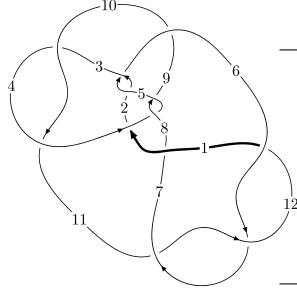
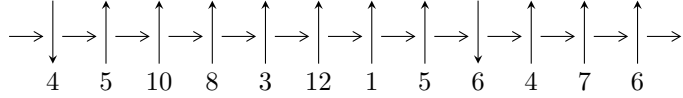


12n<sub>0823</sub> (K12n<sub>0823</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$2,5 \xrightarrow{c_2} 3 \xrightarrow{c_5} 6,8 \xrightarrow{c_8} 9 \xrightarrow{c_9} 10 \xrightarrow{c_4} 4 \xrightarrow{c_1} 1 \xrightarrow{c_7} 7 \xrightarrow{c_{12}} 12 \xrightarrow{c_{11}} 11 \twoheadrightarrow c_3, c_6, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle 257u^{24} - 3084u^{23} + \dots + 64b + 37824, -77u^{24} + 410u^{23} + \dots + 128a + 14912, \\ u^{25} - 12u^{24} + \dots + 640u - 128 \rangle$$

$$I_2^u = \langle -10a^5u^2 + 16a^4u^2 + \dots - 109a + 76, \\ a^6 - a^4u^2 - 2a^4u - 2a^3u^2 - 2a^4 - 3a^3u + a^2u^2 - a^3 + a^2u + 4u^2a - a^2 + 7au - 3u^2 + 4a - 4u - 2, \\ u^3 + u^2 - 1 \rangle$$

$$I_3^u = \langle 2u^{13} + 7u^{12} + u^{11} - 26u^{10} - 32u^9 + 24u^8 + 74u^7 + 23u^6 - 63u^5 - 51u^4 + 16u^3 + 26u^2 + b - 5, \\ 5u^{14} + 17u^{13} + \dots + a - 5, \\ u^{15} + 3u^{14} - u^{13} - 13u^{12} - 11u^{11} + 18u^{10} + 34u^9 - u^8 - 39u^7 - 19u^6 + 19u^5 + 17u^4 - 4u^3 - 6u^2 + 1 \rangle$$

$$I_4^u = \langle -44a^7u^2 - 73a^6u^2 + \dots - 213a + 245, -2a^6u^2 - a^5u^2 + \dots + 7a + 13, u^3 + u^2 - 1 \rangle$$

