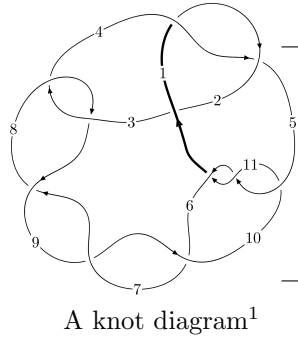
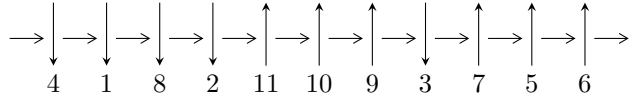


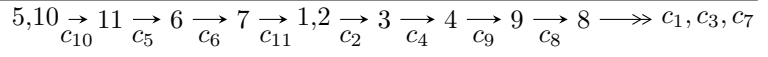
11a₅₈ (K11a₅₈)



Linearized knot diagram



Solving Sequence



Ideals for irreducible components² of X_{par}

$$I_1^u = \langle u^{25} - 9u^{23} + \dots + b + u, -u^{28} - u^{27} + \dots + a - 3, u^{29} + 2u^{28} + \dots + 3u + 1 \rangle$$

$$I_2^u = \langle u^2 + b, a - 1, u^{12} - 4u^{10} + u^9 + 6u^8 - 3u^7 - u^6 + 3u^5 - 5u^4 + u^3 + 3u^2 - 2u + 1 \rangle$$

$$I_3^u = \langle b + 1, a - 1, u - 1 \rangle$$

* 3 irreducible components of $\dim_{\mathbb{C}} = 0$, with total 42 representations.

¹The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

²All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$I_1^u = \langle u^{25} - 9u^{23} + \dots + b + u, -u^{28} - u^{27} + \dots + a - 3, u^{29} + 2u^{28} + \dots + 3u + 1 \rangle \quad \text{I.}$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} u^{28} + u^{27} + \dots - 5u + 3 \\ -u^{25} + 9u^{23} + \dots + 4u^2 - u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^{28} + 11u^{26} + \dots - 8u + 1 \\ u^{28} + u^{27} + \dots + u + 1 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} -u^{27} + 11u^{25} + \dots + 6u - 2 \\ -u^{28} - u^{27} + \dots - u - 1 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^6 - 3u^4 + 2u^2 + 1 \\ u^6 - 2u^4 + u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^9 + 4u^7 - 5u^5 + 3u \\ -u^9 + 3u^7 - 3u^5 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^9 + 4u^7 - 5u^5 + 3u \\ -u^9 + 3u^7 - 3u^5 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes

