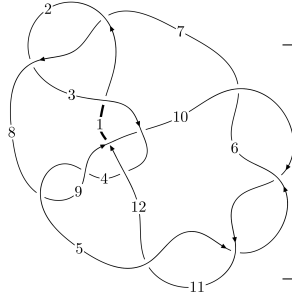
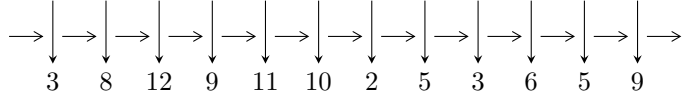


12n<sub>0644</sub> (K12n<sub>0644</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,9 \xrightarrow{c_4} 4 \xrightarrow{c_8} 1,8 \xrightarrow{c_{12}} 12 \xrightarrow{c_3} 3 \xrightarrow{c_2} 2 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 11 \xrightarrow{c_5} 6 \xrightarrow{c_{10}} 10 \twoheadrightarrow c_1, c_6, c_9$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -9649326548650u^{14} + 50820393580641u^{13} + \dots + 871991330612b + 276658983707276, \\ -98118943388815u^{14} + 517725352137249u^{13} + \dots + 1743982661224a + 2846447135872992, \\ u^{15} - 5u^{14} + \dots - 36u - 8 \rangle$$

$$I_2^u = \langle 37u^{11} - 4u^{10} - 19u^9 - 51u^8 - 94u^7 + 35u^6 + 152u^5 - 47u^4 + 184u^3 - 53u^2 + 86b - 97u - 25, \\ 11u^{11} - 7u^{10} - u^9 - 14u^8 - 14u^7 + 29u^6 + 51u^5 - 7u^4 + 64u^3 - 82u^2 + 43a - 30u - 76, \\ u^{12} + u^{11} + u^{10} - 3u^8 - 3u^7 - u^6 - 3u^5 + 3u^4 + u^3 - 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 27 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle -9.65 \times 10^{12}u^{14} + 5.08 \times 10^{13}u^{13} + \dots + 8.72 \times 10^{11}b + 2.77 \times 10^{14}, -9.81 \times 10^{13}u^{14} + 5.18 \times 10^{14}u^{13} + \dots + 1.74 \times 10^{12}a + 2.85 \times 10^{15}, u^{15} - 5u^{14} + \dots - 36u - 8 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 56.2614u^{14} - 296.864u^{13} + \dots - 1427.56u - 1632.15 \\ 11.0659u^{14} - 58.2808u^{13} + \dots - 271.998u - 317.273 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 56.2614u^{14} - 296.864u^{13} + \dots - 1427.56u - 1632.15 \\ 6.82466u^{14} - 35.8416u^{13} + \dots - 162.048u - 192.819 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -64.6576u^{14} + 341.081u^{13} + \dots + 1634.51u + 1875.21 \\ -3.15293u^{14} + 16.6942u^{13} + \dots + 82.5222u + 92.8366 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -59.9171u^{14} + 316.162u^{13} + \dots + 1519.44u + 1740.30 \\ 1.58748u^{14} - 8.22498u^{13} + \dots - 32.5463u - 42.0757 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -69.1241u^{14} + 364.539u^{13} + \dots + 1748.19u + 2001.69 \\ -2.05249u^{14} + 10.7120u^{13} + \dots + 51.5981u + 57.9377 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 63.0861u^{14} - 332.705u^{13} + \dots - 1589.61u - 1824.97 \\ 6.82466u^{14} - 35.8416u^{13} + \dots - 162.048u - 192.819 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 31.2918u^{14} - 165.106u^{13} + \dots - 792.337u - 906.764 \\ 0.796083u^{14} - 4.30252u^{13} + \dots - 26.8018u - 26.2397 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 81.7883u^{14} - 431.479u^{13} + \dots - 2072.39u - 2372.03 \\ 7.57555u^{14} - 40.0591u^{13} + \dots - 195.899u - 222.593 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes**

