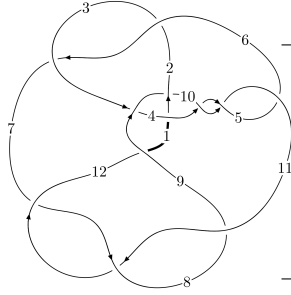
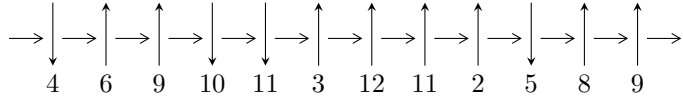


12n<sub>0768</sub> (K12n<sub>0768</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$5,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_5} 6 \xrightarrow{c_4} 2,4 \xrightarrow{c_1} 1 \xrightarrow{c_9} 9 \xrightarrow{c_3} 3 \xrightarrow{c_6} 7 \xrightarrow{c_8} 8 \xrightarrow{c_{12}} 12 \rightsquigarrow c_2, c_7, c_{11}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle -2.92778 \times 10^{21}u^{25} + 2.56531 \times 10^{22}u^{24} + \dots + 3.87990 \times 10^{23}b - 1.26738 \times 10^{24}, \\ 2.71108 \times 10^{23}u^{25} + 1.09424 \times 10^{24}u^{24} + \dots + 1.20277 \times 10^{25}a - 1.27374 \times 10^{26}, u^{26} - u^{25} + \dots + 12u + 3 \rangle$$

$$I_2^u = \langle -u^{13} + 6u^{11} + u^{10} - 14u^9 - 6u^8 + 14u^7 + 15u^6 - 3u^5 - 18u^4 - 5u^3 + 9u^2 + b + 3u - 1, \\ -u^{13} + u^{12} + 6u^{11} - 4u^{10} - 15u^9 + 2u^8 + 19u^7 + 13u^6 - 12u^5 - 22u^4 + 10u^2 + a + 5u - 1, \\ u^{14} - 7u^{12} - u^{11} + 19u^{10} + 7u^9 - 23u^8 - 20u^7 + 8u^6 + 28u^5 + 7u^4 - 17u^3 - 6u^2 + 2u + 1 \rangle$$

