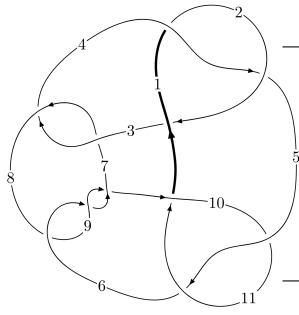
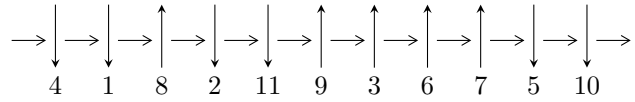


11a<sub>44</sub> (K11a<sub>44</sub>)



A knot diagram<sup>1</sup>

**Linearized knot diagram**



**Solving Sequence**

$$3,7 \xrightarrow{c_7} 8 \xrightarrow{c_3} 4,9 \xrightarrow{c_9} 1,10 \xrightarrow{c_2} 2 \xrightarrow{c_6} 6 \xrightarrow{c_{11}} 11 \xrightarrow{c_5} 5 \longrightarrow c_1, c_4, c_8, c_{10}$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

$$\begin{aligned}
I_1^u &= \langle 295797384u^{18} + 418536515u^{17} + \dots + 3702415268d - 1995040792, \\
&186291706u^{18} + 295294768u^{17} + \dots + 3702415268c - 4955557140, \\
&- 340509075u^{18} - 461083130u^{17} + \dots + 3702415268b + 2243928812, \\
&- 1103288949u^{18} - 1383517078u^{17} + \dots + 7404830536a + 9000488512, \\
&u^{19} + 2u^{18} + \dots + 4u^2 - 8 \rangle \\
I_2^u &= \langle u^7 - 2u^6 + u^5 + 3u^4 - 5u^3 + 3u^2 + d + u - 1, u^7 - 3u^6 + u^5 + 4u^4 - 8u^3 + 5u^2 + 2c + u - 4, \\
&- u^7a + 2u^6a + 2u^7 - 4u^6 - 4u^4a + 2u^5 + 5u^3a + 5u^4 - u^2a - 9u^3 - 3au + 8u^2 + b + 2a - u, \\
&3u^7a - 4u^7 + \dots - 6a + 8, u^8 - 3u^7 + 3u^6 + 2u^5 - 8u^4 + 9u^3 - 3u^2 - 2u + 2 \rangle \\
I_3^u &= \langle u^5a + u^4a - u^5 - u^3a - u^4 - u^2a + u^2 + d, -u^5a - u^4a + u^2a + u^3 + au + u^2 + c - 1, \\
&- u^4a - u^3a + u^4 + 2u^2a + u^3 + au + b - a - u, 2u^5a + 2u^4a - u^5 - 2u^3a - u^4 - 3u^2a + a^2 + u^2 + a, \\
&u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle \\
I_4^u &= \langle u^5c - u^5 - 2u^3c + u^3 + 2cu + d - u + 1, -2u^4c - u^3c + u^4 + 2u^2c + c^2 + 2cu - u^2 - u, -u^2 + b, \\
&- u^2 + a + 1, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle \\
I_5^u &= \langle u^5 - u^3 + d + u, 2u^5 + 2u^4 - 3u^3 - 4u^2 + c + 2u + 2, -u^2 + b, -u^2 + a + 1, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle \\
\\
I_1^v &= \langle a, d, c - 1, b - 1, v + 1 \rangle \\
I_2^v &= \langle c, d + 1, b, a - 1, v - 1 \rangle \\
I_3^v &= \langle a, d + 1, c - a - 1, b + 1, v - 1 \rangle \\
I_4^v &= \langle c, d + 1, -av + c - v - 1, bv + 1 \rangle
\end{aligned}$$

\* 8 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 68 representations.

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 1$

---

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\mathbf{I. } I_1^u = \langle 2.96 \times 10^8 u^{18} + 4.19 \times 10^8 u^{17} + \dots + 3.70 \times 10^9 d - 2.00 \times 10^9, 1.86 \times 10^8 u^{18} + 2.95 \times 10^8 u^{17} + \dots + 3.70 \times 10^9 c - 4.96 \times 10^9, -3.41 \times 10^8 u^{18} - 4.61 \times 10^8 u^{17} + \dots + 3.70 \times 10^9 b + 2.24 \times 10^9, -1.10 \times 10^9 u^{18} - 1.38 \times 10^9 u^{17} + \dots + 7.40 \times 10^9 a + 9.00 \times 10^9, u^{19} + 2u^{18} + \dots + 4u^2 - 8 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -0.0503163u^{18} - 0.0797573u^{17} + \dots - 0.0228247u + 1.33847 \\ -0.0798931u^{18} - 0.113044u^{17} + \dots - 0.992877u + 0.538848 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0.148996u^{18} + 0.186840u^{17} + \dots + 0.656789u - 1.21549 \\ 0.0919694u^{18} + 0.124536u^{17} + \dots + 1.08046u - 0.606072 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -0.130209u^{18} - 0.192802u^{17} + \dots - 1.01570u + 1.87731 \\ -0.0798931u^{18} - 0.113044u^{17} + \dots - 0.992877u + 0.538848 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 0.0237009u^{18} + 0.0450696u^{17} + \dots + 0.0621551u - 0.293810 \\ 0.0895560u^{18} + 0.0824521u^{17} + \dots + 1.48819u - 0.554949 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -0.0503163u^{18} - 0.0797573u^{17} + \dots - 0.0228247u + 1.33847 \\ 0.133048u^{18} + 0.117935u^{17} + \dots + 1.39541u - 0.705850 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0.106508u^{18} + 0.147732u^{17} + \dots + 0.953547u - 1.58350 \\ -0.00966290u^{18} + 0.0305921u^{17} + \dots + 0.504689u + 0.0161009 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0570264u^{18} - 0.0623040u^{17} + \dots + 0.423674u + 0.609417 \\ 0.143944u^{18} + 0.132344u^{17} + \dots + 1.53667u - 1.02006 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -0.0570264u^{18} - 0.0623040u^{17} + \dots + 0.423674u + 0.609417 \\ 0.143944u^{18} + 0.132344u^{17} + \dots + 1.53667u - 1.02006 \end{pmatrix}$$