\* 4 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 82 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle 257u^{24} - 3084u^{23} + \dots + 64b + 37824, -77u^{24} + 410u^{23} + \dots + 128a + 14912, u^{25} - 12u^{24} + \dots + 640u - 128 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} \frac{77}{128}u^{24} - \frac{205}{64}u^{23} + \dots + 432u - \frac{233}{2} \\ -\frac{257}{64}u^{24} + \frac{771}{16}u^{23} + \dots + \frac{4961}{2}u - 591 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} \frac{77}{128}u^{24} - \frac{205}{64}u^{23} + \dots + 432u - \frac{233}{2} \\ -\frac{853}{64}u^{24} + \frac{579}{4}u^{23} + \dots + \frac{9947}{2}u - 1105 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} \frac{77}{128}u^{24} - \frac{801}{64}u^{23} + \dots - 1547u + \frac{795}{2} \\ \frac{715}{64}u^{24} - \frac{1849}{16}u^{23} + \dots - \frac{5931}{2}u + 601 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -\frac{1}{16}u^{24} + \frac{5}{8}u^{23} + \dots + 4u + \frac{1}{2} \\ -\frac{1}{8}u^{23} + \frac{5}{4}u^{22} + \dots - \frac{63}{2}u + 8 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -\frac{15}{16}u^{24} + \frac{167}{16}u^{23} + \dots + \frac{1391}{4}u - 71 \\ -\frac{15}{16}u^{24} + \frac{77}{8}u^{23} + \dots + 128u - 16 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} \frac{65}{8}u^{24} - \frac{1579}{16}u^{23} + \dots - 5798u + 1396 \\ \frac{333}{16}u^{24} - \frac{3509}{16}u^{23} + \dots - 5955u + 1208 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} -\frac{41}{16}u^{24} + \frac{455}{16}u^{23} + \dots + \frac{3727}{4}u - 191 \\ -\frac{41}{16}u^{24} + \frac{199}{8}u^{23} + \dots - 40u + 56 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -\frac{421}{64}u^{24} + \frac{4673}{64}u^{23} + \dots + \frac{11579}{4}u - 663 \\ -\frac{423}{64}u^{24} + \frac{1921}{32}u^{23} + \dots + 110u + 70 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{553}{16}u^{24} - \frac{3059}{8}u^{23} + \dots - 15300u + 3482$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{25} - 3u^{24} + \dots + 2u + 1$
$c_2, c_5$	$u^{25} + 12u^{24} + \dots + 640u + 128$
$c_3, c_4, c_8$ $c_{10}$	$u^{25} - u^{24} + \dots + 2u - 1$
$c_6, c_{11}, c_{12}$	$u^{25} + 6u^{24} + \dots + 40u + 8$
$c_7$	$u^{25} - 6u^{24} + \dots - 56u + 464$
$c_9$	$u^{25} + u^{24} + \dots - 2u + 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{25} - 27y^{24} + \dots + 54y - 1$
$c_2, c_5$	$y^{25} - 12y^{24} + \dots + 114688y - 16384$
$c_3, c_4, c_8$ $c_{10}$	$y^{25} - 5y^{24} + \dots + 18y - 1$
$c_6, c_{11}, c_{12}$	$y^{25} + 22y^{24} + \dots + 416y - 64$
$c_7$	$y^{25} - 2y^{24} + \dots - 995392y - 215296$
$c_9$	$y^{25} - 23y^{24} + \dots + 66y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.439994 + 0.950507I$ $a = 0.449056 + 0.849462I$ $b = 0.905847 + 0.107899I$	$-3.00593 - 0.74051I$	$5.05508 + 0.18570I$
$u = 0.439994 - 0.950507I$ $a = 0.449056 - 0.849462I$ $b = 0.905847 - 0.107899I$	$-3.00593 + 0.74051I$	$5.05508 - 0.18570I$
$u = 0.617552 + 0.911770I$ $a = -0.520485 - 0.949952I$ $b = -1.202860 - 0.092876I$	$-9.79766 + 1.38415I$	$2.19427 - 0.69570I$
$u = 0.617552 - 0.911770I$ $a = -0.520485 + 0.949952I$ $b = -1.202860 + 0.092876I$	$-9.79766 - 1.38415I$	$2.19427 + 0.69570I$
$u = -0.155216 + 0.814496I$ $a = 0.569549 + 0.594113I$ $b = 0.482434 + 0.018405I$	$-2.49837 - 1.57308I$	$4.64082 + 4.61190I$
$u = -0.155216 - 0.814496I$ $a = 0.569549 - 0.594113I$ $b = 0.482434 - 0.018405I$	$-2.49837 + 1.57308I$	$4.64082 - 4.61190I$
$u = 0.473172 + 1.138930I$ $a = -0.327562 - 0.860505I$ $b = -0.840347 - 0.335702I$	$-1.79770 - 4.91771I$	$8.41927 + 6.28509I$
$u = 0.473172 - 1.138930I$ $a = -0.327562 + 0.860505I$ $b = -0.840347 + 0.335702I$	$-1.79770 + 4.91771I$	$8.41927 - 6.28509I$
$u = 1.097810 + 0.681530I$ $a = -0.926077 - 0.303192I$ $b = -1.55305 + 0.96565I$	$-8.25231 + 4.52896I$	$4.39857 - 4.77646I$
$u = 1.097810 - 0.681530I$ $a = -0.926077 + 0.303192I$ $b = -1.55305 - 0.96565I$	$-8.25231 - 4.52896I$	$4.39857 + 4.77646I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.569528 + 1.179720I$ $a = 0.270690 + 0.922850I$ $b = 0.887146 + 0.468456I$	$-7.44241 - 8.72137I$	$5.19162 + 6.35185I$
$u = 0.569528 - 1.179720I$ $a = 0.270690 - 0.922850I$ $b = 0.887146 - 0.468456I$	$-7.44241 + 8.72137I$	$5.19162 - 6.35185I$
$u = 1.32152$ $a = -0.469575$ $b = -1.93007$	5.64216	30.1590
$u = 1.306160 + 0.296832I$ $a = 0.548745 + 0.102029I$ $b = 1.63919 - 0.62194I$	$1.99285 + 5.34908I$	$13.9471 - 13.2059I$
$u = 1.306160 - 0.296832I$ $a = 0.548745 - 0.102029I$ $b = 1.63919 + 0.62194I$	$1.99285 - 5.34908I$	$13.9471 + 13.2059I$
$u = 1.214200 + 0.704239I$ $a = 0.907328 + 0.113165I$ $b = 1.41310 - 1.02138I$	$-0.61951 + 6.87942I$	$8.00000 - 4.38169I$
$u = 1.214200 - 0.704239I$ $a = 0.907328 - 0.113165I$ $b = 1.41310 + 1.02138I$	$-0.61951 - 6.87942I$	$8.00000 + 4.38169I$
$u = 1.22071 + 0.77249I$ $a = -0.990264 - 0.040589I$ $b = -1.37746 + 1.13069I$	$0.51235 + 11.71780I$	$8.00000 - 8.48371I$
$u = 1.22071 - 0.77249I$ $a = -0.990264 + 0.040589I$ $b = -1.37746 - 1.13069I$	$0.51235 - 11.71780I$	$8.00000 + 8.48371I$
$u = 1.20009 + 0.80742I$ $a = 1.066910 + 0.022071I$ $b = 1.40118 - 1.21648I$	$-5.4265 + 15.7509I$	$8.00000 - 8.57855I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.20009 - 0.80742I$ $a = 1.066910 - 0.022071I$ $b = 1.40118 + 1.21648I$	$-5.4265 - 15.7509I$	$8.00000 + 8.57855I$
$u = -0.338292$ $a = -1.19055$ $b = -0.300946$	$0.647725$	$15.2540$
$u = -1.66374$ $a = 0.444714$ $b = 0.277763$	$6.10335$	$20.9380$
$u = -1.64375 + 0.30866I$ $a = -0.440186 - 0.060519I$ $b = -0.278561 - 0.018758I$	$2.17466 - 4.23595I$	$0$
$u = -1.64375 - 0.30866I$ $a = -0.440186 + 0.060519I$ $b = -0.278561 + 0.018758I$	$2.17466 + 4.23595I$	$0$