$$= \frac{23777727583517}{217997832653}u^{14} - \frac{125538144456213}{217997832653}u^{13} + \dots - \frac{605427961030606}{217997832653}u - \frac{696103351358110}{217997832653}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{15} + 23u^{14} + \dots + 6467u + 961$
$c_2, c_7$	$u^{15} + u^{14} + \dots + 71u + 31$
$c_3$	$u^{15} - 4u^{14} + \dots + 312u + 49$
$c_4, c_8$	$u^{15} - 5u^{14} + \dots - 36u - 8$
$c_5, c_6, c_{10}$ $c_{11}$	$u^{15} + u^{14} + \dots - 6u - 1$
$c_9$	$u^{15} - u^{14} + \dots - 167u - 151$
$c_{12}$	$u^{15} + 3u^{14} + \dots - 10u - 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{15} - 51y^{14} + \dots + 52633339y - 923521$
$c_2, c_7$	$y^{15} - 23y^{14} + \dots + 6467y - 961$
$c_3$	$y^{15} - 36y^{14} + \dots + 43640y - 2401$
$c_4, c_8$	$y^{15} - 27y^{14} + \dots + 1936y - 64$
$c_5, c_6, c_{10}$ $c_{11}$	$y^{15} + 11y^{14} + \dots + 18y - 1$
$c_9$	$y^{15} - 41y^{14} + \dots + 123925y - 22801$
$c_{12}$	$y^{15} - 25y^{14} + \dots + 428y - 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.923660 + 0.494347I$ $a = -1.70164 + 0.17855I$ $b = -0.448573 + 0.379515I$	$-2.23565 + 4.29534I$	$-10.91630 - 6.10915I$
$u = -0.923660 - 0.494347I$ $a = -1.70164 - 0.17855I$ $b = -0.448573 - 0.379515I$	$-2.23565 - 4.29534I$	$-10.91630 + 6.10915I$
$u = -0.091749 + 1.089930I$ $a = 0.084694 - 0.589048I$ $b = -0.422185 + 0.856949I$	$2.00776 + 2.59269I$	$-13.6766 - 6.5009I$
$u = -0.091749 - 1.089930I$ $a = 0.084694 + 0.589048I$ $b = -0.422185 - 0.856949I$	$2.00776 - 2.59269I$	$-13.6766 + 6.5009I$
$u = 1.049060 + 0.386860I$ $a = -0.493644 + 0.394908I$ $b = -0.75538 + 1.81023I$	$9.65742 + 0.83037I$	$-11.42036 - 0.07756I$
$u = 1.049060 - 0.386860I$ $a = -0.493644 - 0.394908I$ $b = -0.75538 - 1.81023I$	$9.65742 - 0.83037I$	$-11.42036 + 0.07756I$
$u = 0.824524 + 0.143621I$ $a = 0.906560 + 0.197657I$ $b = 0.295936 - 0.760130I$	$2.39036 - 1.70688I$	$-6.78199 + 3.68703I$
$u = 0.824524 - 0.143621I$ $a = 0.906560 - 0.197657I$ $b = 0.295936 + 0.760130I$	$2.39036 + 1.70688I$	$-6.78199 - 3.68703I$
$u = -0.275761$ $a = 7.05043$ $b = 0.964667$	$-7.21918$	$-7.10970$
