

Ideals for irreducible components $s^{2}$ of $X_{\text {par }}$

$$
\begin{aligned}
I_{1}^{u} & =\left\langle u^{3}-3 u-1\right\rangle \\
I_{2}^{u} & =\langle u-1\rangle
\end{aligned}
$$

* 2 irreducible components of $\operatorname{dim}_{\mathbb{C}}=0$, with total 4 representations.

[^0]$$
\text { I. } I_{1}^{u}=\left\langle u^{3}-3 u-1\right\rangle
$$
(i) Arc colorings
\[

$$
\begin{aligned}
& a_{1}=\binom{1}{0} \\
& a_{6}=\binom{0}{u} \\
& a_{2}=\binom{1}{u^{2}} \\
& a_{7}=\binom{-u}{-2 u-1} \\
& a_{3}=\binom{-u^{2}+1}{-u^{2}-u} \\
& a_{5}=\binom{u}{u} \\
& a_{9}=\binom{-u^{2}+1}{-u^{2}} \\
& a_{4}=\binom{-u-1}{-2 u-1} \\
& a_{8}=\binom{u+1}{u^{2}+u} \\
& a_{8}=\binom{u+1}{u^{2}+u}
\end{aligned}
$$
\]

(ii) Obstruction class $=-1$
(iii) Cusp Shapes $=-18$
(iv) u-Polynomials at the component

| Crossings | u -Polynomials at each crossing |
| :--- | :--- |
|  |  |
| $c_{1}, c_{2}, c_{3}$ |  |
| $c_{4}, c_{5}, c_{6}$ | $u^{3}-3 u-1$ |
| $c_{7}, c_{8}, c_{9}$ |  |
|  |  |

(v) Riley Polynomials at the component

| Crossings | Riley Polynomials at each crossing |
| :--- | :--- |
|  |  |
| $c_{1}, c_{2}, c_{3}$ |  |
| $c_{4}, c_{5}, c_{6}$ | $y^{3}-6 y^{2}+9 y-1$ |
| $c_{7}, c_{8}, c_{9}$ |  |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_{1}^{u}$ | $\sqrt{-1}(\mathrm{vol}+\sqrt{-1} C S)$ | Cusp shape |
| :---: | :---: | :---: |
| $u=-1.53209$ | -13.7078 | -18.0000 |
| $u=-0.347296$ | -0.548311 | -18.0000 |
| $u=1.87939$ | 12.6112 | -18.0000 |

II. $I_{2}^{u}=\langle u-1\rangle$
(i) Arc colorings

$$
\begin{aligned}
& a_{1}=\binom{1}{0} \\
& a_{6}=\binom{0}{1} \\
& a_{2}=\binom{1}{1} \\
& a_{7}=\binom{-1}{0} \\
& a_{3}=\binom{0}{1} \\
& a_{5}=\binom{1}{1} \\
& a_{9}=\binom{0}{-1} \\
& a_{4}=\binom{1}{0} \\
& a_{8}=\binom{-1}{-1} \\
& a_{8}=\binom{-1}{-1}
\end{aligned}
$$

(ii) Obstruction class $=-1$
(iii) Cusp Shapes $=-18$
(iv) u-Polynomials at the component

| Crossings | u -Polynomials at each crossing |
| :--- | :--- |
|  |  |
| $c_{1}, c_{2}, c_{3}$ |  |
| $c_{4}, c_{5}, c_{6}$ | $u-1$ |
| $c_{7}, c_{8}, c_{9}$ |  |
|  |  |

(v) Riley Polynomials at the component

| Crossings |  |
| :--- | :--- |
|  |  |
| $c_{1}, c_{2}, c_{3}$ |  |
| $c_{4}, c_{5}, c_{6}$ | $y-1$ |
| $c_{7}, c_{8}, c_{9}$ |  |

(vi) Complex Volumes and Cusp Shapes

| Solutions to $I_{2}^{u}$ | $\sqrt{-1}(\mathrm{vol}+\sqrt{-1} C S)$ | Cusp shape |
| :--- | :--- | :--- |
| $u=1.00000$ | -4.93480 | -18.0000 |

III. u-Polynomials

| Crossings | u -Polynomials at each crossing |
| :--- | :--- |
|  |  |
| $c_{1}, c_{2}, c_{3}$ |  |
| $c_{4}, c_{5}, c_{6}$ | $(u-1)\left(u^{3}-3 u-1\right)$ |
| $c_{7}, c_{8}, c_{9}$ |  |

## IV. Riley Polynomials

| Crossings | Riley Polynomials at each crossing |
| :--- | :--- |
|  |  |
| $c_{1}, c_{2}, c_{3}$ |  |
| $c_{4}, c_{5}, c_{6}$ | $(y-1)\left(y^{3}-6 y^{2}+9 y-1\right)$ |
| $c_{7}, c_{8}, c_{9}$ |  |


[^0]:    ${ }^{1}$ The image of knot diagram is generated by the software "Draw programme" developed by Andrew Bartholomew(http://www.layer8.co.uk/maths/draw/index.htm\#Running-draw), where we modified some parts for our purpose(https://github.com/CATsTAILs/LinksPainter).
    ${ }^{2}$ All coefficients of polynomials are rational numbers. But the coetficients are sometimes approximated in decimal forms when there is not enough margin.

