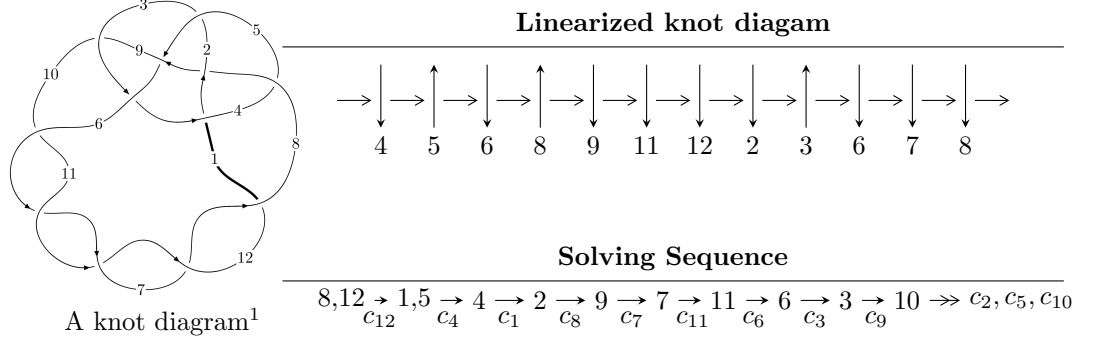


12n<sub>0666</sub> (K12n<sub>0666</sub>)



**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$\begin{aligned}
 I_1^u &= \langle -u^{15} + 6u^{13} + \dots + b - 4, -5u^{15} - 4u^{14} + \dots + 3a - 13, u^{16} + 2u^{15} + \dots - 13u + 3 \rangle \\
 I_2^u &= \langle -u^{13}a + u^{13} + \dots - a + 1, -u^{13}a - 2u^{13} + \dots + a + 7, \\
 &\quad u^{14} - u^{13} - 7u^{12} + 5u^{11} + 19u^{10} - 4u^9 - 26u^8 - 13u^7 + 17u^6 + 21u^5 + u^4 - 4u^3 - 6u^2 - 3u - 1 \rangle \\
 I_3^u &= \langle u^6 - 4u^4 + 2u^3 + 4u^2 + b - 3u + 1, -u^5 - u^4 + 4u^3 + 2u^2 + a - 5u - 1, \\
 &\quad u^7 + 2u^6 - 3u^5 - 6u^4 + 3u^3 + 5u^2 + 1 \rangle \\
 I_4^u &= \langle b - 1, a^2 + a + u - 2, u^2 - u - 1 \rangle \\
 I_5^u &= \langle b - 1, a, u + 1 \rangle \\
 I_6^u &= \langle -u^2 + b + 2, -u^2 + 3a - 2u + 1, u^3 + 2u^2 - u - 3 \rangle \\
 I_7^u &= \langle b, a - 1, u - 1 \rangle \\
 I_8^u &= \langle b + 1, a - 1, u - 1 \rangle \\
 \\ 
 I_1^v &= \langle a, b - 1, v + 1 \rangle
 \end{aligned}$$

\* 9 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 62 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\langle -u^{15} + 6u^{13} + \dots + b - 4, -5u^{15} - 4u^{14} + \dots + 3a - 13, u^{16} + 2u^{15} + \dots - 13u + 3 \rangle$$

