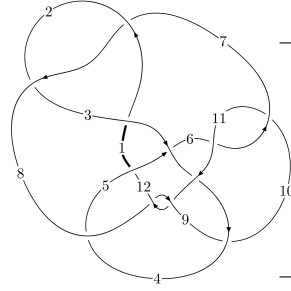
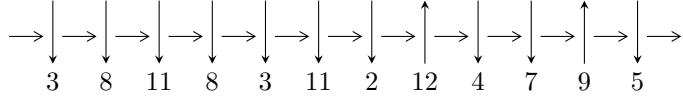


12n₀₆₂₄ (K12n₀₆₂₄)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$8,12 \xrightarrow{c_8} 3,9 \xrightarrow{c_2} 2 \xrightarrow{c_1} 1 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 11 \xrightarrow{c_3} 4 \xrightarrow{c_4} 5 \xrightarrow{c_5} 6 \xrightarrow{c_{10}} 10 \rightsquigarrow c_6, c_9, c_{12}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{16} - u^{15} + 6u^{14} - 5u^{13} + 13u^{12} - 10u^{11} + 8u^{10} - 9u^9 - 9u^8 - 4u^7 - 9u^6 + 8u^4 + 2u^3 + 9u^2 + b + u - 1, \\ u^{16} - 3u^{15} + \dots + a + 5, u^{18} - 2u^{17} + \dots - 8u + 1 \rangle$$

$$I_2^u = \langle u^{11} + 2u^{10} + 6u^9 + 8u^8 + 12u^7 + 12u^6 + 9u^5 + 6u^4 - u^2 + b - 2u - 2, \\ -u^{11} - 3u^{10} - 10u^9 - 18u^8 - 30u^7 - 35u^6 - 33u^5 - 23u^4 - 6u^3 + 4u^2 + a + 9u + 6, \\ u^{12} + 3u^{11} + 9u^{10} + 16u^9 + 25u^8 + 30u^7 + 28u^6 + 21u^5 + 8u^4 - u^3 - 5u^2 - 5u - 1 \rangle$$