\* 2 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 40 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle -2.93 \times 10^{21}u^{25} + 2.57 \times 10^{22}u^{24} + \dots + 3.88 \times 10^{23}b - 1.27 \times 10^{24}, 2.71 \times 10^{23}u^{25} + 1.09 \times 10^{24}u^{24} + \dots + 1.20 \times 10^{25}a - 1.27 \times 10^{26}, u^{26} - u^{25} + \dots + 12u + 31 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -0.0225403u^{25} - 0.0909766u^{24} + \dots + 5.26309u + 10.5900 \\ 0.00754601u^{25} - 0.0661178u^{24} + \dots - 2.55257u + 3.26654 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -0.0460308u^{25} - 0.0975533u^{24} + \dots + 3.67107u + 8.88673 \\ -0.0159445u^{25} - 0.0726945u^{24} + \dots - 4.14458u + 1.56324 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0228681u^{25} - 0.107777u^{24} + \dots - 0.424141u + 6.30289 \\ 0.105094u^{25} - 0.0463805u^{24} + \dots - 7.82285u - 2.16744 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.0714029u^{25} - 0.131292u^{24} + \dots + 7.63526u + 15.5015 \\ 0.00756581u^{25} - 0.0451761u^{24} + \dots - 2.33987u + 1.11953 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.466848u^{25} + 0.229048u^{24} + \dots + 25.8666u + 8.47181 \\ 0.0444585u^{25} + 0.0166367u^{24} + \dots - 2.65167u - 3.76153 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.192283u^{25} - 0.0910018u^{24} + \dots + 9.67536u + 12.5203 \\ -0.00596389u^{25} - 0.0322573u^{24} + \dots - 0.739325u + 2.56438 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.235482u^{25} - 0.154199u^{24} + \dots - 20.6106u - 7.26827 \\ 0.0223603u^{25} - 0.0205281u^{24} + \dots - 3.27390u - 0.0676271 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = -\frac{46652502203510047014961}{129330126954099989822173}u^{25} + \frac{99744336497876668876271}{387990380862299969466519}u^{24} + \dots + \frac{7467042075154247618912122}{387990380862299969466519}u - \frac{1919651047154391762384890}{387990380862299969466519}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{26} - 24u^{24} + \dots - 352u + 41$
$c_2, c_6$	$u^{26} - 4u^{25} + \dots - 322u - 529$
$c_3$	$u^{26} - u^{25} + \dots - 12769u - 1781$
$c_4, c_5, c_{10}$	$u^{26} + u^{25} + \dots - 12u + 31$
$c_7, c_8, c_{11}$	$u^{26} + u^{25} + \dots - 34u - 4$
$c_9$	$u^{26} + 2u^{25} + \dots + 36u - 19$
$c_{12}$	$u^{26} - u^{25} + \dots - 304218u - 40564$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{26} - 48y^{25} + \dots + 19924y + 1681$
$c_2, c_6$	$y^{26} + 12y^{25} + \dots - 348082y + 279841$
$c_3$	$y^{26} + 69y^{25} + \dots - 266466469y + 3171961$
$c_4, c_5, c_{10}$	$y^{26} - 33y^{25} + \dots - 12482y + 961$
$c_7, c_8, c_{11}$	$y^{26} + 43y^{25} + \dots - 716y + 16$
$c_9$	$y^{26} + 6y^{25} + \dots + 1782y + 361$
$c_{12}$	$y^{26} + 147y^{25} + \dots - 80260701260y + 1645438096$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.764982 + 0.335496I$ $a = 0.043942 - 0.279919I$ $b = 1.019140 - 0.401366I$	$-1.38320 - 3.64635I$	$1.35824 + 7.32767I$
$u = 0.764982 - 0.335496I$ $a = 0.043942 + 0.279919I$ $b = 1.019140 + 0.401366I$	$-1.38320 + 3.64635I$	$1.35824 - 7.32767I$
$u = 0.777607 + 0.118039I$ $a = 2.55907 - 0.95852I$ $b = -0.478055 - 0.742412I$	$-13.15060 - 0.37776I$	$-1.22408 - 1.34498I$
$u = 0.777607 - 0.118039I$ $a = 2.55907 + 0.95852I$ $b = -0.478055 + 0.742412I$	$-13.15060 + 0.37776I$	$-1.22408 + 1.34498I$
$u = 0.842907 + 0.881469I$ $a = -0.571747 + 0.134450I$ $b = -0.469429 - 0.674553I$	$-1.203930 - 0.496037I$	$0.79686 - 2.54300I$
$u = 0.842907 - 0.881469I$ $a = -0.571747 - 0.134450I$ $b = -0.469429 + 0.674553I$	$-1.203930 + 0.496037I$	$0.79686 + 2.54300I$
$u = -0.719777$ $a = -0.187725$ $b = -1.16272$	2.17524	2.79410
$u = 0.159981 + 0.568954I$ $a = 0.445478 + 0.461168I$ $b = -0.321692 + 0.362997I$	$0.333623 - 1.008960I$	$5.28376 + 6.66934I$
$u = 0.159981 - 0.568954I$ $a = 0.445478 - 0.461168I$ $b = -0.321692 - 0.362997I$	$0.333623 + 1.008960I$	$5.28376 - 6.66934I$
$u = -1.40068 + 0.23284I$ $a = -0.23778 + 1.47903I$ $b = 0.413279 + 0.877413I$	$-4.79645 + 4.01069I$	$0.34699 - 9.12487I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.40068 - 0.23284I$ $a = -0.23778 - 1.47903I$ $b = 0.413279 - 0.877413I$	$-4.79645 - 4.01069I$	$0.34699 + 9.12487I$
$u = -0.571043$ $a = 2.07972$ $b = 0.907867$	$2.93787$	$-5.61080$
$u = -0.484610 + 0.243441I$ $a = -1.71290 + 0.53126I$ $b = 0.461065 + 0.861987I$	$-3.51192 + 0.62346I$	$-2.84586 - 0.67416I$
$u = -0.484610 - 0.243441I$ $a = -1.71290 - 0.53126I$ $b = 0.461065 - 0.861987I$	$-3.51192 - 0.62346I$	$-2.84586 + 0.67416I$
$u = 1.52698 + 0.20871I$ $a = 0.133555 + 1.387270I$ $b = -1.051380 + 0.928731I$	$-10.29450 - 2.62985I$	$-1.70383 + 1.78381I$
$u = 1.52698 - 0.20871I$ $a = 0.133555 - 1.387270I$ $b = -1.051380 - 0.928731I$	$-10.29450 + 2.62985I$	$-1.70383 - 1.78381I$
$u = -0.82721 + 1.33251I$ $a = 0.352400 - 0.194950I$ $b = -0.445225 - 1.242010I$	$-15.2105 + 4.3640I$	$-1.41577 - 3.17462I$
$u = -0.82721 - 1.33251I$ $a = 0.352400 + 0.194950I$ $b = -0.445225 + 1.242010I$	$-15.2105 - 4.3640I$	$-1.41577 + 3.17462I$
$u = 1.65746 + 0.14713I$ $a = 0.159581 + 0.992092I$ $b = 0.250667 + 1.107520I$	$-5.67875 - 1.02437I$	$-0.521896 - 0.910763I$
$u = 1.65746 - 0.14713I$ $a = 0.159581 - 0.992092I$ $b = 0.250667 - 1.107520I$	$-5.67875 + 1.02437I$	$-0.521896 + 0.910763I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.77337 + 0.06842I$		
$a = 0.294799 - 0.960179I$	$16.7710 + 1.3129I$	$-1.252333 - 0.225172I$
$b = 1.44079 - 1.23613I$		
$u = -1.77337 - 0.06842I$		
$a = 0.294799 + 0.960179I$	$16.7710 - 1.3129I$	$-1.252333 + 0.225172I$
$b = 1.44079 + 1.23613I$		
$u = 1.74642 + 0.44620I$		
$a = -0.080704 - 1.254640I$	$16.0643 - 11.0020I$	$-1.09431 + 4.10898I$
$b = 1.18154 - 1.35502I$		
$u = 1.74642 - 0.44620I$		
$a = -0.080704 + 1.254640I$	$16.0643 + 11.0020I$	$-1.09431 - 4.10898I$
$b = 1.18154 + 1.35502I$		
$u = -1.84505 + 0.14739I$		
$a = -0.154266 - 1.018760I$	$-11.74950 + 5.10402I$	$-1.81943 - 2.88501I$
$b = -0.87327 - 1.36223I$		
$u = -1.84505 - 0.14739I$		
$a = -0.154266 + 1.018760I$	$-11.74950 - 5.10402I$	$-1.81943 + 2.88501I$
$b = -0.87327 + 1.36223I$		

