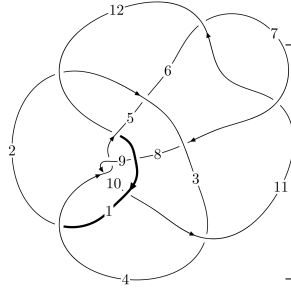
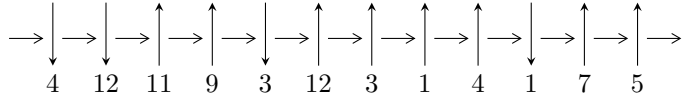


12n₀₇₉₈ (K12n₀₇₉₈)



A knot diagram¹

Linearized knot diagram



Solving Sequence

$$1,4 \xrightarrow{c_1} 2,10 \xrightarrow{c_{10}} 11 \xrightarrow{c_3} 3 \xrightarrow{c_9} 9 \xrightarrow{c_4} 5 \xrightarrow{c_5} 6 \xrightarrow{c_8} 8 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 12 \Rightarrow c_2, c_6, c_{11}$$

Ideals for irreducible components² of X_{par}

$$I_1^u = \langle 1283u^{12} - 662u^{11} + \dots + 5739b + 1160, -630u^{12} + 3164u^{11} + \dots + 1913a - 753, \\ u^{13} - 3u^{12} + 8u^{11} - 20u^{10} + 36u^9 - 61u^8 + 84u^7 - 97u^6 + 97u^5 - 68u^4 + 41u^3 - 13u^2 + 3u + 1 \rangle$$

$$I_2^u = \langle -1.18123 \times 10^{153}u^{55} - 4.51937 \times 10^{153}u^{54} + \dots + 2.08930 \times 10^{155}b - 7.05789 \times 10^{155}, \\ 8.87232 \times 10^{153}u^{55} + 3.38341 \times 10^{154}u^{54} + \dots + 6.26789 \times 10^{155}a + 3.97690 \times 10^{156}, \\ u^{56} + 4u^{55} + \dots + 1346u + 111 \rangle$$

$$I_3^u = \langle -135214u^{15} + 515373u^{14} + \dots + 267063b + 30946, \\ -570167u^{15} + 1972254u^{14} + \dots + 1335315a - 4248919, u^{16} - 4u^{15} + \dots - u + 1 \rangle$$

$$I_4^u = \langle -u^3 + u^2 + b - u, u^2 + a - u + 2, u^4 - u^3 + 2u^2 + 1 \rangle$$

$$I_5^u = \langle -u^2 + b + u, a + u, u^4 - u^3 + u^2 - u + 1 \rangle$$

* 5 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 93 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 1283u^{12} - 662u^{11} + \dots + 5739b + 1160, -630u^{12} + 3164u^{11} + \dots + 1913a - 753, u^{13} - 3u^{12} + \dots + 3u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0.329326u^{12} - 1.65395u^{11} + \dots - 12.3325u + 0.393623 \\ -0.223558u^{12} + 0.115351u^{11} + \dots - 2.77749u - 0.202126 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.552884u^{12} - 1.76930u^{11} + \dots - 9.55497u + 0.595748 \\ -0.223558u^{12} + 0.115351u^{11} + \dots - 2.77749u - 0.202126 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -0.744555u^{12} + 1.43562u^{11} + \dots - 4.66423u + 0.635477 \\ -0.238021u^{12} + 0.958355u^{11} + \dots + 3.13870u + 0.798048 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0.329326u^{12} - 1.65395u^{11} + \dots - 12.3325u + 0.393623 \\ -0.499042u^{12} + 1.07667u^{11} + \dots - 1.10890u + 0.463844 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1.02248u^{12} - 2.20178u^{11} + \dots + 4.08207u - 1.12075 \\ -0.110646u^{12} + 0.148284u^{11} + \dots - 1.06290u - 0.552884 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0.905558u^{12} - 2.55532u^{11} + \dots - 1.63164u - 1.70971 \\ -0.659697u^{12} + 2.22426u^{11} + \dots + 3.05646u + 0.706743 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 0.828367u^{12} - 2.73062u^{11} + \dots - 11.2236u - 0.0702213 \\ -0.499042u^{12} + 1.07667u^{11} + \dots - 1.10890u + 0.463844 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1.44642u^{12} - 3.28646u^{11} + \dots - 1.18400u + 1.06691 \\ 0.158564u^{12} - 1.31486u^{11} + \dots - 7.38230u - 1.25492 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.364523u^{12} + 1.83813u^{11} + \dots + 7.51403u + 3.57066 \\ 0.798048u^{12} - 2.15612u^{11} + \dots - 2.86914u - 0.744555 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{27061}{5739}u^{12} - \frac{84808}{5739}u^{11} + \dots - \frac{197266}{5739}u + \frac{6865}{5739}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|---------------------------------------|
| c_1, c_2 | $u^{13} + 3u^{12} + \dots + 3u - 1$ |
| c_3, c_{12} | $u^{13} + u^{12} + \dots - 3u - 1$ |
| c_4, c_6, c_9 c_{11} | $u^{13} - 2u^{12} + \dots + 7u^3 - 1$ |
| c_5, c_{10} | $u^{13} - u^{12} + \dots + 3u - 3$ |
| c_7, c_8 | $u^{13} + 3u^{12} + \dots - 8u - 3$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|---------------------------------------|
| c_1, c_2 | $y^{13} + 7y^{12} + \dots + 35y - 1$ |
| c_3, c_{12} | $y^{13} + 7y^{12} + \dots + 3y - 1$ |
| c_4, c_6, c_9 c_{11} | $y^{13} + 4y^{11} + \dots - 2y^2 - 1$ |
| c_5, c_{10} | $y^{13} + 15y^{12} + \dots + 39y - 9$ |
| c_7, c_8 | $y^{13} - 3y^{12} + \dots + 34y - 9$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.125889 + 0.791075I$ $a = -0.42819 + 1.60424I$ $b = 0.06421 + 1.99251I$ | $3.78832 - 0.68098I$ | $3.18600 + 10.56387I$ |
| $u = 0.125889 - 0.791075I$ $a = -0.42819 - 1.60424I$ $b = 0.06421 - 1.99251I$ | $3.78832 + 0.68098I$ | $3.18600 - 10.56387I$ |
| $u = 0.435895 + 1.153550I$ $a = -0.166988 - 0.397762I$ $b = -1.101790 - 0.664354I$ | $-1.60930 - 2.98509I$ | $6.45992 + 2.62910I$ |
| $u = 0.435895 - 1.153550I$ $a = -0.166988 + 0.397762I$ $b = -1.101790 + 0.664354I$ | $-1.60930 + 2.98509I$ | $6.45992 - 2.62910I$ |
| $u = 0.405751 + 0.538490I$ $a = -1.29934 - 1.45999I$ $b = 0.613689 - 0.351552I$ | $-8.20006 - 2.65719I$ | $-7.53293 + 6.11651I$ |
| $u = 0.405751 - 0.538490I$ $a = -1.29934 + 1.45999I$ $b = 0.613689 + 0.351552I$ | $-8.20006 + 2.65719I$ | $-7.53293 - 6.11651I$ |
| $u = -0.21582 + 1.42915I$ $a = 0.743610 + 0.701361I$ $b = 0.17608 + 1.54701I$ | $9.07015 + 0.94105I$ | $7.27747 - 1.09961I$ |
| $u = -0.21582 - 1.42915I$ $a = 0.743610 - 0.701361I$ $b = 0.17608 - 1.54701I$ | $9.07015 - 0.94105I$ | $7.27747 + 1.09961I$ |
| $u = 1.52678 + 0.05294I$ $a = 0.101352 + 0.424061I$ $b = -0.310928 + 0.347924I$ | $-3.37050 + 0.66803I$ | $1.81891 - 10.95758I$ |
| $u = 1.52678 - 0.05294I$ $a = 0.101352 - 0.424061I$ $b = -0.310928 - 0.347924I$ | $-3.37050 - 0.66803I$ | $1.81891 + 10.95758I$ |

