

Ideals for irreducible components $s^{2}$ of $X_{\text {par }}$

$$
\begin{aligned}
I_{1}^{u} & =\left\langle b+u+1, a+1, u^{2}-2 u-1\right\rangle \\
I_{2}^{u} & =\langle b, a+1, u+1\rangle
\end{aligned}
$$

* 2 irreducible components of $\operatorname{dim}_{\mathbb{C}}=0$, with total 3 representations.

[^0]$$
\text { I. } I_{1}^{u}=\left\langle b+u+1, a+1, u^{2}-2 u-1\right\rangle
$$
(i) Arc colorings
\[

$$
\begin{aligned}
& a_{2}=\binom{0}{u} \\
& a_{4}=\binom{1}{0} \\
& a_{5}=\binom{1}{2 u+1} \\
& a_{7}=\binom{-1}{-u-1} \\
& a_{1}=\binom{u}{4 u+1} \\
& a_{3}=\binom{-u}{-4 u-2} \\
& a_{6}=\binom{-2 u}{-8 u-3} \\
& a_{8}=\binom{u}{-u-1}
\end{aligned}
$$
\]

(ii) Obstruction class $=-1$
(iii) Cusp Shapes $=-12$
(iv) u-Polynomials at the component

| Crossings | u -Polynomials at each crossing |
| :---: | :---: |
| $c_{1}, c_{2}, c_{4}$ | $u^{2}-2 u-1$ |
| $c_{5}, c_{6}$ |  |
| $c_{3}, c_{7}$ | $u^{2}+4 u+2$ |
| $c_{8}$ | $u^{2}+6 u+1$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
| :---: | :---: |
| $c_{1}, c_{2}, c_{4}$ | $y^{2}-6 y+1$ |
| $c_{5}, c_{6}$ |  |
| $c_{3}, c_{7}$ | $y^{2}-12 y+4$ |
| $c_{8}$ | $y^{2}-34 y+1$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_{1}^{u}$ | $\sqrt{-1}(\mathrm{vol}+\sqrt{-1} C S)$ | Cusp shape |
| :--- | :---: | :---: |
| $u=-0.414214$ | -0.822467 | -12.0000 |
| $a=-1.00000$ |  |  |
| $b=-0.585786$ | 18.9167 | -12.0000 |
| $u=2.41421$ |  |  |
| $a=-1.00000$ |  |  |

$$
\text { II. } I_{2}^{u}=\langle b, a+1, u+1\rangle
$$

(i) Arc colorings

$$
\begin{aligned}
& a_{2}=\binom{0}{-1} \\
& a_{4}=\binom{1}{0} \\
& a_{5}=\binom{1}{1} \\
& a_{7}=\binom{-1}{0} \\
& a_{1}=\binom{-1}{-1} \\
& a_{3}=\binom{1}{0} \\
& a_{6}=\binom{0}{1} \\
& a_{8}=\binom{-1}{0}
\end{aligned}
$$

(ii) Obstruction class $=1$
(iii) Cusp Shapes $=-12$
(iv) u-Polynomials at the component

| Crossings |  |
| :---: | :---: |
| $c_{1}, c_{4}, c_{5}$ | $u+1$ |
| $c_{2}, c_{6}, c_{8}$ | $u-1$ |
| $c_{3}, c_{7}$ | $u$ |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
| :---: | :---: |
|  |  |
| $c_{1}, c_{2}, c_{4}$ | $y-1$ |
| $c_{5}, c_{6}, c_{8}$ |  |
|  |  |
| $c_{3}, c_{7}$ | $y$ |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_{2}^{u}$ |  | $\sqrt{-1}(\mathrm{vol}+\sqrt{-1} C S)$ |
| :--- | :--- | ---: |
| $u=-1.00000$ |  | Cusp shape |
| $a=-1.00000$ | -3.28987 | -12.0000 |
| $b=$ | 0 |  |

III. u-Polynomials

| Crossings | u -Polynomials at each crossing |
| :---: | :---: |
| $c_{1}, c_{4}, c_{5}$ | $(u+1)\left(u^{2}-2 u-1\right)$ |
| $c_{2}, c_{6}$ | $(u-1)\left(u^{2}-2 u-1\right)$ |
| $c_{3}, c_{7}$ | $u\left(u^{2}+4 u+2\right)$ |
| $c_{8}$ | $(u-1)\left(u^{2}+6 u+1\right)$ |

## IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
| :---: | :---: |
| $c_{1}, c_{2}, c_{4}$ | $(y-1)\left(y^{2}-6 y+1\right)$ |
| $c_{5}, c_{6}$ |  |
| $c_{3}, c_{7}$ | $y\left(y^{2}-12 y+4\right)$ |
| $c_{8}$ | $(y-1)\left(y^{2}-34 y+1\right)$ |


[^0]:    ${ }^{1}$ The image of knot diagram is generated by the software "Draw programme" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm\#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).
    ${ }^{2}$ All coefficients of polynomials are rational numbers. But the coetficients are sometimes approximated in decimal forms when there is not enough margin.

