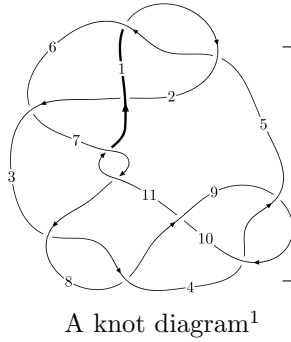
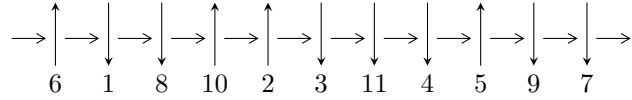


11a<sub>89</sub> (K11a<sub>89</sub>)



**Linearized knot diagram**



**Solving Sequence**

$$5,10 \xrightarrow{c_4} 4 \xrightarrow{c_9} 9 \xrightarrow{c_{10}} 11 \xrightarrow{c_8} 8 \xrightarrow{c_3} 3 \xrightarrow{c_7} 7 \xrightarrow{c_{11}} 1 \xrightarrow{c_2} 2 \xrightarrow{c_6} 6 \Rightarrow c_1, c_5$$

**Ideals for irreducible components<sup>2</sup> of  $X_{\text{par}}$**

$$I_1^u = \langle u^{59} - u^{58} + \dots + 2u - 1 \rangle$$

\* 1 irreducible components of  $\dim_{\mathbb{C}} = 0$ , with total 59 representations.

<sup>1</sup>The image of knot diagram is generated by the software “**Draw programme**” developed by Andrew Bartholomew(<http://www.layer8.co.uk/maths/draw/index.htm#Running-draw>), where we modified some parts for our purpose(<https://github.com/CATsTAILs/LinksPainter>).

<sup>2</sup>All coefficients of polynomials are rational numbers. But the coefficients are sometimes approximated in decimal forms when there is not enough margin.

$$\text{I. } I_1^u = \langle u^{59} - u^{58} + \dots + 2u - 1 \rangle$$

(i) Arc colorings

$$a_5 = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$$

$$a_{10} = \begin{pmatrix} 0 \\ u \end{pmatrix}$$

$$a_4 = \begin{pmatrix} 1 \\ u^2 \end{pmatrix}$$

$$a_9 = \begin{pmatrix} -u \\ u \end{pmatrix}$$

$$a_{11} = \begin{pmatrix} -u^3 \\ u^3 + u \end{pmatrix}$$

$$a_8 = \begin{pmatrix} u^3 \\ u^5 + u^3 + u \end{pmatrix}$$

$$a_3 = \begin{pmatrix} -u^6 - u^4 + 1 \\ -u^8 - 2u^6 - 2u^4 \end{pmatrix}$$

$$a_7 = \begin{pmatrix} u^{11} + 2u^9 + 2u^7 + u^3 \\ -u^{11} - 3u^9 - 4u^7 - u^5 + u^3 + u \end{pmatrix}$$

$$a_1 = \begin{pmatrix} -u^{19} - 4u^{17} - 8u^{15} - 8u^{13} - 5u^{11} - 2u^9 - 2u^7 - u^3 \\ u^{19} + 5u^{17} + 12u^{15} + 15u^{13} + 9u^{11} - u^9 - 4u^7 - 2u^5 + u^3 + u \end{pmatrix}$$

$$a_2 = \begin{pmatrix} -u^{46} - 11u^{44} + \dots - u^8 + 1 \\ u^{46} + 12u^{44} + \dots - 4u^4 - u^2 \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^{25} - 6u^{23} + \dots + 2u^3 + u \\ -u^{27} - 7u^{25} + \dots + u^3 + u \end{pmatrix}$$

$$a_6 = \begin{pmatrix} -u^{25} - 6u^{23} + \dots + 2u^3 + u \\ -u^{27} - 7u^{25} + \dots + u^3 + u \end{pmatrix}$$

(ii) Obstruction class = -1

(iii) Cusp Shapes =  $4u^{57} - 4u^{56} + \dots + 16u - 10$

(iv) u-Polynomials at the component

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{59} - u^{58} + \dots + u^2 + 1$
$c_2$	$u^{59} + 27u^{58} + \dots - 2u - 1$
$c_3, c_8$	$u^{59} - u^{58} + \dots - 122u + 17$
$c_4, c_9$	$u^{59} + u^{58} + \dots + 2u + 1$
$c_6$	$u^{59} + u^{58} + \dots - 12u + 1$
$c_7, c_{11}$	$u^{59} - 5u^{58} + \dots - 82u + 13$
$c_{10}$	$u^{59} + 31u^{58} + \dots - 2u - 1$