(ii) Obstruction class = -1

$$\mathbf{(iii) Cusp Shapes} = -\frac{1436975081}{1851207634}u^{18} - \frac{348795105}{1851207634}u^{17} + \dots - \frac{4741127818}{925603817}u + \frac{7721567164}{925603817}$$

(iv) u-Polynomials at the component

| Crossings                   | u-Polynomials at each crossing        |
|-----------------------------|---------------------------------------|
| $c_1, c_4, c_5$<br>$c_{10}$ | $u^{19} - 2u^{18} + \dots + 3u - 1$   |
| $c_2, c_{11}$               | $u^{19} + 8u^{18} + \dots + 19u + 1$  |
| $c_3, c_7$                  | $u^{19} + 2u^{18} + \dots + 4u^2 - 8$ |
| $c_6, c_8, c_9$             | $u^{19} + 2u^{18} + \dots - 8u - 4$   |

(v) Riley Polynomials at the component

| Crossings                   | Riley Polynomials at each crossing     |
|-----------------------------|--|
| $c_1, c_4, c_5$<br>$c_{10}$ | $y^{19} - 8y^{18} + \dots + 19y - 1$   |
| $c_2, c_{11}$               | $y^{19} + 12y^{18} + \dots + 195y - 1$ |
| $c_3, c_7$                  | $y^{19} - 6y^{18} + \dots + 64y - 64$  |
| $c_6, c_8, c_9$             | $y^{19} - 18y^{18} + \dots + 88y - 16$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -1.085440 + 0.040618I$<br>$a = -0.082939 - 0.820035I$<br>$b = -0.548223 - 0.458686I$<br>$c = 0.526397 + 0.204170I$<br>$d = -0.651290 + 0.640476I$ | $2.40223 - 3.63220I$                  | $3.52732 + 6.81616I$  |
| $u = -1.085440 - 0.040618I$<br>$a = -0.082939 + 0.820035I$<br>$b = -0.548223 + 0.458686I$<br>$c = 0.526397 - 0.204170I$<br>$d = -0.651290 - 0.640476I$ | $2.40223 + 3.63220I$                  | $3.52732 - 6.81616I$  |
| $u = -0.122471 + 1.080680I$<br>$a = 0.718026 + 0.002764I$<br>$b = 1.002700 + 0.800999I$<br>$c = 0.423035 - 0.010382I$<br>$d = -1.362450 - 0.057980I$   | $4.14406 - 1.22871I$                  | $4.10945 + 3.37998I$  |
| $u = -0.122471 - 1.080680I$<br>$a = 0.718026 - 0.002764I$<br>$b = 1.002700 - 0.800999I$<br>$c = 0.423035 + 0.010382I$<br>$d = -1.362450 + 0.057980I$   | $4.14406 + 1.22871I$                  | $4.10945 - 3.37998I$  |
| $u = 0.583709 + 0.932517I$<br>$a = 1.248640 - 0.243760I$<br>$b = 0.757420 - 1.122890I$<br>$c = 0.663350 - 0.622962I$<br>$d = 0.198964 - 0.752266I$     | $-4.29720 - 4.85510I$                 | $-5.63265 + 5.33490I$ |
| $u = 0.583709 - 0.932517I$<br>$a = 1.248640 + 0.243760I$<br>$b = 0.757420 + 1.122890I$<br>$c = 0.663350 + 0.622962I$<br>$d = 0.198964 + 0.752266I$     | $-4.29720 + 4.85510I$                 | $-5.63265 - 5.33490I$ |

| Solutions to $I_1^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.628638 + 1.123100I$<br>$a = -1.232770 - 0.120292I$<br>$b = -1.30952 - 1.42851I$<br>$c = 0.413232 - 0.052969I$<br>$d = -1.380830 - 0.305181I$ | $0.71510 + 8.68076I$                  | $-0.47305 - 6.48182I$ |
| $u = -0.628638 - 1.123100I$<br>$a = -1.232770 + 0.120292I$<br>$b = -1.30952 + 1.42851I$<br>$c = 0.413232 + 0.052969I$<br>$d = -1.380830 + 0.305181I$ | $0.71510 - 8.68076I$                  | $-0.47305 + 6.48182I$ |
| $u = 1.114960 + 0.705316I$<br>$a = 0.111878 - 1.272940I$<br>$b = -1.46155 - 1.34018I$<br>$c = 0.523314 - 0.396742I$<br>$d = -0.213448 - 0.919956I$   | $-2.61225 + 10.89710I$                | $-3.23641 - 8.50579I$ |
| $u = 1.114960 - 0.705316I$<br>$a = 0.111878 + 1.272940I$<br>$b = -1.46155 + 1.34018I$<br>$c = 0.523314 + 0.396742I$<br>$d = -0.213448 + 0.919956I$   | $-2.61225 - 10.89710I$                | $-3.23641 + 8.50579I$ |
| $u = -0.072034 + 0.667244I$<br>$a = -0.502161 - 0.640166I$<br>$b = -0.246691 + 0.049771I$<br>$c = 1.56560 + 0.68284I$<br>$d = 0.463352 + 0.234060I$  | $-1.32552 + 1.22673I$                 | $-3.58366 - 5.47914I$ |
| $u = -0.072034 - 0.667244I$<br>$a = -0.502161 + 0.640166I$<br>$b = -0.246691 - 0.049771I$<br>$c = 1.56560 - 0.68284I$<br>$d = 0.463352 - 0.234060I$  | $-1.32552 - 1.22673I$                 | $-3.58366 + 5.47914I$ |