**II.**

$$I_2^u = \langle -u^{13} + 6u^{11} + \dots + b - 1, -u^{13} + u^{12} + \dots + a - 1, u^{14} - 7u^{12} + \dots + 2u + 1 \rangle$$

**(i) Arc colorings**

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u \\ -u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{13} - u^{12} + \dots - 5u + 1 \\ u^{13} - 6u^{11} + \dots - 3u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^{13} + u^{12} + \dots - 4u^2 - 7u \\ u^{13} + 2u^{12} + \dots - 3u^2 - 5u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^{13} + 2u^{12} + \dots + 10u^3 + 3 \\ 2u^{12} - u^{11} + \dots - u + 1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^{13} - 6u^{11} + \dots - 5u^2 - 8u \\ u^{13} - 6u^{11} + \dots - 2u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^{13} - 5u^{11} - u^{10} + 8u^9 + 4u^8 - u^7 - 5u^6 - 6u^5 - u^3 + 3u^2 + 6u \\ u^{12} + u^{11} + \dots + u - 2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -3u^{13} + 4u^{12} + \dots + 20u^2 - 2u \\ -2u^{13} + 5u^{12} + \dots - 3u - 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -4u^{13} + 5u^{12} + \dots - 5u - 7 \\ -3u^{13} + 6u^{12} + \dots - 8u - 4 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes =**