I.  $I_1^u =$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{5}{3}u^{15} + \frac{4}{3}u^{14} + \dots - 18u + \frac{13}{3} \\ u^{15} - 6u^{13} + \dots - 18u + 4 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{5}{3}u^{15} + \frac{4}{3}u^{14} + \dots - 18u + \frac{13}{3} \\ 5u^{15} + 3u^{14} + \dots - 49u + 10 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} \frac{2}{3}u^{15} - \frac{2}{3}u^{14} + \dots - 13u + \frac{10}{3} \\ 3u^{15} + u^{14} + \dots - 35u + 7 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{1}{3}u^{15} - \frac{4}{3}u^{14} + \dots - 20u + \frac{11}{3} \\ u^{15} - u^{14} + \dots - 24u + 5 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} \frac{2}{3}u^{15} - \frac{2}{3}u^{14} + \dots + 6u - \frac{5}{3} \\ 2u^{15} + u^{14} + \dots - 8u + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^4 + 3u^2 - 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = 5u^{15} + 4u^{14} - 36u^{13} - 14u^{12} + 103u^{11} - 32u^{10} - 158u^9 + 170u^8 + 88u^7 - 217u^6 + 91u^5 + 87u^4 - 95u^3 + 35u^2 + 10u - 18$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^{16} + u^{15} + \dots + 13u + 1$
$c_2$	$u^{16} + 10u^{15} + \dots - 5u - 3$
$c_4, c_9$	$u^{16} - 5u^{15} + \dots - 17u + 5$
$c_5, c_8$	$u^{16} + 2u^{15} + \dots - 2u - 1$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$u^{16} - 2u^{15} + \dots + 13u + 3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^{16} + 13y^{15} + \dots - 49y + 1$
$c_2$	$y^{16} - 4y^{14} + \dots + 113y + 9$
$c_4, c_9$	$y^{16} - 11y^{15} + \dots - 199y + 25$
$c_5, c_8$	$y^{16} - 10y^{15} + \dots - 18y + 1$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$y^{16} - 16y^{15} + \dots - 43y + 9$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.548500 + 0.853725I$ $a = 0.30836 - 1.43712I$ $b = -0.66590 - 1.54507I$	$5.38391 - 10.31740I$	$-5.41022 + 7.34778I$
$u = 0.548500 - 0.853725I$ $a = 0.30836 + 1.43712I$ $b = -0.66590 + 1.54507I$	$5.38391 + 10.31740I$	$-5.41022 - 7.34778I$
$u = 0.578322 + 0.876148I$ $a = -0.869193 + 0.857447I$ $b = -0.18633 + 1.46072I$	$5.31272 + 4.64447I$	$-4.44340 - 2.64217I$
$u = 0.578322 - 0.876148I$ $a = -0.869193 - 0.857447I$ $b = -0.18633 - 1.46072I$	$5.31272 - 4.64447I$	$-4.44340 + 2.64217I$
$u = 0.217481 + 0.592732I$ $a = 0.47227 + 1.50811I$ $b = 0.203575 + 0.996171I$	$0.50766 - 2.36838I$	$-7.45824 + 4.04010I$
$u = 0.217481 - 0.592732I$ $a = 0.47227 - 1.50811I$ $b = 0.203575 - 0.996171I$	$0.50766 + 2.36838I$	$-7.45824 - 4.04010I$
$u = 1.39667$ $a = -1.16562$ $b = 1.59448$	$-6.42671$	$-13.8540$
$u = -1.384810 + 0.218261I$ $a = -0.413538 - 0.720270I$ $b = 0.78536 - 1.50062I$	$-4.59888 + 5.31561I$	$-16.0697 - 5.0195I$
$u = -1.384810 - 0.218261I$ $a = -0.413538 + 0.720270I$ $b = 0.78536 + 1.50062I$	$-4.59888 - 5.31561I$	$-16.0697 + 5.0195I$
$u = -1.48477 + 0.03326I$ $a = 0.374186 + 0.661888I$ $b = 0.159333 + 0.652088I$	$-7.28530 - 0.33372I$	$-13.77762 + 1.31768I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.48477 - 0.03326I$		
$a = 0.374186 - 0.661888I$	$-7.28530 + 0.33372I$	$-13.77762 - 1.31768I$
$b = 0.159333 - 0.652088I$		
$u = 0.471433 + 0.149281I$		
$a = 1.189440 + 0.539880I$	$-0.951255 - 0.232345I$	$-11.11372 + 2.61454I$
$b = 0.190619 - 0.017488I$		
$u = 0.471433 - 0.149281I$		
$a = 1.189440 - 0.539880I$	$-0.951255 + 0.232345I$	$-11.11372 - 2.61454I$
$b = 0.190619 + 0.017488I$		
$u = -1.54560 + 0.31071I$		
$a = 0.806991 + 0.667934I$	$-1.4014 + 14.5984I$	$-9.03391 - 7.72929I$
$b = -1.09400 + 1.47232I$		
$u = -1.54560 - 0.31071I$		
$a = 0.806991 - 0.667934I$	$-1.4014 - 14.5984I$	$-9.03391 + 7.72929I$
$b = -1.09400 - 1.47232I$		
$u = 1.80224$		
$a = -0.238089$	$-15.4721$	$-27.5320$
$b = 0.620201$		