| Solutions to $I_1^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = -1.241950 + 0.516338I$<br>$a = 0.276604 + 0.673540I$<br>$b = -1.46152 + 0.68811I$<br>$c = -1.72308 - 0.97561I$<br>$d = 1.43947 - 0.24883I$   | $7.80660 - 4.21764I$                  | $6.24313 + 1.77538I$ |
| $u = -1.241950 - 0.516338I$<br>$a = 0.276604 - 0.673540I$<br>$b = -1.46152 - 0.68811I$<br>$c = -1.72308 + 0.97561I$<br>$d = 1.43947 + 0.24883I$   | $7.80660 + 4.21764I$                  | $6.24313 - 1.77538I$ |
| $u = 1.391220 + 0.215371I$<br>$a = -0.043768 - 1.017560I$<br>$b = -0.031342 + 0.273386I$<br>$c = -1.88210 + 0.37845I$<br>$d = 1.51067 + 0.10269I$ | $9.74824 + 5.99256I$                  | $5.35093 - 5.49640I$ |
| $u = 1.391220 - 0.215371I$<br>$a = -0.043768 + 1.017560I$<br>$b = -0.031342 - 0.273386I$<br>$c = -1.88210 - 0.37845I$<br>$d = 1.51067 - 0.10269I$ | $9.74824 - 5.99256I$                  | $5.35093 + 5.49640I$ |
| $u = -1.18800 + 0.79635I$<br>$a = -0.064734 - 1.301180I$<br>$b = 1.97753 - 1.24306I$<br>$c = -1.28148 - 1.20067I$<br>$d = 1.41555 - 0.38935I$     | $2.5538 - 15.5977I$                   | $0.09598 + 9.40344I$ |
| $u = -1.18800 - 0.79635I$<br>$a = -0.064734 + 1.301180I$<br>$b = 1.97753 + 1.24306I$<br>$c = -1.28148 + 1.20067I$<br>$d = 1.41555 + 0.38935I$     | $2.5538 + 15.5977I$                   | $0.09598 - 9.40344I$ |



| Solutions to $I_1^u$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $u = 0.497291$       |                                       |            |
| $a = 0.142445$       |                                       |            |
| $b = 0.642422$       | 1.20822                               | 9.19790    |
| $c = 0.543479$       |                                       |            |
| $d = -0.839998$      |                                       |            |

$$\text{II. } I_2^u = \langle u^7 - 2u^6 + \cdots + d - 1, u^7 - 3u^6 + \cdots + 2c - 4, -u^7a + 2u^7 + \cdots + b + 2a, 3u^7a - 4u^7 + \cdots - 6a + 8, u^8 - 3u^7 + \cdots - 2u + 2 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -\frac{1}{2}u^7 + \frac{3}{2}u^6 + \cdots - \frac{1}{2}u + 2 \\ -u^7 + 2u^6 - u^5 - 3u^4 + 5u^3 - 3u^2 - u + 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ u^7a - 2u^7 + \cdots - 2a + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -\frac{3}{2}u^7 + \frac{7}{2}u^6 + \cdots - \frac{3}{2}u + 3 \\ -u^7 + 2u^6 - u^5 - 3u^4 + 5u^3 - 3u^2 - u + 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^6a + 2u^7 + \cdots + 3a - 4 \\ -u^7a + 3u^6a + \cdots + 2a - 2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -\frac{1}{2}u^7 + \frac{3}{2}u^6 + \cdots - \frac{1}{2}u + 2 \\ -u^6 + u^5 + u^4 - 3u^3 + 2u^2 - 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^7a + \frac{5}{2}u^7 + \cdots + 4a - 5 \\ -u^7 + 2u^6 + \cdots + 2u - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^7a - 2u^7 + \cdots - 3a + u \\ u^7a - u^6a + \cdots + u - 4 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^7a - 2u^7 + \cdots - 3a + u \\ u^7a - u^6a + \cdots + u - 4 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-2u^7 + 4u^5 - 6u^4 - 4u^3 + 6u^2 - 8u - 4$

(iv) u-Polynomials at the component

| Crossings                   | u-Polynomials at each crossing                               |
|-----------------------------|--|
| $c_1, c_4, c_5$<br>$c_{10}$ | $u^{16} - u^{15} + \dots + 4u - 4$                           |
| $c_2, c_{11}$               | $u^{16} + 7u^{15} + \dots + 40u + 16$                        |
| $c_3, c_7$                  | $(u^8 - 3u^7 + 3u^6 + 2u^5 - 8u^4 + 9u^3 - 3u^2 - 2u + 2)^2$ |
| $c_6, c_8, c_9$             | $(u^8 + u^7 - 4u^6 - 3u^5 + 5u^4 + u^3 - u^2 + 3u - 1)^2$    |