| Solutions to I_1^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -0.70010 + 1.56807I$ $a = 0.383909 - 0.789778I$ $b = 0.82111 - 1.72051I$ | $7.2980 + 16.4758I$ | $4.42093 - 8.40539I$ |
| $u = -0.70010 - 1.56807I$ $a = 0.383909 + 0.789778I$ $b = 0.82111 + 1.72051I$ | $7.2980 - 16.4758I$ | $4.42093 + 8.40539I$ |
| $u = -0.156796$ $a = 3.33128$ $b = 0.475252$ | 0.851273 | 11.7390 |

$$\text{II. } I_2^u = \langle -1.18 \times 10^{153} u^{55} - 4.52 \times 10^{153} u^{54} + \dots + 2.09 \times 10^{155} b - 7.06 \times 10^{155}, 8.87 \times 10^{153} u^{55} + 3.38 \times 10^{154} u^{54} + \dots + 6.27 \times 10^{155} a + 3.98 \times 10^{156}, u^{56} + 4u^{55} + \dots + 1346u + 111 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.0141552u^{55} - 0.0539800u^{54} + \dots - 28.3025u - 6.34487 \\ 0.00565370u^{55} + 0.0216310u^{54} + \dots + 16.5561u + 3.37812 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.0198089u^{55} - 0.0756110u^{54} + \dots - 44.8585u - 9.72299 \\ 0.00565370u^{55} + 0.0216310u^{54} + \dots + 16.5561u + 3.37812 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 0.0144678u^{55} + 0.0586721u^{54} + \dots + 73.1975u + 12.4499 \\ -0.00267933u^{55} - 0.00908580u^{54} + \dots - 12.7090u - 3.57215 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0141552u^{55} - 0.0539800u^{54} + \dots - 28.3025u - 6.34487 \\ 0.00718179u^{55} + 0.0273575u^{54} + \dots + 14.5728u + 3.08499 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.00877254u^{55} - 0.0387439u^{54} + \dots - 48.2032u - 6.38465 \\ 0.00314979u^{55} + 0.0134163u^{54} + \dots + 18.1770u + 2.89867 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0116448u^{55} - 0.0480523u^{54} + \dots - 48.8452u + 1.49968 \\ 0.00331140u^{55} + 0.0134797u^{54} + \dots + 33.1904u + 2.23101 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -0.0213370u^{55} - 0.0813374u^{54} + \dots - 42.8753u - 9.42987 \\ 0.00718179u^{55} + 0.0273575u^{54} + \dots + 14.5728u + 3.08499 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 0.0106076u^{55} + 0.0439229u^{54} + \dots + 51.7711u + 2.93855 \\ -0.00286600u^{55} - 0.0111012u^{54} + \dots - 25.2269u - 2.36948 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -0.00420227u^{55} - 0.0147886u^{54} + \dots - 32.7418u - 2.34305 \\ 0.00309502u^{55} + 0.0110761u^{54} + \dots + 17.1401u + 2.03269 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $-0.000431876u^{55} - 0.00131056u^{54} + \dots - 42.1688u + 5.52954$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|---|
| c_1, c_2 | $u^{56} - 4u^{55} + \dots - 1346u + 111$ |
| c_3, c_{12} | $u^{56} + 2u^{54} + \dots + 907u + 193$ |
| c_4, c_6, c_9 c_{11} | $u^{56} + u^{55} + \dots + 13u + 3$ |
| c_5, c_{10} | $u^{56} + 2u^{55} + \dots + 82u + 37$ |
| c_7, c_8 | $u^{56} - u^{55} + \dots + 29361u + 1951$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1, c_2 | $y^{56} + 50y^{55} + \dots - 249724y + 12321$ |
| c_3, c_{12} | $y^{56} + 4y^{55} + \dots - 242491y + 37249$ |
| c_4, c_6, c_9 c_{11} | $y^{56} + 15y^{55} + \dots + 275y + 9$ |
| c_5, c_{10} | $y^{56} + 52y^{55} + \dots - 39284y + 1369$ |