(v) Riley Polynomials at the component

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^{59} + 27y^{58} + \dots - 2y - 1$
$c_2$	$y^{59} + 11y^{58} + \dots - 10y - 1$
$c_3, c_8$	$y^{59} - 41y^{58} + \dots + 8186y - 289$
$c_4, c_9$	$y^{59} + 31y^{58} + \dots - 2y - 1$
$c_6$	$y^{59} - 5y^{58} + \dots + 158y - 1$
$c_7, c_{11}$	$y^{59} + 39y^{58} + \dots - 790y - 169$
$c_{10}$	$y^{59} - 5y^{58} + \dots - 2y - 1$

(vi) Complex Volumes and Cusp Shapes

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.583032 + 0.813066I$	$3.26959 - 8.77818I$	$-0.47164 + 8.68429I$
$u = -0.583032 - 0.813066I$	$3.26959 + 8.77818I$	$-0.47164 - 8.68429I$
$u = 0.580211 + 0.794129I$	$5.10030 + 3.64576I$	$2.63542 - 3.97208I$
$u = 0.580211 - 0.794129I$	$5.10030 - 3.64576I$	$2.63542 + 3.97208I$
$u = 0.105740 + 0.954737I$	$-3.61435 - 0.81482I$	$-11.81807 + 0.39125I$
$u = 0.105740 - 0.954737I$	$-3.61435 + 0.81482I$	$-11.81807 - 0.39125I$
$u = 0.583734 + 0.745935I$	$5.23854 + 0.95699I$	$3.16051 - 3.05625I$
$u = 0.583734 - 0.745935I$	$5.23854 - 0.95699I$	$3.16051 + 3.05625I$
$u = -0.513490 + 0.784053I$	$0.12062 - 2.09029I$	$-3.61559 + 4.04072I$
$u = -0.513490 - 0.784053I$	$0.12062 + 2.09029I$	$-3.61559 - 4.04072I$
$u = 0.267008 + 1.029790I$	$-2.27337 + 5.68828I$	$-7.21814 - 7.12378I$
$u = 0.267008 - 1.029790I$	$-2.27337 - 5.68828I$	$-7.21814 + 7.12378I$
$u = -0.590577 + 0.723804I$	$3.52494 + 4.14809I$	$0.42761 - 2.02743I$
$u = -0.590577 - 0.723804I$	$3.52494 - 4.14809I$	$0.42761 + 2.02743I$
$u = -0.277374 + 0.855227I$	$-0.47179 - 1.53127I$	$-3.18476 + 4.49987I$
$u = -0.277374 - 0.855227I$	$-0.47179 + 1.53127I$	$-3.18476 - 4.49987I$
$u = 0.402583 + 1.057810I$	$-2.16744 + 5.71812I$	$-4.90219 - 7.50071I$
$u = 0.402583 - 1.057810I$	$-2.16744 - 5.71812I$	$-4.90219 + 7.50071I$
$u = -0.343840 + 1.124430I$	$-0.89986 - 1.11007I$	0
$u = -0.343840 - 1.124430I$	$-0.89986 + 1.11007I$	0
$u = 0.791530 + 0.188709I$	$0.29452 - 9.84540I$	$-2.45493 + 7.04615I$
$u = 0.791530 - 0.188709I$	$0.29452 + 9.84540I$	$-2.45493 - 7.04615I$
$u = -0.776617 + 0.194322I$	$2.34089 + 4.71915I$	$0.72234 - 2.89887I$
$u = -0.776617 - 0.194322I$	$2.34089 - 4.71915I$	$0.72234 + 2.89887I$
$u = 0.760501 + 0.155795I$	$-2.48885 - 2.55680I$	$-6.01367 + 2.15869I$
$u = 0.760501 - 0.155795I$	$-2.48885 + 2.55680I$	$-6.01367 - 2.15869I$
$u = -0.345622 + 1.179020I$	$-1.76168 + 1.10867I$	0
$u = -0.345622 - 1.179020I$	$-1.76168 - 1.10867I$	0
$u = -0.734385 + 0.223140I$	$3.02131 + 2.16148I$	$1.92228 - 2.64869I$
$u = -0.734385 - 0.223140I$	$3.02131 - 2.16148I$	$1.92228 + 2.64869I$

