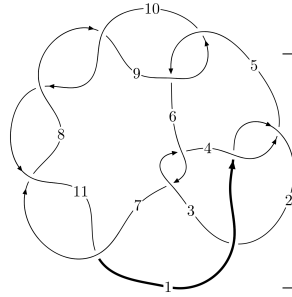
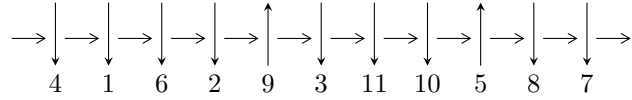


11a<sub>21</sub> (K11a<sub>21</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$7, 11 \xrightarrow{c_7} 8 \xrightarrow{c_{11}} 1, 3 \xrightarrow{c_2} 2 \xrightarrow{c_6} 6 \xrightarrow{c_3} 4 \xrightarrow{c_{10}} 10 \xrightarrow{c_8} 9 \xrightarrow{c_5} 5 \longrightarrow c_1, c_4, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 1428543776353u^{40} + 10013523822393u^{39} + \dots + 2380906293938b - 13661168161, \\ - 857126265809u^{40} - 5059671029533u^{39} + \dots + 2380906293938a + 15522003749453, \\ u^{41} + 8u^{40} + \dots + 9u - 1 \rangle$$

$$I_2^u = \langle b, -u^3 + u^2 + a - 3u + 2, u^4 - u^3 + 3u^2 - 2u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 45 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

I.