| c_7, c_8 | $y^{56} - 31y^{55} + \dots - 114413905y + 3806401$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|----------------------|
| $u = 0.973175 + 0.358698I$ $a = 0.223686 + 0.715699I$ $b = -0.141495 - 0.212809I$ | $-2.35105 - 1.37665I$ | $0. + 4.49216I$ |
| $u = 0.973175 - 0.358698I$ $a = 0.223686 - 0.715699I$ $b = -0.141495 + 0.212809I$ | $-2.35105 + 1.37665I$ | $0. - 4.49216I$ |
| $u = -0.847096 + 0.638226I$ $a = -0.404462 + 0.469747I$ $b = 0.15766 + 1.46714I$ | $1.93596 + 5.90600I$ | $0. - 3.51945I$ |
| $u = -0.847096 - 0.638226I$ $a = -0.404462 - 0.469747I$ $b = 0.15766 - 1.46714I$ | $1.93596 - 5.90600I$ | $0. + 3.51945I$ |
| $u = -0.561985 + 0.926870I$ $a = 0.331742 - 1.143620I$ $b = 0.25987 - 1.69030I$ | $-3.01211 + 5.08083I$ | $8.72700 + 0.I$ |
| $u = -0.561985 - 0.926870I$ $a = 0.331742 + 1.143620I$ $b = 0.25987 + 1.69030I$ | $-3.01211 - 5.08083I$ | $8.72700 + 0.I$ |
| $u = -0.401455 + 0.819963I$ $a = 0.524050 - 0.252083I$ $b = -0.232565 - 1.287120I$ | $3.14992 - 0.89303I$ | $3.36391 + 1.60851I$ |
| $u = -0.401455 - 0.819963I$ $a = 0.524050 + 0.252083I$ $b = -0.232565 + 1.287120I$ | $3.14992 + 0.89303I$ | $3.36391 - 1.60851I$ |
| $u = 0.428842 + 0.782748I$ $a = 1.39747 + 0.43456I$ $b = -0.093467 - 0.473397I$ | $-2.65912 - 0.69416I$ | $5.49287 + 3.59719I$ |
| $u = 0.428842 - 0.782748I$ $a = 1.39747 - 0.43456I$ $b = -0.093467 + 0.473397I$ | $-2.65912 + 0.69416I$ | $5.49287 - 3.59719I$ |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|------------------------|
| $u = -0.293234 + 1.071580I$ $a = -0.398636 + 1.032790I$ $b = 0.105708 + 1.267210I$ | $3.14992 + 0.89303I$ | $4.00000 + 0.I$ |
| $u = -0.293234 - 1.071580I$ $a = -0.398636 - 1.032790I$ $b = 0.105708 - 1.267210I$ | $3.14992 - 0.89303I$ | $4.00000 + 0.I$ |
| $u = -0.087731 + 1.118910I$ $a = -0.686073 + 0.991907I$ $b = 0.06046 + 1.60533I$ | $3.57949 + 0.97368I$ | $7.35348 - 5.23167I$ |
| $u = -0.087731 - 1.118910I$ $a = -0.686073 - 0.991907I$ $b = 0.06046 - 1.60533I$ | $3.57949 - 0.97368I$ | $7.35348 + 5.23167I$ |
| $u = 0.683985 + 0.326867I$ $a = 0.76677 + 1.25863I$ $b = -0.876249 - 0.500129I$ | $-4.38515 - 0.94897I$ | $-10.21959 + 1.75938I$ |
| $u = 0.683985 - 0.326867I$ $a = 0.76677 - 1.25863I$ $b = -0.876249 + 0.500129I$ | $-4.38515 + 0.94897I$ | $-10.21959 - 1.75938I$ |
| $u = -0.463157 + 1.179820I$ $a = -0.692781 - 0.317187I$ $b = -0.447756 - 0.568276I$ | $-2.65912 - 0.69416I$ | 0 |
| $u = -0.463157 - 1.179820I$ $a = -0.692781 + 0.317187I$ $b = -0.447756 + 0.568276I$ | $-2.65912 + 0.69416I$ | 0 |
| $u = -1.250640 + 0.306528I$ $a = 0.350610 + 0.608692I$ $b = -0.076204 + 0.243308I$ | $3.22350 + 2.16516I$ | 0 |
| $u = -1.250640 - 0.306528I$ $a = 0.350610 - 0.608692I$ $b = -0.076204 - 0.243308I$ | $3.22350 - 2.16516I$ | 0 |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|----------------------|
| $u = -0.150720 + 1.306260I$ $a = 0.728240 + 0.063856I$ $b = 1.105270 + 0.474638I$ | $-0.60047 - 5.02443I$ | 0 |
| $u = -0.150720 - 1.306260I$ $a = 0.728240 - 0.063856I$ $b = 1.105270 - 0.474638I$ | $-0.60047 + 5.02443I$ | 0 |
| $u = 0.118150 + 1.326950I$ $a = 0.824150 + 0.704249I$ $b = -0.25793 + 1.46755I$ | 7.25514 | 0 |