$$= -4u^{28} - 6u^{27} + 40u^{26} + 58u^{25} - 176u^{24} - 236u^{23} + 428u^{22} + 482u^{21} - 568u^{20} - 370u^{19} + 236u^{18} - 414u^{17} + 460u^{16} + 1092u^{15} - 788u^{14} - 532u^{13} + 356u^{12} - 584u^{11} + 236u^{10} + 608u^9 - 308u^8 + 84u^7 + 40u^6 - 178u^5 + 60u^4 - 26u^3 + 8u^2 + 6u - 8$$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4	$u^{29} - 2u^{28} + \dots - u + 1$
c_2	$u^{29} + 16u^{28} + \dots + 7u + 1$
c_3, c_8	$u^{29} + 2u^{28} + \dots + 2u + 2$
c_5, c_{10}, c_{11}	$u^{29} + 2u^{28} + \dots + 3u + 1$
c_6, c_7, c_9	$u^{29} - 6u^{28} + \dots + 8u + 4$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4	$y^{29} - 16y^{28} + \dots + 7y - 1$
c_2	$y^{29} - 4y^{28} + \dots - 17y - 1$
c_3, c_8	$y^{29} + 6y^{28} + \dots + 8y - 4$
c_5, c_{10}, c_{11}	$y^{29} - 24y^{28} + \dots + 23y - 1$
c_6, c_7, c_9	$y^{29} + 30y^{28} + \dots + 504y - 16$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.050913 + 0.910185I$ $a = -0.45193 - 1.39576I$ $b = 0.00992 - 2.35228I$	$-10.46170 + 8.03356I$	$-4.76249 - 5.59744I$
$u = 0.050913 - 0.910185I$ $a = -0.45193 + 1.39576I$ $b = 0.00992 + 2.35228I$	$-10.46170 - 8.03356I$	$-4.76249 + 5.59744I$
$u = -0.008721 + 0.887960I$ $a = -0.49123 + 1.42056I$ $b = 0.14380 + 2.36020I$	$-10.71030 - 1.52343I$	$-5.35413 + 0.68771I$
$u = -0.008721 - 0.887960I$ $a = -0.49123 - 1.42056I$ $b = 0.14380 - 2.36020I$	$-10.71030 + 1.52343I$	$-5.35413 - 0.68771I$
$u = 1.189730 + 0.056062I$ $a = -0.370086 - 0.255115I$ $b = -1.23899 - 0.69502I$	$2.39907 + 0.12369I$	$3.50407 + 1.07759I$
$u = 1.189730 - 0.056062I$ $a = -0.370086 + 0.255115I$ $b = -1.23899 + 0.69502I$	$2.39907 - 0.12369I$	$3.50407 - 1.07759I$
$u = 1.242320 + 0.189774I$ $a = -0.715591 + 0.438399I$ $b = 0.20240 + 2.88734I$	$0.91595 + 3.56420I$	$0.67873 - 4.99863I$
$u = 1.242320 - 0.189774I$ $a = -0.715591 - 0.438399I$ $b = 0.20240 - 2.88734I$	$0.91595 - 3.56420I$	$0.67873 + 4.99863I$
$u = 0.230236 + 0.672244I$ $a = -0.11327 - 1.56979I$ $b = -0.07670 - 1.55700I$	$-1.85869 + 5.19499I$	$-2.04173 - 8.30480I$
$u = 0.230236 - 0.672244I$ $a = -0.11327 + 1.56979I$ $b = -0.07670 + 1.55700I$	$-1.85869 - 5.19499I$	$-2.04173 + 8.30480I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.249690 + 0.417811I$ $a = -0.215564 - 0.608911I$ $b = -0.927812 - 0.165212I$	$-3.02235 + 1.47420I$	$1.47993 - 0.60903I$
$u = 1.249690 - 0.417811I$ $a = -0.215564 + 0.608911I$ $b = -0.927812 + 0.165212I$	$-3.02235 - 1.47420I$	$1.47993 + 0.60903I$
$u = -1.311940 + 0.179476I$ $a = -0.339083 + 0.475947I$ $b = -0.644137 + 0.471467I$	$4.98921 - 3.78682I$	$7.27007 + 4.16727I$
$u = -1.311940 - 0.179476I$ $a = -0.339083 - 0.475947I$ $b = -0.644137 - 0.471467I$	$4.98921 + 3.78682I$	$7.27007 - 4.16727I$
$u = -1.342150 + 0.040293I$ $a = -0.537408 - 0.444706I$ $b = -0.23164 - 1.41782I$	$6.61715 - 2.27209I$	$8.89752 + 3.80982I$
$u = -1.342150 - 0.040293I$ $a = -0.537408 + 0.444706I$ $b = -0.23164 + 1.41782I$	$6.61715 + 2.27209I$	$8.89752 - 3.80982I$
$u = 1.286000 + 0.418935I$ $a = -0.762208 + 0.613998I$ $b = 1.69138 + 2.74611I$	$-6.68464 + 6.20004I$	$-1.73580 - 3.81481I$
$u = 1.286000 - 0.418935I$ $a = -0.762208 - 0.613998I$ $b = 1.69138 - 2.74611I$	$-6.68464 - 6.20004I$	$-1.73580 + 3.81481I$
$u = -1.333980 + 0.244603I$ $a = -0.683762 - 0.524847I$ $b = 0.83387 - 2.33932I$	$3.04589 - 8.42692I$	$3.52830 + 8.66921I$
$u = -1.333980 - 0.244603I$ $a = -0.683762 + 0.524847I$ $b = 0.83387 + 2.33932I$	$3.04589 + 8.42692I$	$3.52830 - 8.66921I$