$$\text{II. } I_2^u = \langle -10a^5u^2 + 16a^4u^2 + \dots - 109a + 76, -a^4u^2 - 2a^3u^2 + \dots + 4a - 2, u^3 + u^2 - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a \\ 0.169492a^5u^2 - 0.271186a^4u^2 + \dots + 1.84746a - 1.28814 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 0.169492a^5u^2 - 0.271186a^4u^2 + \dots + 1.84746a - 1.28814 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.135593a^5u^2 + 0.0169492a^4u^2 + \dots - 0.677966a + 0.830508 \\ -0.457627a^5u^2 - 0.0677966a^4u^2 + \dots + 0.711864a - 1.32203 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -a^2u \\ 0.0677966a^5u^2 + 0.491525a^4u^2 + \dots - 0.661017a + 1.08475 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.203390a^5u^2 - 0.525424a^4u^2 + \dots + 1.01695a + 1.25424 \\ 0.610169a^5u^2 + 0.423729a^4u^2 + \dots + 1.05085a + 0.762712 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -0.271186a^5u^2 + 1.03390a^4u^2 + \dots - 1.35593a + 0.661017 \\ -a^5u^2 - a^3u^2 + \dots - a^2 + 1 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.0677966a^5u^2 - 0.508475a^4u^2 + \dots + 0.338983a + 2.08475 \\ -0.0169492a^5u^2 + 0.627119a^4u^2 + \dots + 0.915254a + 0.728814 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.237288a^5u^2 + 0.220339a^4u^2 + \dots + 1.18644a - 1.20339 \\ 1.67797a^5u^2 - 0.0847458a^4u^2 + \dots + 0.389831a + 0.847458 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\text{(iii) Cusp Shapes} = \frac{152}{59}a^5u^2 + \frac{40}{59}a^4u^2 + \dots - \frac{184}{59}a + \frac{1134}{59}$$