| $u = 0.118150 - 1.326950I$ $a = 0.824150 - 0.704249I$ $b = -0.25793 - 1.46755I$ | 7.25514 | 0 |
| $u = 0.855631 + 1.049130I$ $a = -0.036172 - 0.766616I$ $b = -0.62639 - 1.44617I$ | $-0.60047 - 5.02443I$ | 0 |
| $u = 0.855631 - 1.049130I$ $a = -0.036172 + 0.766616I$ $b = -0.62639 + 1.44617I$ | $-0.60047 + 5.02443I$ | 0 |
| $u = 0.110352 + 0.636373I$ $a = -2.55589 - 0.04098I$ $b = -0.423182 + 0.031837I$ | $-3.01211 + 5.08083I$ | $8.72700 - 0.16788I$ |
| $u = 0.110352 - 0.636373I$ $a = -2.55589 + 0.04098I$ $b = -0.423182 - 0.031837I$ | $-3.01211 - 5.08083I$ | $8.72700 + 0.16788I$ |
| $u = -0.002625 + 1.377270I$ $a = 0.508986 - 0.612116I$ $b = -0.09477 - 1.51750I$ | $3.22350 - 2.16516I$ | 0 |
| $u = -0.002625 - 1.377270I$ $a = 0.508986 + 0.612116I$ $b = -0.09477 + 1.51750I$ | $3.22350 + 2.16516I$ | 0 |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.150210 + 0.569344I$ $a = -0.824610 - 0.889775I$ $b = -1.046740 + 0.070502I$ | $-2.35105 - 1.37665I$ | $-0.14056 + 4.49216I$ |
| $u = 0.150210 - 0.569344I$ $a = -0.824610 + 0.889775I$ $b = -1.046740 - 0.070502I$ | $-2.35105 + 1.37665I$ | $-0.14056 - 4.49216I$ |
| $u = -0.23885 + 1.42021I$ $a = -0.724589 - 0.727418I$ $b = 0.07102 - 1.58823I$ | $8.32665 + 8.69653I$ | 0 |
| $u = -0.23885 - 1.42021I$ $a = -0.724589 + 0.727418I$ $b = 0.07102 + 1.58823I$ | $8.32665 - 8.69653I$ | 0 |
| $u = 0.46400 + 1.40989I$ $a = 0.467280 + 0.871972I$ $b = 0.93856 + 1.51643I$ | $2.96962 - 6.50699I$ | 0 |
| $u = 0.46400 - 1.40989I$ $a = 0.467280 - 0.871972I$ $b = 0.93856 - 1.51643I$ | $2.96962 + 6.50699I$ | 0 |
| $u = 0.12171 + 1.48953I$ $a = -0.732149 - 0.618254I$ $b = 0.02724 - 1.64380I$ | $8.61168 - 6.87817I$ | 0 |
| $u = 0.12171 - 1.48953I$ $a = -0.732149 + 0.618254I$ $b = 0.02724 + 1.64380I$ | $8.61168 + 6.87817I$ | 0 |
| $u = 0.46868 + 1.43810I$ $a = 0.529642 + 0.769097I$ $b = 0.656517 + 1.172790I$ | $1.93596 - 5.90600I$ | 0 |
| $u = 0.46868 - 1.43810I$ $a = 0.529642 - 0.769097I$ $b = 0.656517 - 1.172790I$ | $1.93596 + 5.90600I$ | 0 |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|----------------------|
| $u = -0.61255 + 1.47138I$ $a = -0.411818 + 0.844957I$ $b = -0.66961 + 1.79906I$ | $8.32665 + 8.69653I$ | 0 |
| $u = -0.61255 - 1.47138I$ $a = -0.411818 - 0.844957I$ $b = -0.66961 - 1.79906I$ | $8.32665 - 8.69653I$ | 0 |
| $u = 0.57163 + 1.63667I$ $a = -0.425730 - 0.627977I$ $b = -0.67894 - 1.58354I$ | $2.19558 - 8.29138I$ | 0 |
| $u = 0.57163 - 1.63667I$ $a = -0.425730 + 0.627977I$ $b = -0.67894 + 1.58354I$ | $2.19558 + 8.29138I$ | 0 |
| $u = -0.021719 + 0.263335I$ $a = 0.31401 + 2.13706I$ $b = -1.29778 - 0.84140I$ | $3.57949 - 0.97368I$ | $7.35348 + 5.23167I$ |
| $u = -0.021719 - 0.263335I$ $a = 0.31401 - 2.13706I$ $b = -1.29778 + 0.84140I$ | $3.57949 + 0.97368I$ | $7.35348 - 5.23167I$ |
| $u = -0.37410 + 1.70455I$ $a = 0.285913 - 0.668539I$ $b = 0.58599 - 1.56113I$ | 9.99346 | 0 |
| $u = -0.37410 - 1.70455I$ $a = 0.285913 + 0.668539I$ $b = 0.58599 + 1.56113I$ | 9.99346 | 0 |
| $u = -1.78299 + 0.07540I$ $a = -0.258059 - 0.376840I$ $b = 0.170261 + 0.007329I$ | $2.19558 + 8.29138I$ | 0 |
| $u = -1.78299 - 0.07540I$ $a = -0.258059 + 0.376840I$ $b = 0.170261 - 0.007329I$ | $2.19558 - 8.29138I$ | 0 |