$$I_1^u = \langle 1.43 \times 10^{12} u^{40} + 1.00 \times 10^{13} u^{39} + \dots + 2.38 \times 10^{12} b - 1.37 \times 10^{10}, -8.57 \times 10^{11} u^{40} - 5.06 \times 10^{12} u^{39} + \dots + 2.38 \times 10^{12} a + 1.55 \times 10^{13}, u^{41} + 8u^{40} + \dots + 9u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.360000u^{40} + 2.12510u^{39} + \dots - 57.3965u - 6.51937 \\ -0.600000u^{40} - 4.20576u^{39} + \dots - 5.97164u + 0.00573780 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.160000u^{40} + 0.886423u^{39} + \dots - 56.1906u - 6.68003 \\ -0.400000u^{40} - 2.96708u^{39} + \dots - 7.17757u + 0.166396 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.604092u^{40} - 5.23273u^{39} + \dots - 27.0571u - 2.48000 \\ 0.598354u^{40} + 4.78683u^{39} + \dots + 2.11593u - 0.600000 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0.160000u^{40} + 0.668312u^{39} + \dots - 66.4027u - 8.31995 \\ -0.600000u^{40} - 4.14815u^{39} + \dots - 7.25524u - 0.0516402 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ u^4 + 2u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.200000u^{40} - 2.00411u^{39} + \dots - 22.3773u - 2.67998 \\ -0.400000u^{40} - 2.19754u^{39} + \dots + 2.95683u - 0.604092 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.200000u^{40} - 2.00411u^{39} + \dots - 22.3773u - 2.67998 \\ -0.400000u^{40} - 2.19754u^{39} + \dots + 2.95683u - 0.604092 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= \frac{3866826976577}{1190453146969} u^{40} + \frac{30172725798597}{1190453146969} u^{39} + \dots + \frac{97267270764267}{1190453146969} u - \frac{19437718983710}{1190453146969}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_4$	$u^{41} - 5u^{40} + \dots - 7u + 1$
$c_2$	$u^{41} + 17u^{40} + \dots - 21u + 1$
$c_3, c_6$	$u^{41} - u^{40} + \dots + 24u + 16$
$c_5, c_9$	$u^{41} - 2u^{40} + \dots + u + 1$
$c_7, c_8, c_{10}$ $c_{11}$	$u^{41} + 8u^{40} + \dots + 9u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$y^{41} - 17y^{40} + \dots - 21y - 1$
$c_2$	$y^{41} + 19y^{40} + \dots + 319y - 1$
$c_3, c_6$	$y^{41} + 27y^{40} + \dots - 3264y - 256$
$c_5, c_9$	$y^{41} + 8y^{40} + \dots + 9y - 1$
$c_7, c_8, c_{10}$ $c_{11}$	$y^{41} + 52y^{40} + \dots + 289y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.371997 + 0.911661I$ $a = 0.0887599 - 0.0951085I$ $b = 0.944034 + 0.301769I$	$0.02027 + 4.12007I$	$-7.00000 - 7.00432I$
$u = -0.371997 - 0.911661I$ $a = 0.0887599 + 0.0951085I$ $b = 0.944034 - 0.301769I$	$0.02027 - 4.12007I$	$-7.00000 + 7.00432I$
$u = 0.123662 + 0.937506I$ $a = 0.94133 - 1.41174I$ $b = 0.152966 + 1.275670I$	$5.54405 + 0.90504I$	$0. - 2.30521I$
$u = 0.123662 - 0.937506I$ $a = 0.94133 + 1.41174I$ $b = 0.152966 - 1.275670I$	$5.54405 - 0.90504I$	$0. + 2.30521I$
$u = -0.744727 + 0.518203I$ $a = -0.330115 - 0.059884I$ $b = 0.127427 + 0.966899I$	$-0.343144 + 0.381292I$	$-7.00000 + 0.I$
$u = -0.744727 - 0.518203I$ $a = -0.330115 + 0.059884I$ $b = 0.127427 - 0.966899I$	$-0.343144 - 0.381292I$	$-7.00000 + 0.I$
$u = -0.860587 + 0.281389I$ $a = 0.620418 + 0.125659I$ $b = 0.383866 - 1.083520I$	$-1.07493 + 4.80769I$	$-9.34122 - 6.74048I$
$u = -0.860587 - 0.281389I$ $a = 0.620418 - 0.125659I$ $b = 0.383866 + 1.083520I$	$-1.07493 - 4.80769I$	$-9.34122 + 6.74048I$
$u = 0.250188 + 0.801720I$ $a = -1.38496 + 1.41699I$ $b = -0.452932 - 1.292530I$	$4.35267 - 4.76438I$	$-1.23872 + 3.17616I$
$u = 0.250188 - 0.801720I$ $a = -1.38496 - 1.41699I$ $b = -0.452932 + 1.292530I$	$4.35267 + 4.76438I$	$-1.23872 - 3.17616I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.298760 + 0.775703I$		
$a = 0.30126 + 2.51541I$	$-1.09017 + 1.98652I$	$-2.92718 - 5.89159I$
$b = 0.152801 - 0.776585I$		
$u = -0.298760 - 0.775703I$		
$a = 0.30126 - 2.51541I$	$-1.09017 - 1.98652I$	$-2.92718 + 5.89159I$
$b = 0.152801 + 0.776585I$		
$u = -0.402696 + 1.111770I$		
$a = -0.448898 - 1.278070I$	$4.72505 + 4.10019I$	0
$b = -0.300924 + 1.194930I$		
$u = -0.402696 - 1.111770I$		
$a = -0.448898 + 1.278070I$	$4.72505 - 4.10019I$	0
$b = -0.300924 - 1.194930I$		
$u = -0.563543 + 1.076360I$		
$a = 0.77154 + 1.22276I$	$3.04149 + 9.59886I$	0
$b = 0.544305 - 1.241970I$		
$u = -0.563543 - 1.076360I$		
$a = 0.77154 - 1.22276I$	$3.04149 - 9.59886I$	0
$b = 0.544305 + 1.241970I$		
$u = -0.094895 + 0.764233I$		
$a = 0.081309 + 0.430953I$	$0.550320 + 0.199179I$	$-3.56736 - 0.22812I$
$b = -0.903364 + 0.108240I$		
$u = -0.094895 - 0.764233I$		
$a = 0.081309 - 0.430953I$	$0.550320 - 0.199179I$	$-3.56736 + 0.22812I$
$b = -0.903364 - 0.108240I$		
$u = -0.560839 + 0.097240I$		
$a = 1.30596 - 1.04621I$	$-3.06538 + 0.92602I$	$-14.9814 - 0.1523I$
$b = 0.579988 + 0.456802I$		
$u = -0.560839 - 0.097240I$		
$a = 1.30596 + 1.04621I$	$-3.06538 - 0.92602I$	$-14.9814 + 0.1523I$
$b = 0.579988 - 0.456802I$		

