2y^3 + \dots - 10y + 9)(y^{20} + y^{19} + \dots - 1220y + 529)$ $\cdot (y^{55} - 6y^{54} + \dots - 12656y - 576)$
$c_{12}$	$y^5(y - 1)^3(y^{20} + 13y^{19} + \dots - 5y + 1)$ $\cdot (y^{55} + 85y^{54} + \dots + 3623181372652y - 103372538256)$