$u = -0.275217$ $a = 0.940995$ $b = -0.225404$	$-0.524379$	$-18.9810$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 2.11029 + 0.07886I$ $a = -0.765111 - 0.046752I$ $b = -2.21963 - 1.07578I$	$-5.55478 + 1.31578I$	$-12.00000 - 1.63162I$
$u = 2.11029 - 0.07886I$ $a = -0.765111 + 0.046752I$ $b = -2.21963 + 1.07578I$	$-5.55478 - 1.31578I$	$-12.00000 + 1.63162I$
$u = -1.95045 + 1.42970I$ $a = 0.695006 + 0.403378I$ $b = 2.77095 - 1.36080I$	$-14.3627 + 9.6247I$	$-10.73924 - 3.33714I$
$u = -1.95045 - 1.42970I$ $a = 0.695006 - 0.403378I$ $b = 2.77095 + 1.36080I$	$-14.3627 - 9.6247I$	$-10.73924 + 3.33714I$
$u = 3.51497$ $a = 0.556839$ $b = 4.81849$	19.0038	0

$$\text{II. } I_2^u = \langle 37u^{11} - 4u^{10} + \dots + 86b - 25, 11u^{11} - 7u^{10} + \dots + 43a - 76, u^{12} + u^{11} + \dots + u^3 - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.255814u^{11} + 0.162791u^{10} + \dots + 0.697674u + 1.76744 \\ -0.430233u^{11} + 0.0465116u^{10} + \dots + 1.12791u + 0.290698 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.255814u^{11} + 0.162791u^{10} + \dots + 0.697674u + 1.76744 \\ -0.290698u^{11} + 0.139535u^{10} + \dots + 1.38372u - 0.127907 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{10} - u^9 - u^8 + 3u^6 + 3u^5 + u^4 + 3u^3 - 3u^2 - u \\ -0.430233u^{11} - 0.953488u^{10} + \dots + 0.127907u + 1.29070 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.174419u^{11} - 0.883721u^{10} + \dots - 1.43023u + 0.476744 \\ -0.255814u^{11} - 0.837209u^{10} + \dots - 0.302326u + 1.76744 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1.34884u^{11} + 1.23256u^{10} + \dots + 0.139535u + 0.953488 \\ -0.127907u^{11} - 0.418605u^{10} + \dots - 1.15116u + 1.38372 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.546512u^{11} + 0.302326u^{10} + \dots + 2.08140u + 1.63953 \\ -0.290698u^{11} + 0.139535u^{10} + \dots + 1.38372u - 0.127907 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.197674u^{11} + 1.46512u^{10} + \dots + 0.779070u - 1.59302 \\ -0.290698u^{11} + 0.139535u^{10} + \dots - 0.616279u - 2.12791 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^9 - u^8 - u^7 + 3u^5 + 3u^4 + u^3 + 3u^2 - 3u - 1 \\ 1.29070u^{11} + 0.860465u^{10} + \dots - 1.38372u + 0.127907 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes

$$= \frac{121}{43}u^{11} - \frac{34}{43}u^{10} - \frac{11}{43}u^9 - \frac{154}{43}u^8 - \frac{326}{43}u^7 + \frac{147}{43}u^6 + \frac{346}{43}u^5 - \frac{206}{43}u^4 + \frac{747}{43}u^3 - \frac{558}{43}u^2 - \frac{115}{43}u - \frac{492}{43}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{12} - 10u^{11} + \dots - 13u + 1$