**II.**

$$I_2^u = \langle -u^{13}a + u^{13} + \dots - a + 1, -u^{13}a - 2u^{13} + \dots + a + 7, u^{14} - u^{13} + \dots - 3u - 1 \rangle$$

**(i) Arc colorings**

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ u^{13}a - u^{13} + \dots + a - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ u^{13}a - u^{13} + \dots + a - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u^{13}a - u^{12}a + \dots + a - 2 \\ 2u^{13} - 14u^{11} + \dots - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{13}a + u^{13} + \dots + u + 2 \\ -u^{13}a + u^{13} + \dots + 8u + 3 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{13}a - u^{12} + \dots + 2a - 2 \\ u^{13}a - u^{12} + \dots + a - 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^4 + 3u^2 - 1 \\ -u^4 + 2u^2 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes** =  $11u^{13} - 10u^{12} - 72u^{11} + 49u^{10} + 176u^9 - 43u^8 - 211u^7 - 87u^6 + 135u^5 + 125u^4 - 27u^3 - 12u^2 - 25u - 14$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^{28} - 4u^{27} + \dots + 82u - 11$
$c_2$	$(u^{14} - 6u^{13} + \dots - 10u + 4)^2$
$c_4, c_9$	$u^{28} - 2u^{27} + \dots - 264u + 24$
$c_5, c_8$	$u^{28} - u^{27} + \dots - 11u - 1$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$(u^{14} + u^{13} + \dots + 3u - 1)^2$