| Solutions to I_2^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|---------------------|
| $u = -0.47184 + 1.75013I$ $a = -0.252592 + 0.650075I$ $b = -0.71080 + 1.36535I$ | $8.61168 + 6.87817I$ | 0 |
| $u = -0.47184 - 1.75013I$ $a = -0.252592 - 0.650075I$ $b = -0.71080 - 1.36535I$ | $8.61168 - 6.87817I$ | 0 |
| $u = 0.76269 + 1.66617I$ $a = 0.168983 + 0.041887I$ $b = 0.580641 + 0.363782I$ | $-4.38515 - 0.94897I$ | 0 |
| $u = 0.76269 - 1.66617I$ $a = 0.168983 - 0.041887I$ $b = 0.580641 - 0.363782I$ | $-4.38515 + 0.94897I$ | 0 |
| $u = -0.148356 + 0.045126I$ $a = -3.00896 - 2.49575I$ $b = 1.95470 + 0.87168I$ | $2.96962 + 6.50699I$ | $13.7787 - 5.9700I$ |
| $u = -0.148356 - 0.045126I$ $a = -3.00896 + 2.49575I$ $b = 1.95470 - 0.87168I$ | $2.96962 - 6.50699I$ | $13.7787 + 5.9700I$ |

III.

$$I_3^u = \langle -1.35 \times 10^5 u^{15} + 5.15 \times 10^5 u^{14} + \dots + 2.67 \times 10^5 b + 3.09 \times 10^4, -5.70 \times 10^5 u^{15} + 1.97 \times 10^6 u^{14} + \dots + 1.34 \times 10^6 a - 4.25 \times 10^6, u^{16} - 4u^{15} + \dots - u + 1 \rangle$$

(i) Arc colorings

$$\begin{aligned} a_1 &= \begin{pmatrix} 1 \\ 0 \end{pmatrix} \\ a_4 &= \begin{pmatrix} 0 \\ u \end{pmatrix} \\ a_2 &= \begin{pmatrix} 1 \\ u^2 \end{pmatrix} \\ a_{10} &= \begin{pmatrix} 0.426991u^{15} - 1.47700u^{14} + \dots - 1.64833u + 3.18196 \\ 0.506300u^{15} - 1.92978u^{14} + \dots + 0.204210u - 0.115875 \end{pmatrix} \\ a_{11} &= \begin{pmatrix} -0.0793094u^{15} + 0.452785u^{14} + \dots - 1.85254u + 3.29784 \\ 0.506300u^{15} - 1.92978u^{14} + \dots + 0.204210u - 0.115875 \end{pmatrix} \\ a_3 &= \begin{pmatrix} -1.66162u^{15} + 5.75525u^{14} + \dots - 9.16104u - 0.00841824 \\ -0.194335u^{15} + 1.26058u^{14} + \dots - 0.801647u + 0.663182 \end{pmatrix} \\ a_9 &= \begin{pmatrix} 0.426991u^{15} - 1.47700u^{14} + \dots - 1.64833u + 3.18196 \\ 0.510721u^{15} - 1.77893u^{14} + \dots + 0.00818683u - 0.346843 \end{pmatrix} \\ a_5 &= \begin{pmatrix} 1.53255u^{15} - 6.54843u^{14} + \dots + 13.1760u - 1.49836 \\ 0.0802492u^{15} - 0.689561u^{14} + \dots + 1.26250u - 0.425375 \end{pmatrix} \\ a_6 &= \begin{pmatrix} -1.07106u^{15} + 2.28793u^{14} + \dots + 12.6165u - 5.85293 \\ -0.0709555u^{15} + 0.340250u^{14} + \dots + 2.32523u - 1.20232 \end{pmatrix} \\ a_8 &= \begin{pmatrix} -0.0837301u^{15} + 0.301938u^{14} + \dots - 1.65651u + 3.52880 \\ 0.510721u^{15} - 1.77893u^{14} + \dots + 0.00818683u - 0.346843 \end{pmatrix} \\ a_7 &= \begin{pmatrix} 0.636679u^{15} - 3.36717u^{14} + \dots + 10.0876u - 2.20527 \\ 0.0721897u^{15} - 0.414518u^{14} + \dots + 1.95733u - 0.879098 \end{pmatrix} \\ a_{12} &= \begin{pmatrix} -0.445408u^{15} + 0.788567u^{14} + \dots + 7.00998u - 1.98390 \\ 0.287778u^{15} - 1.19976u^{14} + \dots + 1.25399u - 0.670117 \end{pmatrix} \end{aligned}$$