* 2 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 30 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{16} - u^{15} + \dots + b - 1, u^{16} - 3u^{15} + \dots + a + 5, u^{18} - 2u^{17} + \dots - 8u + 1 \rangle \quad \mathbf{I.}$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{16} + 3u^{15} + \dots + 18u - 5 \\ -u^{16} + u^{15} + \dots - u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -2u^{16} + 4u^{15} + \dots + 17u - 4 \\ -u^{16} + u^{15} + \dots - u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^{15} + u^{14} + \dots - 10u + 1 \\ u^{16} - u^{15} + \dots + 3u^3 + 10u^2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{17} - 5u^{15} + \dots + 5u + 1 \\ -u^{16} + u^{15} + \dots - 11u^2 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{17} - 2u^{16} + \dots + 19u - 5 \\ -u^{17} + u^{16} + \dots - 9u + 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2u^{17} - 3u^{16} + \dots + 28u - 7 \\ -u^{17} + u^{16} + \dots - 9u + 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^{16} - 2u^{15} + \dots - 6u - 1 \\ u^{17} - u^{16} + \dots + 7u - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^{17} + u^{16} + \dots - 4u + 1 \\ -u^{16} + u^{15} + \dots + 7u - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 2u^{17} - 3u^{16} + 19u^{15} - 23u^{14} + 70u^{13} - 72u^{12} + 124u^{11} - 114u^{10} + 89u^9 - 89u^8 - 15u^7 - 26u^6 - 27u^5 - 2u^4 + 51u^3 - 15u^2 + 50u - 24$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{18} + 14u^{17} + \dots + 21504u + 4096$
c_2, c_7	$u^{18} - 16u^{17} + \dots + 224u - 64$
c_3, c_6, c_{10}	$u^{18} + 2u^{17} + \dots - 2u - 1$
c_4, c_{12}	$u^{18} + 3u^{17} + \dots - 2u - 1$
c_5	$u^{18} - 5u^{17} + \dots - 4u + 1$
c_8, c_{11}	$u^{18} + 2u^{17} + \dots + 8u + 1$
c_9	$u^{18} - u^{17} + \dots - 120u - 61$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{18} + 82y^{17} + \dots - 437256192y + 16777216$
c_2, c_7	$y^{18} - 14y^{17} + \dots - 21504y + 4096$
c_3, c_6, c_{10}	$y^{18} + 28y^{17} + \dots - 18y + 1$
c_4, c_{12}	$y^{18} + 35y^{17} + \dots + 20y + 1$
c_5	$y^{18} - 45y^{17} + \dots - 20y + 1$
c_8, c_{11}	$y^{18} + 14y^{17} + \dots - 32y + 1$
c_9	$y^{18} + 33y^{17} + \dots + 24762y + 3721$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.957035 + 0.038927I$ $a = 1.29444 - 2.14220I$ $b = -1.52646 + 1.38753I$	$12.15720 + 5.50571I$	$-6.58833 - 2.14870I$
$u = 0.957035 - 0.038927I$ $a = 1.29444 + 2.14220I$ $b = -1.52646 - 1.38753I$	$12.15720 - 5.50571I$	$-6.58833 + 2.14870I$
$u = -0.292699 + 1.060130I$ $a = 0.130715 - 0.442861I$ $b = -0.090901 + 0.653348I$	$-0.84836 - 1.94165I$	$-6.35139 + 2.74428I$
$u = -0.292699 - 1.060130I$ $a = 0.130715 + 0.442861I$ $b = -0.090901 - 0.653348I$	$-0.84836 + 1.94165I$	$-6.35139 - 2.74428I$
$u = 0.074993 + 1.132910I$ $a = 0.751791 + 0.803103I$ $b = 0.794717 - 0.290190I$	$-3.55462 + 1.02828I$	$-12.61847 - 1.28084I$
$u = 0.074993 - 1.132910I$ $a = 0.751791 - 0.803103I$ $b = 0.794717 + 0.290190I$	$-3.55462 - 1.02828I$	$-12.61847 + 1.28084I$
$u = -0.796441 + 0.291195I$ $a = 0.151574 + 0.889968I$ $b = -0.775836 - 0.472537I$	$1.24471 - 1.98200I$	$-5.60868 + 9.18970I$
$u = -0.796441 - 0.291195I$ $a = 0.151574 - 0.889968I$ $b = -0.775836 + 0.472537I$	$1.24471 + 1.98200I$	$-5.60868 - 9.18970I$
$u = 0.147448 + 1.249270I$ $a = -1.46732 - 1.39599I$ $b = -1.62783 + 0.04234I$	$-11.88260 + 2.10947I$	$-15.7034 - 5.8224I$
$u = 0.147448 - 1.249270I$ $a = -1.46732 + 1.39599I$ $b = -1.62783 - 0.04234I$	$-11.88260 - 2.10947I$	$-15.7034 + 5.8224I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.490413 + 1.272180I$ $a = 1.140910 + 0.046544I$ $b = -1.42593 - 1.40587I$	$8.34549 - 0.36039I$	$-9.48611 - 0.73252I$
$u = 0.490413 - 1.272180I$ $a = 1.140910 - 0.046544I$ $b = -1.42593 + 1.40587I$	$8.34549 + 0.36039I$	$-9.48611 + 0.73252I$
$u = 0.458123 + 1.327850I$ $a = -0.80670 - 2.00900I$ $b = -1.59701 + 1.33472I$	$7.89248 + 10.55150I$	$-10.01468 - 4.70572I$
$u = 0.458123 - 1.327850I$ $a = -0.80670 + 2.00900I$ $b = -1.59701 - 1.33472I$	$7.89248 - 10.55150I$	$-10.01468 + 4.70572I$
$u = -0.35310 + 1.38486I$ $a = -0.684948 + 0.964946I$ $b = -1.194280 - 0.456860I$	$-4.04162 - 6.18627I$	$-15.0481 + 5.4779I$
$u = -0.35310 - 1.38486I$ $a = -0.684948 - 0.964946I$ $b = -1.194280 + 0.456860I$	$-4.04162 + 6.18627I$	$-15.0481 - 5.4779I$
$u = 0.443581$ $a = 1.93499$ $b = -1.59894$	-8.07946	-1.20520
$u = 0.184865$ $a = -1.95591$ $b = 0.485984$	-0.676311	-14.9570

II.