$c_2$	$u^{12} - 5u^{10} + u^9 + 11u^8 - 4u^7 - 15u^6 + 6u^5 + 13u^4 - 5u^3 - 6u^2 + u + 1$
$c_3$	$u^{12} + 3u^{11} + 3u^{10} + u^9 - 3u^8 - 6u^7 - u^6 + 4u^5 + 4u^4 + u^3 - 3u^2 - 2u - 1$
$c_4$	$u^{12} + u^{11} + u^{10} - 3u^8 - 3u^7 - u^6 - 3u^5 + 3u^4 + u^3 - 1$
$c_5, c_6$	$u^{12} + 8u^{10} + 24u^8 + 32u^6 + u^5 + 15u^4 + 3u^3 - 2u^2 + 2u - 1$
$c_7$	$u^{12} - 5u^{10} - u^9 + 11u^8 + 4u^7 - 15u^6 - 6u^5 + 13u^4 + 5u^3 - 6u^2 - u + 1$
$c_8$	$u^{12} - u^{11} + u^{10} - 3u^8 + 3u^7 - u^6 + 3u^5 + 3u^4 - u^3 - 1$
$c_9$	$u^{12} - u^9 - 3u^8 + 3u^7 + u^6 + 3u^5 + 3u^4 - u^2 - u - 1$
$c_{10}, c_{11}$	$u^{12} + 8u^{10} + 24u^8 + 32u^6 - u^5 + 15u^4 - 3u^3 - 2u^2 - 2u - 1$
$c_{12}$	$u^{12} - 4u^{11} + \dots + 10u + 4$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{12} - 6y^{11} + \dots - 25y + 1$
$c_2, c_7$	$y^{12} - 10y^{11} + \dots - 13y + 1$
$c_3$	$y^{12} - 3y^{11} + \dots + 2y + 1$
$c_4, c_8$	$y^{12} + y^{11} - 5y^{10} - 2y^9 + 19y^8 + y^7 - 37y^6 - 11y^5 + 21y^4 + y^3 - 6y^2 + 1$
$c_5, c_6, c_{10}$ $c_{11}$	$y^{12} + 16y^{11} + \dots - 38y^2 + 1$
$c_9$	$y^{12} - 6y^{10} + y^9 + 21y^8 - 11y^7 - 37y^6 + y^5 + 19y^4 - 2y^3 - 5y^2 + y + 1$
$c_{12}$	$y^{12} - 20y^{11} + \dots - 44y + 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.197166 + 1.055630I$ $a = 0.269314 + 0.350716I$ $b = -0.297880 - 0.774287I$	$2.52801 - 2.27257I$	$-2.24792 + 0.35874I$
$u = 0.197166 - 1.055630I$ $a = 0.269314 - 0.350716I$ $b = -0.297880 + 0.774287I$	$2.52801 + 2.27257I$	$-2.24792 - 0.35874I$
$u = 0.699703 + 0.248857I$ $a = 2.79474 + 0.04243I$ $b = 0.854478 - 0.422647I$	$-2.92889 - 3.37800I$	$-15.0144 + 0.9526I$
$u = 0.699703 - 0.248857I$ $a = 2.79474 - 0.04243I$ $b = 0.854478 + 0.422647I$	$-2.92889 + 3.37800I$	$-15.0144 - 0.9526I$
$u = 1.26306$ $a = -1.13258$ $b = -1.43639$	$-4.03974$	$-8.57740$
$u = -0.721730$ $a = 3.00075$ $b = 0.973015$	$-7.69678$	$-24.7790$
$u = -0.154674 + 0.692367I$ $a = 0.726797 + 0.523291I$ $b = -0.171464 + 1.286840I$	$10.64100 + 1.46286I$	$-4.09278 - 4.80437I$
$u = -0.154674 - 0.692367I$ $a = 0.726797 - 0.523291I$ $b = -0.171464 - 1.286840I$	$10.64100 - 1.46286I$	$-4.09278 + 4.80437I$
$u = -1.246550 + 0.486161I$ $a = -1.067620 - 0.103337I$ $b = -1.343420 - 0.224193I$	$0.66596 + 2.08092I$	$-11.59767 - 2.54425I$