(ii) Obstruction class = 1

$$\text{(iii) Cusp Shapes} = -\frac{1668929}{445105}u^{15} + \frac{8331783}{445105}u^{14} + \dots - \frac{10787371}{445105}u + \frac{3576652}{445105}$$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|-------------------------------------|
| c_1 | $u^{16} - 4u^{15} + \dots - u + 1$ |
| c_2 | $u^{16} + 4u^{15} + \dots + u + 1$ |
| c_3 | $u^{16} + 2u^{15} + \dots + 2u + 1$ |
| c_4, c_6 | $u^{16} + u^{15} + \dots - 4u + 1$ |
| c_5 | $u^{16} - u^{15} + \dots + 9u + 9$ |
| c_7 | $u^{16} + u^{15} + \dots - u + 1$ |
| c_8 | $u^{16} - u^{15} + \dots + u + 1$ |
| c_9, c_{11} | $u^{16} - u^{15} + \dots + 4u + 1$ |
| c_{10} | $u^{16} + u^{15} + \dots - 9u + 9$ |
| c_{12} | $u^{16} - 2u^{15} + \dots - 2u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|---|
| c_1, c_2 | $y^{16} + 10y^{15} + \dots + 11y + 1$ |
| c_3, c_{12} | $y^{16} + 12y^{15} + \dots + 4y + 1$ |
| c_4, c_6, c_9 c_{11} | $y^{16} + 7y^{15} + \dots + 2y + 1$ |
| c_5, c_{10} | $y^{16} + 13y^{15} + \dots - 927y + 81$ |
| c_7, c_8 | $y^{16} - y^{15} + \dots + 27y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|-----------------------|
| $u = 0.626932 + 0.939202I$ $a = 0.245461 + 1.107320I$ $b = 0.45758 + 1.67741I$ | $-3.44371 - 5.36963I$ | $-4.65919 + 8.71627I$ |
| $u = 0.626932 - 0.939202I$ $a = 0.245461 - 1.107320I$ $b = 0.45758 - 1.67741I$ | $-3.44371 + 5.36963I$ | $-4.65919 - 8.71627I$ |
| $u = 0.561928 + 0.646656I$ $a = 1.122090 + 0.719975I$ $b = -0.824183 - 0.541509I$ | $-3.98555 - 1.28538I$ | $1.78219 + 9.46171I$ |
| $u = 0.561928 - 0.646656I$ $a = 1.122090 - 0.719975I$ $b = -0.824183 + 0.541509I$ | $-3.98555 + 1.28538I$ | $1.78219 - 9.46171I$ |
| $u = -0.044845 + 0.844688I$ $a = 0.201470 - 1.383010I$ $b = -0.35203 - 1.95828I$ | 4.11885 | $12.68263 + 0.I$ |
| $u = -0.044845 - 0.844688I$ $a = 0.201470 + 1.383010I$ $b = -0.35203 + 1.95828I$ | 4.11885 | $12.68263 + 0.I$ |
| $u = -0.770410 + 0.331199I$ $a = 0.236785 + 0.596788I$ $b = 1.06833 + 1.33459I$ | $2.42763 + 6.73512I$ | $1.81921 - 10.54756I$ |
| $u = -0.770410 - 0.331199I$ $a = 0.236785 - 0.596788I$ $b = 1.06833 - 1.33459I$ | $2.42763 - 6.73512I$ | $1.81921 + 10.54756I$ |
| $u = 1.134980 + 0.398912I$ $a = -0.326610 - 0.608866I$ $b = -0.471617 + 0.101971I$ | -3.98521 | $-7.56704 + 0.I$ |
| $u = 1.134980 - 0.398912I$ $a = -0.326610 + 0.608866I$ $b = -0.471617 - 0.101971I$ | -3.98521 | $-7.56704 + 0.I$ |

| Solutions to I_3^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|---|---------------------------------------|-----------------------|
| $u = 0.44558 + 1.49412I$ $a = -0.522013 - 0.746739I$ $b = -0.87827 - 1.36350I$ | $2.42763 - 6.73512I$ | $1.81921 + 10.54756I$ |
| $u = 0.44558 - 1.49412I$ $a = -0.522013 + 0.746739I$ $b = -0.87827 + 1.36350I$ | $2.42763 + 6.73512I$ | $1.81921 - 10.54756I$ |
| $u = -0.117840 + 0.420370I$ $a = 3.38072 - 1.31571I$ $b = 0.798526 - 0.197831I$ | $-3.44371 + 5.36963I$ | $-4.65919 - 8.71627I$ |
| $u = -0.117840 - 0.420370I$ $a = 3.38072 + 1.31571I$ $b = 0.798526 + 0.197831I$ | $-3.44371 - 5.36963I$ | $-4.65919 + 8.71627I$ |
| $u = 0.16367 + 1.77202I$ $a = 0.162097 + 0.279051I$ $b = 0.701667 + 0.382156I$ | $-3.98555 - 1.28538I$ | $1.78219 + 9.46171I$ |
| $u = 0.16367 - 1.77202I$ $a = 0.162097 - 0.279051I$ $b = 0.701667 - 0.382156I$ | $-3.98555 + 1.28538I$ | $1.78219 - 9.46171I$ |