(v) Riley Polynomials at the component

| Crossings                   | Riley Polynomials at each crossing                                |
|-----------------------------|---|
| $c_1, c_4, c_5$<br>$c_{10}$ | $y^{16} - 7y^{15} + \dots - 40y + 16$                             |
| $c_2, c_{11}$               | $y^{16} + y^{15} + \dots - 544y + 256$                            |
| $c_3, c_7$                  | $(y^8 - 3y^7 + 5y^6 - 4y^5 + 2y^4 - 13y^3 + 13y^2 - 16y + 4)^2$   |
| $c_6, c_8, c_9$             | $(y^8 - 9y^7 + 32y^6 - 53y^5 + 31y^4 + 15y^3 - 15y^2 - 7y + 1)^2$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---|---------------------------------------|-----------------------|
| $u = 0.821613 + 0.567011I$<br>$a = 0.327841 - 1.281680I$<br>$b = -0.32411 - 2.07852I$<br>$c = 0.647330 - 0.378425I$<br>$d = -0.151337 - 0.673064I$  | $-4.77492 + 2.26376I$                 | $-6.05872 - 4.53378I$ |
| $u = 0.821613 + 0.567011I$<br>$a = 1.55977 - 0.26895I$<br>$b = -0.408126 - 1.151440I$<br>$c = 0.647330 - 0.378425I$<br>$d = -0.151337 - 0.673064I$  | $-4.77492 + 2.26376I$                 | $-6.05872 - 4.53378I$ |
| $u = 0.821613 - 0.567011I$<br>$a = 0.327841 + 1.281680I$<br>$b = -0.32411 + 2.07852I$<br>$c = 0.647330 + 0.378425I$<br>$d = -0.151337 + 0.673064I$  | $-4.77492 - 2.26376I$                 | $-6.05872 + 4.53378I$ |
| $u = 0.821613 - 0.567011I$<br>$a = 1.55977 + 0.26895I$<br>$b = -0.408126 + 1.151440I$<br>$c = 0.647330 + 0.378425I$<br>$d = -0.151337 + 0.673064I$  | $-4.77492 - 2.26376I$                 | $-6.05872 + 4.53378I$ |
| $u = 0.432344 + 1.079150I$<br>$a = 1.115680 - 0.168353I$<br>$b = 1.27697 - 0.76242I$<br>$c = 0.420583 + 0.036953I$<br>$d = -1.359440 + 0.207304I$   | $2.93531 - 3.55755I$                  | $2.52739 + 2.62489I$  |
| $u = 0.432344 + 1.079150I$<br>$a = -0.603271 + 0.193035I$<br>$b = -0.50994 + 1.48491I$<br>$c = 0.420583 + 0.036953I$<br>$d = -1.359440 + 0.207304I$ | $2.93531 - 3.55755I$                  | $2.52739 + 2.62489I$  |

| Solutions to $I_2^u$  | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|---|---------------------------------------|----------------------|
| $u = 0.432344 - 1.079150I$<br>$a = 1.115680 + 0.168353I$<br>$b = 1.27697 + 0.76242I$<br>$c = 0.420583 - 0.036953I$<br>$d = -1.359440 - 0.207304I$   | $2.93531 + 3.55755I$                  | $2.52739 - 2.62489I$ |
| $u = 0.432344 - 1.079150I$<br>$a = -0.603271 - 0.193035I$<br>$b = -0.50994 - 1.48491I$<br>$c = 0.420583 - 0.036953I$<br>$d = -1.359440 - 0.207304I$ | $2.93531 + 3.55755I$                  | $2.52739 - 2.62489I$ |
| $u = -1.38845$<br>$a = 0.099908 + 0.914602I$<br>$b = -0.636148 - 0.242515I$<br>$c = -1.96418$<br>$d = 1.50912$                                      | 10.1546                               | 6.33750              |
| $u = -1.38845$<br>$a = 0.099908 - 0.914602I$<br>$b = -0.636148 + 0.242515I$<br>$c = -1.96418$<br>$d = 1.50912$                                      | 10.1546                               | 6.33750              |
| $u = 1.215250 + 0.684012I$<br>$a = 0.067480 - 1.248660I$<br>$b = -1.57665 - 0.90527I$<br>$c = -1.45820 + 1.13316I$<br>$d = 1.42757 + 0.33227I$      | $5.44991 + 9.88301I$                  | $3.28252 - 6.06963I$ |
| $u = 1.215250 + 0.684012I$<br>$a = -0.355893 + 0.630356I$<br>$b = 1.56027 + 1.09581I$<br>$c = -1.45820 + 1.13316I$<br>$d = 1.42757 + 0.33227I$      | $5.44991 + 9.88301I$                  | $3.28252 - 6.06963I$ |

| Solutions to $I_2^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape           |
|--|---------------------------------------|----------------------|
| $u = 1.215250 - 0.684012I$<br>$a = 0.067480 + 1.248660I$<br>$b = -1.57665 + 0.90527I$<br>$c = -1.45820 - 1.13316I$<br>$d = 1.42757 - 0.33227I$ | $5.44991 - 9.88301I$                  | $3.28252 + 6.06963I$ |
| $u = 1.215250 - 0.684012I$<br>$a = -0.355893 - 0.630356I$<br>$b = 1.56027 - 1.09581I$<br>$c = -1.45820 - 1.13316I$<br>$d = 1.42757 - 0.33227I$ | $5.44991 - 9.88301I$                  | $3.28252 + 6.06963I$ |
| $u = -0.549965$<br>$a = -1.11644$<br>$b = -2.20354$<br>$c = 0.744760$<br>$d = -0.342714$   | $-2.57083$                            | $2.16010$            |
| $u = -0.549965$<br>$a = -2.30659$<br>$b = 0.439006$<br>$c = 0.744760$<br>$d = -0.342714$   | $-2.57083$                            | $2.16010$            |

$$\text{III. } I_3^u = \langle u^5 a - u^5 + \cdots + u^2 + d, -u^5 a - u^4 a + \cdots + c - 1, -u^4 a + u^4 + \cdots + b - a, 2u^5 a - u^5 + \cdots + a^2 + a, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^5 a + u^4 a - u^2 a - u^3 - au - u^2 + 1 \\ -u^5 a - u^4 a + u^5 + u^3 a + u^4 + u^2 a - u^2 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ u^4 a + u^3 a - u^4 - 2u^2 a - u^3 - au + a + u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} u^5 + u^3 a + u^4 - u^3 - au - 2u^2 + 1 \\ -u^5 a - u^4 a + u^5 + u^3 a + u^4 + u^2 a - u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^3 a + u^4 + u^3 + au + 2a - u - 1 \\ u^5 a + u^4 a - u^3 a - u^4 - 3u^2 a - u^3 + u^2 + 2a + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u^5 a + u^4 a - u^2 a - u^3 - au - u^2 + 1 \\ au \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} u^5 a + u^4 a - 2u^3 a - u^2 a + au + u^2 + 2a - 1 \\ u^5 a + u^4 a - u^3 a - u^4 - 3u^2 a - u^3 + u^2 + 2a + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^4 a + u^3 a - u^4 - 2u^2 a - u^3 - au + u \\ 2u^4 a - 2u^2 a + 2a - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} u^4 a + u^3 a - u^4 - 2u^2 a - u^3 - au + u \\ 2u^4 a - 2u^2 a + 2a - 1 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^4 + 4u^2 + 4u - 2$