Solutions to I_1^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -1.301320 + 0.407588I$ $a = -0.248387 + 0.609615I$ $b = -0.872384 + 0.107277I$	$-2.63518 - 7.77071I$	$2.10858 + 5.30383I$
$u = -1.301320 - 0.407588I$ $a = -0.248387 - 0.609615I$ $b = -0.872384 - 0.107277I$	$-2.63518 + 7.77071I$	$2.10858 - 5.30383I$
$u = 0.529946 + 0.329108I$ $a = 0.667313 - 0.986592I$ $b = -0.347726 - 0.588274I$	$0.93542 + 1.41053I$	$5.39446 - 5.74020I$
$u = 0.529946 - 0.329108I$ $a = 0.667313 + 0.986592I$ $b = -0.347726 + 0.588274I$	$0.93542 - 1.41053I$	$5.39446 + 5.74020I$
$u = -1.320520 + 0.424615I$ $a = -0.743481 - 0.622059I$ $b = 1.72687 - 2.60904I$	$-6.1783 - 12.8069I$	$-0.92308 + 8.12569I$
$u = -1.320520 - 0.424615I$ $a = -0.743481 + 0.622059I$ $b = 1.72687 + 2.60904I$	$-6.1783 + 12.8069I$	$-0.92308 - 8.12569I$
$u = -0.063245 + 0.516212I$ $a = -0.28684 + 2.09363I$ $b = 0.49644 + 1.38676I$	$-3.02142 - 1.01433I$	$-6.77496 + 0.83339I$
$u = -0.063245 - 0.516212I$ $a = -0.28684 - 2.09363I$ $b = 0.49644 - 1.38676I$	$-3.02142 + 1.01433I$	$-6.77496 - 0.83339I$
$u = -0.193938$ $a = 4.58305$ $b = 0.469396$	-1.29813	-8.53890

$$\text{II. } I_2^u = \langle u^2 + b, a - 1, u^{12} - 4u^{10} + \dots - 2u + 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_7 = \begin{pmatrix} -u^3 + 2u \\ -u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^2 + 1 \\ u^4 - 2u^2 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -u^2 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} u^4 - u^2 + 1 \\ -u^6 + 2u^4 - u^2 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} u \\ -u^3 + u \end{pmatrix}$$

$$a_9 = \begin{pmatrix} u^6 - 3u^4 + 2u^2 + 1 \\ u^6 - 2u^4 + u^2 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^9 + 4u^7 - 5u^5 + 3u \\ -u^9 + 3u^7 - 3u^5 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} -u^9 + 4u^7 - 5u^5 + 3u \\ -u^9 + 3u^7 - 3u^5 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes = $4u^9 - 12u^7 + 4u^6 + 12u^5 - 8u^4 + 8u^3 + 4u^2 - 12u + 6$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
c_1, c_4, c_5 c_{10}, c_{11}	$u^{12} - 4u^{10} + u^9 + 6u^8 - 3u^7 - u^6 + 3u^5 - 5u^4 + u^3 + 3u^2 - 2u + 1$
c_2	$u^{12} + 8u^{11} + \dots - 2u + 1$
c_3, c_8	$(u^4 - u^3 + u^2 + 1)^3$
c_6, c_7, c_9	$(u^4 - u^3 + 3u^2 - 2u + 1)^3$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_4, c_5 c_{10}, c_{11}	$y^{12} - 8y^{11} + \dots + 2y + 1$
c_2	$y^{12} - 8y^{11} + \dots + 2y + 1$
c_3, c_8	$(y^4 + y^3 + 3y^2 + 2y + 1)^3$
c_6, c_7, c_9	$(y^4 + 5y^3 + 7y^2 + 2y + 1)^3$

(vi) Complex Volumes and Cusp Shapes

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.944825 + 0.321917I$ $a = 1.00000$ $b = -0.789064 - 0.608311I$	$0.21101 - 1.41510I$	$1.82674 + 4.90874I$
$u = 0.944825 - 0.321917I$ $a = 1.00000$ $b = -0.789064 + 0.608311I$	$0.21101 + 1.41510I$	$1.82674 - 4.90874I$
$u = 0.031664 + 0.878090I$ $a = 1.00000$ $b = 0.770039 - 0.055609I$	$-6.79074 + 3.16396I$	$-1.82674 - 2.56480I$
$u = 0.031664 - 0.878090I$ $a = 1.00000$ $b = 0.770039 + 0.055609I$	$-6.79074 - 3.16396I$	$-1.82674 + 2.56480I$
$u = -1.186690 + 0.158407I$ $a = 1.00000$ $b = -1.38315 + 0.37596I$	$0.21101 - 1.41510I$	$1.82674 + 4.90874I$
$u = -1.186690 - 0.158407I$ $a = 1.00000$ $b = -1.38315 - 0.37596I$	$0.21101 + 1.41510I$	$1.82674 - 4.90874I$
$u = 1.240280 + 0.455646I$ $a = 1.00000$ $b = -1.33067 - 1.13025I$	$-6.79074 - 3.16396I$	$-1.82674 + 2.56480I$
$u = 1.240280 - 0.455646I$ $a = 1.00000$ $b = -1.33067 + 1.13025I$	$-6.79074 + 3.16396I$	$-1.82674 - 2.56480I$
$u = -1.271940 + 0.422443I$ $a = 1.00000$ $b = -1.43937 + 1.07464I$	$-6.79074 - 3.16396I$	$-1.82674 + 2.56480I$
$u = -1.271940 - 0.422443I$ $a = 1.00000$ $b = -1.43937 - 1.07464I$	$-6.79074 + 3.16396I$	$-1.82674 - 2.56480I$

