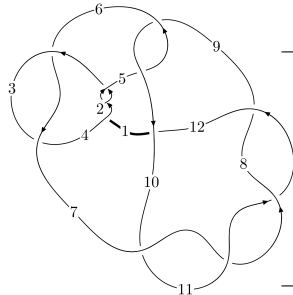
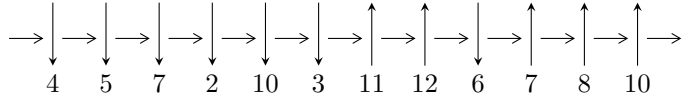


12n₀₆₇₅ (K12n₀₆₇₅)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$7, 10 \xrightarrow{c_{10}} 11 \xrightarrow{c_7} 8 \xrightarrow{c_{11}} 12 \xrightarrow{c_{12}} 1, 4 \xrightarrow{c_3} 3 \xrightarrow{c_6} 6 \xrightarrow{c_5} 5 \xrightarrow{c_2} 2 \xrightarrow{c_9} 9 \rightsquigarrow c_1, c_4, c_8$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 53226740u^{26} - 42852864u^{25} + \dots + 64758649b + 11501166, \\ 64856230u^{26} - 108182252u^{25} + \dots + 129517298a - 547630611, u^{27} - 4u^{26} + \dots + 4u + 1 \rangle$$