$$\text{IV. } I_4^u = \langle -u^3 + u^2 + b - u, u^2 + a - u + 2, u^4 - u^3 + 2u^2 + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^2 + u - 2 \\ u^3 - u^2 + u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3 - 2 \\ u^3 - u^2 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -2u^3 + 3u^2 - 5u + 1 \\ 2u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u^2 + u - 2 \\ u^3 - u^2 + u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 2u^3 - 2u^2 + 3u + 1 \\ -u^3 + 2u^2 - 2u + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 2u^3 + u + 4 \\ -2u^3 + u^2 - 3u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^3 - 3 \\ u^3 - u^2 + u + 1 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -3u^3 + 5u^2 - 7u + 1 \\ -2u^2 + 2u - 2 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 2u^2 - 3u + 5 \\ -u^3 + u^2 - u - 2 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $4u^3 + 3u^2 + 4u + 7$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|---------------|--------------------------------|
| c_1 | $u^4 - u^3 + 2u^2 + 1$ |
| c_2 | $u^4 + u^3 + 2u^2 + 1$ |
| c_3 | $u^4 + u^3 + 4u^2 + 2u + 3$ |
| c_4, c_6 | $u^4 + 2u^2 + u + 1$ |
| c_5 | $u^4 + u^3 + 1$ |
| c_7 | $u^4 - 3u^3 + 3u^2 - u + 1$ |
| c_8 | $u^4 + 3u^3 + 3u^2 + u + 1$ |
| c_9, c_{11} | $u^4 + 2u^2 - u + 1$ |
| c_{10} | $u^4 - u^3 + 1$ |
| c_{12} | $u^4 - u^3 + 4u^2 - 2u + 3$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|------------------------------------|
| c_1, c_2 | $y^4 + 3y^3 + 6y^2 + 4y + 1$ |
| c_3, c_{12} | $y^4 + 7y^3 + 18y^2 + 20y + 9$ |
| c_4, c_6, c_9 c_{11} | $y^4 + 4y^3 + 6y^2 + 3y + 1$ |
| c_5, c_{10} | $y^4 - y^3 + 2y^2 + 1$ |
| c_7, c_8 | $y^4 - 3y^3 + 5y^2 + 5y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_4^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|-----------------------------|---------------------------------------|-----------------------|
| $u = -0.175098 + 0.691825I$ | | |
| $a = -1.72714 + 0.93410I$ | $-7.71788 + 2.37936I$ | $5.93992 + 0.97052I$ |
| $b = 0.518913 + 0.666610I$ | | |
| $u = -0.175098 - 0.691825I$ | | |
| $a = -1.72714 - 0.93410I$ | $-7.71788 - 2.37936I$ | $5.93992 - 0.97052I$ |
| $b = 0.518913 - 0.666610I$ | | |
| $u = 0.675098 + 1.227920I$ | | |
| $a = -0.272864 - 0.430014I$ | $-2.15173 - 3.38562I$ | $-4.43992 + 9.19530I$ |
| $b = -1.018910 - 0.602565I$ | | |
| $u = 0.675098 - 1.227920I$ | | |
| $a = -0.272864 + 0.430014I$ | $-2.15173 + 3.38562I$ | $-4.43992 - 9.19530I$ |
| $b = -1.018910 + 0.602565I$ | | |

$$V. I_5^u = \langle -u^2 + b + u, a + u, u^4 - u^3 + u^2 - u + 1 \rangle$$

(i) Arc colorings

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u \\ u^2 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^2 \\ u^2 - u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^3 + u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ -u^3 + u^2 - u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^3 \\ u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^3 - u^2 + u - 1 \\ 2u^2 - 2u + 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 - u^2 \\ -u^3 + u^2 - u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^3 - u^2 + u - 1 \\ u^2 - 2u + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0 \\ u^3 - u^2 + u - 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = $6u^3 - 6u^2 - 1$

(iv) u-Polynomials at the component

| Crossings | u-Polynomials at each crossing |
|-----------------------------|--------------------------------|
| c_1, c_3, c_9 c_{11} | $u^4 - u^3 + u^2 - u + 1$ |
| c_2, c_4, c_6 c_{12} | $u^4 + u^3 + u^2 + u + 1$ |
| c_5 | $u^4 + 2u^3 + 4u^2 + 3u + 1$ |
| c_7 | $u^4 + 3u^3 + 4u^2 + 2u + 1$ |
| c_8 | $u^4 - 3u^3 + 4u^2 - 2u + 1$ |
| c_{10} | $u^4 - 2u^3 + 4u^2 - 3u + 1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
|--|------------------------------------|
| c_1, c_2, c_3 c_4, c_6, c_9 c_{11}, c_{12} | $y^4 + y^3 + y^2 + y + 1$ |
| c_5, c_{10} | $y^4 + 4y^3 + 6y^2 - y + 1$ |
| c_7, c_8 | $y^4 - y^3 + 6y^2 + 4y + 1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to I_5^u | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|--|---------------------------------------|------------------|
| $u = -0.309017 + 0.951057I$ $a = 0.309017 - 0.951057I$ $b = -0.50000 - 1.53884I$ | 3.94784 | $8.70820 + 0.I$ |
| $u = -0.309017 - 0.951057I$ $a = 0.309017 + 0.951057I$ $b = -0.50000 + 1.53884I$ | 3.94784 | $8.70820 + 0.I$ |
| $u = 0.809017 + 0.587785I$ $a = -0.809017 - 0.587785I$ $b = -0.500000 + 0.363271I$ | -3.94784 | $-4.70820 + 0.I$ |
| $u = 0.809017 - 0.587785I$ $a = -0.809017 + 0.587785I$ $b = -0.500000 - 0.363271I$ | -3.94784 | $-4.70820 + 0.I$ |