(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{18} - 2u^{17} + \dots - 252u - 27$
$c_2, c_5$	$(u^3 - u^2 + 1)^6$
$c_3, c_4, c_8$ $c_{10}$	$u^{18} - 3u^{16} + \dots + 6u - 11$
$c_6, c_{11}, c_{12}$	$(u^3 + 2u + 1)^6$
$c_7$	$(u^3 + 3u^2 + 5u + 2)^6$
$c_9$	$u^{18} + u^{16} + \dots - 52u - 43$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{18} - 6y^{17} + \dots - 81000y + 729$
$c_2, c_5$	$(y^3 - y^2 + 2y - 1)^6$
$c_3, c_4, c_8$ $c_{10}$	$y^{18} - 6y^{17} + \dots - 1136y + 121$
$c_6, c_{11}, c_{12}$	$(y^3 + 4y^2 + 4y - 1)^6$
$c_7$	$(y^3 + y^2 + 13y - 4)^6$
$c_9$	$y^{18} + 2y^{17} + \dots - 17840y + 1849$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 + 0.744862I$ $a = -0.927224 - 0.015489I$ $b = -0.407238 - 0.969235I$	$2.69787 - 2.82812I$	$17.1261 + 2.9794I$
$u = -0.877439 + 0.744862I$ $a = 1.104550 - 0.072177I$ $b = 1.63644 + 0.28753I$	$-7.53006 + 2.30982I$	$5.17231 - 0.22957I$
$u = -0.877439 + 0.744862I$ $a = 0.187603 + 1.191150I$ $b = -0.734633 + 0.080557I$	$-7.53006 + 2.30982I$	$5.17231 - 0.22957I$
$u = -0.877439 + 0.744862I$ $a = -1.241110 - 0.215785I$ $b = -1.66753 - 0.94699I$	$-7.53006 - 7.96606I$	$5.17231 + 6.18847I$
$u = -0.877439 + 0.744862I$ $a = 0.346778 - 1.240900I$ $b = 0.918807 + 0.323963I$	$-7.53006 - 7.96606I$	$5.17231 + 6.18847I$
$u = -0.877439 + 0.744862I$ $a = 0.529395 + 0.353208I$ $b = 0.254152 + 1.224170I$	$2.69787 - 2.82812I$	$17.1261 + 2.9794I$
$u = -0.877439 - 0.744862I$ $a = -0.927224 + 0.015489I$ $b = -0.407238 + 0.969235I$	$2.69787 + 2.82812I$	$17.1261 - 2.9794I$
$u = -0.877439 - 0.744862I$ $a = 1.104550 + 0.072177I$ $b = 1.63644 - 0.28753I$	$-7.53006 - 2.30982I$	$5.17231 + 0.22957I$
$u = -0.877439 - 0.744862I$ $a = 0.187603 - 1.191150I$ $b = -0.734633 - 0.080557I$	$-7.53006 - 2.30982I$	$5.17231 + 0.22957I$
$u = -0.877439 - 0.744862I$ $a = -1.241110 + 0.215785I$ $b = -1.66753 + 0.94699I$	$-7.53006 + 7.96606I$	$5.17231 - 6.18847I$

Solutions to $I_2^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 - 0.744862I$ $a = 0.346778 + 1.240900I$ $b = 0.918807 - 0.323963I$	$-7.53006 + 7.96606I$	$5.17231 - 6.18847I$
$u = -0.877439 - 0.744862I$ $a = 0.529395 - 0.353208I$ $b = 0.254152 - 1.224170I$	$2.69787 + 2.82812I$	$17.1261 - 2.9794I$
$u = 0.754878$ $a = 0.737750 + 0.212805I$ $b = 0.61766 + 2.03584I$	$-3.39248 + 5.13794I$	$11.70158 - 3.20902I$
$u = 0.754878$ $a = 0.737750 - 0.212805I$ $b = 0.61766 - 2.03584I$	$-3.39248 - 5.13794I$	$11.70158 + 3.20902I$
$u = 0.754878$ $a = -0.90888 + 1.32075I$ $b = -0.090652 - 1.376170I$	$-3.39248 - 5.13794I$	$11.70158 + 3.20902I$
$u = 0.754878$ $a = -0.90888 - 1.32075I$ $b = -0.090652 + 1.376170I$	$-3.39248 + 5.13794I$	$11.70158 - 3.20902I$
$u = 0.754878$ $a = -1.94302$ $b = -1.43643$	$6.83546$	$23.6550$
$u = 0.754878$ $a = 2.28528$ $b = 0.382411$	$6.83546$	$23.6550$

**III.**

$$I_3^u = \langle 2u^{13} + 7u^{12} + \dots + b - 5, 5u^{14} + 17u^{13} + \dots + a - 5, u^{15} + 3u^{14} + \dots - 6u^2 + 1 \rangle$$