$$I_2^u = \langle b + u, a + u + 2, u^2 + u - 1 \rangle$$

$$I_3^u = \langle b + u, a - 1, u^2 + u - 1 \rangle$$

$$I_4^u = \langle b + 1, a, u - 1 \rangle$$

* 4 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 32 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } J_1^u = \langle 5.32 \times 10^7 u^{26} - 4.29 \times 10^7 u^{25} + \dots + 6.48 \times 10^7 b + 1.15 \times 10^7, 6.49 \times 10^7 u^{26} - 1.08 \times 10^8 u^{25} + \dots + 1.30 \times 10^8 a - 5.48 \times 10^8, u^{27} - 4u^{26} + \dots + 4u + 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^4 - 3u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -0.500753u^{26} + 0.835273u^{25} + \dots - 23.9653u + 4.22824 \\ -0.821925u^{26} + 0.661732u^{25} + \dots - 3.64955u - 0.177600 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.500753u^{26} + 0.835273u^{25} + \dots - 23.9653u + 4.22824 \\ 0.858098u^{26} - 3.24135u^{25} + \dots - 8.82126u - 1.34534 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2.71316u^{26} - 6.18461u^{25} + \dots + 6.88730u - 3.99351 \\ -2.21391u^{26} + 5.01988u^{25} + \dots + 8.14742u + 1.22175 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0.499247u^{26} - 1.16473u^{25} + \dots + 15.0347u - 2.77176 \\ -2.21391u^{26} + 5.01988u^{25} + \dots + 8.14742u + 1.22175 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.499247u^{26} + 1.16473u^{25} + \dots - 15.0347u + 2.77176 \\ -1.71408u^{26} + 2.71888u^{25} + \dots - 0.116110u + 0.211149 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^3 + 2u \\ u^5 - 3u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{1678565237}{129517298} u^{26} - \frac{2789533850}{64758649} u^{25} + \dots - \frac{5239074250}{64758649} u - \frac{3637568297}{129517298}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_4	$u^{27} - 4u^{26} + \dots - 8u + 1$
c_3, c_6	$u^{27} + 3u^{26} + \dots - 5u^2 + 2$
c_5, c_9	$u^{27} + 2u^{26} + \dots + 64u + 16$
c_7, c_8, c_{10} c_{11}	$u^{27} - 4u^{26} + \dots + 4u + 1$
c_{12}	$u^{27} + 18u^{26} + \dots + 3596u - 79$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$y^{27} - 18y^{26} + \dots + 32y - 1$
c_3, c_6	$y^{27} + 3y^{26} + \dots + 20y - 4$
c_5, c_9	$y^{27} + 24y^{26} + \dots + 5760y - 256$
c_7, c_8, c_{10} c_{11}	$y^{27} - 38y^{26} + \dots + 124y - 1$
c_{12}	$y^{27} - 98y^{26} + \dots + 19523924y - 6241$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.121780 + 0.081011I$ $a = 0.927106 - 0.741069I$ $b = -0.180646 - 0.935031I$	$3.25561 - 1.59407I$	$1.48399 + 1.30043I$
$u = -1.121780 - 0.081011I$ $a = 0.927106 + 0.741069I$ $b = -0.180646 + 0.935031I$	$3.25561 + 1.59407I$	$1.48399 - 1.30043I$
$u = 0.676956 + 0.533355I$ $a = -0.448265 - 0.714880I$ $b = -0.426855 - 0.510105I$	$1.49150 + 0.51721I$	$4.06426 - 0.81218I$
$u = 0.676956 - 0.533355I$ $a = -0.448265 + 0.714880I$ $b = -0.426855 + 0.510105I$	$1.49150 - 0.51721I$	$4.06426 + 0.81218I$
$u = 0.791066 + 0.310151I$ $a = -0.264806 - 0.568080I$ $b = -0.454975 - 0.578171I$	$1.41628 + 0.49520I$	$5.40104 - 1.30639I$
$u = 0.791066 - 0.310151I$ $a = -0.264806 + 0.568080I$ $b = -0.454975 + 0.578171I$	$1.41628 - 0.49520I$	$5.40104 + 1.30639I$
$u = 0.228516 + 0.809567I$ $a = 0.877576 + 0.806986I$ $b = 0.241186 + 0.308813I$	$0.00983 + 4.15530I$	$-1.52548 - 6.50197I$
$u = 0.228516 - 0.809567I$ $a = 0.877576 - 0.806986I$ $b = 0.241186 - 0.308813I$	$0.00983 - 4.15530I$	$-1.52548 + 6.50197I$
$u = -1.100020 + 0.502260I$ $a = 0.243788 + 1.127340I$ $b = 0.07217 + 1.44072I$	$4.12391 - 8.58608I$	$0.18359 + 6.75545I$
$u = -1.100020 - 0.502260I$ $a = 0.243788 - 1.127340I$ $b = 0.07217 - 1.44072I$	$4.12391 + 8.58608I$	$0.18359 - 6.75545I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.240020 + 0.262480I$ $a = -0.444851 - 0.925878I$ $b = 0.124876 - 1.372680I$	$7.42745 - 3.21213I$	$3.92477 + 2.89567I$
$u = -1.240020 - 0.262480I$ $a = -0.444851 + 0.925878I$ $b = 0.124876 + 1.372680I$	$7.42745 + 3.21213I$	$3.92477 - 2.89567I$
$u = 0.687500$ $a = 0.446145$ $b = -3.22294$	-0.443313	-52.6840
$u = 1.42416$ $a = 0.788121$ $b = 1.37734$	-1.56955	-5.83560
$u = -0.505186$ $a = -3.09428$ $b = -0.715357$	-8.08146	-27.4200
$u = -1.62890$ $a = -0.330211$ $b = 2.82377$	7.71976	-34.5090
$u = 0.272815 + 0.206929I$ $a = -1.71928 - 0.05752I$ $b = 1.028070 + 0.618606I$	$-1.240020 + 0.678999I$	$-6.54613 + 1.58470I$
$u = 0.272815 - 0.206929I$ $a = -1.71928 + 0.05752I$ $b = 1.028070 - 0.618606I$	$-1.240020 - 0.678999I$	$-6.54613 - 1.58470I$
$u = 1.75657 + 0.14232I$ $a = -0.583385 + 0.775944I$ $b = -0.52277 + 2.72994I$	$14.1973 + 11.3192I$	0
$u = 1.75657 - 0.14232I$ $a = -0.583385 - 0.775944I$ $b = -0.52277 - 2.72994I$	$14.1973 - 11.3192I$	0

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.76109 + 0.08264I$ $a = -0.058331 - 0.610400I$ $b = 0.11130 - 2.01234I$	$11.07900 - 2.32684I$	0
$u = -1.76109 - 0.08264I$ $a = -0.058331 + 0.610400I$ $b = 0.11130 + 2.01234I$	$11.07900 + 2.32684I$	0
$u = 1.76627 + 0.02002I$ $a = -0.752423 - 0.715336I$ $b = -1.05997 - 2.28626I$	$13.78760 + 2.02303I$	0
$u = 1.76627 - 0.02002I$ $a = -0.752423 + 0.715336I$ $b = -1.05997 + 2.28626I$	$13.78760 - 2.02303I$	0
$u = 1.79047 + 0.06797I$ $a = 0.655019 - 0.749285I$ $b = 0.73536 - 2.51744I$	$18.4512 + 4.7028I$	0
$u = 1.79047 - 0.06797I$ $a = 0.655019 + 0.749285I$ $b = 0.73536 + 2.51744I$	$18.4512 - 4.7028I$	0
$u = -0.0970792$ $a = 6.32592$ $b = 0.401694$	-0.870483	-12.0480

$$\text{II. } I_2^u = \langle b + u, a + u + 2, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u - 2 \\ -u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u - 2 \\ -u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2u + 3 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2u + 3 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 2u + 3 \\ -u + 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 16