(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^{28} + 24y^{27} + \dots + 3132y + 121$
$c_2$	$(y^{14} - 4y^{13} + \dots - 188y + 16)^2$
$c_4, c_9$	$y^{28} - 18y^{27} + \dots - 12000y + 576$
$c_5, c_8$	$y^{28} + y^{27} + \dots - 47y + 1$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$(y^{14} - 15y^{13} + \dots + 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.543841 + 0.788845I$ $a = -0.786499 - 1.127240I$ $b = -0.15757 - 1.50904I$	$6.74935 + 2.61367I$	$-3.08817 - 3.10085I$
$u = -0.543841 + 0.788845I$ $a = 0.59080 + 1.44573I$ $b = -0.57036 + 1.40275I$	$6.74935 + 2.61367I$	$-3.08817 - 3.10085I$
$u = -0.543841 - 0.788845I$ $a = -0.786499 + 1.127240I$ $b = -0.15757 + 1.50904I$	$6.74935 - 2.61367I$	$-3.08817 + 3.10085I$
$u = -0.543841 - 0.788845I$ $a = 0.59080 - 1.44573I$ $b = -0.57036 - 1.40275I$	$6.74935 - 2.61367I$	$-3.08817 + 3.10085I$
$u = 1.10803$ $a = 0.948288$ $b = -0.313019$	$-1.64992$	$-5.91590$
$u = 1.10803$ $a = 0.875781$ $b = -0.967676$	$-1.64992$	$-5.91590$
$u = -1.315420 + 0.077239I$ $a = -1.053540 - 0.890197I$ $b = 0.734783 - 1.046780I$	$-2.09644 + 4.46056I$	$-6.21772 - 5.02110I$
$u = -1.315420 + 0.077239I$ $a = 0.461982 - 0.077443I$ $b = -1.17028 - 1.69999I$	$-2.09644 + 4.46056I$	$-6.21772 - 5.02110I$
$u = -1.315420 - 0.077239I$ $a = -1.053540 + 0.890197I$ $b = 0.734783 + 1.046780I$	$-2.09644 - 4.46056I$	$-6.21772 + 5.02110I$
$u = -1.315420 - 0.077239I$ $a = 0.461982 + 0.077443I$ $b = -1.17028 + 1.69999I$	$-2.09644 - 4.46056I$	$-6.21772 + 5.02110I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.45797 + 0.12777I$ $a = -0.697357 + 0.508441I$ $b = 1.08158 + 1.81362I$	$-5.60858 - 6.11443I$	$-13.6408 + 6.9717I$
$u = 1.45797 + 0.12777I$ $a = -0.139548 - 1.280800I$ $b = -0.085041 - 0.349273I$	$-5.60858 - 6.11443I$	$-13.6408 + 6.9717I$
$u = 1.45797 - 0.12777I$ $a = -0.697357 - 0.508441I$ $b = 1.08158 - 1.81362I$	$-5.60858 + 6.11443I$	$-13.6408 - 6.9717I$
$u = 1.45797 - 0.12777I$ $a = -0.139548 + 1.280800I$ $b = -0.085041 + 0.349273I$	$-5.60858 + 6.11443I$	$-13.6408 - 6.9717I$
$u = -0.019410 + 0.530789I$ $a = -0.270655 + 0.346124I$ $b = -1.106740 + 0.564246I$	$1.71604 - 2.54798I$	$-1.07278 + 1.43352I$
$u = -0.019410 + 0.530789I$ $a = 1.01173 + 2.29513I$ $b = 0.289802 + 1.068640I$	$1.71604 - 2.54798I$	$-1.07278 + 1.43352I$
$u = -0.019410 - 0.530789I$ $a = -0.270655 - 0.346124I$ $b = -1.106740 - 0.564246I$	$1.71604 + 2.54798I$	$-1.07278 - 1.43352I$
$u = -0.019410 - 0.530789I$ $a = 1.01173 - 2.29513I$ $b = 0.289802 - 1.068640I$	$1.71604 + 2.54798I$	$-1.07278 - 1.43352I$
$u = -0.357381 + 0.324231I$ $a = -0.75149 - 2.13461I$ $b = 0.39490 - 1.51758I$	$0.35035 + 4.37070I$	$-10.2424 - 10.7977I$
$u = -0.357381 + 0.324231I$ $a = -1.29088 + 2.35828I$ $b = -0.049630 - 0.292724I$	$0.35035 + 4.37070I$	$-10.2424 - 10.7977I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.357381 - 0.324231I$ $a = -0.75149 + 2.13461I$ $b = 0.39490 + 1.51758I$	$0.35035 - 4.37070I$	$-10.2424 + 10.7977I$
$u = -0.357381 - 0.324231I$ $a = -1.29088 - 2.35828I$ $b = -0.049630 + 0.292724I$	$0.35035 - 4.37070I$	$-10.2424 + 10.7977I$
$u = 1.54231 + 0.28303I$ $a = 0.901435 - 0.599841I$ $b = -0.93554 - 1.19334I$	$-0.04950 - 6.56214I$	$-6.38364 + 4.80522I$
$u = 1.54231 + 0.28303I$ $a = -0.669860 + 0.302514I$ $b = 0.29812 + 1.50281I$	$-0.04950 - 6.56214I$	$-6.38364 + 4.80522I$
$u = 1.54231 - 0.28303I$ $a = 0.901435 + 0.599841I$ $b = -0.93554 + 1.19334I$	$-0.04950 + 6.56214I$	$-6.38364 - 4.80522I$
$u = 1.54231 - 0.28303I$ $a = -0.669860 - 0.302514I$ $b = 0.29812 - 1.50281I$	$-0.04950 + 6.56214I$	$-6.38364 - 4.80522I$
$u = -1.63650$ $a = 1.21145$ $b = -0.967540$	$-10.3421$	$10.2070$
$u = -1.63650$ $a = 0.352250$ $b = 0.800198$	$-10.3421$	$10.2070$