**(i) Arc colorings**

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -5u^{14} - 17u^{13} + \dots + 4u + 5 \\ -2u^{13} - 7u^{12} + \dots - 26u^2 + 5 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -5u^{14} - 17u^{13} + \dots + 4u + 5 \\ 3u^{14} + 8u^{13} + \dots - 5u + 3 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -7u^{14} - 24u^{13} + \dots + 9u + 5 \\ u^{14} + 2u^{13} + \dots - 2u + 2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u^{14} + 4u^{13} + \dots - 10u - 6 \\ u^{14} + 3u^{13} + \dots - 4u^2 - 5u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 5u^{14} + 16u^{13} + \dots - 17u - 8 \\ u^{13} + 3u^{12} + \dots - 4u - 4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -9u^{14} - 32u^{13} + \dots + 15u + 15 \\ -4u^{14} - 14u^{13} + \dots + 10u + 3 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 6u^{14} + 19u^{13} + \dots - 21u - 8 \\ u^{14} + 4u^{13} + \dots - 7u - 4 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 3u^{14} + 13u^{13} + \dots - 3u - 4 \\ 3u^{14} + 9u^{13} + \dots - u - 1 \end{pmatrix}$$

**(ii) Obstruction class = 1**

**(iii) Cusp Shapes** =  $8u^{14} + 21u^{13} - 11u^{12} - 84u^{11} - 54u^{10} + 113u^9 + 166u^8 - 35u^7 - 173u^6 - 38u^5 + 82u^4 + 34u^3 - 32u^2 - 6u + 9$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{15} + 3u^{14} + \dots + 4u^2 - 1$
$c_2$	$u^{15} + 3u^{14} + \dots - 6u^2 + 1$
$c_3, c_8$	$u^{15} + u^{14} + \dots + 6u^2 - 1$
$c_4, c_{10}$	$u^{15} - u^{14} + \dots - 6u^2 + 1$
$c_5$	$u^{15} - 3u^{14} + \dots + 6u^2 - 1$
$c_6$	$u^{15} + u^{14} + \dots - 3u^2 + 1$
$c_7$	$u^{15} - u^{14} + \dots - 2u + 1$
$c_9$	$u^{15} + u^{14} + \dots - 4u^2 + 1$
$c_{11}, c_{12}$	$u^{15} - u^{14} + \dots + 3u^2 - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{15} + 7y^{14} + \dots + 8y - 1$
$c_2, c_5$	$y^{15} - 11y^{14} + \dots + 12y - 1$
$c_3, c_4, c_8$ $c_{10}$	$y^{15} - 15y^{14} + \dots + 12y - 1$
$c_6, c_{11}, c_{12}$	$y^{15} + 15y^{14} + \dots + 6y - 1$
$c_7$	$y^{15} - 5y^{14} + \dots + 2y - 1$
$c_9$	$y^{15} + 3y^{14} + \dots + 8y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.772963 + 0.597189I$ $a = -0.827811 - 0.016279I$ $b = -0.343553 - 1.218360I$	$1.77519 - 3.34740I$	$8.50075 + 8.05329I$
$u = -0.772963 - 0.597189I$ $a = -0.827811 + 0.016279I$ $b = -0.343553 + 1.218360I$	$1.77519 + 3.34740I$	$8.50075 - 8.05329I$
$u = 1.21630$ $a = -1.10982$ $b = -0.609066$	$8.60341$	$19.2250$
$u = 1.216020 + 0.268411I$ $a = 1.037430 - 0.282211I$ $b = 0.591253 - 0.100818I$	$4.59696 + 3.78442I$	$13.45506 - 3.52568I$
$u = 1.216020 - 0.268411I$ $a = 1.037430 + 0.282211I$ $b = 0.591253 + 0.100818I$	$4.59696 - 3.78442I$	$13.45506 + 3.52568I$
$u = -0.741693 + 1.001970I$ $a = 0.645240 + 0.343179I$ $b = 0.168411 + 0.864224I$	$-1.02527 - 2.06106I$	$10.76904 + 5.89866I$
$u = -0.741693 - 1.001970I$ $a = 0.645240 - 0.343179I$ $b = 0.168411 - 0.864224I$	$-1.02527 + 2.06106I$	$10.76904 - 5.89866I$
$u = -0.581097 + 0.353670I$ $a = 1.215450 - 0.514042I$ $b = 0.12631 + 1.63261I$	$-4.31889 - 5.65349I$	$3.28441 + 7.61935I$
$u = -0.581097 - 0.353670I$ $a = 1.215450 + 0.514042I$ $b = 0.12631 - 1.63261I$	$-4.31889 + 5.65349I$	$3.28441 - 7.61935I$
$u = 0.661672$ $a = 2.39502$ $b = 0.953687$	$6.37007$	$2.43460$