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.369951 + 0.353558I$ $a = 0.185674 - 0.401147I$ $b = -0.276914 + 0.386438I$	$-0.304070 + 1.129050I$	$-4.15006 - 5.99735I$
$u = -0.369951 - 0.353558I$ $a = 0.185674 + 0.401147I$ $b = -0.276914 - 0.386438I$	$-0.304070 - 1.129050I$	$-4.15006 + 5.99735I$
$u = -0.12602 + 1.51041I$ $a = -0.013258 - 0.326775I$ $b = 0.008065 + 0.612774I$	$5.86173 + 3.10796I$	0
$u = -0.12602 - 1.51041I$ $a = -0.013258 + 0.326775I$ $b = 0.008065 - 0.612774I$	$5.86173 - 3.10796I$	0
$u = 0.379955 + 0.102142I$ $a = 0.22338 + 1.77156I$ $b = -0.210011 + 1.175300I$	$2.27591 + 2.55277I$	$-0.28600 - 3.41736I$
$u = 0.379955 - 0.102142I$ $a = 0.22338 - 1.77156I$ $b = -0.210011 - 1.175300I$	$2.27591 - 2.55277I$	$-0.28600 + 3.41736I$
$u = -0.06786 + 1.66115I$ $a = 0.00695 + 2.26459I$ $b = 0.022295 - 1.118440I$	$7.48443 + 3.29627I$	0
$u = -0.06786 - 1.66115I$ $a = 0.00695 - 2.26459I$ $b = 0.022295 + 1.118440I$	$7.48443 - 3.29627I$	0
$u = -0.02762 + 1.66408I$ $a = 0.518524 - 0.032043I$ $b = -1.212440 + 0.190127I$	$9.18847 + 0.68171I$	0
$u = -0.02762 - 1.66408I$ $a = 0.518524 + 0.032043I$ $b = -1.212440 - 0.190127I$	$9.18847 - 0.68171I$	0

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.06444 + 1.66622I$ $a = -0.40564 + 1.80984I$ $b = -0.63341 - 1.39654I$	$13.0504 - 5.9463I$	0
$u = 0.06444 - 1.66622I$ $a = -0.40564 - 1.80984I$ $b = -0.63341 + 1.39654I$	$13.0504 + 5.9463I$	0
$u = -0.09721 + 1.68666I$ $a = -0.502494 - 0.093711I$ $b = 1.213200 + 0.228523I$	$9.10647 + 5.94562I$	0
$u = -0.09721 - 1.68666I$ $a = -0.502494 + 0.093711I$ $b = 1.213200 - 0.228523I$	$9.10647 - 5.94562I$	0
$u = 0.02231 + 1.69742I$ $a = 0.26842 - 1.88152I$ $b = 0.37989 + 1.47255I$	$14.9053 + 0.3952I$	0
$u = 0.02231 - 1.69742I$ $a = 0.26842 + 1.88152I$ $b = 0.37989 - 1.47255I$	$14.9053 - 0.3952I$	0
$u = -0.11803 + 1.73749I$ $a = -0.21725 - 1.84068I$ $b = -0.41152 + 1.45863I$	$14.7445 + 6.3325I$	0
$u = -0.11803 - 1.73749I$ $a = -0.21725 + 1.84068I$ $b = -0.41152 - 1.45863I$	$14.7445 - 6.3325I$	0
$u = -0.16530 + 1.73400I$ $a = 0.35701 + 1.74321I$ $b = 0.65439 - 1.38049I$	$12.7852 + 12.6394I$	0
$u = -0.16530 - 1.73400I$ $a = 0.35701 - 1.74321I$ $b = 0.65439 + 1.38049I$	$12.7852 - 12.6394I$	0



Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.0589447$		
$a = -10.7359$	-1.19034	-8.28720
$b = -0.523441$		

$$\text{II. } I_2^u = \langle b, -u^3 + u^2 + a - 3u + 2, u^4 - u^3 + 3u^2 - 2u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^3 - u^2 + 3u - 2 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^3 - u^2 + 2u - 2 \\ u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^3 - u^2 + 3u - 2 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u \\ u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 + 1 \\ u^3 - u^2 + 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ -u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $2u^3 - 2u^2 + 7u - 13$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$(u - 1)^4$
$c_2, c_4$	$(u + 1)^4$
$c_3, c_6$	$u^4$
$c_5$	$u^4 - u^3 + u^2 + 1$
$c_7, c_8$	$u^4 - u^3 + 3u^2 - 2u + 1$
$c_9$	$u^4 + u^3 + u^2 + 1$
$c_{10}, c_{11}$	$u^4 + u^3 + 3u^2 + 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$	$(y - 1)^4$
$c_3, c_6$	$y^4$
$c_5, c_9$	$y^4 + y^3 + 3y^2 + 2y + 1$
$c_7, c_8, c_{10}$ $c_{11}$	$y^4 + 5y^3 + 7y^2 + 2y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.395123 + 0.506844I$ $a = -0.95668 + 1.22719I$ $b = 0$	$-1.85594 - 1.41510I$	$-10.51825 + 2.96122I$
$u = 0.395123 - 0.506844I$ $a = -0.95668 - 1.22719I$ $b = 0$	$-1.85594 + 1.41510I$	$-10.51825 - 2.96122I$
$u = 0.10488 + 1.55249I$ $a = -0.043315 + 0.641200I$ $b = 0$	$5.14581 - 3.16396I$	$-8.98175 + 2.83489I$
$u = 0.10488 - 1.55249I$ $a = -0.043315 - 0.641200I$ $b = 0$	$5.14581 + 3.16396I$	$-8.98175 - 2.83489I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$((u-1)^4)(u^{41} - 5u^{40} + \dots - 7u + 1)$
$c_2$	$((u+1)^4)(u^{41} + 17u^{40} + \dots - 21u + 1)$
$c_3, c_6$	$u^4(u^{41} - u^{40} + \dots + 24u + 16)$
$c_4$	$((u+1)^4)(u^{41} - 5u^{40} + \dots - 7u + 1)$
$c_5$	$(u^4 - u^3 + u^2 + 1)(u^{41} - 2u^{40} + \dots + u + 1)$
$c_7, c_8$	$(u^4 - u^3 + 3u^2 - 2u + 1)(u^{41} + 8u^{40} + \dots + 9u - 1)$
$c_9$	$(u^4 + u^3 + u^2 + 1)(u^{41} - 2u^{40} + \dots + u + 1)$
$c_{10}, c_{11}$	$(u^4 + u^3 + 3u^2 + 2u + 1)(u^{41} + 8u^{40} + \dots + 9u - 1)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_4$	$((y - 1)^4)(y^{41} - 17y^{40} + \dots - 21y - 1)$
$c_2$	$((y - 1)^4)(y^{41} + 19y^{40} + \dots + 319y - 1)$
$c_3, c_6$	$y^4(y^{41} + 27y^{40} + \dots - 3264y - 256)$
$c_5, c_9$	$(y^4 + y^3 + 3y^2 + 2y + 1)(y^{41} + 8y^{40} + \dots + 9y - 1)$
$c_7, c_8, c_{10}$ $c_{11}$	$(y^4 + 5y^3 + 7y^2 + 2y + 1)(y^{41} + 52y^{40} + \dots + 289y - 1)$