$$\text{III. } I_3^u = \langle u^6 - 4u^4 + 2u^3 + 4u^2 + b - 3u + 1, -u^5 - u^4 + 4u^3 + 2u^2 + a - 5u - 1, u^7 + 2u^6 - 3u^5 - 6u^4 + 3u^3 + 5u^2 + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^5 + u^4 - 4u^3 - 2u^2 + 5u + 1 \\ -u^6 + 4u^4 - 2u^3 - 4u^2 + 3u - 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^5 + u^4 - 4u^3 - 2u^2 + 5u + 1 \\ -2u^6 - u^5 + 8u^4 - 8u^2 + 3u - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^6 + u^5 - 4u^4 - 3u^3 + 5u^2 + 3u - 1 \\ -u^5 + 3u^3 - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^2 - 2 \\ -u^6 - u^5 + 4u^4 + 2u^3 - 4u^2 - u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^5 + u^4 - 4u^3 - 2u^2 + 5u + 2 \\ -u^3 + 2u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^4 - 3u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-3u^6 + u^5 + 15u^4 - 12u^3 - 20u^2 + 17u - 7$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^7 + u^6 + 4u^5 + 5u^4 + 7u^3 + 6u^2 + 4u + 1$
$c_2$	$u^7 + 8u^6 + 31u^5 + 75u^4 + 122u^3 + 133u^2 + 90u + 29$
$c_4, c_9$	$u^7 - u^6 + u^4 + u^3 - 2u^2 + 1$
$c_5, c_8$	$u^7 - 2u^5 - u^4 + u^3 - u - 1$
$c_6, c_7$	$u^7 - 2u^6 - 3u^5 + 6u^4 + 3u^3 - 5u^2 - 1$
$c_{10}, c_{11}, c_{12}$	$u^7 + 2u^6 - 3u^5 - 6u^4 + 3u^3 + 5u^2 + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^7 + 7y^6 + 20y^5 + 27y^4 + 19y^3 + 10y^2 + 4y - 1$
$c_2$	$y^7 - 2y^6 + 5y^5 - 9y^4 + 50y^3 - 79y^2 + 386y - 841$
$c_4, c_9$	$y^7 - y^6 + 4y^5 - 5y^4 + 7y^3 - 6y^2 + 4y - 1$
$c_5, c_8$	$y^7 - 4y^6 + 6y^5 - 7y^4 + 5y^3 - 4y^2 + y - 1$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$y^7 - 10y^6 + 39y^5 - 74y^4 + 65y^3 - 13y^2 - 10y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.278170 + 0.302690I$ $a = 0.690513 + 0.118128I$ $b = -0.587538 - 0.609722I$	$-3.01119 + 1.09708I$	$-11.40523 - 3.58425I$
$u = 1.278170 - 0.302690I$ $a = 0.690513 - 0.118128I$ $b = -0.587538 + 0.609722I$	$-3.01119 - 1.09708I$	$-11.40523 + 3.58425I$
$u = -1.399450 + 0.156175I$ $a = -0.465734 - 0.770245I$ $b = 0.41431 - 1.55213I$	$-3.71133 + 5.67264I$	$-7.64975 - 7.54460I$
$u = -1.399450 - 0.156175I$ $a = -0.465734 + 0.770245I$ $b = 0.41431 + 1.55213I$	$-3.71133 - 5.67264I$	$-7.64975 + 7.54460I$
$u = 0.037900 + 0.397504I$ $a = 1.60254 + 2.17123I$ $b = -0.126346 + 1.154250I$	$1.16830 - 3.69824I$	$-2.64032 + 6.74904I$
$u = 0.037900 - 0.397504I$ $a = 1.60254 - 2.17123I$ $b = -0.126346 - 1.154250I$	$1.16830 + 3.69824I$	$-2.64032 - 6.74904I$
$u = -1.83325$ $a = 0.345358$ $b = -0.400851$	$-15.2105$	$3.39060$



$$\text{IV. } I_4^u = \langle b - 1, a^2 + a + u - 2, u^2 - u - 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} a \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} a \\ au + a + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + 1 \\ au + a + u + 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -au - 2u + 1 \\ -3au - a - 3u - 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u \\ -u - 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ -u - 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} a + 1 \\ au + a + u + 2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes =  $-7u - 22$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$(u - 1)^4$
$c_2$	$u^4$
$c_4, c_5, c_8$ $c_9$	$u^4 + u^3 - 3u^2 - u + 1$
$c_6, c_7$	$(u^2 + u - 1)^2$
$c_{10}, c_{11}, c_{12}$	$(u^2 - u - 1)^2$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$(y - 1)^4$
$c_2$	$y^4$
$c_4, c_5, c_8$ $c_9$	$y^4 - 7y^3 + 13y^2 - 7y + 1$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$(y^2 - 3y + 1)^2$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.618034$ $a = 1.19353$ $b = 1.00000$	-2.63189	-17.6740
$u = -0.618034$ $a = -2.19353$ $b = 1.00000$	-2.63189	-17.6740
$u = 1.61803$ $a = -1.29496$ $b = 1.00000$	-10.5276	-33.3260
$u = 1.61803$ $a = 0.294963$ $b = 1.00000$	-10.5276	-33.3260