$u = -1.246550 - 0.486161I$ $a = -1.067620 + 0.103337I$ $b = -1.343420 + 0.224193I$	$0.66596 - 2.08092I$	$-11.59767 + 2.54425I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.266310 + 1.357680I$	$4.83179 + 2.98242I$	$-8.86878 - 3.33225I$
$a = -0.157319 - 0.900117I$		
$b = -0.310027 + 0.519410I$		
$u = -0.266310 - 1.357680I$	$4.83179 - 2.98242I$	$-8.86878 + 3.33225I$
$a = -0.157319 + 0.900117I$		
$b = -0.310027 - 0.519410I$		

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{12} - 10u^{11} + \dots - 13u + 1)(u^{15} + 23u^{14} + \dots + 6467u + 961)$
$c_2$	$(u^{12} - 5u^{10} + u^9 + 11u^8 - 4u^7 - 15u^6 + 6u^5 + 13u^4 - 5u^3 - 6u^2 + u + 1)$ $\cdot (u^{15} + u^{14} + \dots + 71u + 31)$
$c_3$	$(u^{12} + 3u^{11} + 3u^{10} + u^9 - 3u^8 - 6u^7 - u^6 + 4u^5 + 4u^4 + u^3 - 3u^2 - 2u - 1)$ $\cdot (u^{15} - 4u^{14} + \dots + 312u + 49)$
$c_4$	$(u^{12} + u^{11} + u^{10} - 3u^8 - 3u^7 - u^6 - 3u^5 + 3u^4 + u^3 - 1)$ $\cdot (u^{15} - 5u^{14} + \dots - 36u - 8)$
$c_5, c_6$	$(u^{12} + 8u^{10} + 24u^8 + 32u^6 + u^5 + 15u^4 + 3u^3 - 2u^2 + 2u - 1)$ $\cdot (u^{15} + u^{14} + \dots - 6u - 1)$
$c_7$	$(u^{12} - 5u^{10} - u^9 + 11u^8 + 4u^7 - 15u^6 - 6u^5 + 13u^4 + 5u^3 - 6u^2 - u + 1)$ $\cdot (u^{15} + u^{14} + \dots + 71u + 31)$
$c_8$	$(u^{12} - u^{11} + u^{10} - 3u^8 + 3u^7 - u^6 + 3u^5 + 3u^4 - u^3 - 1)$ $\cdot (u^{15} - 5u^{14} + \dots - 36u - 8)$
$c_9$	$(u^{12} - u^9 - 3u^8 + 3u^7 + u^6 + 3u^5 + 3u^4 - u^2 - u - 1)$ $\cdot (u^{15} - u^{14} + \dots - 167u - 151)$
$c_{10}, c_{11}$	$(u^{12} + 8u^{10} + 24u^8 + 32u^6 - u^5 + 15u^4 - 3u^3 - 2u^2 - 2u - 1)$ $\cdot (u^{15} + u^{14} + \dots - 6u - 1)$
$c_{12}$	$(u^{12} - 4u^{11} + \dots + 10u + 4)(u^{15} + 3u^{14} + \dots - 10u - 4)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{12} - 6y^{11} + \dots - 25y + 1)$ $\cdot (y^{15} - 51y^{14} + \dots + 52633339y - 923521)$
$c_2, c_7$	$(y^{12} - 10y^{11} + \dots - 13y + 1)(y^{15} - 23y^{14} + \dots + 6467y - 961)$
$c_3$	$(y^{12} - 3y^{11} + \dots + 2y + 1)(y^{15} - 36y^{14} + \dots + 43640y - 2401)$
$c_4, c_8$	$(y^{12} + y^{11} - 5y^{10} - 2y^9 + 19y^8 + y^7 - 37y^6 - 11y^5 + 21y^4 + y^3 - 6y^2 + 1)$ $\cdot (y^{15} - 27y^{14} + \dots + 1936y - 64)$
$c_5, c_6, c_{10}$ $c_{11}$	$(y^{12} + 16y^{11} + \dots - 38y^2 + 1)(y^{15} + 11y^{14} + \dots + 18y - 1)$
$c_9$	$(y^{12} - 6y^{10} + y^9 + 21y^8 - 11y^7 - 37y^6 + y^5 + 19y^4 - 2y^3 - 5y^2 + y + 1)$ $\cdot (y^{15} - 41y^{14} + \dots + 123925y - 22801)$
$c_{12}$	$(y^{12} - 20y^{11} + \dots - 44y + 16)(y^{15} - 25y^{14} + \dots + 428y - 16)$