Solutions to I_2^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 0.241868 + 0.480324I$	$0.21101 + 1.41510I$	$1.82674 - 4.90874I$
$a = 1.00000$		
$b = 0.172212 - 0.232350I$		
$u = 0.241868 - 0.480324I$	$0.21101 - 1.41510I$	$1.82674 + 4.90874I$
$a = 1.00000$		
$b = 0.172212 + 0.232350I$		

$$\text{III. } I_3^u = \langle b + 1, a - 1, u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 0 \\ 1 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_1 = \begin{pmatrix} 0 \\ -1 \end{pmatrix}$$

$$a_2 = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$$

$$a_3 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_8 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

(ii) Obstruction class = 1

(iii) Cusp Shapes = 0

(iv) **u**-Polynomials at the component

Crossings	u -Polynomials at each crossing
c_1, c_{10}, c_{11}	$u - 1$
c_2, c_4, c_5	$u + 1$
c_3, c_6, c_7 c_8, c_9	u

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
c_1, c_2, c_4 c_5, c_{10}, c_{11}	$y - 1$
c_3, c_6, c_7 c_8, c_9	y

(vi) Complex Volumes and Cusp Shapes

Solutions to I_3^u	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = 1.00000$		
$a = 1.00000$	0	0
$b = -1.00000$		

IV. u-Polynomials

Crossings	u-Polynomials at each crossing
c_1	$(u - 1)(u^{12} - 4u^{10} + \dots - 2u + 1)$ $\cdot (u^{29} - 2u^{28} + \dots - u + 1)$
c_2	$(u + 1)(u^{12} + 8u^{11} + \dots - 2u + 1)(u^{29} + 16u^{28} + \dots + 7u + 1)$
c_3, c_8	$u(u^4 - u^3 + u^2 + 1)^3(u^{29} + 2u^{28} + \dots + 2u + 2)$
c_4	$(u + 1)(u^{12} - 4u^{10} + \dots - 2u + 1)$ $\cdot (u^{29} - 2u^{28} + \dots - u + 1)$
c_5	$(u + 1)(u^{12} - 4u^{10} + \dots - 2u + 1)$ $\cdot (u^{29} + 2u^{28} + \dots + 3u + 1)$
c_6, c_7, c_9	$u(u^4 - u^3 + 3u^2 - 2u + 1)^3(u^{29} - 6u^{28} + \dots + 8u + 4)$
c_{10}, c_{11}	$(u - 1)(u^{12} - 4u^{10} + \dots - 2u + 1)$ $\cdot (u^{29} + 2u^{28} + \dots + 3u + 1)$

V. Riley Polynomials

Crossings	Riley Polynomials at each crossing
c_1, c_4	$(y - 1)(y^{12} - 8y^{11} + \dots + 2y + 1)(y^{29} - 16y^{28} + \dots + 7y - 1)$
c_2	$(y - 1)(y^{12} - 8y^{11} + \dots + 2y + 1)(y^{29} - 4y^{28} + \dots - 17y - 1)$
c_3, c_8	$y(y^4 + y^3 + 3y^2 + 2y + 1)^3(y^{29} + 6y^{28} + \dots + 8y - 4)$
c_5, c_{10}, c_{11}	$(y - 1)(y^{12} - 8y^{11} + \dots + 2y + 1)(y^{29} - 24y^{28} + \dots + 23y - 1)$
c_6, c_7, c_9	$y(y^4 + 5y^3 + \dots + 2y + 1)^3(y^{29} + 30y^{28} + \dots + 504y - 16)$