(iv) u-Polynomials at the component

| Crossings                     | u-Polynomials at each crossing  |
|-------------------------------|---|
| $c_1, c_4, c_6$<br>$c_8, c_9$ | $u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1$ |
| $c_2$                         | $u^{12} + 9u^{11} + \dots - 4u + 1$   |
| $c_3, c_7$                    | $(u^6 + u^5 - u^4 - 2u^3 + u + 1)^2$  |
| $c_5, c_{10}$                 | $(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$  |
| $c_{11}$                      | $(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^2$   |

(v) Riley Polynomials at the component

| Crossings                     | Riley Polynomials at each crossing            |
|-------------------------------|---|
| $c_1, c_4, c_6$<br>$c_8, c_9$ | $y^{12} - 9y^{11} + \dots + 4y + 1$           |
| $c_2$                         | $y^{12} - 13y^{11} + \dots - 12y + 1$         |
| $c_3, c_5, c_7$<br>$c_{10}$   | $(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$ |
| $c_{11}$                      | $(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$        |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 1.002190 + 0.295542I$<br>$a = 0.228720 - 1.004780I$<br>$b = 0.103539 - 0.942817I$<br>$c = 0.490081 + 0.135670I$<br>$d = -0.895235 + 0.524661I$  | $1.89061 + 0.92430I$                  | $3.71672 - 0.79423I$  |
| $u = 1.002190 + 0.295542I$<br>$a = 1.69020 - 0.12901I$<br>$b = -1.18901 - 0.78206I$<br>$c = -2.60446 + 1.12615I$<br>$d = 1.323480 + 0.139870I$       | $1.89061 + 0.92430I$                  | $3.71672 - 0.79423I$  |
| $u = 1.002190 - 0.295542I$<br>$a = 0.228720 + 1.004780I$<br>$b = 0.103539 + 0.942817I$<br>$c = 0.490081 - 0.135670I$<br>$d = -0.895235 - 0.524661I$  | $1.89061 - 0.92430I$                  | $3.71672 + 0.79423I$  |
| $u = 1.002190 - 0.295542I$<br>$a = 1.69020 + 0.12901I$<br>$b = -1.18901 + 0.78206I$<br>$c = -2.60446 - 1.12615I$<br>$d = 1.323480 - 0.139870I$       | $1.89061 - 0.92430I$                  | $3.71672 + 0.79423I$  |
| $u = -0.428243 + 0.664531I$<br>$a = 0.305248 + 0.125739I$<br>$b = -0.101098 + 0.828455I$<br>$c = 0.886780 + 0.510268I$<br>$d = 0.152828 + 0.487477I$ | $-1.89061 + 0.92430I$                 | $-3.71672 - 0.79423I$ |
| $u = -0.428243 + 0.664531I$<br>$a = -0.41743 - 1.68310I$<br>$b = -0.15460 - 3.71488I$<br>$c = 0.460381 - 0.041004I$<br>$d = -1.155020 - 0.191936I$   | $-1.89061 + 0.92430I$                 | $-3.71672 - 0.79423I$ |

| Solutions to $I_3^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.428243 - 0.664531I$<br>$a = 0.305248 - 0.125739I$<br>$b = -0.101098 - 0.828455I$<br>$c = 0.886780 - 0.510268I$<br>$d = 0.152828 - 0.487477I$ | $-1.89061 - 0.92430I$                 | $-3.71672 + 0.79423I$ |
| $u = -0.428243 - 0.664531I$<br>$a = -0.41743 + 1.68310I$<br>$b = -0.15460 + 3.71488I$<br>$c = 0.460381 + 0.041004I$<br>$d = -1.155020 + 0.191936I$   | $-1.89061 - 0.92430I$                 | $-3.71672 + 0.79423I$ |
| $u = -1.073950 + 0.558752I$<br>$a = 0.266694 + 0.574266I$<br>$b = -1.16959 + 0.91104I$<br>$c = 0.550084 + 0.355577I$<br>$d = -0.282166 + 0.828798I$  | $-5.69302I$                           | $0. + 5.51057I$       |
| $u = -1.073950 + 0.558752I$<br>$a = -1.57343 - 0.13663I$<br>$b = 1.01075 - 1.59090I$<br>$c = -1.78287 - 1.35197I$<br>$d = 1.356120 - 0.270046I$      | $-5.69302I$                           | $0. + 5.51057I$       |
| $u = -1.073950 - 0.558752I$<br>$a = 0.266694 - 0.574266I$<br>$b = -1.16959 - 0.91104I$<br>$c = 0.550084 - 0.355577I$<br>$d = -0.282166 - 0.828798I$  | $5.69302I$                            | $0. - 5.51057I$       |
| $u = -1.073950 - 0.558752I$<br>$a = -1.57343 + 0.13663I$<br>$b = 1.01075 + 1.59090I$<br>$c = -1.78287 + 1.35197I$<br>$d = 1.356120 + 0.270046I$      | $5.69302I$                            | $0. - 5.51057I$       |

$$\text{IV. } I_4^u = \langle u^5c - u^5 + \cdots + d + 1, -2u^4c + u^4 + \cdots + c^2 - u, -u^2 + b, -u^2 + a + 1, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} c \\ -u^5c + u^5 + 2u^3c - u^3 - 2cu + u - 1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -u^5c + u^5 + 2u^3c - u^3 - 2cu + c + u - 1 \\ -u^5c + u^5 + 2u^3c - u^3 - 2cu + u - 1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^5 - 2u^3 + u \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} c \\ u^5c - u^5 - 2u^3c - u^2c + u^3 + 2cu - u + 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -c \\ u^5c - u^5 - 2u^3c + u^3 + 2cu - u + 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^4 + 4u^2 + 4u - 2$