$$-2u^{13} - 3u^{12} + 16u^{11} + 20u^{10} - 44u^9 - 56u^8 + 40u^7 + 84u^6 + 28u^5 - 71u^4 - 68u^3 + 24u^2 + 27u + 7$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{14} - 5u^{13} + \dots - u^2 + 1$
$c_2$	$u^{14} - 3u^{13} + 8u^{11} - 9u^{10} + 13u^8 - 16u^7 + 14u^5 - 9u^4 - 3u^3 + 4u^2 - 1$
$c_3$	$u^{14} + 4u^{12} + 5u^{10} + 2u^9 - 3u^8 + 4u^7 - u^6 - u^5 + u^4 + 2u^3 + u^2 - u - 1$
$c_4, c_5$	$u^{14} - 7u^{12} + \dots - 2u + 1$
$c_6$	$u^{14} + 3u^{13} - 8u^{11} - 9u^{10} + 13u^8 + 16u^7 - 14u^5 - 9u^4 + 3u^3 + 4u^2 - 1$
$c_7, c_8$	$u^{14} + 9u^{12} + \dots + 2u - 1$
$c_9$	$u^{14} + u^{13} - u^{12} - 2u^{11} - u^{10} + u^9 + u^8 - 4u^7 + 3u^6 - 2u^5 - 5u^4 - 4u^2 - 1$
$c_{10}$	$u^{14} - 7u^{12} + \dots + 2u + 1$
$c_{11}$	$u^{14} + 9u^{12} + \dots - 2u - 1$
$c_{12}$	$u^{14} + 11u^{12} + \dots - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{14} - 17y^{13} + \dots - 2y + 1$
$c_2, c_6$	$y^{14} - 9y^{13} + \dots - 8y + 1$
$c_3$	$y^{14} + 8y^{13} + \dots - 3y + 1$
$c_4, c_5, c_{10}$	$y^{14} - 14y^{13} + \dots - 16y + 1$
$c_7, c_8, c_{11}$	$y^{14} + 18y^{13} + \dots - 6y + 1$
$c_9$	$y^{14} - 3y^{13} + \dots + 8y + 1$
$c_{12}$	$y^{14} + 22y^{13} + \dots - 4y + 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.388251 + 0.920456I$		
$a = 0.055423 - 0.175899I$	$-1.29955 + 1.48242I$	$0.47756 - 5.07450I$
$b = 0.169523 + 0.638462I$		
$u = -0.388251 - 0.920456I$		
$a = 0.055423 + 0.175899I$	$-1.29955 - 1.48242I$	$0.47756 + 5.07450I$
$b = 0.169523 - 0.638462I$		
$u = 1.132050 + 0.372393I$		
$a = 1.77286 + 0.32994I$	$-13.37670 - 1.61202I$	$-3.25492 + 4.00039I$
$b = -0.171528 + 0.571644I$		
$u = 1.132050 - 0.372393I$		
$a = 1.77286 - 0.32994I$	$-13.37670 + 1.61202I$	$-3.25492 - 4.00039I$
$b = -0.171528 - 0.571644I$		
$u = 1.28132$		
$a = 0.283790$	$0.241511$	$-0.487210$
$b = 1.39820$		
$u = -1.290010 + 0.033553I$		
$a = -0.507609 + 0.986318I$	$-4.48352 - 1.89225I$	$-0.38957 + 1.57022I$
$b = -1.39611 + 0.51797I$		
$u = -1.290010 - 0.033553I$		
$a = -0.507609 - 0.986318I$	$-4.48352 + 1.89225I$	$-0.38957 - 1.57022I$
$b = -1.39611 - 0.51797I$		
$u = -1.38089 + 0.32443I$		
$a = -0.496730 + 1.151660I$	$-5.02225 + 3.24893I$	$-3.06027 - 0.56445I$
$b = 0.353075 + 0.853393I$		
$u = -1.38089 - 0.32443I$		
$a = -0.496730 - 1.151660I$	$-5.02225 - 3.24893I$	$-3.06027 + 0.56445I$
$b = 0.353075 - 0.853393I$		
$u = 1.45042 + 0.21038I$		
$a = -0.11773 + 1.53514I$	$-7.62759 - 4.80166I$	$-1.22227 + 4.11227I$
$b = -0.623035 + 1.209470I$		