$$\mathbf{V}. I_5^u = \langle b - 1, a, u + 1 \rangle$$

**(i) Arc colorings**

$$a_8 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes = -18**

(iv) **u**-Polynomials at the component

Crossings	<b>u</b> -Polynomials at each crossing
$c_1, c_2, c_3$	$u + 1$
$c_4, c_9$	$u$
$c_5, c_6, c_7$ $c_8, c_{10}, c_{11}$ $c_{12}$	$u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_3$ $c_5, c_6, c_7$ $c_8, c_{10}, c_{11}$ $c_{12}$	$y - 1$
$c_4, c_9$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_5^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.00000$		
$a = 0$	-4.93480	-18.0000
$b = 1.00000$		



$$\text{VI. } I_6^u = \langle -u^2 + b + 2, -u^2 + 3a - 2u + 1, u^3 + 2u^2 - u - 3 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} \frac{1}{3}u^2 + \frac{2}{3}u - \frac{1}{3} \\ u^2 - 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} \frac{1}{3}u^2 + \frac{2}{3}u - \frac{1}{3} \\ u^2 + u - 2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -\frac{2}{3}u^2 - \frac{1}{3}u + \frac{5}{3} \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{4}{3}u^2 - \frac{2}{3}u + \frac{7}{3} \\ -u^2 + 2 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 + 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2u^2 + u - 3 \\ 2u^2 - 3 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -\frac{2}{3}u^2 - \frac{1}{3}u + \frac{8}{3} \\ -2u^2 - u + 4 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -2u^2 - u + 5 \\ -3u^2 - u + 6 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u^3 + u - 1$
$c_2$	$u^3 + 2u^2 - u - 3$
$c_4, c_9$	$(u + 1)^3$
$c_5, c_8$	$u^3 - 2u^2 + u + 1$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$u^3 - 2u^2 - u + 3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y^3 + 2y^2 + y - 1$
$c_2, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$y^3 - 6y^2 + 13y - 9$
$c_4, c_9$	$(y - 1)^3$
$c_5, c_8$	$y^3 - 2y^2 + 5y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_6^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.14790$ $a = 0.871157$ $b = -0.682328$	-1.64493	-6.00000
$u = -1.57395 + 0.36899I$ $a = -0.602245 - 0.141188I$ $b = 0.341164 - 1.161540I$	-1.64493	-6.00000
$u = -1.57395 - 0.36899I$ $a = -0.602245 + 0.141188I$ $b = 0.341164 + 1.161540I$	-1.64493	-6.00000

VII.  $I_7^u = \langle b, a - 1, u - 1 \rangle$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 2 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u$
$c_2, c_3$	$u - 1$
$c_4, c_6, c_7$ $c_8, c_9, c_{10}$ $c_{11}, c_{12}$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y$
$c_2, c_3, c_4$ $c_6, c_7, c_8$ $c_9, c_{10}, c_{11}$ $c_{12}$	$y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_7^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 1.00000$	-1.64493	-6.00000
$b = 0$		



VIII.  $I_g^u = \langle b + 1, a - 1, u - 1 \rangle$

(i) Arc colorings

$$a_8 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = -6

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_2$	$u - 1$
$c_3, c_8$	$u$
$c_4, c_5, c_6$ $c_7, c_9, c_{10}$ $c_{11}, c_{12}$	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_2, c_4$ $c_5, c_6, c_7$ $c_9, c_{10}, c_{11}$ $c_{12}$	$y - 1$
$c_3, c_8$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_{\mathfrak{g}}^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 1.00000$	-1.64493	-6.00000
$b = -1.00000$		

$$\text{IX. } I_1^v = \langle a, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_8 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class =  $-1$