(iv) u-Polynomials at the component

| Crossings                        | u-Polynomials at each crossing  |
|----------------------------------|---|
| $c_1, c_4$                       | $(u^6 - u^5 - u^4 + 2u^3 - u + 1)^2$  |
| $c_2$                            | $(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^2$   |
| $c_3, c_7$                       | $(u^6 + u^5 - u^4 - 2u^3 + u + 1)^2$  |
| $c_5, c_6, c_8$<br>$c_9, c_{10}$ | $u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1$ |
| $c_{11}$                         | $u^{12} + 9u^{11} + \dots - 4u + 1$   |

(v) Riley Polynomials at the component

| Crossings                        | Riley Polynomials at each crossing            |
|----------------------------------|---|
| $c_1, c_3, c_4$<br>$c_7$         | $(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^2$ |
| $c_2$                            | $(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^2$        |
| $c_5, c_6, c_8$<br>$c_9, c_{10}$ | $y^{12} - 9y^{11} + \dots + 4y + 1$           |
| $c_{11}$                         | $y^{12} - 13y^{11} + \dots - 12y + 1$         |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_4^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 1.002190 + 0.295542I$<br>$a = -0.082955 + 0.592379I$<br>$b = 0.917045 + 0.592379I$<br>$c = 0.490081 + 0.135670I$<br>$d = -0.895235 + 0.524661I$   | $1.89061 + 0.92430I$                  | $3.71672 - 0.79423I$  |
| $u = 1.002190 + 0.295542I$<br>$a = -0.082955 + 0.592379I$<br>$b = 0.917045 + 0.592379I$<br>$c = -2.60446 + 1.12615I$<br>$d = 1.323480 + 0.139870I$     | $1.89061 + 0.92430I$                  | $3.71672 - 0.79423I$  |
| $u = 1.002190 - 0.295542I$<br>$a = -0.082955 - 0.592379I$<br>$b = 0.917045 - 0.592379I$<br>$c = 0.490081 - 0.135670I$<br>$d = -0.895235 - 0.524661I$   | $1.89061 - 0.92430I$                  | $3.71672 + 0.79423I$  |
| $u = 1.002190 - 0.295542I$<br>$a = -0.082955 - 0.592379I$<br>$b = 0.917045 - 0.592379I$<br>$c = -2.60446 - 1.12615I$<br>$d = 1.323480 - 0.139870I$     | $1.89061 - 0.92430I$                  | $3.71672 + 0.79423I$  |
| $u = -0.428243 + 0.664531I$<br>$a = -1.258210 - 0.569162I$<br>$b = -0.258209 - 0.569162I$<br>$c = 0.886780 + 0.510268I$<br>$d = 0.152828 + 0.487477I$  | $-1.89061 + 0.92430I$                 | $-3.71672 - 0.79423I$ |
| $u = -0.428243 + 0.664531I$<br>$a = -1.258210 - 0.569162I$<br>$b = -0.258209 - 0.569162I$<br>$c = 0.460381 - 0.041004I$<br>$d = -1.155020 - 0.191936I$ | $-1.89061 + 0.92430I$                 | $-3.71672 - 0.79423I$ |



| Solutions to $I_4^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = -0.428243 - 0.664531I$<br>$a = -1.258210 + 0.569162I$<br>$b = -0.258209 + 0.569162I$<br>$c = 0.886780 - 0.510268I$<br>$d = 0.152828 - 0.487477I$  | $-1.89061 - 0.92430I$                 | $-3.71672 + 0.79423I$ |
| $u = -0.428243 - 0.664531I$<br>$a = -1.258210 + 0.569162I$<br>$b = -0.258209 + 0.569162I$<br>$c = 0.460381 + 0.041004I$<br>$d = -1.155020 + 0.191936I$ | $-1.89061 - 0.92430I$                 | $-3.71672 + 0.79423I$ |
| $u = -1.073950 + 0.558752I$<br>$a = -0.158836 - 1.200140I$<br>$b = 0.84116 - 1.20014I$<br>$c = 0.550084 + 0.355577I$<br>$d = -0.282166 + 0.828798I$    | $-5.69302I$                           | $0. + 5.51057I$       |
| $u = -1.073950 + 0.558752I$<br>$a = -0.158836 - 1.200140I$<br>$b = 0.84116 - 1.20014I$<br>$c = -1.78287 - 1.35197I$<br>$d = 1.356120 - 0.270046I$      | $-5.69302I$                           | $0. + 5.51057I$       |
| $u = -1.073950 - 0.558752I$<br>$a = -0.158836 + 1.200140I$<br>$b = 0.84116 + 1.20014I$<br>$c = 0.550084 - 0.355577I$<br>$d = -0.282166 - 0.828798I$    | $5.69302I$                            | $0. - 5.51057I$       |
| $u = -1.073950 - 0.558752I$<br>$a = -0.158836 + 1.200140I$<br>$b = 0.84116 + 1.20014I$<br>$c = -1.78287 + 1.35197I$<br>$d = 1.356120 + 0.270046I$      | $5.69302I$                            | $0. - 5.51057I$       |

$$\mathbf{V. } I_5^u = \langle u^5 - u^3 + d + u, 2u^5 + 2u^4 + \dots + c + 2, -u^2 + b, -u^2 + a + 1, u^6 + u^5 - u^4 - 2u^3 + u + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -2u^5 - 2u^4 + 3u^3 + 4u^2 - 2u - 2 \\ -u^5 + u^3 - u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} u^2 - 1 \\ u^2 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -3u^5 - 2u^4 + 4u^3 + 4u^2 - 3u - 2 \\ -u^5 + u^3 - u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^5 - 2u^3 + u \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -2u^5 - 2u^4 + 3u^3 + 4u^2 - 2u - 2 \\ u^3 - u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 2u^5 + 2u^4 - 3u^3 - 4u^2 + 2u + 2 \\ u^5 - u^3 + u \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $-4u^4 + 4u^2 + 4u - 2$