VI. u-Polynomials

| Crossings | u-Polynomials at each crossing |
|---------------|--|
| c_1 | $(u^4 - u^3 + u^2 - u + 1)(u^4 - u^3 + 2u^2 + 1)(u^{13} + 3u^{12} + \dots + 3u - 1)$ $\cdot (u^{16} - 4u^{15} + \dots - u + 1)(u^{56} - 4u^{55} + \dots - 1346u + 111)$ |
| c_2 | $(u^4 + u^3 + u^2 + u + 1)(u^4 + u^3 + 2u^2 + 1)(u^{13} + 3u^{12} + \dots + 3u - 1)$ $\cdot (u^{16} + 4u^{15} + \dots + u + 1)(u^{56} - 4u^{55} + \dots - 1346u + 111)$ |
| c_3 | $(u^4 - u^3 + u^2 - u + 1)(u^4 + u^3 + 4u^2 + 2u + 3)(u^{13} + u^{12} + \dots - 3u - 1)$ $\cdot (u^{16} + 2u^{15} + \dots + 2u + 1)(u^{56} + 2u^{54} + \dots + 907u + 193)$ |
| c_4, c_6 | $(u^4 + 2u^2 + u + 1)(u^4 + u^3 + u^2 + u + 1)(u^{13} - 2u^{12} + \dots + 7u^3 - 1)$ $\cdot (u^{16} + u^{15} + \dots - 4u + 1)(u^{56} + u^{55} + \dots + 13u + 3)$ |
| c_5 | $(u^4 + u^3 + 1)(u^4 + 2u^3 + \dots + 3u + 1)(u^{13} - u^{12} + \dots + 3u - 3)$ $\cdot (u^{16} - u^{15} + \dots + 9u + 9)(u^{56} + 2u^{55} + \dots + 82u + 37)$ |
| c_7 | $(u^4 - 3u^3 + 3u^2 - u + 1)(u^4 + 3u^3 + 4u^2 + 2u + 1)$ $\cdot (u^{13} + 3u^{12} + \dots - 8u - 3)(u^{16} + u^{15} + \dots - u + 1)$ $\cdot (u^{56} - u^{55} + \dots + 29361u + 1951)$ |
| c_8 | $(u^4 - 3u^3 + 4u^2 - 2u + 1)(u^4 + 3u^3 + 3u^2 + u + 1)$ $\cdot (u^{13} + 3u^{12} + \dots - 8u - 3)(u^{16} - u^{15} + \dots + u + 1)$ $\cdot (u^{56} - u^{55} + \dots + 29361u + 1951)$ |
| c_9, c_{11} | $(u^4 + 2u^2 - u + 1)(u^4 - u^3 + u^2 - u + 1)(u^{13} - 2u^{12} + \dots + 7u^3 - 1)$ $\cdot (u^{16} - u^{15} + \dots + 4u + 1)(u^{56} + u^{55} + \dots + 13u + 3)$ |
| c_{10} | $(u^4 - 2u^3 + \dots - 3u + 1)(u^4 - u^3 + 1)(u^{13} - u^{12} + \dots + 3u - 3)$ $\cdot (u^{16} + u^{15} + \dots - 9u + 9)(u^{56} + 2u^{55} + \dots + 82u + 37)$ |
| c_{12} | $(u^4 - u^3 + 4u^2 - 2u + 3)(u^4 + u^3 + u^2 + u + 1)(u^{13} + u^{12} + \dots - 3u - 1)$ $\cdot (u^{16} - 2u^{15} + \dots - 2u + 1)(u^{56} + 2u^{54} + \dots + 907u + 193)$ |

VII. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
|-----------------------------|--|
| c_1, c_2 | $(y^4 + y^3 + y^2 + y + 1)(y^4 + 3y^3 + 6y^2 + 4y + 1)$ $\cdot (y^{13} + 7y^{12} + \dots + 35y - 1)(y^{16} + 10y^{15} + \dots + 11y + 1)$ $\cdot (y^{56} + 50y^{55} + \dots - 249724y + 12321)$ |
| c_3, c_{12} | $(y^4 + y^3 + y^2 + y + 1)(y^4 + 7y^3 + 18y^2 + 20y + 9)$ $\cdot (y^{13} + 7y^{12} + \dots + 3y - 1)(y^{16} + 12y^{15} + \dots + 4y + 1)$ $\cdot (y^{56} + 4y^{55} + \dots - 242491y + 37249)$ |
| c_4, c_6, c_9 c_{11} | $(y^4 + y^3 + y^2 + y + 1)(y^4 + 4y^3 + \dots + 3y + 1)(y^{13} + 4y^{11} + \dots - 2y^2 - 1)$ $\cdot (y^{16} + 7y^{15} + \dots + 2y + 1)(y^{56} + 15y^{55} + \dots + 275y + 9)$ |
| c_5, c_{10} | $(y^4 - y^3 + 2y^2 + 1)(y^4 + 4y^3 + 6y^2 - y + 1)(y^{13} + 15y^{12} + \dots + 39y - 9)$ $\cdot (y^{16} + 13y^{15} + \dots - 927y + 81)(y^{56} + 52y^{55} + \dots - 39284y + 1369)$ |
| c_7, c_8 | $(y^4 - 3y^3 + 5y^2 + 5y + 1)(y^4 - y^3 + 6y^2 + 4y + 1)$ $\cdot (y^{13} - 3y^{12} + \dots + 34y - 9)(y^{16} - y^{15} + \dots + 27y + 1)$ $\cdot (y^{56} - 31y^{55} + \dots - 114413905y + 3806401)$ |