(iii) Cusp Shapes =  $-6$

(iv) **u-Polynomials at the component**

Crossings	u-Polynomials at each crossing
$c_1, c_3, c_4$ $c_5, c_8, c_9$	$u + 1$
$c_2, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$u$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_3, c_4$ $c_5, c_8, c_9$	$y - 1$
$c_2, c_6, c_7$ $c_{10}, c_{11}, c_{12}$	$y$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^v$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$v = -1.00000$		
$a = 0$	-1.64493	-6.00000
$b = 1.00000$		



## X. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_3$	$u(u-1)^5(u+1)^2(u^3+u-1)(u^7+u^6+\dots+4u+1)$ $\cdot (u^{16}+u^{15}+\dots+13u+1)(u^{28}-4u^{27}+\dots+82u-11)$
$c_2$	$u^5(u-1)^2(u+1)(u^3+2u^2-u-3)$ $\cdot (u^7+8u^6+31u^5+75u^4+122u^3+133u^2+90u+29)$ $\cdot ((u^{14}-6u^{13}+\dots-10u+4)^2)(u^{16}+10u^{15}+\dots-5u-3)$
$c_4, c_9$	$u(u+1)^6(u^4+u^3-3u^2-u+1)(u^7-u^6+u^4+u^3-2u^2+1)$ $\cdot (u^{16}-5u^{15}+\dots-17u+5)(u^{28}-2u^{27}+\dots-264u+24)$
$c_5, c_8$	$u(u-1)(u+1)^2(u^3-2u^2+u+1)(u^4+u^3-3u^2-u+1)$ $\cdot (u^7-2u^5-u^4+u^3-u-1)(u^{16}+2u^{15}+\dots-2u-1)$ $\cdot (u^{28}-u^{27}+\dots-11u-1)$
$c_6, c_7$	$u(u-1)(u+1)^2(u^2+u-1)^2(u^3-2u^2-u+3)$ $\cdot (u^7-2u^6+\dots-5u^2-1)(u^{14}+u^{13}+\dots+3u-1)^2$ $\cdot (u^{16}-2u^{15}+\dots+13u+3)$
$c_{10}, c_{11}, c_{12}$	$u(u-1)(u+1)^2(u^2-u-1)^2(u^3-2u^2-u+3)$ $\cdot (u^7+2u^6+\dots+5u^2+1)(u^{14}+u^{13}+\dots+3u-1)^2$ $\cdot (u^{16}-2u^{15}+\dots+13u+3)$

## XI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_3$	$y(y-1)^7(y^3+2y^2+y-1)$ $\cdot (y^7+7y^6+20y^5+27y^4+19y^3+10y^2+4y-1)$ $\cdot (y^{16}+13y^{15}+\dots-49y+1)(y^{28}+24y^{27}+\dots+3132y+121)$
$c_2$	$y^5(y-1)^3(y^3-6y^2+13y-9)$ $\cdot (y^7-2y^6+5y^5-9y^4+50y^3-79y^2+386y-841)$ $\cdot ((y^{14}-4y^{13}+\dots-188y+16)^2)(y^{16}-4y^{14}+\dots+113y+9)$
$c_4, c_9$	$y(y-1)^6(y^4-7y^3+13y^2-7y+1)$ $\cdot (y^7-y^6+4y^5-5y^4+7y^3-6y^2+4y-1)$ $\cdot (y^{16}-11y^{15}+\dots-199y+25)(y^{28}-18y^{27}+\dots-12000y+576)$
$c_5, c_8$	$y(y-1)^3(y^3-2y^2+5y-1)(y^4-7y^3+13y^2-7y+1)$ $\cdot (y^7-4y^6+\dots+y-1)(y^{16}-10y^{15}+\dots-18y+1)$ $\cdot (y^{28}+y^{27}+\dots-47y+1)$
$c_6, c_7, c_{10}$ $c_{11}, c_{12}$	$y(y-1)^3(y^2-3y+1)^2(y^3-6y^2+13y-9)$ $\cdot (y^7-10y^6+39y^5-74y^4+65y^3-13y^2-10y-1)$ $\cdot ((y^{14}-15y^{13}+\dots+3y+1)^2)(y^{16}-16y^{15}+\dots-43y+9)$