Solutions to $I_3^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.577868 + 0.178736I$ $a = -2.47388 + 1.02720I$ $b = -0.998690 + 0.209089I$	$1.98344 - 1.67719I$	$4.13214 - 1.25424I$
$u = 0.577868 - 0.178736I$ $a = -2.47388 - 1.02720I$ $b = -0.998690 - 0.209089I$	$1.98344 + 1.67719I$	$4.13214 + 1.25424I$
$u = -1.41521$ $a = 0.382739$ $b = 1.30454$	5.30168	4.34420
$u = -1.42952 + 0.46018I$ $a = -0.430407 - 0.024659I$ $b = -0.868313 - 0.551235I$	$1.65539 - 4.71343I$	$7.35653 + 5.31534I$
$u = -1.42952 - 0.46018I$ $a = -0.430407 + 0.024659I$ $b = -0.868313 + 0.551235I$	$1.65539 + 4.71343I$	$7.35653 - 5.31534I$

$$\text{IV. } I_4^u = \langle -44a^7u^2 - 73a^6u^2 + \dots - 213a + 245, -2a^6u^2 - a^5u^2 + \dots + 7a + 13, u^3 + u^2 - 1 \rangle$$

(i) Arc colorings

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ u^2 + u - 1 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} a \\ 0.273292a^7u^2 + 0.453416a^6u^2 + \dots + 1.32298a - 1.52174 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} a \\ 0.273292a^7u^2 + 0.453416a^6u^2 + \dots + 1.32298a - 1.52174 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.677019a^7u^2 - 0.645963a^6u^2 + \dots + 0.745342a + 1.56522 \\ -0.658385a^7u^2 - 0.683230a^6u^2 + \dots + 1.40373a - 0.652174 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -a^2u \\ 1.36025a^7u^2 + 0.279503a^6u^2 + \dots + 0.0621118a - 0.869565 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -1.02484a^7u^2 - 1.95031a^6u^2 + \dots + 2.78882a + 0.956522 \\ -1.16149a^7u^2 - 0.677019a^6u^2 + \dots - 0.372671a + 1.21739 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -1.72671a^7u^2 - 2.54658a^6u^2 + \dots + 5.32298a + 2.47826 \\ 0.00621118a^7u^2 - 2.01242a^6u^2 + \dots + 2.55280a - 1.73913 \end{pmatrix}$$

$$a_{12} = \begin{pmatrix} 0.608696a^7u^2 - 2.21739a^6u^2 + \dots + 3.17391a - 0.434783 \\ -\frac{15}{7}a^7u^2 - \frac{5}{7}a^6u^2 + \dots + \frac{9}{7}a + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -0.950311a^7u^2 + 1.90062a^6u^2 + \dots - 2.57764a - 2.91304 \\ 0.124224a^7u^2 + 3.75155a^6u^2 + \dots - 4.94410a - 0.782609 \end{pmatrix}$$