Solutions to $I_1^u$	$\sqrt{-1}(\text{vol} + \sqrt{-1}CS)$	Cusp shape
$u = -0.762070 + 0.031702I$	$-4.96969 + 3.70348I$	$-7.82347 - 4.14921I$
$u = -0.762070 - 0.031702I$	$-4.96969 - 3.70348I$	$-7.82347 + 4.14921I$
$u = 0.375195 + 1.182380I$	$-6.39612 + 1.21454I$	0
$u = 0.375195 - 1.182380I$	$-6.39612 - 1.21454I$	0
$u = 0.345299 + 1.192710I$	$-3.87250 - 6.14988I$	0
$u = 0.345299 - 1.192710I$	$-3.87250 + 6.14988I$	0
$u = 0.711490 + 0.247959I$	$1.56541 + 2.82997I$	$-0.36876 - 2.80903I$
$u = 0.711490 - 0.247959I$	$1.56541 - 2.82997I$	$-0.36876 + 2.80903I$
$u = 0.517320 + 1.138620I$	$-1.02512 + 1.83845I$	0
$u = 0.517320 - 1.138620I$	$-1.02512 - 1.83845I$	0
$u = 0.449779 + 1.176350I$	$-5.36932 + 4.22831I$	0
$u = 0.449779 - 1.176350I$	$-5.36932 - 4.22831I$	0
$u = -0.520078 + 1.151590I$	$0.31706 - 6.89044I$	0
$u = -0.520078 - 1.151590I$	$0.31706 + 6.89044I$	0
$u = -0.435858 + 1.193120I$	$-8.51972 - 0.54462I$	0
$u = -0.435858 - 1.193120I$	$-8.51972 + 0.54462I$	0
$u = -0.462214 + 1.191570I$	$-8.33359 - 8.13937I$	0
$u = -0.462214 - 1.191570I$	$-8.33359 + 8.13937I$	0
$u = 0.509182 + 1.174820I$	$-5.45452 + 7.27810I$	0
$u = 0.509182 - 1.174820I$	$-5.45452 - 7.27810I$	0
$u = -0.524148 + 1.171460I$	$-0.52516 - 9.55823I$	0
$u = -0.524148 - 1.171460I$	$-0.52516 + 9.55823I$	0
$u = 0.715690$	$-2.04472$	$-3.85390$
$u = 0.526243 + 1.177590I$	$-2.6156 + 14.7281I$	0
$u = 0.526243 - 1.177590I$	$-2.6156 - 14.7281I$	0
$u = -0.380000 + 0.590467I$	$0.23726 - 1.53414I$	$0.41319 + 4.58156I$
$u = -0.380000 - 0.590467I$	$0.23726 + 1.53414I$	$0.41319 - 4.58156I$
$u = 0.465645 + 0.351838I$	$-0.26046 - 2.03230I$	$-0.35610 + 3.52270I$
$u = 0.465645 - 0.351838I$	$-0.26046 + 2.03230I$	$-0.35610 - 3.52270I$

## II. u-Polynomials

Crossings	u-Polynomials at each crossing
$c_1, c_5$	$u^{59} - u^{58} + \dots + u^2 + 1$
$c_2$	$u^{59} + 27u^{58} + \dots - 2u - 1$
$c_3, c_8$	$u^{59} - u^{58} + \dots - 122u + 17$
$c_4, c_9$	$u^{59} + u^{58} + \dots + 2u + 1$
$c_6$	$u^{59} + u^{58} + \dots - 12u + 1$
$c_7, c_{11}$	$u^{59} - 5u^{58} + \dots - 82u + 13$
$c_{10}$	$u^{59} + 31u^{58} + \dots - 2u - 1$

### III. Riley Polynomials

Crossings	Riley Polynomials at each crossing
$c_1, c_5$	$y^{59} + 27y^{58} + \dots - 2y - 1$
$c_2$	$y^{59} + 11y^{58} + \dots - 10y - 1$
$c_3, c_8$	$y^{59} - 41y^{58} + \dots + 8186y - 289$
$c_4, c_9$	$y^{59} + 31y^{58} + \dots - 2y - 1$
$c_6$	$y^{59} - 5y^{58} + \dots + 158y - 1$
$c_7, c_{11}$	$y^{59} + 39y^{58} + \dots - 790y - 169$
$c_{10}$	$y^{59} - 5y^{58} + \dots - 2y - 1$