$$I_2^u = \langle u^{11} + 2u^{10} + \dots + b - 2, -u^{11} - 3u^{10} + \dots + a + 6, u^{12} + 3u^{11} + \dots - 5u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{11} + 3u^{10} + \dots - 9u - 6 \\ -u^{11} - 2u^{10} - 6u^9 - 8u^8 - 12u^7 - 12u^6 - 9u^5 - 6u^4 + u^2 + 2u + 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{10} + 4u^9 + 10u^8 + 18u^7 + 23u^6 + 24u^5 + 17u^4 + 6u^3 - 3u^2 - 7u - 4 \\ -u^{11} - 2u^{10} - 6u^9 - 8u^8 - 12u^7 - 12u^6 - 9u^5 - 6u^4 + u^2 + 2u + 2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -2u^{11} - 6u^{10} + \dots + 14u + 10 \\ -u^{10} - 2u^9 - 5u^8 - 5u^7 - 5u^6 - 2u^5 + 2u^4 + 3u^3 + 4u^2 + u - 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^{11} - 5u^{10} + \dots + 15u + 8 \\ -u^{10} - 2u^9 - 5u^8 - 6u^7 - 6u^6 - 5u^5 + u^3 + 3u^2 + 2u - 2 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ u^3 + u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{11} + 4u^{10} + \dots - 10u - 6 \\ u^{10} + 2u^9 + 5u^8 + 6u^7 + 6u^6 + 5u^5 - u^3 - 3u^2 - 2u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^{11} + 3u^{10} + \dots - 8u - 7 \\ u^{10} + 2u^9 + 5u^8 + 6u^7 + 6u^6 + 5u^5 - u^3 - 3u^2 - 2u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^{11} - 4u^{10} + \dots + 14u + 8 \\ u^{11} + 2u^{10} + 6u^9 + 8u^8 + 12u^7 + 12u^6 + 9u^5 + 6u^4 - u^2 - 2u - 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 3u^{11} + 8u^{10} + \dots - 5u - 4 \\ -u^{10} - 4u^9 + \dots + 7u + 3 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= 7u^{11} + 15u^{10} + 48u^9 + 70u^8 + 112u^7 + 121u^6 + 105u^5 + 81u^4 + 18u^3 - 2u^2 - 21u - 29$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1	$u^{12} - 14u^{11} + \dots - 67u + 9$
c_2	$u^{12} + 2u^{11} + \dots - u + 3$
c_3, c_{10}	$u^{12} - u^{11} - 2u^{10} - u^9 + 2u^8 + 4u^7 - 2u^6 + 3u^5 - 3u^4 + 4u^3 - 2u^2 + u - 1$
c_4, c_{12}	$u^{12} + 2u^{11} - u^{10} - u^9 + 6u^8 - 3u^7 + u^6 + 5u^5 - 5u^4 + 7u^3 - 5u^2 + 3u - 1$
c_5	$u^{12} + 14u^{11} + \dots + 3u + 1$
c_6	$u^{12} + u^{11} - 2u^{10} + u^9 + 2u^8 - 4u^7 - 2u^6 - 3u^5 - 3u^4 - 4u^3 - 2u^2 - u - 1$
c_7	$u^{12} - 2u^{11} + \dots + u + 3$
c_8	$u^{12} + 3u^{11} + \dots - 5u - 1$
c_9	$u^{12} - 2u^{10} - 6u^9 + 13u^8 + u^7 + 2u^6 - 9u^5 - 8u^4 + 9u^3 - 4u^2 + 5u - 3$
c_{11}	$u^{12} - 3u^{11} + \dots + 5u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1	$y^{12} - 22y^{11} + \dots + 29y + 81$
c_2, c_7	$y^{12} - 14y^{11} + \dots - 67y + 9$
c_3, c_6, c_{10}	$y^{12} - 5y^{11} + \dots + 3y + 1$
c_4, c_{12}	$y^{12} - 6y^{11} + \dots + y + 1$
c_5	$y^{12} - 30y^{11} + \dots + 21y + 1$
c_8, c_{11}	$y^{12} + 9y^{11} + \dots - 15y + 1$
c_9	$y^{12} - 4y^{11} + \dots - y + 9$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.945559 + 0.176012I$ $a = 0.384985 + 0.661564I$ $b = -0.934205 - 0.378092I$	$1.63828 - 1.45323I$	$1.054104 + 0.917158I$
$u = -0.945559 - 0.176012I$ $a = 0.384985 - 0.661564I$ $b = -0.934205 + 0.378092I$	$1.63828 + 1.45323I$	$1.054104 - 0.917158I$
$u = -0.083486 + 1.161420I$ $a = 1.36019 - 1.88104I$ $b = 1.71485 + 0.22346I$	$-11.61070 - 1.25522I$	$-12.48094 - 2.13033I$
$u = -0.083486 - 1.161420I$ $a = 1.36019 + 1.88104I$ $b = 1.71485 - 0.22346I$	$-11.61070 + 1.25522I$	$-12.48094 + 2.13033I$
$u = 0.262959 + 1.174910I$ $a = -0.73282 + 1.30130I$ $b = 0.886932 - 0.447310I$	$-8.28259 + 3.18829I$	$-11.15779 - 3.99090I$
$u = 0.262959 - 1.174910I$ $a = -0.73282 - 1.30130I$ $b = 0.886932 + 0.447310I$	$-8.28259 - 3.18829I$	$-11.15779 + 3.99090I$
$u = -0.451022 + 1.172390I$ $a = -0.0134217 + 0.1288200I$ $b = -0.609088 + 0.508190I$	$-1.38760 - 3.47878I$	$-6.82613 + 4.40874I$
$u = -0.451022 - 1.172390I$ $a = -0.0134217 - 0.1288200I$ $b = -0.609088 - 0.508190I$	$-1.38760 + 3.47878I$	$-6.82613 - 4.40874I$
$u = 0.612728$ $a = -2.21290$ $b = 0.702300$	-4.82802	-5.83830
$u = -0.45888 + 1.40396I$ $a = -0.414406 + 0.891813I$ $b = -1.172970 - 0.328171I$	$-3.32828 - 6.54831I$	$-6.31944 + 10.84380I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.45888 - 1.40396I$	$-3.32828 + 6.54831I$	$-6.31944 - 10.84380I$
$a = -0.414406 - 0.891813I$		
$b = -1.172970 + 0.328171I$		
$u = -0.260752$	-8.44787	-23.7010
$a = -3.95615$		
$b = 1.52667$		

III. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u^{12} - 14u^{11} + \dots - 67u + 9)(u^{18} + 14u^{17} + \dots + 21504u + 4096)$
c_2	$(u^{12} + 2u^{11} + \dots - u + 3)(u^{18} - 16u^{17} + \dots + 224u - 64)$
c_3, c_{10}	$(u^{12} - u^{11} - 2u^{10} - u^9 + 2u^8 + 4u^7 - 2u^6 + 3u^5 - 3u^4 + 4u^3 - 2u^2 + u - 1)$ $\cdot (u^{18} + 2u^{17} + \dots - 2u - 1)$
c_4, c_{12}	$(u^{12} + 2u^{11} - u^{10} - u^9 + 6u^8 - 3u^7 + u^6 + 5u^5 - 5u^4 + 7u^3 - 5u^2 + 3u - 1)$ $\cdot (u^{18} + 3u^{17} + \dots - 2u - 1)$
c_5	$(u^{12} + 14u^{11} + \dots + 3u + 1)(u^{18} - 5u^{17} + \dots - 4u + 1)$
c_6	$(u^{12} + u^{11} - 2u^{10} + u^9 + 2u^8 - 4u^7 - 2u^6 - 3u^5 - 3u^4 - 4u^3 - 2u^2 - u - 1)$ $\cdot (u^{18} + 2u^{17} + \dots - 2u - 1)$
c_7	$(u^{12} - 2u^{11} + \dots + u + 3)(u^{18} - 16u^{17} + \dots + 224u - 64)$
c_8	$(u^{12} + 3u^{11} + \dots - 5u - 1)(u^{18} + 2u^{17} + \dots + 8u + 1)$
c_9	$(u^{12} - 2u^{10} - 6u^9 + 13u^8 + u^7 + 2u^6 - 9u^5 - 8u^4 + 9u^3 - 4u^2 + 5u - 3)$ $\cdot (u^{18} - u^{17} + \dots - 120u - 61)$
c_{11}	$(u^{12} - 3u^{11} + \dots + 5u - 1)(u^{18} + 2u^{17} + \dots + 8u + 1)$

IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1	$(y^{12} - 22y^{11} + \dots + 29y + 81)$ $\cdot (y^{18} + 82y^{17} + \dots - 437256192y + 16777216)$
c_2, c_7	$(y^{12} - 14y^{11} + \dots - 67y + 9)(y^{18} - 14y^{17} + \dots - 21504y + 4096)$
c_3, c_6, c_{10}	$(y^{12} - 5y^{11} + \dots + 3y + 1)(y^{18} + 28y^{17} + \dots - 18y + 1)$
c_4, c_{12}	$(y^{12} - 6y^{11} + \dots + y + 1)(y^{18} + 35y^{17} + \dots + 20y + 1)$
c_5	$(y^{12} - 30y^{11} + \dots + 21y + 1)(y^{18} - 45y^{17} + \dots - 20y + 1)$
c_8, c_{11}	$(y^{12} + 9y^{11} + \dots - 15y + 1)(y^{18} + 14y^{17} + \dots - 32y + 1)$
c_9	$(y^{12} - 4y^{11} + \dots - y + 9)(y^{18} + 33y^{17} + \dots + 24762y + 3721)$