(iv) u-Polynomials at the component

| Crossings                                      | u-Polynomials at each crossing            |
|--|---|
| $c_1, c_4, c_5$<br>$c_6, c_8, c_9$<br>$c_{10}$ | $u^6 - u^5 - u^4 + 2u^3 - u + 1$          |
| $c_2, c_{11}$                                  | $u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1$ |
| $c_3, c_7$                                     | $u^6 + u^5 - u^4 - 2u^3 + u + 1$          |

(v) Riley Polynomials at the component

| Crossings  | Riley Polynomials at each crossing        |
|--|---|
| $c_1, c_3, c_4$<br>$c_5, c_6, c_7$<br>$c_8, c_9, c_{10}$ | $y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1$ |
| $c_2, c_{11}$  | $y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1$        |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_5^u$   | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|--|---------------------------------------|-----------------------|
| $u = 1.002190 + 0.295542I$<br>$a = -0.082955 + 0.592379I$<br>$b = 0.917045 + 0.592379I$<br>$c = 0.575561 - 0.267796I$<br>$d = -0.428243 - 0.664531I$ | $1.89061 + 0.92430I$                  | $3.71672 - 0.79423I$  |
| $u = 1.002190 - 0.295542I$<br>$a = -0.082955 - 0.592379I$<br>$b = 0.917045 - 0.592379I$<br>$c = 0.575561 + 0.267796I$<br>$d = -0.428243 + 0.664531I$ | $1.89061 - 0.92430I$                  | $3.71672 + 0.79423I$  |
| $u = -0.428243 + 0.664531I$<br>$a = -1.258210 - 0.569162I$<br>$b = -0.258209 - 0.569162I$<br>$c = -0.02510 - 3.38343I$<br>$d = 1.002190 - 0.295542I$ | $-1.89061 + 0.92430I$                 | $-3.71672 - 0.79423I$ |
| $u = -0.428243 - 0.664531I$<br>$a = -1.258210 + 0.569162I$<br>$b = -0.258209 + 0.569162I$<br>$c = -0.02510 + 3.38343I$<br>$d = 1.002190 + 0.295542I$ | $-1.89061 - 0.92430I$                 | $-3.71672 + 0.79423I$ |
| $u = -1.073950 + 0.558752I$<br>$a = -0.158836 - 1.200140I$<br>$b = 0.84116 - 1.20014I$<br>$c = 0.449542 - 0.121113I$<br>$d = -1.073950 - 0.558752I$  | $-5.69302I$                           | $0. + 5.51057I$       |
| $u = -1.073950 - 0.558752I$<br>$a = -0.158836 + 1.200140I$<br>$b = 0.84116 + 1.20014I$<br>$c = 0.449542 + 0.121113I$<br>$d = -1.073950 + 0.558752I$  | $5.69302I$                            | $0. - 5.51057I$       |

$$\text{VI. } I_1^v = \langle a, d, c - 1, b - 1, v + 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -1 \\ 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = -12

(iv) **u**-Polynomials at the component

| Crossings                      | <b>u</b> -Polynomials at each crossing |
|--------------------------------|--|
| $c_1, c_5$                     | $u - 1$                                |
| $c_2, c_4, c_{10}$<br>$c_{11}$ | $u + 1$                                |
| $c_3, c_6, c_7$<br>$c_8, c_9$  | $u$                                    |

(v) Riley Polynomials at the component

| Crossings                                | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_4$<br>$c_5, c_{10}, c_{11}$ | $y - 1$                            |
| $c_3, c_6, c_7$<br>$c_8, c_9$            | $y$                                |



(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_1^v$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $v = -1.00000$       |                                       |            |
| $a = 0$              |                                       |            |
| $b = 1.00000$        | -3.28987                              | -12.0000   |
| $c = 1.00000$        |                                       |            |
| $d = 0$              |                                       |            |

$$\text{VII. } I_2^v = \langle c, d + 1, b, a - 1, v - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u-Polynomials at the component**

| Crossings                     | u-Polynomials at each crossing |
|-------------------------------|--------------------------------|
| $c_1, c_2, c_3$<br>$c_4, c_7$ | $u$                            |
| $c_5, c_6, c_{11}$            | $u + 1$                        |
| $c_8, c_9, c_{10}$            | $u - 1$                        |

(v) Riley Polynomials at the component

| Crossings                                | Riley Polynomials at each crossing |
|--|------------------------------------|
| $c_1, c_2, c_3$<br>$c_4, c_7$            | $y$                                |
| $c_5, c_6, c_8$<br>$c_9, c_{10}, c_{11}$ | $y - 1$                            |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_2^v$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $v = 1.00000$        |                                       |            |
| $a = 1.00000$        |                                       |            |
| $b = 0$              | 0                                     | 0          |
| $c = 0$              |                                       |            |
| $d = -1.00000$       |                                       |            |

$$\text{VIII. } I_3^v = \langle a, d + 1, c - a - 1, b + 1, v - 1 \rangle$$

(i) Arc colorings

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u**-Polynomials at the component

| Crossings                           | <b>u</b> -Polynomials at each crossing |
|-------------------------------------|--|
| $c_1, c_8, c_9$                     | $u - 1$                                |
| $c_2, c_4, c_6$                     | $u + 1$                                |
| $c_3, c_5, c_7$<br>$c_{10}, c_{11}$ | $u$                                    |

(v) Riley Polynomials at the component

| Crossings                           | Riley Polynomials at each crossing |
|-------------------------------------|------------------------------------|
| $c_1, c_2, c_4$<br>$c_6, c_8, c_9$  | $y - 1$                            |
| $c_3, c_5, c_7$<br>$c_{10}, c_{11}$ | $y$                                |