(ii) Obstruction class = -1

$$(iii) \text{ Cusp Shapes} = -\frac{52}{23}a^7u^2 - \frac{80}{23}a^6u^2 + \dots + \frac{248}{23}a + \frac{254}{23}$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1$	$u^{24} - 5u^{23} + \dots - 20u + 109$
$c_2, c_5$	$(u^3 - u^2 + 1)^8$
$c_3, c_4, c_8$ $c_{10}$	$u^{24} + u^{23} + \dots - 24u + 7$
$c_6, c_{11}, c_{12}$	$(u^4 - u^3 + 2u^2 - 2u + 1)^6$
$c_7$	$(u^2 - u + 1)^{12}$
$c_9$	$u^{24} + 3u^{23} + \dots + 20u + 19$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1$	$y^{24} + 9y^{23} + \dots + 27504y + 11881$
$c_2, c_5$	$(y^3 - y^2 + 2y - 1)^8$
$c_3, c_4, c_8$ $c_{10}$	$y^{24} - 15y^{23} + \dots - 716y + 49$
$c_6, c_{11}, c_{12}$	$(y^4 + 3y^3 + 2y^2 + 1)^6$
$c_7$	$(y^2 + y + 1)^{12}$
$c_9$	$y^{24} + 5y^{23} + \dots + 1424y + 361$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 + 0.744862I$ $a = -0.040773 - 0.997477I$ $b = 0.617792 + 0.097671I$	$-1.37919 - 0.79824I$	$8.49024 - 0.48465I$
$u = -0.877439 + 0.744862I$ $a = 0.964624 - 0.327636I$ $b = 0.525863 + 0.945972I$	$-1.37919 - 4.85801I$	$8.49024 + 6.44355I$
$u = -0.877439 + 0.744862I$ $a = -1.039300 - 0.058321I$ $b = -1.39358 - 0.47039I$	$-1.37919 - 0.79824I$	$8.49024 - 0.48465I$
$u = -0.877439 + 0.744862I$ $a = 1.033460 + 0.263154I$ $b = 0.303126 + 0.916009I$	$-1.37919 - 0.79824I$	$8.49024 - 0.48465I$
$u = -0.877439 + 0.744862I$ $a = -0.254667 + 1.040960I$ $b = -0.745244 - 0.312818I$	$-1.37919 - 4.85801I$	$8.49024 + 6.44355I$
$u = -0.877439 + 0.744862I$ $a = -0.747266 - 0.522075I$ $b = -0.56367 - 1.44433I$	$-1.37919 - 4.85801I$	$8.49024 + 6.44355I$
$u = -0.877439 + 0.744862I$ $a = 1.121100 + 0.196208I$ $b = 1.43883 + 0.82244I$	$-1.37919 - 4.85801I$	$8.49024 + 6.44355I$
$u = -0.877439 + 0.744862I$ $a = -0.159736 - 0.339671I$ $b = 0.154539 - 1.116840I$	$-1.37919 - 0.79824I$	$8.49024 - 0.48465I$
$u = -0.877439 - 0.744862I$ $a = -0.040773 + 0.997477I$ $b = 0.617792 - 0.097671I$	$-1.37919 + 0.79824I$	$8.49024 + 0.48465I$
$u = -0.877439 - 0.744862I$ $a = 0.964624 + 0.327636I$ $b = 0.525863 - 0.945972I$	$-1.37919 + 4.85801I$	$8.49024 - 6.44355I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.877439 - 0.744862I$ $a = -1.039300 + 0.058321I$ $b = -1.39358 + 0.47039I$	$-1.37919 + 0.79824I$	$8.49024 + 0.48465I$
$u = -0.877439 - 0.744862I$ $a = 1.033460 - 0.263154I$ $b = 0.303126 - 0.916009I$	$-1.37919 + 0.79824I$	$8.49024 + 0.48465I$
$u = -0.877439 - 0.744862I$ $a = -0.254667 - 1.040960I$ $b = -0.745244 + 0.312818I$	$-1.37919 + 4.85801I$	$8.49024 - 6.44355I$
$u = -0.877439 - 0.744862I$ $a = -0.747266 + 0.522075I$ $b = -0.56367 + 1.44433I$	$-1.37919 + 4.85801I$	$8.49024 - 6.44355I$
$u = -0.877439 - 0.744862I$ $a = 1.121100 - 0.196208I$ $b = 1.43883 - 0.82244I$	$-1.37919 + 4.85801I$	$8.49024 - 6.44355I$
$u = -0.877439 - 0.744862I$ $a = -0.159736 + 0.339671I$ $b = 0.154539 + 1.116840I$	$-1.37919 + 0.79824I$	$8.49024 + 0.48465I$
$u = 0.754878$ $a = -0.935402 + 0.185618I$ $b = -0.56365 - 1.65106I$	$2.75839 + 2.02988I$	$15.0195 - 3.4641I$
$u = 0.754878$ $a = -0.935402 - 0.185618I$ $b = -0.56365 + 1.65106I$	$2.75839 - 2.02988I$	$15.0195 + 3.4641I$
$u = 0.754878$ $a = 1.027300 + 0.800722I$ $b = 0.28063 - 1.38647I$	$2.75839 + 2.02988I$	$15.0195 - 3.4641I$
$u = 0.754878$ $a = 1.027300 - 0.800722I$ $b = 0.28063 + 1.38647I$	$2.75839 - 2.02988I$	$15.0195 + 3.4641I$

Solutions to $I_4^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.754878$ $a = 1.88775 + 0.07859I$ $b = 1.63567 + 0.61747I$	$2.75839 + 2.02988I$	$15.0195 - 3.4641I$
$u = 0.754878$ $a = 1.88775 - 0.07859I$ $b = 1.63567 - 0.61747I$	$2.75839 - 2.02988I$	$15.0195 + 3.4641I$
$u = 0.754878$ $a = -2.35710 + 0.41119I$ $b = -0.190292 - 0.406791I$	$2.75839 - 2.02988I$	$15.0195 + 3.4641I$
$u = 0.754878$ $a = -2.35710 - 0.41119I$ $b = -0.190292 + 0.406791I$	$2.75839 + 2.02988I$	$15.0195 - 3.4641I$