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.45042 - 0.21038I$ $a = -0.11773 - 1.53514I$ $b = -0.623035 - 1.209470I$	$-7.62759 + 4.80166I$	$-1.22227 - 4.11227I$
$u = 0.434339$ $a = -2.22641$ $b = -1.03128$	3.32890	16.1810
$u = -0.381146 + 0.175722I$ $a = 1.76509 - 0.05508I$ $b = 0.984611 + 0.552289I$	$-1.22934 + 2.47209I$	$1.10273 - 1.06165I$
$u = -0.381146 - 0.175722I$ $a = 1.76509 + 0.05508I$ $b = 0.984611 - 0.552289I$	$-1.22934 - 2.47209I$	$1.10273 + 1.06165I$

### III. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{14} - 5u^{13} + \dots - u^2 + 1)(u^{26} - 24u^{24} + \dots - 352u + 41)$
$c_2$	$(u^{14} - 3u^{13} + 8u^{11} - 9u^{10} + 13u^8 - 16u^7 + 14u^5 - 9u^4 - 3u^3 + 4u^2 - 1)$ $\cdot (u^{26} - 4u^{25} + \dots - 322u - 529)$
$c_3$	$(u^{14} + 4u^{12} + 5u^{10} + 2u^9 - 3u^8 + 4u^7 - u^6 - u^5 + u^4 + 2u^3 + u^2 - u - 1)$ $\cdot (u^{26} - u^{25} + \dots - 12769u - 1781)$
$c_4, c_5$	$(u^{14} - 7u^{12} + \dots - 2u + 1)(u^{26} + u^{25} + \dots - 12u + 31)$
$c_6$	$(u^{14} + 3u^{13} - 8u^{11} - 9u^{10} + 13u^8 + 16u^7 - 14u^5 - 9u^4 + 3u^3 + 4u^2 - 1)$ $\cdot (u^{26} - 4u^{25} + \dots - 322u - 529)$
$c_7, c_8$	$(u^{14} + 9u^{12} + \dots + 2u - 1)(u^{26} + u^{25} + \dots - 34u - 4)$
$c_9$	$(u^{14} + u^{13} - u^{12} - 2u^{11} - u^{10} + u^9 + u^8 - 4u^7 + 3u^6 - 2u^5 - 5u^4 - 4u^2 - 1)$ $\cdot (u^{26} + 2u^{25} + \dots + 36u - 19)$
$c_{10}$	$(u^{14} - 7u^{12} + \dots + 2u + 1)(u^{26} + u^{25} + \dots - 12u + 31)$
$c_{11}$	$(u^{14} + 9u^{12} + \dots - 2u - 1)(u^{26} + u^{25} + \dots - 34u - 4)$
$c_{12}$	$(u^{14} + 11u^{12} + \dots - 2u - 1)(u^{26} - u^{25} + \dots - 304218u - 40564)$

#### IV. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{14} - 17y^{13} + \dots - 2y + 1)(y^{26} - 48y^{25} + \dots + 19924y + 1681)$
$c_2, c_6$	$(y^{14} - 9y^{13} + \dots - 8y + 1)(y^{26} + 12y^{25} + \dots - 348082y + 279841)$
$c_3$	$(y^{14} + 8y^{13} + \dots - 3y + 1)$ $\cdot (y^{26} + 69y^{25} + \dots - 266466469y + 3171961)$
$c_4, c_5, c_{10}$	$(y^{14} - 14y^{13} + \dots - 16y + 1)(y^{26} - 33y^{25} + \dots - 12482y + 961)$
$c_7, c_8, c_{11}$	$(y^{14} + 18y^{13} + \dots - 6y + 1)(y^{26} + 43y^{25} + \dots - 716y + 16)$
$c_9$	$(y^{14} - 3y^{13} + \dots + 8y + 1)(y^{26} + 6y^{25} + \dots + 1782y + 361)$
$c_{12}$	$(y^{14} + 22y^{13} + \dots - 4y + 1)$ $\cdot (y^{26} + 147y^{25} + \dots - 80260701260y + 1645438096)$