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_3 c_{10}, c_{11}, c_{12}	$u^2 + u - 1$
c_4, c_6, c_7 c_8	$u^2 - u - 1$
c_5, c_9	u^2

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3 c_4, c_6, c_7 c_8, c_{10}, c_{11} c_{12}	$y^2 - 3y + 1$
c_5, c_9	y^2

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$ $a = -2.61803$ $b = -0.618034$	-7.89568	16.0000
$u = -1.61803$ $a = -0.381966$ $b = 1.61803$	7.89568	16.0000

$$\text{III. } \Gamma_3^u = \langle b + u, a - 1, u^2 + u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u \\ -u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} u \\ -u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ -u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u \\ -1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 1

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_2, c_3 c_{10}, c_{11}, c_{12}	$u^2 + u - 1$
c_4, c_6, c_7 c_8	$u^2 - u - 1$
c_5, c_9	u^2

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_3 c_4, c_6, c_7 c_8, c_{10}, c_{11} c_{12}	$y^2 - 3y + 1$
c_5, c_9	y^2

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.618034$ $a = 1.00000$ $b = -0.618034$	0	1.00000
$u = -1.61803$ $a = 1.00000$ $b = 1.61803$	0	1.00000

$$\text{IV. } I_4^u = \langle b + 1, a, u - 1 \rangle$$

(i) Arc colorings

$$a_7 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ -2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u**-Polynomials at the component

Crossings	u -Polynomials at each crossing
c_1, c_2, c_9 c_{10}, c_{11}, c_{12}	$u - 1$
c_3, c_6	u
c_4, c_5, c_7 c_8	$u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_5, c_7, c_8 c_9, c_{10}, c_{11} c_{12}	$y - 1$
c_3, c_6	y

(vi) Complex Volumes and Cusp Shapes

Solutions to I_4^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 0$	0	0
$b = -1.00000$		

V. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1, c_2	$(u - 1)(u^2 + u - 1)^2(u^{27} - 4u^{26} + \dots - 8u + 1)$
c_3	$u(u^2 + u - 1)^2(u^{27} + 3u^{26} + \dots - 5u^2 + 2)$
c_4	$(u + 1)(u^2 - u - 1)^2(u^{27} - 4u^{26} + \dots - 8u + 1)$
c_5	$u^4(u + 1)(u^{27} + 2u^{26} + \dots + 64u + 16)$
c_6	$u(u^2 - u - 1)^2(u^{27} + 3u^{26} + \dots - 5u^2 + 2)$
c_7, c_8	$(u + 1)(u^2 - u - 1)^2(u^{27} - 4u^{26} + \dots + 4u + 1)$
c_9	$u^4(u - 1)(u^{27} + 2u^{26} + \dots + 64u + 16)$
c_{10}, c_{11}	$(u - 1)(u^2 + u - 1)^2(u^{27} - 4u^{26} + \dots + 4u + 1)$
c_{12}	$(u - 1)(u^2 + u - 1)^2(u^{27} + 18u^{26} + \dots + 3596u - 79)$

VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4	$(y - 1)(y^2 - 3y + 1)^2(y^{27} - 18y^{26} + \dots + 32y - 1)$
c_3, c_6	$y(y^2 - 3y + 1)^2(y^{27} + 3y^{26} + \dots + 20y - 4)$
c_5, c_9	$y^4(y - 1)(y^{27} + 24y^{26} + \dots + 5760y - 256)$
c_7, c_8, c_{10} c_{11}	$(y - 1)(y^2 - 3y + 1)^2(y^{27} - 38y^{26} + \dots + 124y - 1)$
c_{12}	$(y - 1)(y^2 - 3y + 1)^2(y^{27} - 98y^{26} + \dots + 1.95239 \times 10^7 y - 6241)$