(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_3^v$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape |
|----------------------|---------------------------------------|------------|
| $v = 1.00000$        |                                       |            |
| $a = 0$              |                                       |            |
| $b = -1.00000$       | 0                                     | 0          |
| $c = 1.00000$        |                                       |            |
| $d = -1.00000$       |                                       |            |

$$\text{IX. } I_4^v = \langle c, d + 1, -av + c - v - 1, bv + 1 \rangle$$

**(i) Arc colorings**

$$a_3 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} v \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} a \\ a + 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} a + v \\ a + 1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} a + 1 \\ a + 2 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a \\ -a - 1 \end{pmatrix}$$

$$a_5 = \begin{pmatrix} -a \\ -a - 1 \end{pmatrix}$$

**(ii) Obstruction class = -1**

**(iii) Cusp Shapes =  $-a^2 - v^2 - 2a - 5$**

**(iv) u-Polynomials at the component :** It cannot be defined for a positive dimension component.

**(v) Riley Polynomials at the component :** It cannot be defined for a positive dimension component.

(iv) Complex Volumes and Cusp Shapes

| Solution to $I_4^v$ | $\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$ | Cusp shape            |
|---------------------|---------------------------------------|-----------------------|
| $v = \dots$         |                                       |                       |
| $a = \dots$         |                                       |                       |
| $b = \dots$         | -1.64493                              | $-3.42386 - 0.27749I$ |
| $c = \dots$         |                                       |                       |
| $d = \dots$         |                                       |                       |

## X. u-Polynomials

| Crossings     | u-Polynomials at each crossing   |
|---------------|--|
| $c_1$         | $u(u-1)^2(u^6 - u^5 - u^4 + 2u^3 - u + 1)^3$ $\cdot (u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)$ $\cdot (u^{16} - u^{15} + \dots + 4u - 4)(u^{19} - 2u^{18} + \dots + 3u - 1)$                               |
| $c_2, c_{11}$ | $u(u+1)^2(u^6 + 3u^5 + 5u^4 + 4u^3 + 2u^2 + u + 1)^3$ $\cdot (u^{12} + 9u^{11} + \dots - 4u + 1)(u^{16} + 7u^{15} + \dots + 40u + 16)$ $\cdot (u^{19} + 8u^{18} + \dots + 19u + 1)$  |
| $c_3, c_7$    | $u^3(u^6 + u^5 - u^4 - 2u^3 + u + 1)^5$ $\cdot (u^8 - 3u^7 + 3u^6 + 2u^5 - 8u^4 + 9u^3 - 3u^2 - 2u + 2)^2$ $\cdot (u^{19} + 2u^{18} + \dots + 4u^2 - 8)$   |
| $c_4$         | $u(u+1)^2(u^6 - u^5 - u^4 + 2u^3 - u + 1)^3$ $\cdot (u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)$ $\cdot (u^{16} - u^{15} + \dots + 4u - 4)(u^{19} - 2u^{18} + \dots + 3u - 1)$                               |
| $c_5, c_{10}$ | $u(u-1)(u+1)(u^6 - u^5 - u^4 + 2u^3 - u + 1)^3$ $\cdot (u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)$ $\cdot (u^{16} - u^{15} + \dots + 4u - 4)(u^{19} - 2u^{18} + \dots + 3u - 1)$                            |
| $c_6$         | $u(u+1)^2(u^6 - u^5 - u^4 + 2u^3 - u + 1)$ $\cdot (u^8 + u^7 - 4u^6 - 3u^5 + 5u^4 + u^3 - u^2 + 3u - 1)^2$ $\cdot (u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)^2$ $\cdot (u^{19} + 2u^{18} + \dots - 8u - 4)$ |
| $c_8, c_9$    | $u(u-1)^2(u^6 - u^5 - u^4 + 2u^3 - u + 1)$ $\cdot (u^8 + u^7 - 4u^6 - 3u^5 + 5u^4 + u^3 - u^2 + 3u - 1)^2$ $\cdot (u^{12} + u^{11} - 4u^{10} - 2u^9 + 7u^8 - u^7 - 5u^6 + 5u^5 - u^4 - 3u^3 + 2u^2 + 1)^2$ $\cdot (u^{19} + 2u^{18} + \dots - 8u - 4)$ |

## XI. Riley Polynomials

| Crossings                   | Riley Polynomials at each crossing  |
|-----------------------------|---|
| $c_1, c_4, c_5$<br>$c_{10}$ | $y(y-1)^2(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^3$ $\cdot (y^{12} - 9y^{11} + \dots + 4y + 1)(y^{16} - 7y^{15} + \dots - 40y + 16)$ $\cdot (y^{19} - 8y^{18} + \dots + 19y - 1)$                               |
| $c_2, c_{11}$               | $y(y-1)^2(y^6 + y^5 + 5y^4 + 6y^2 + 3y + 1)^3$ $\cdot (y^{12} - 13y^{11} + \dots - 12y + 1)(y^{16} + y^{15} + \dots - 544y + 256)$ $\cdot (y^{19} + 12y^{18} + \dots + 195y - 1)$                                 |
| $c_3, c_7$                  | $y^3(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)^5$ $\cdot (y^8 - 3y^7 + 5y^6 - 4y^5 + 2y^4 - 13y^3 + 13y^2 - 16y + 4)^2$ $\cdot (y^{19} - 6y^{18} + \dots + 64y - 64)$  |
| $c_6, c_8, c_9$             | $y(y-1)^2(y^6 - 3y^5 + 5y^4 - 4y^3 + 2y^2 - y + 1)$ $\cdot (y^8 - 9y^7 + 32y^6 - 53y^5 + 31y^4 + 15y^3 - 15y^2 - 7y + 1)^2$ $\cdot ((y^{12} - 9y^{11} + \dots + 4y + 1)^2)(y^{19} - 18y^{18} + \dots + 88y - 16)$ |