## V. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1$	$(u^{15} + 3u^{14} + \dots + 4u^2 - 1)(u^{18} - 2u^{17} + \dots - 252u - 27)$ $\cdot (u^{24} - 5u^{23} + \dots - 20u + 109)(u^{25} - 3u^{24} + \dots + 2u + 1)$
$c_2$	$((u^3 - u^2 + 1)^{14})(u^{15} + 3u^{14} + \dots - 6u^2 + 1)$ $\cdot (u^{25} + 12u^{24} + \dots + 640u + 128)$
$c_3, c_8$	$(u^{15} + u^{14} + \dots + 6u^2 - 1)(u^{18} - 3u^{16} + \dots + 6u - 11)$ $\cdot (u^{24} + u^{23} + \dots - 24u + 7)(u^{25} - u^{24} + \dots + 2u - 1)$
$c_4, c_{10}$	$(u^{15} - u^{14} + \dots - 6u^2 + 1)(u^{18} - 3u^{16} + \dots + 6u - 11)$ $\cdot (u^{24} + u^{23} + \dots - 24u + 7)(u^{25} - u^{24} + \dots + 2u - 1)$
$c_5$	$((u^3 - u^2 + 1)^{14})(u^{15} - 3u^{14} + \dots + 6u^2 - 1)$ $\cdot (u^{25} + 12u^{24} + \dots + 640u + 128)$
$c_6$	$((u^3 + 2u + 1)^6)(u^4 - u^3 + 2u^2 - 2u + 1)^6(u^{15} + u^{14} + \dots - 3u^2 + 1)$ $\cdot (u^{25} + 6u^{24} + \dots + 40u + 8)$
$c_7$	$((u^2 - u + 1)^{12})(u^3 + 3u^2 + 5u + 2)^6(u^{15} - u^{14} + \dots - 2u + 1)$ $\cdot (u^{25} - 6u^{24} + \dots - 56u + 464)$
$c_9$	$(u^{15} + u^{14} + \dots - 4u^2 + 1)(u^{18} + u^{16} + \dots - 52u - 43)$ $\cdot (u^{24} + 3u^{23} + \dots + 20u + 19)(u^{25} + u^{24} + \dots - 2u + 1)$
$c_{11}, c_{12}$	$((u^3 + 2u + 1)^6)(u^4 - u^3 + 2u^2 - 2u + 1)^6(u^{15} - u^{14} + \dots + 3u^2 - 1)$ $\cdot (u^{25} + 6u^{24} + \dots + 40u + 8)$



## VI. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1$	$(y^{15} + 7y^{14} + \dots + 8y - 1)(y^{18} - 6y^{17} + \dots - 81000y + 729)$ $\cdot (y^{24} + 9y^{23} + \dots + 27504y + 11881)(y^{25} - 27y^{24} + \dots + 54y - 1)$
$c_2, c_5$	$((y^3 - y^2 + 2y - 1)^{14})(y^{15} - 11y^{14} + \dots + 12y - 1)$ $\cdot (y^{25} - 12y^{24} + \dots + 114688y - 16384)$
$c_3, c_4, c_8$ $c_{10}$	$(y^{15} - 15y^{14} + \dots + 12y - 1)(y^{18} - 6y^{17} + \dots - 1136y + 121)$ $\cdot (y^{24} - 15y^{23} + \dots - 716y + 49)(y^{25} - 5y^{24} + \dots + 18y - 1)$
$c_6, c_{11}, c_{12}$	$((y^3 + 4y^2 + 4y - 1)^6)(y^4 + 3y^3 + 2y^2 + 1)^6(y^{15} + 15y^{14} + \dots + 6y - 1)$ $\cdot (y^{25} + 22y^{24} + \dots + 416y - 64)$
$c_7$	$((y^2 + y + 1)^{12})(y^3 + y^2 + 13y - 4)^6(y^{15} - 5y^{14} + \dots + 2y - 1)$ $\cdot (y^{25} - 2y^{24} + \dots - 995392y - 215296)$
$c_9$	$(y^{15} + 3y^{14} + \dots + 8y - 1)(y^{18} + 2y^{17} + \dots - 17840y + 1849)$ $\cdot (y^{24} + 5y^{23} + \dots + 1424y + 361)(y^{25} - 23y^{24} + \dots + 66y - 1)$